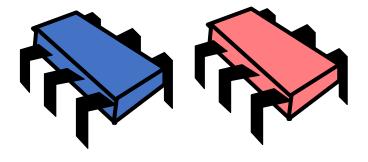
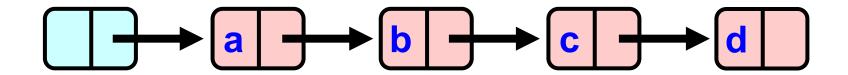
# CSE113: Parallel Programming

#### • Topics:

- Concurrent general set
- Barriers





#### Announcements

• HW 4 grades will be released this week.

#### Announcements

• HW 5 was released last week.

#### Announcements

SETs are out, please do them! It helps us out a lot.

Concurrent linked lists can be implemented using locks on every node if:

- O Locks are always acquired in the same order
- O Two locks are acquired at a time
- O Both of the above
- O Neither of the above

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Lock coupling provides higher performance than a single global lock because threads can traverse the list in parallel

- True
- False

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- True
- False

Optimistic concurrency refers to the pattern where functions optimistically assume that no other thread will interfere. In the case where another thread interferes, the program is left in an erroneous state, but since this is so rare, it does not tend to happen in practice.

- True
- False

Optimistic concurrency refers to the pattern where functions optimistically assume that no other thread will interfere. In the case where another thread interferes, the program is left in an erroneous state, but since this is so rare, it does not tend to happen in practice.

True

False

After this lecture, do you think you would be able to optimize your implementation of the concurrent stack in homework 2? Write a few sentences on what you might try.

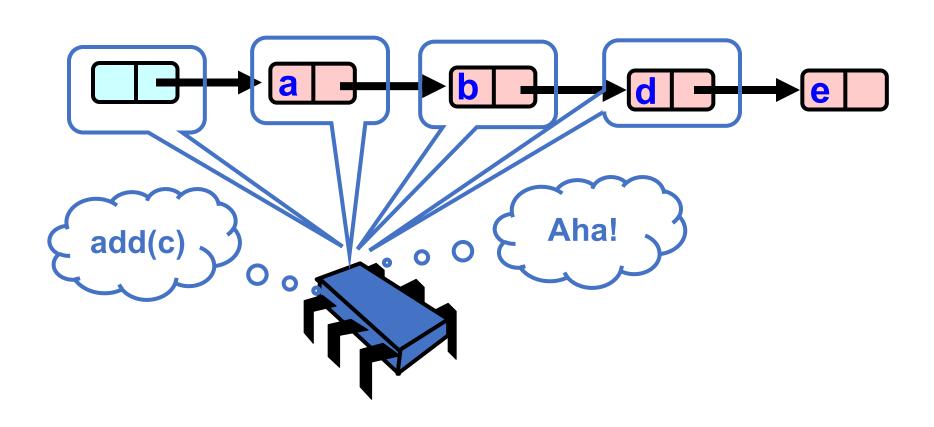
After this lecture, do you think you would be able to optimize your implementation of the concurrent stack in homework 2? Write a few sentences on what you might try.

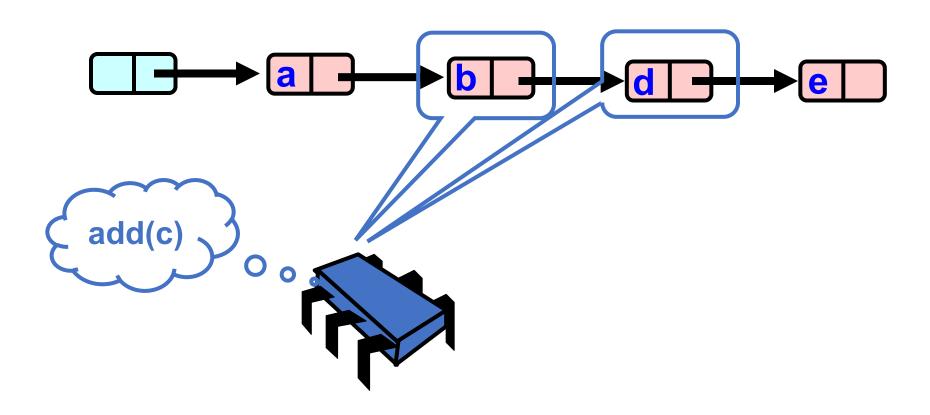
Coarse-grained vs. Fine-grained locking?

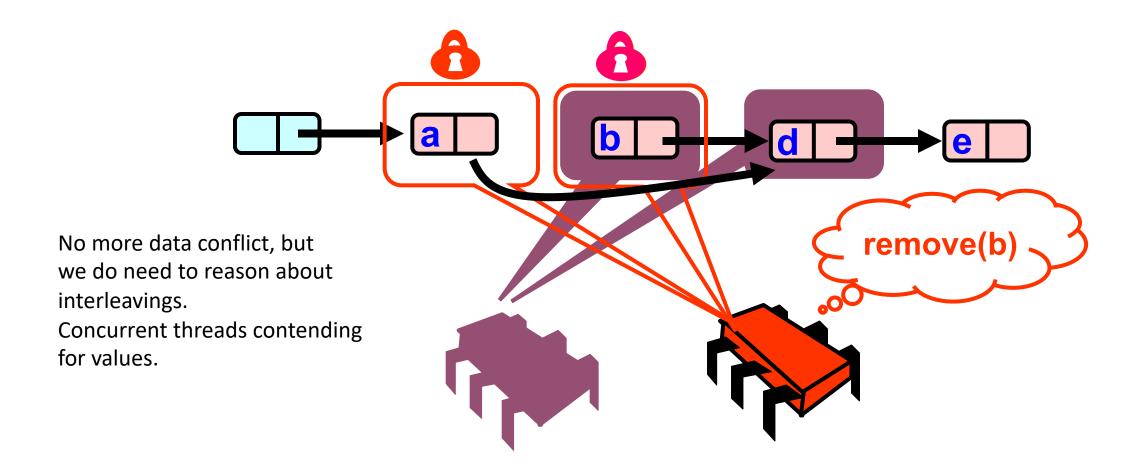
# Review

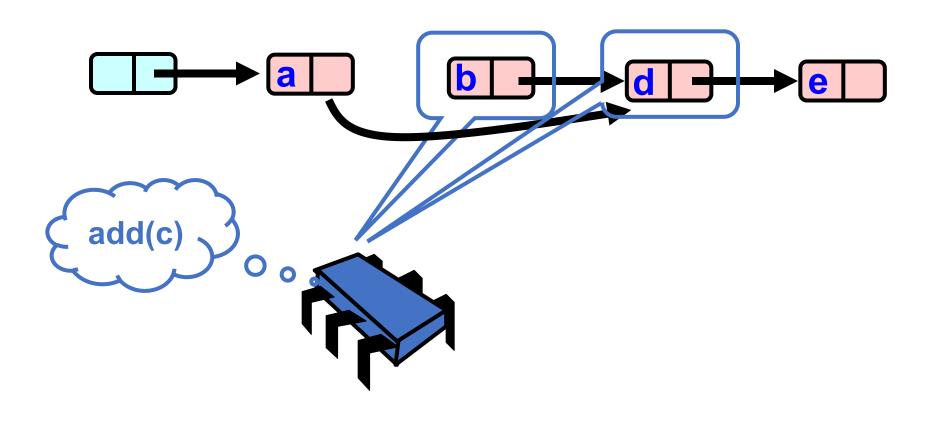
Add and remove: What could go wrong?

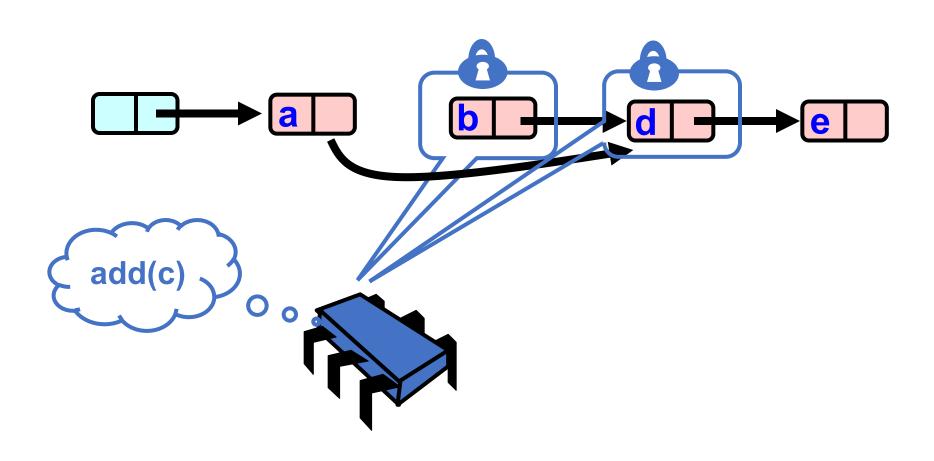
#### Add and remove: What could go wrong?

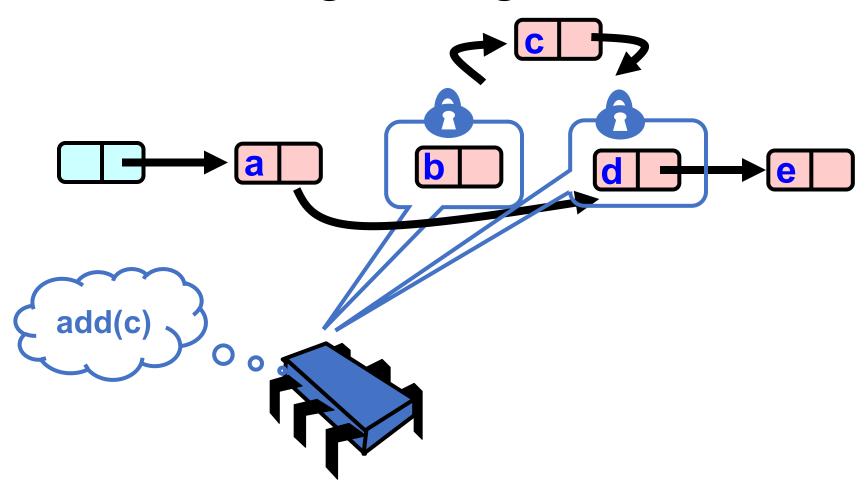


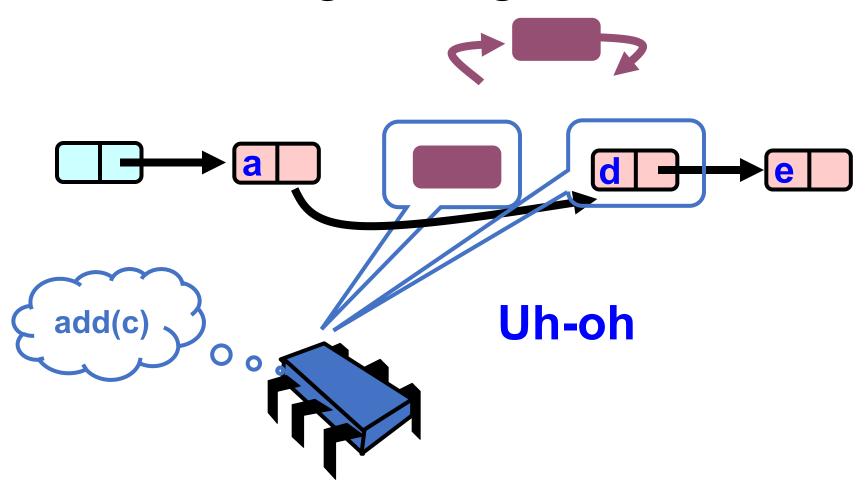




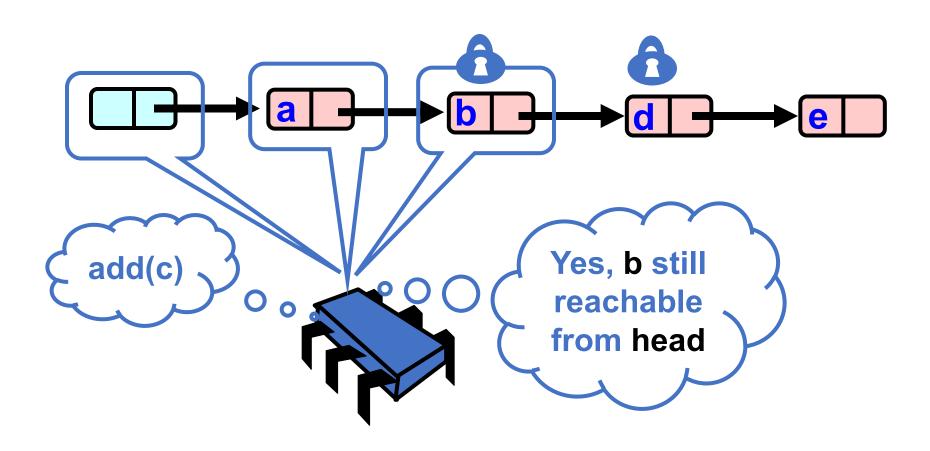




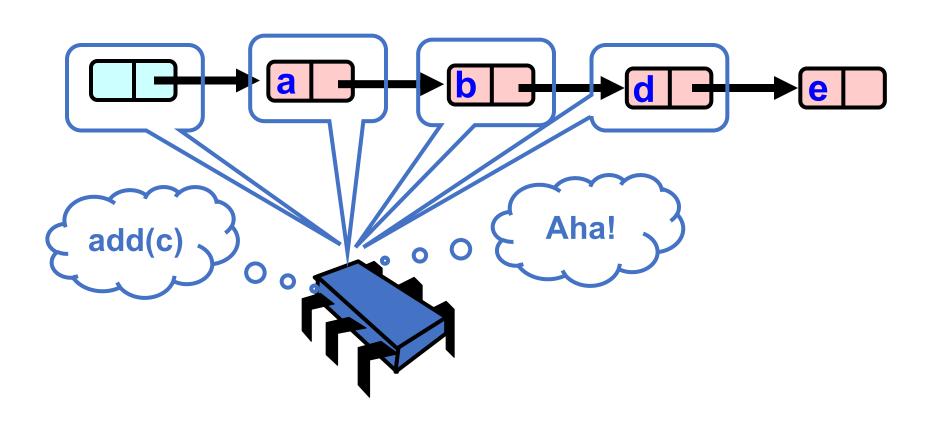


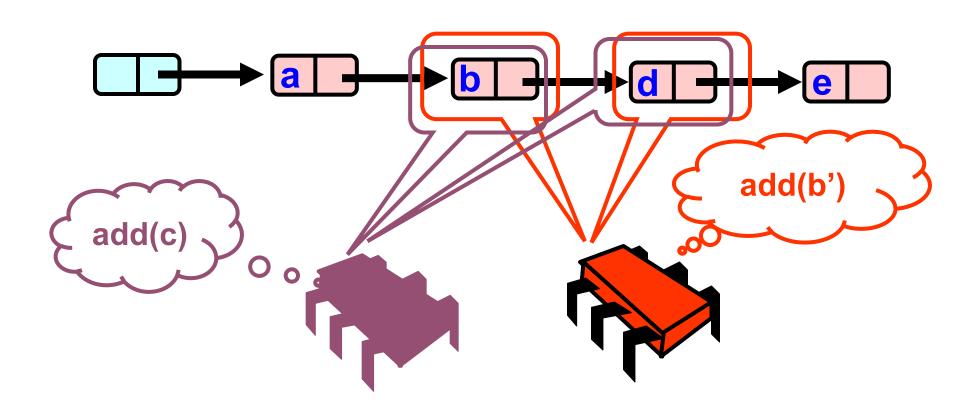


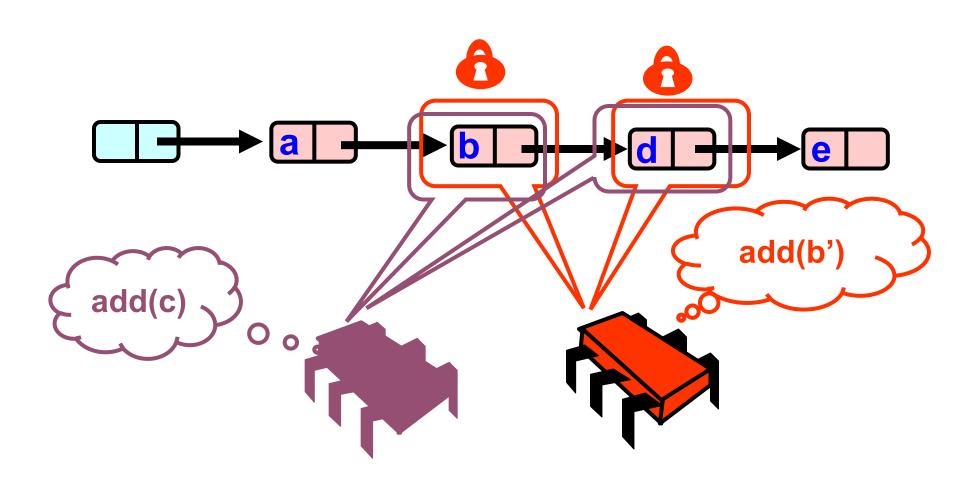
#### Validate – Part 1

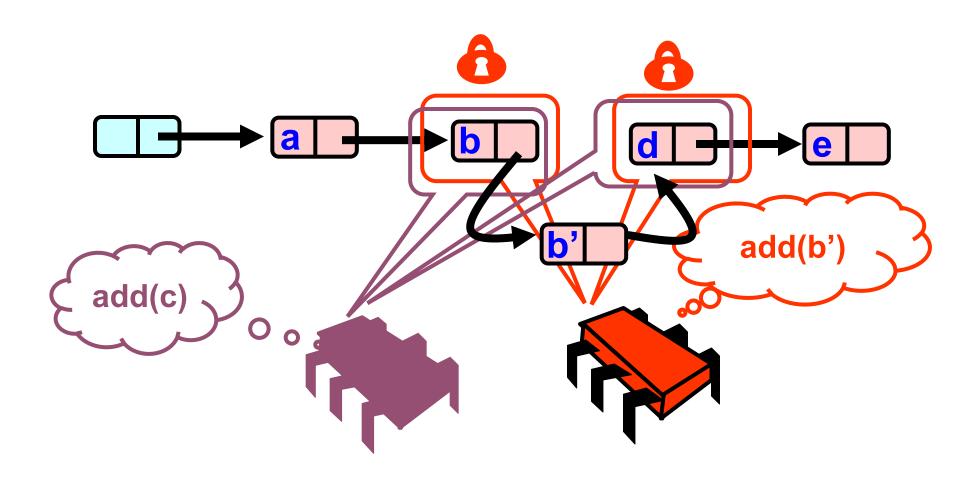


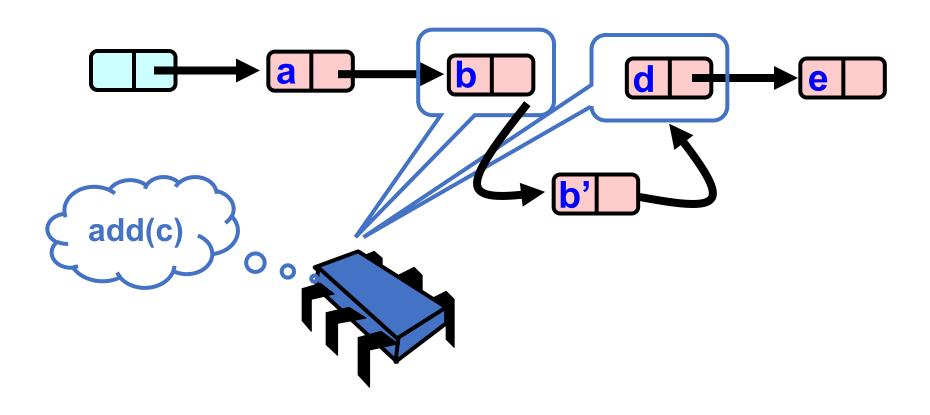
Add and Add: What could go wrong?

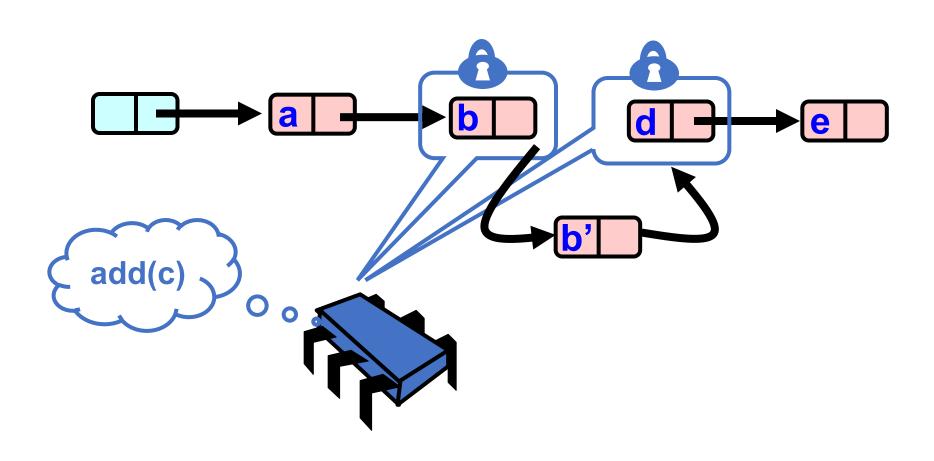


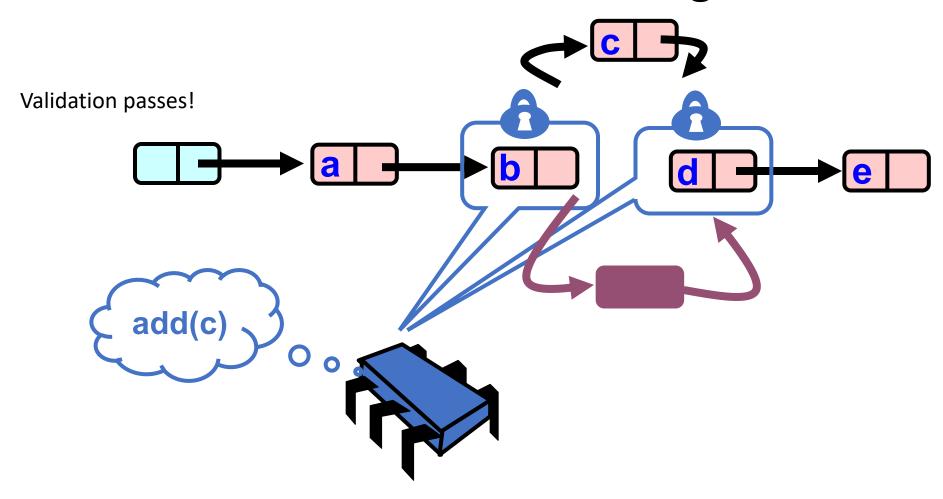




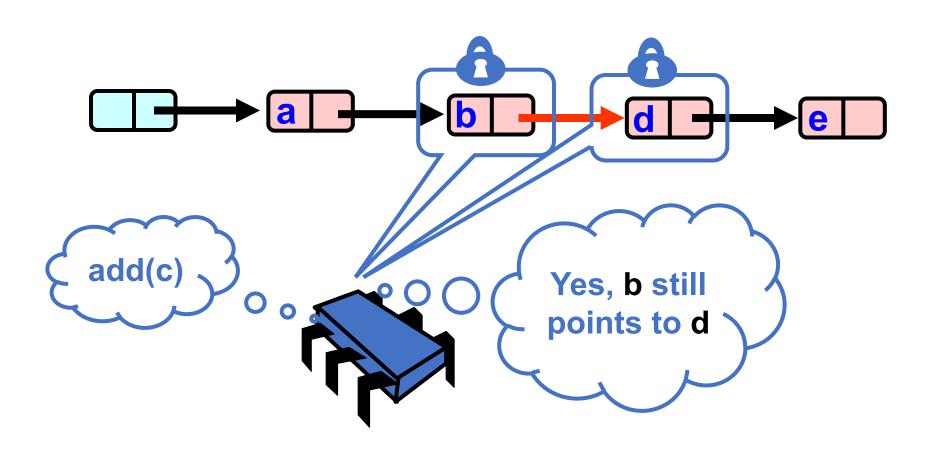


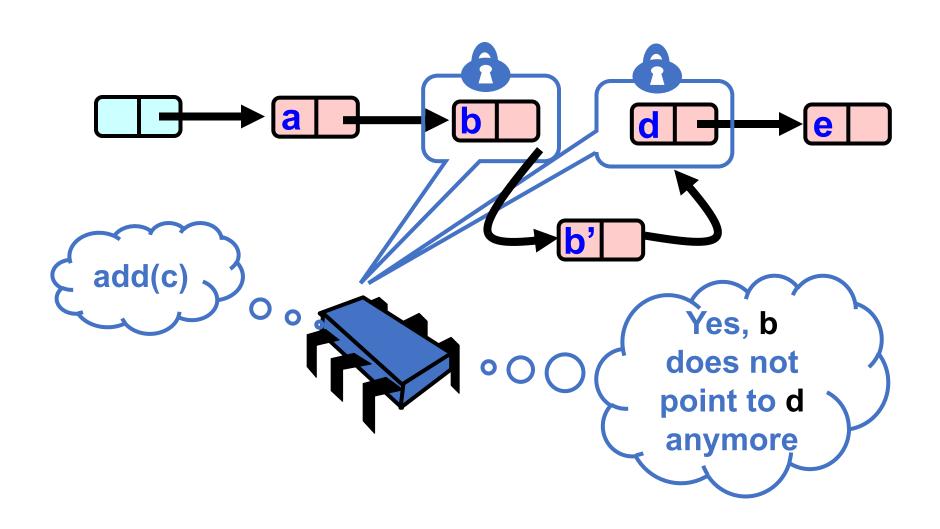






# Validate Part 2 (while holding locks)





# New Material

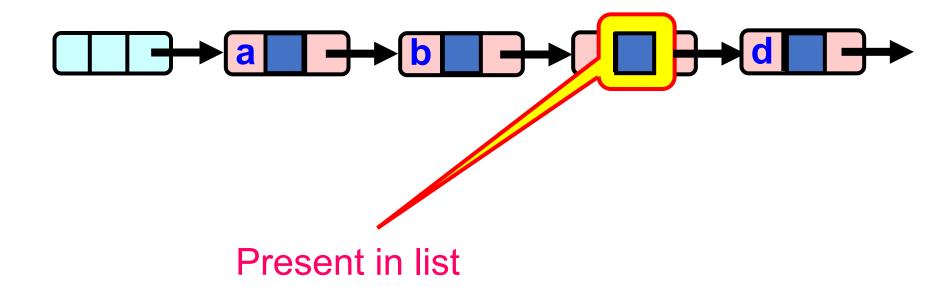
## Can we optimize more?

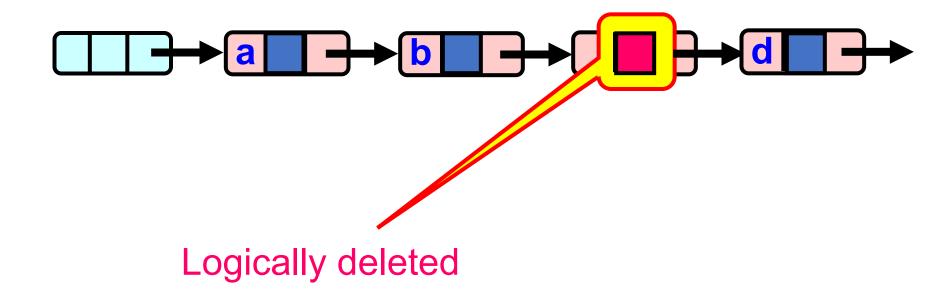
- Scan the list once?
- We need to make sure that the node is not removed.
- Instead of scanning to check reachability, leave a mark on removed nodes.

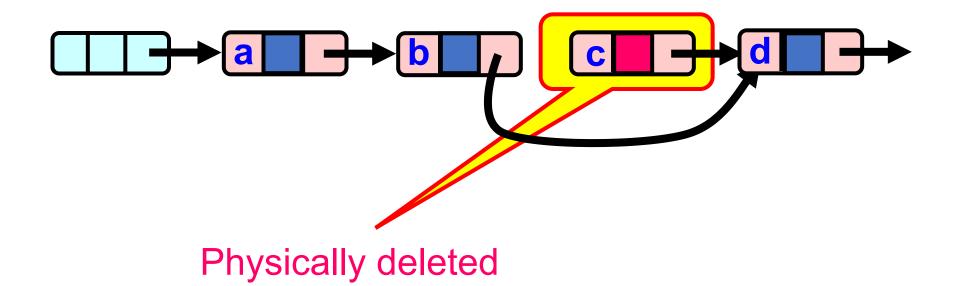
## Two step removal List

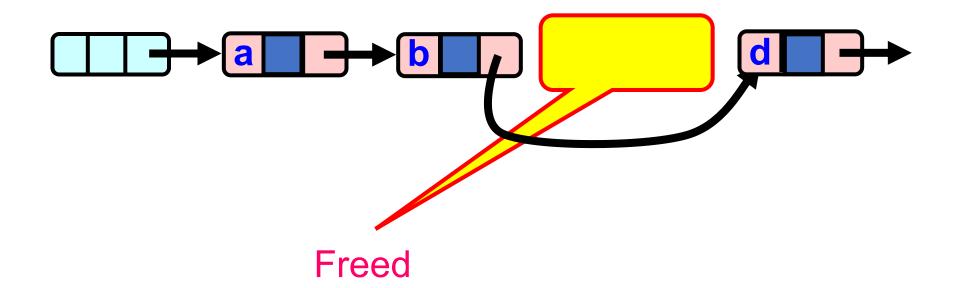
- remove()
  - Scans list (as before)
  - Locks predecessor & current (as before)
- Logical delete
  - Marks current node as removed (new!)
- Physical delete
  - Redirects predecessor's next (as before)









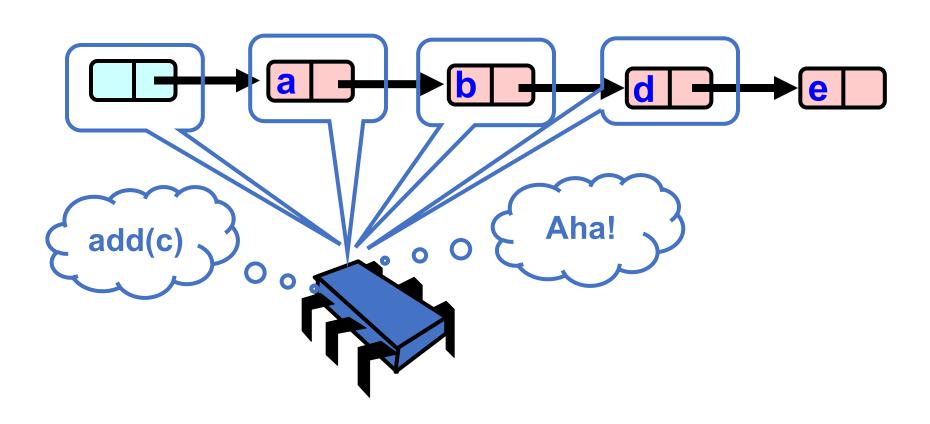


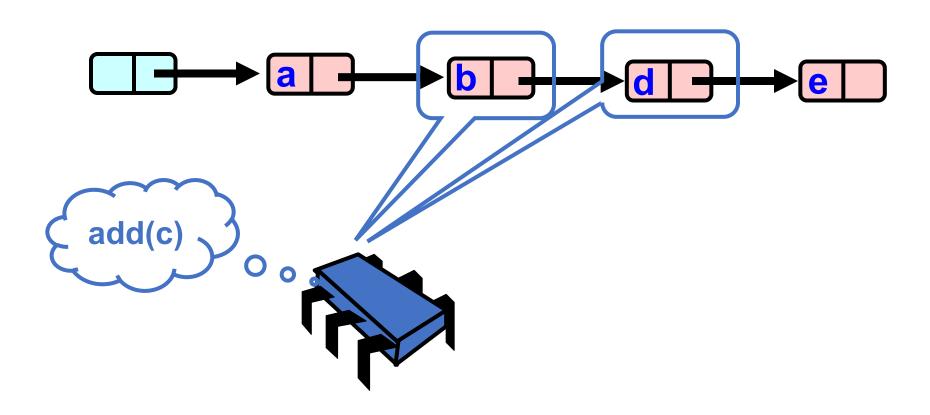
#### Two step remove list

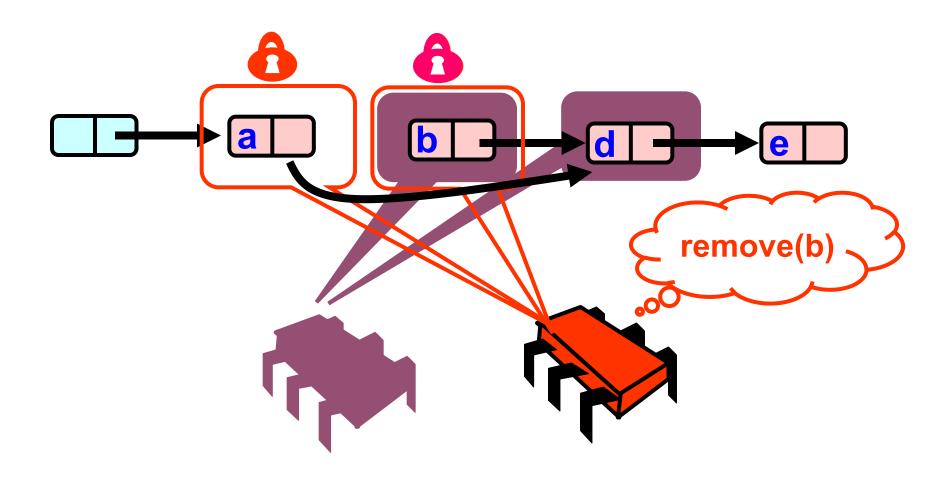
- All Methods
  - Scan through locked and marked nodes
- Must still lock pred and curr nodes.

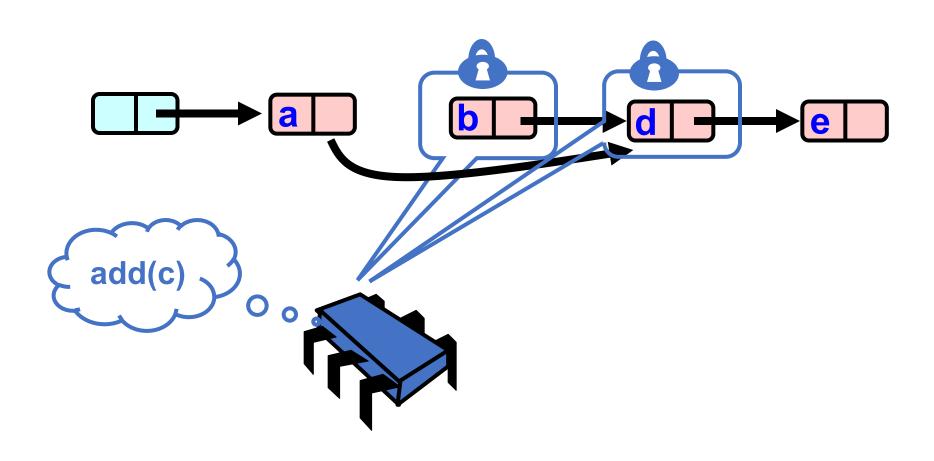
#### Validation

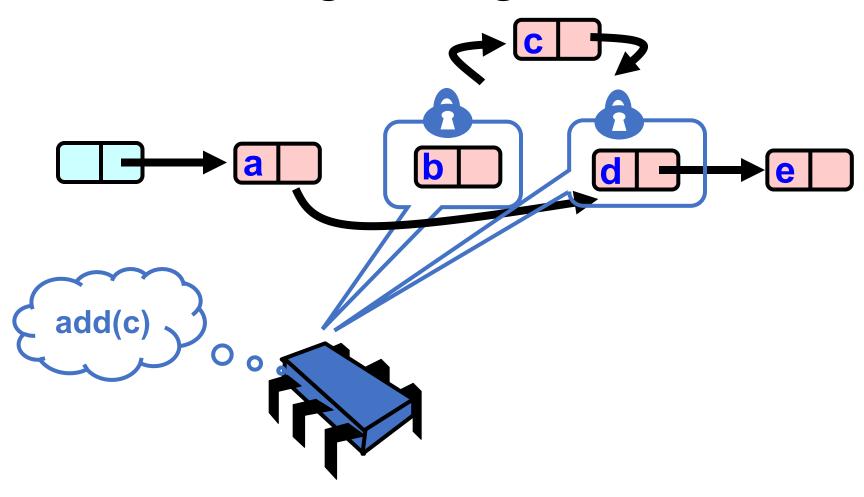
- No need to rescan list!
- Check that pred is not marked.
- Check that curr is not marked.
- Check that pred points to curr.

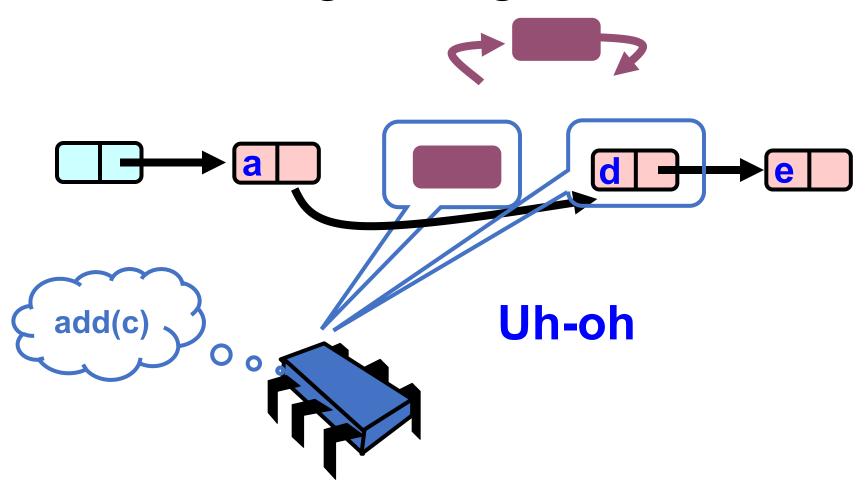


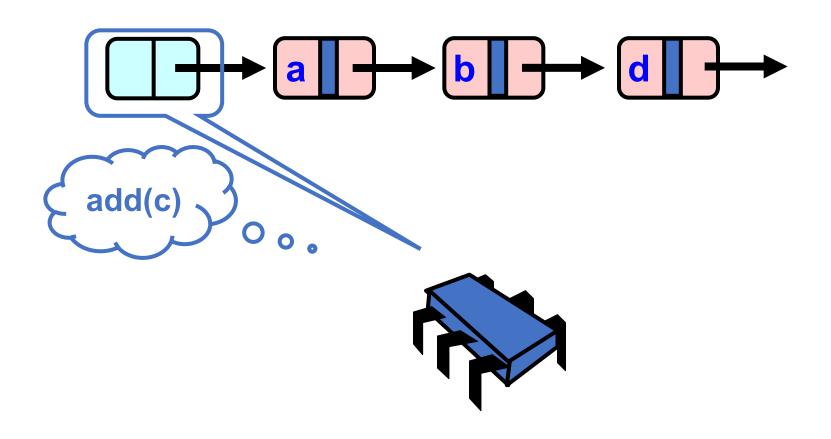


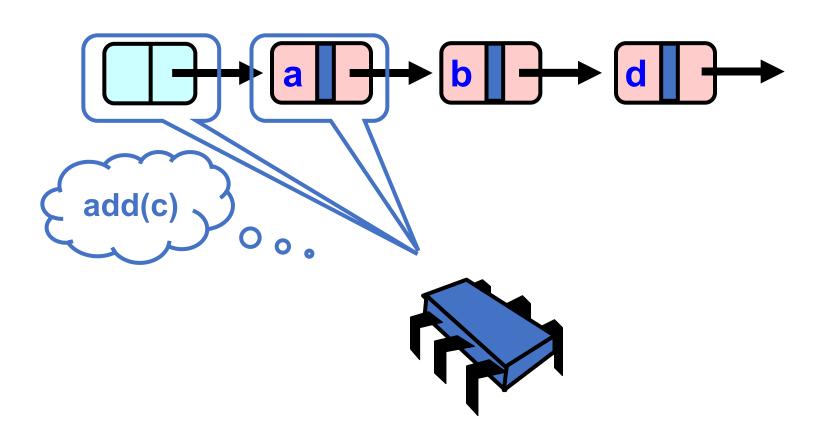


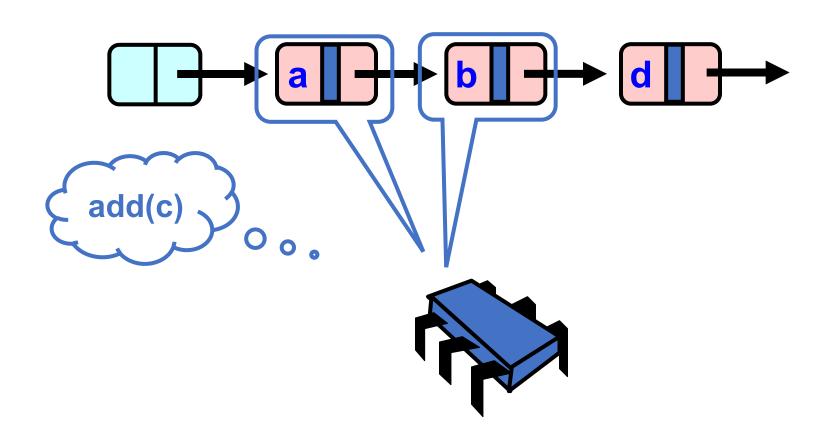


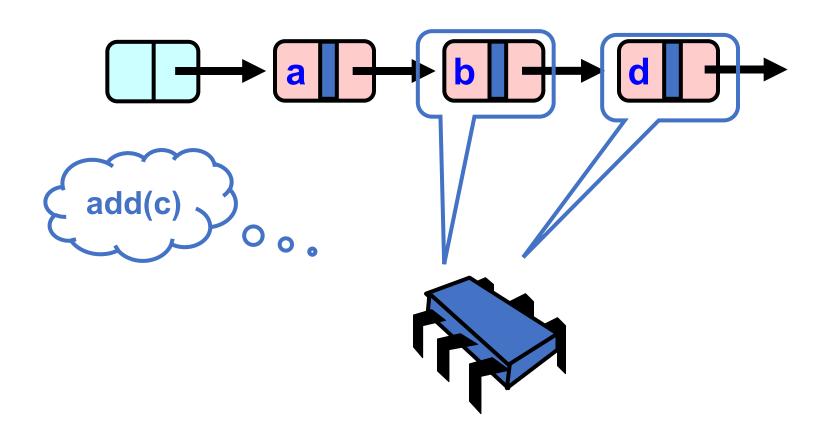


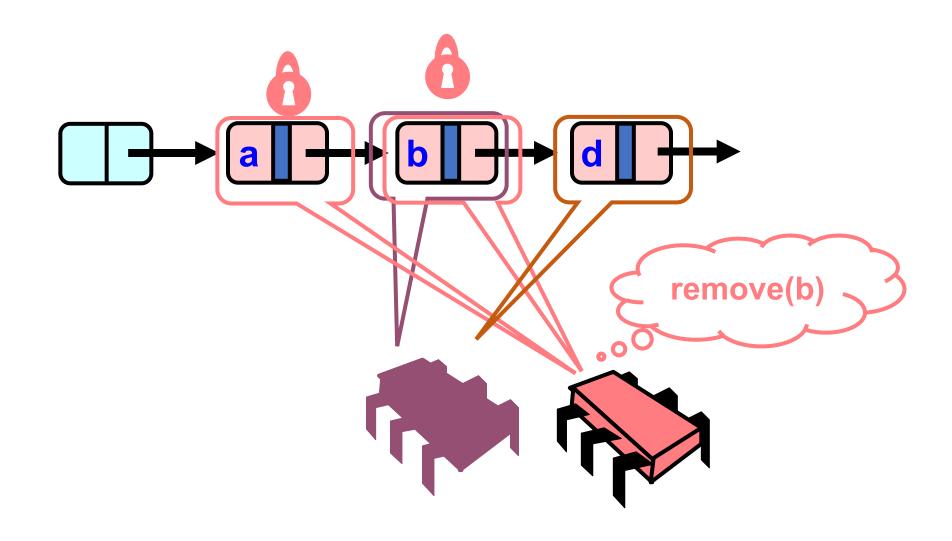


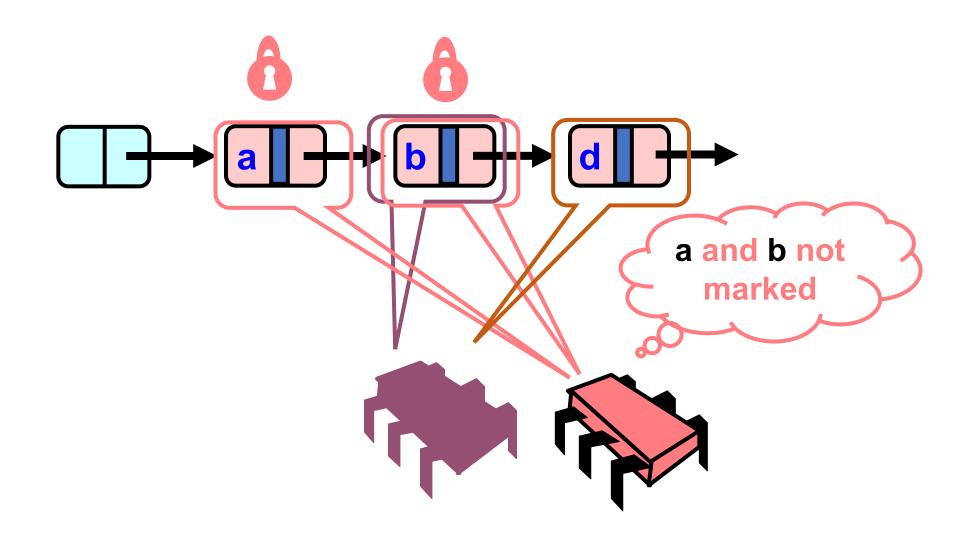


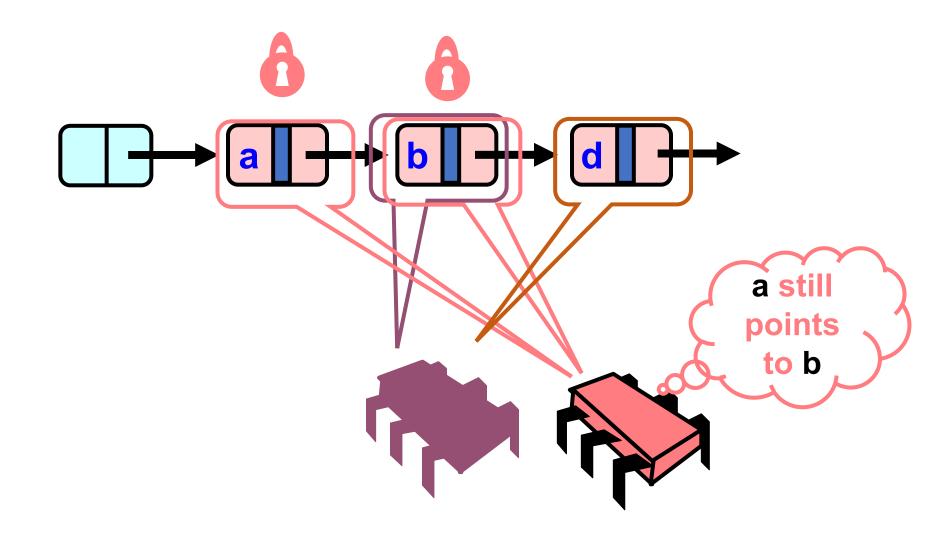


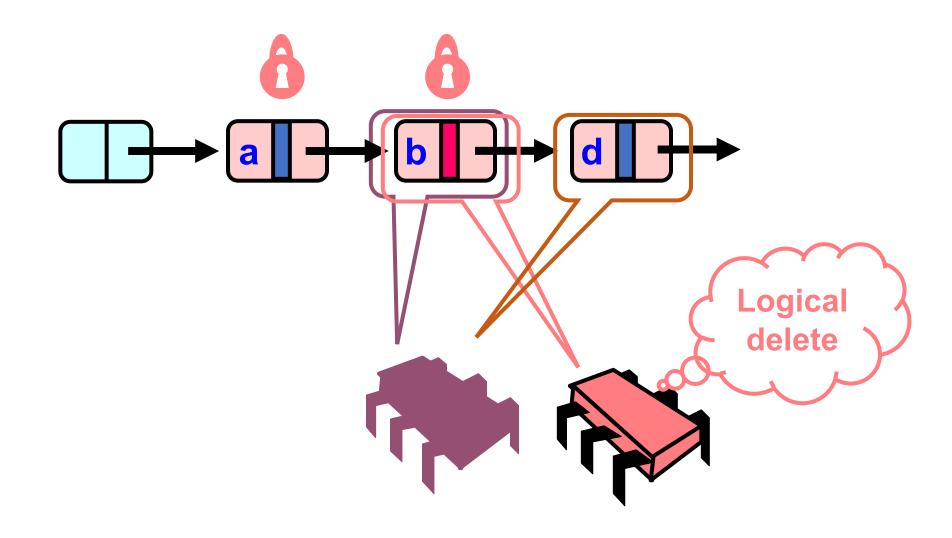


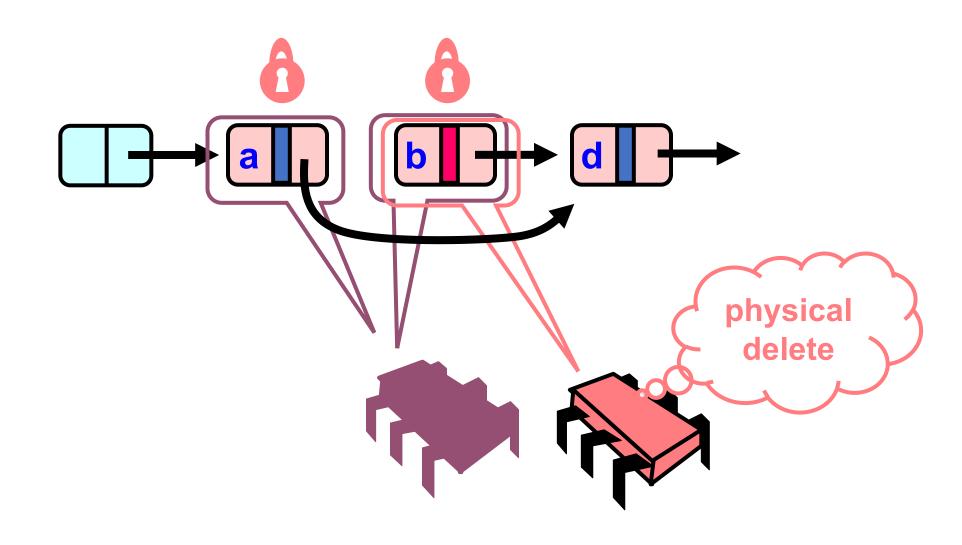


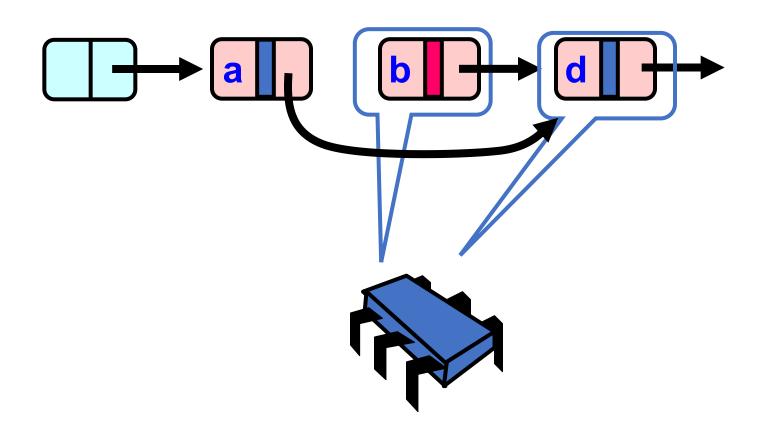


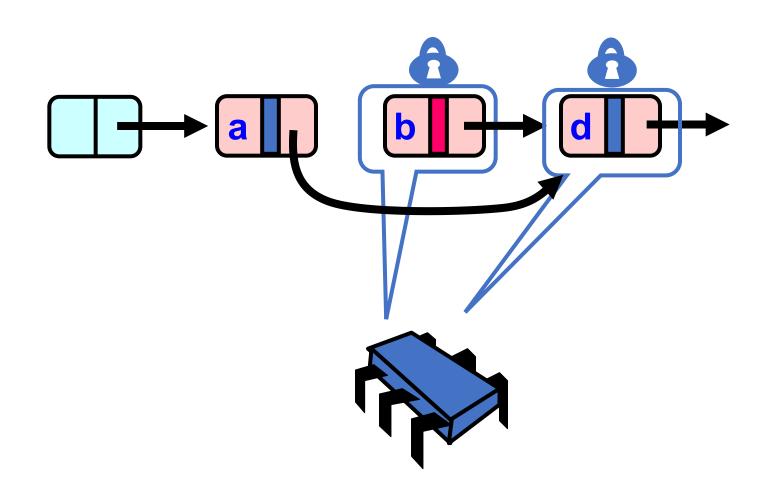


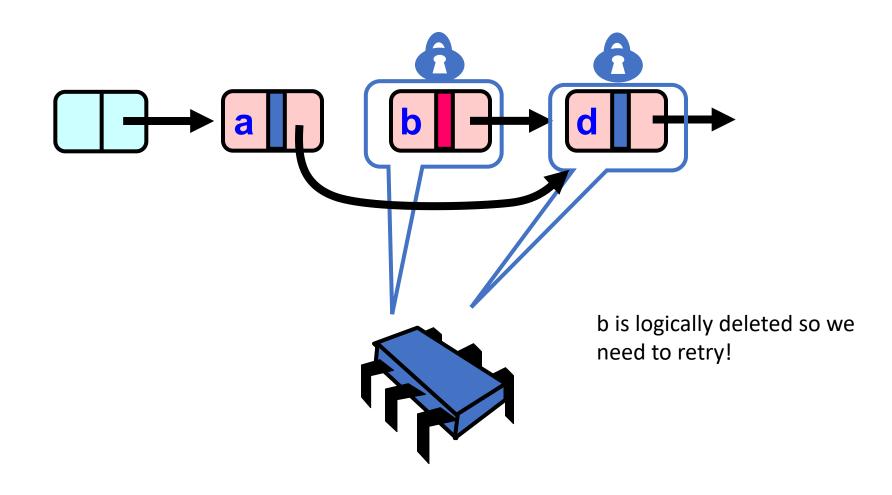












#### To complete the picture

- Need to do similar reasoning with all combination of object methods.
- More information in the book!

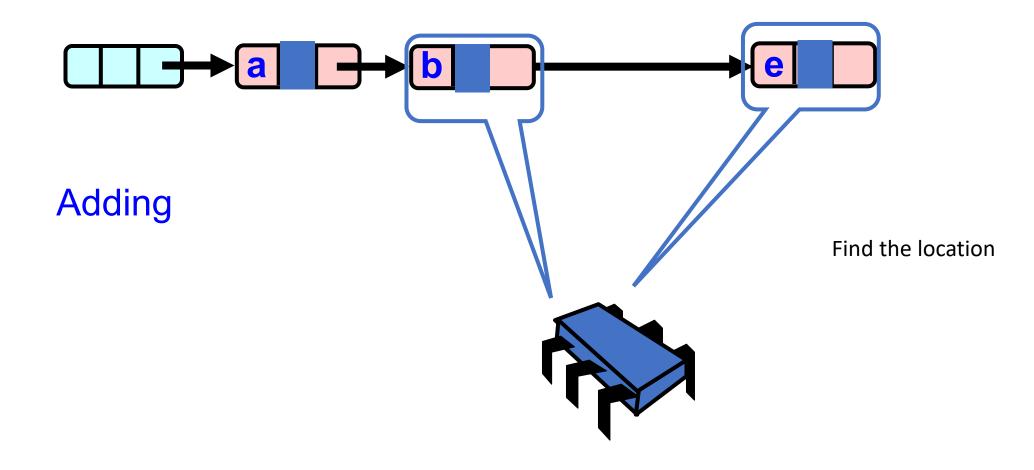
### How good?

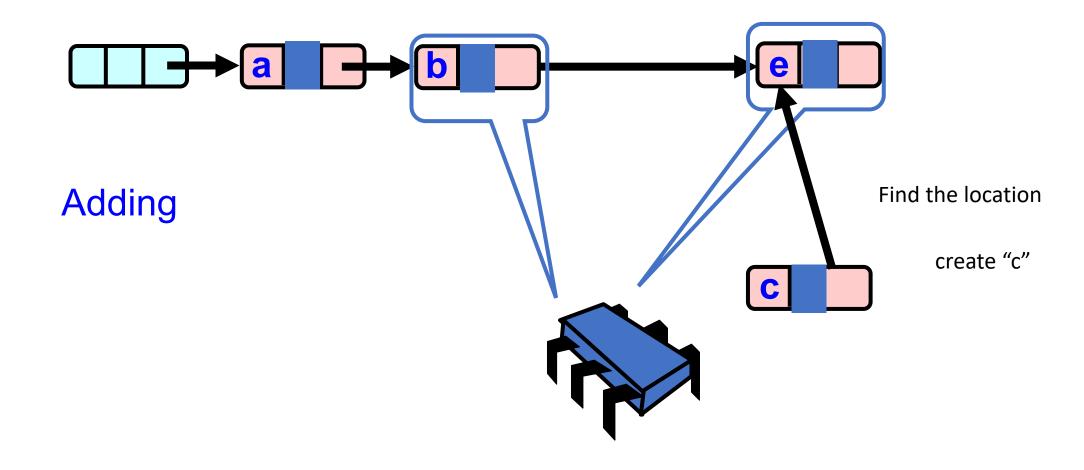
- Good:
  - Uncontended calls don't re-traverse
- Bad
  - add() and remove() use locks

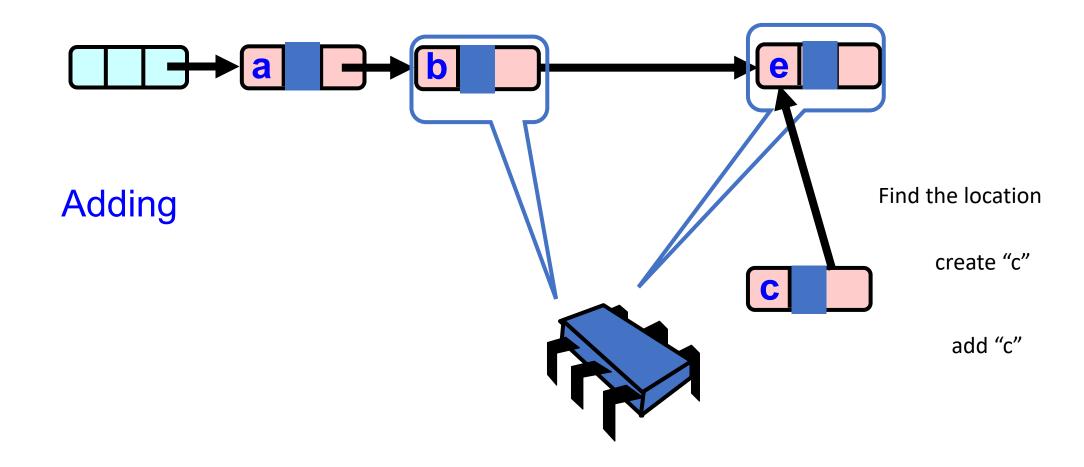
- Next logical step
  - lock-free add() and remove()
- What sort of atomics do we need?
  - Loads/stores -> RMWs?

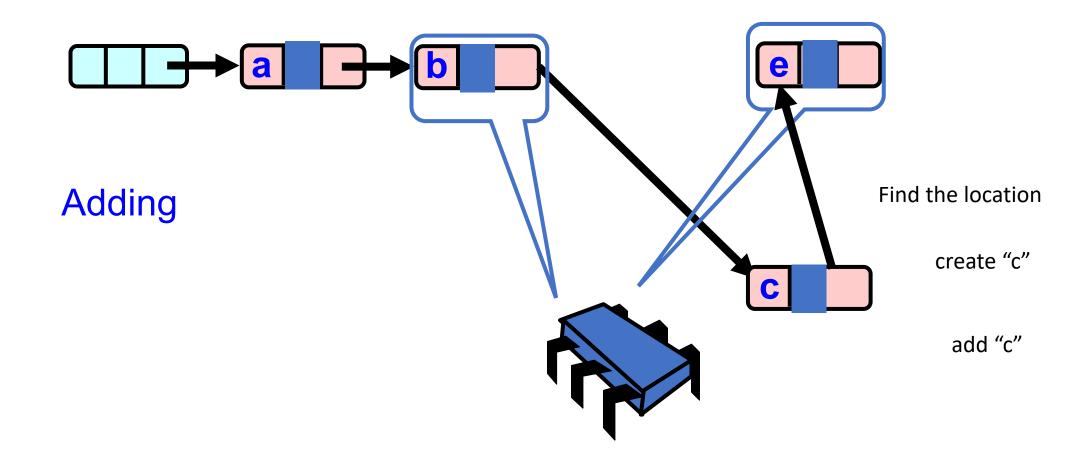


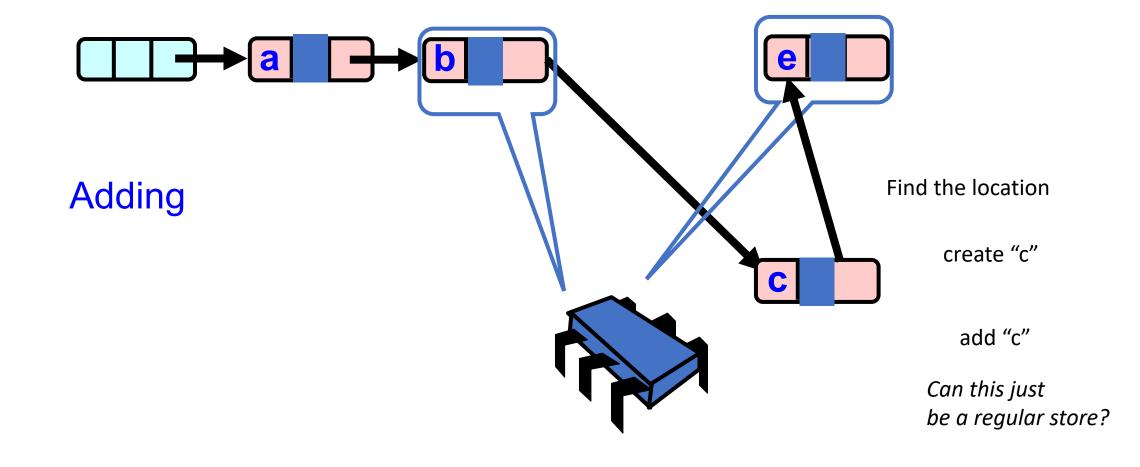
**Adding** 

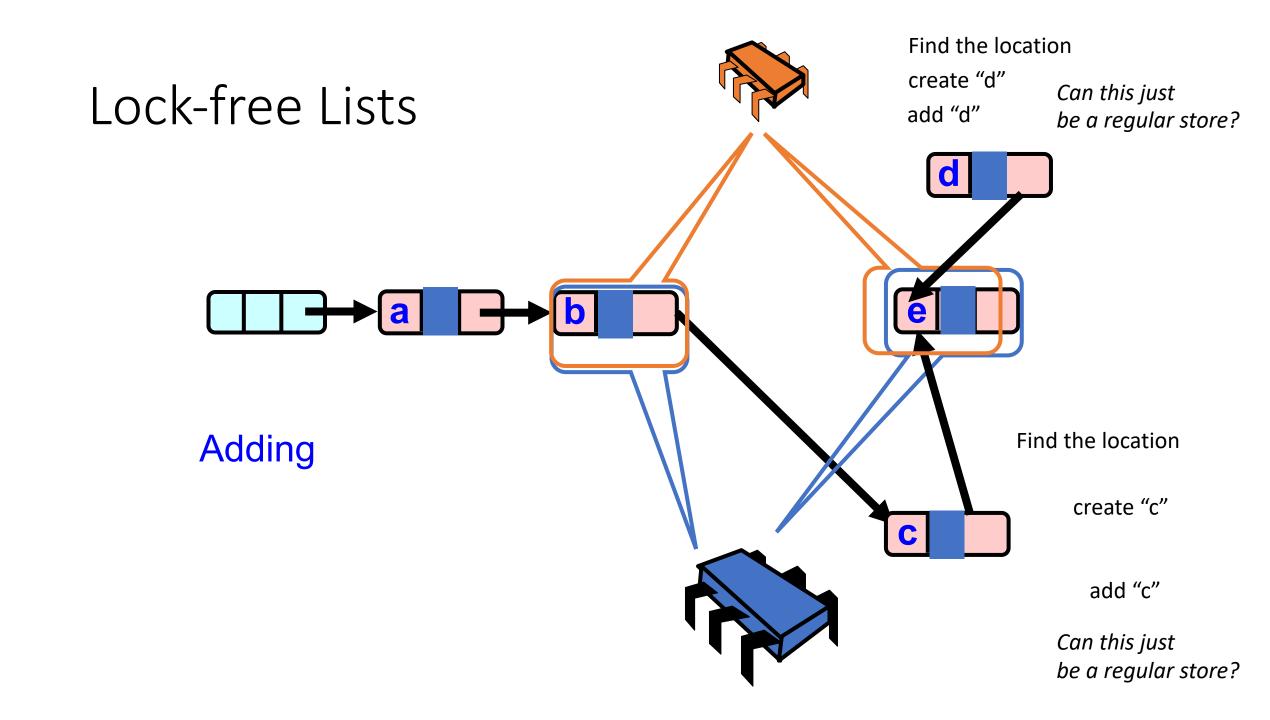


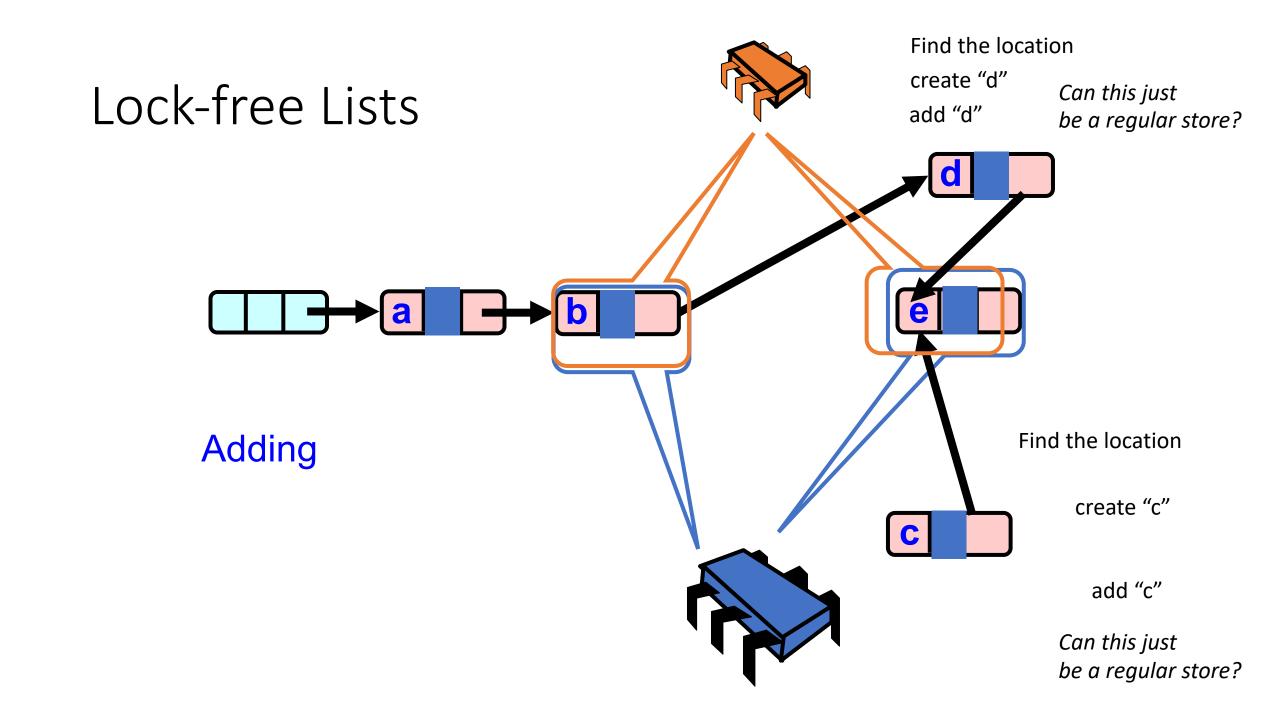


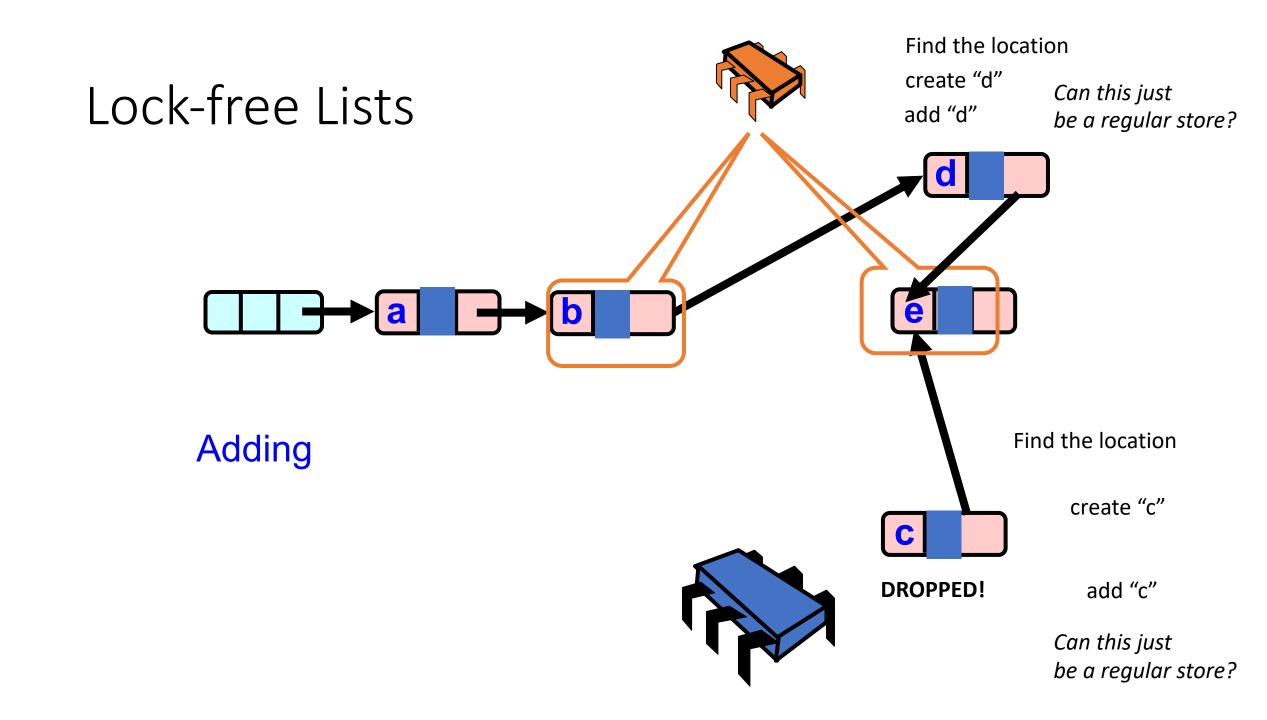


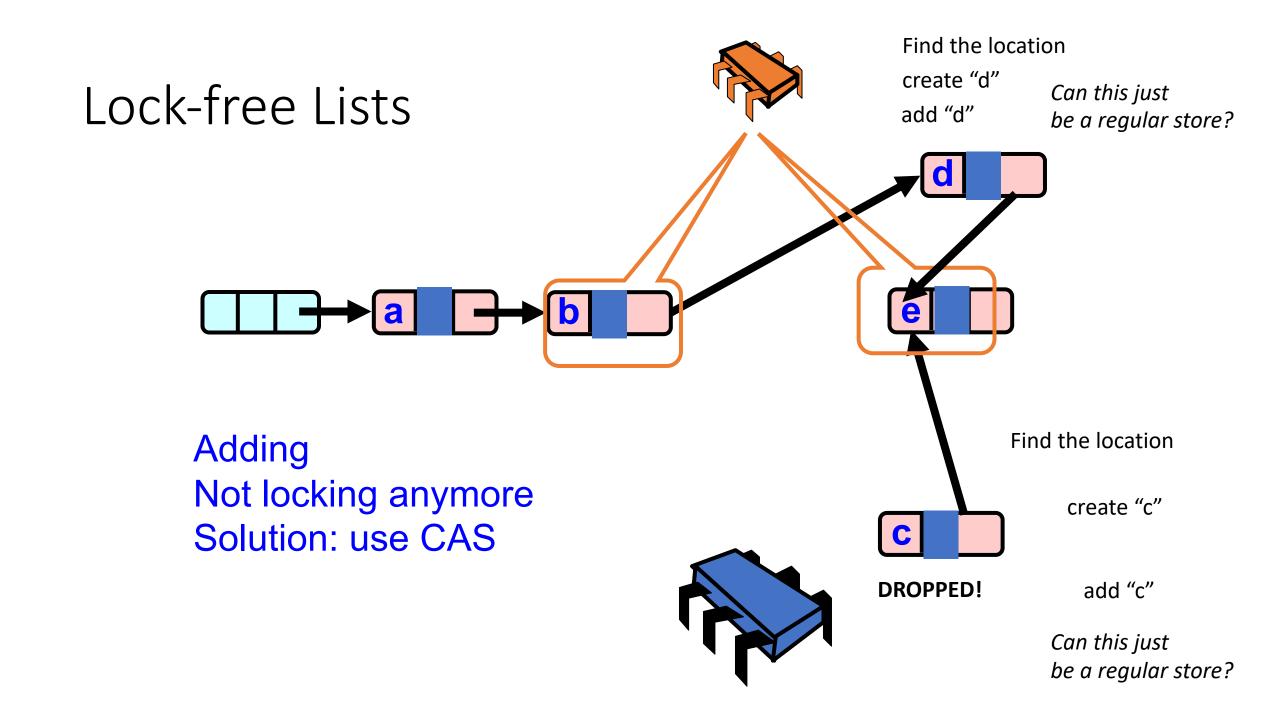






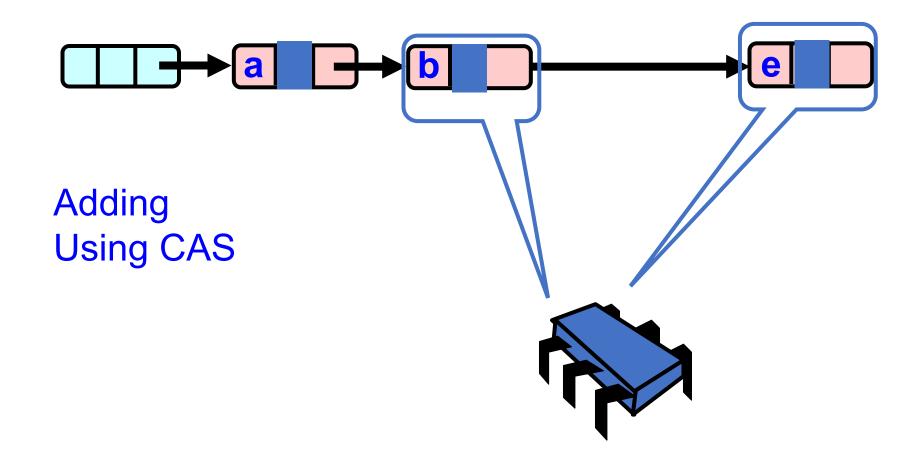






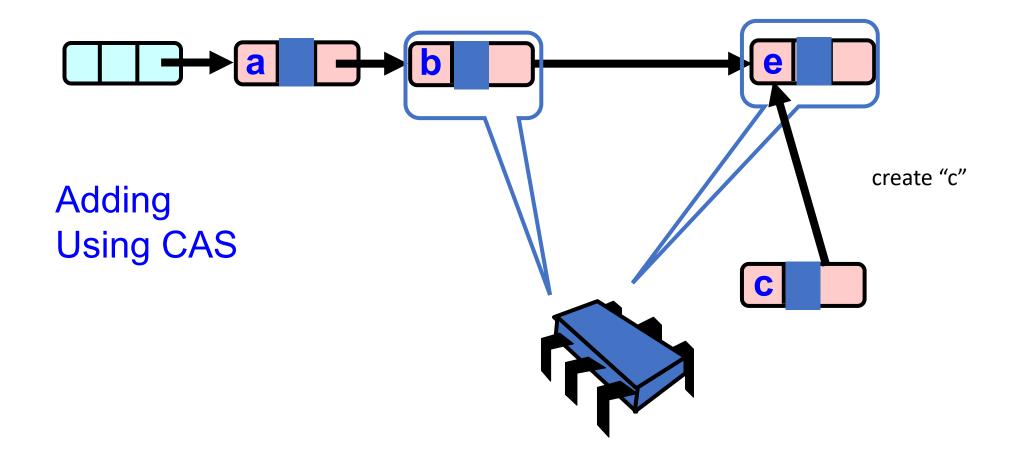
Find the location
Cache your insertion
point!

b.next == e



Find the location
Cache your insertion
point!

b.next == e

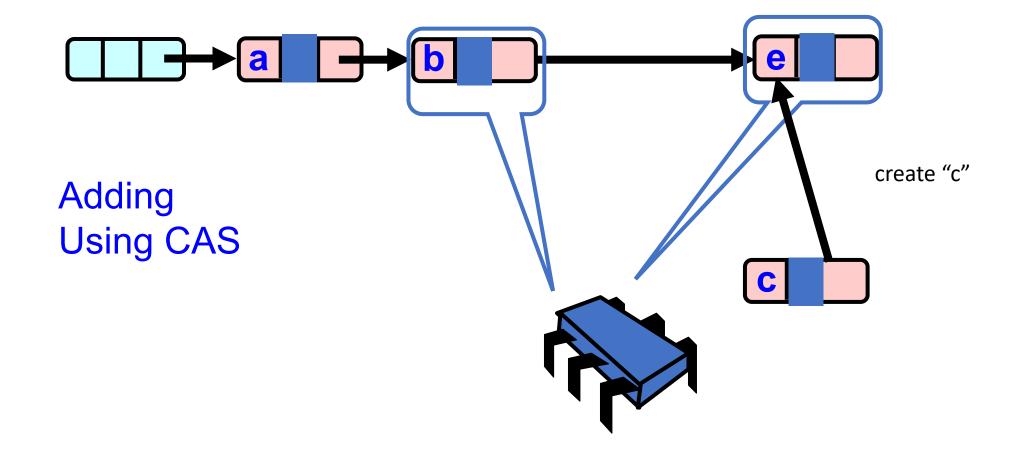


Only add if your insertion point is valid!

CAS(b.next, e, c);

Find the location Cache your insertion point!

b.next == e

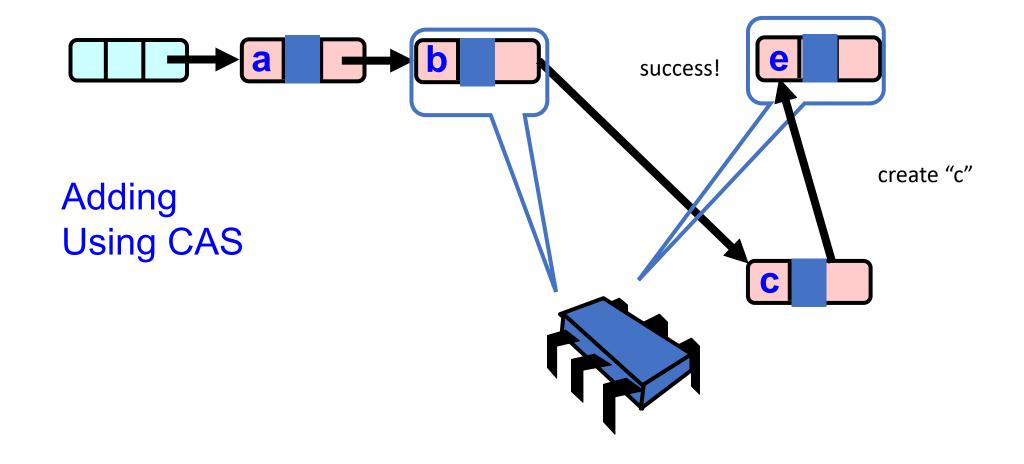


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CAS(b.next, e, c);

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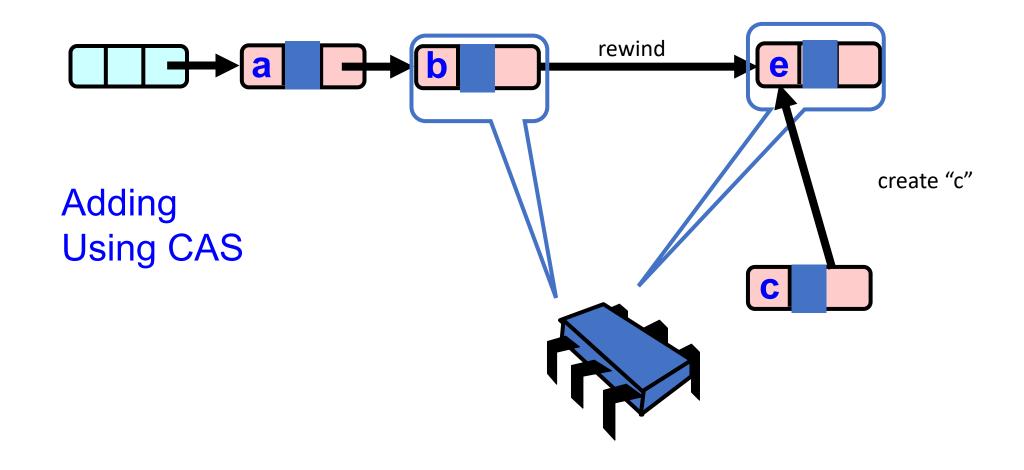


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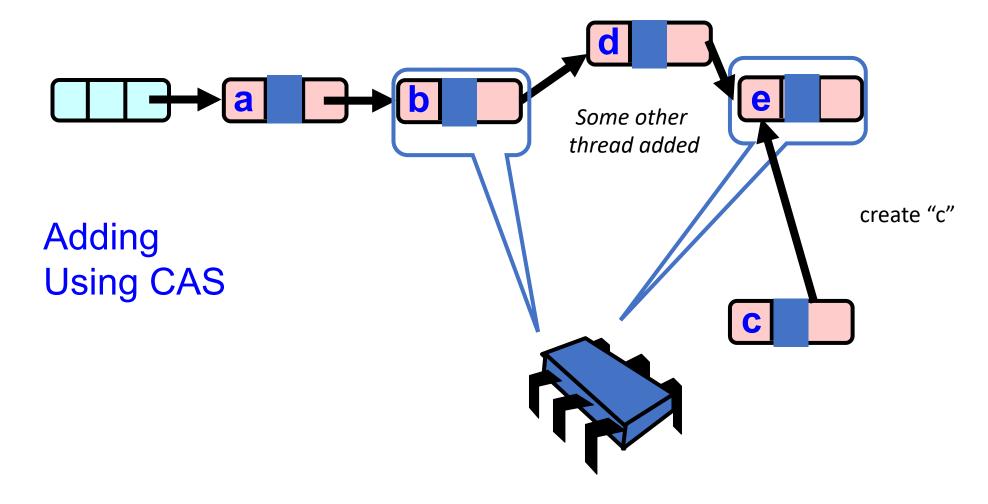


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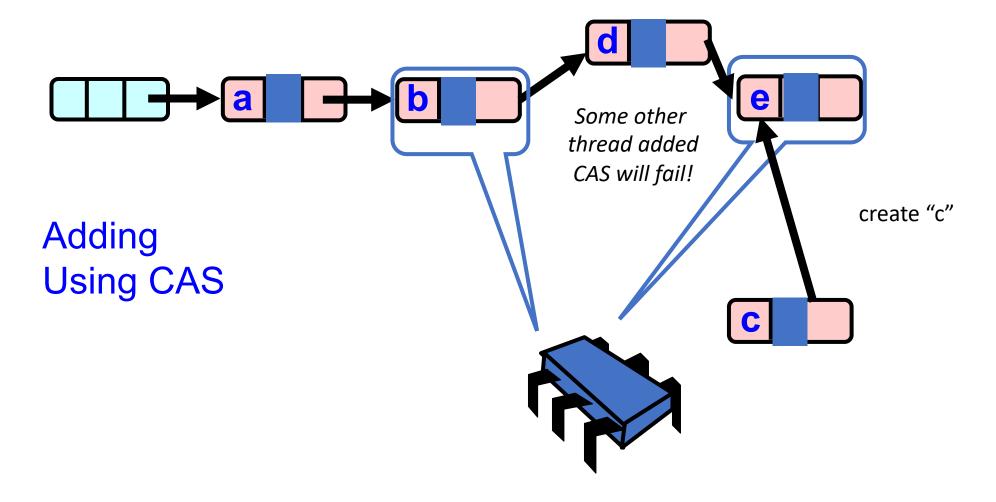


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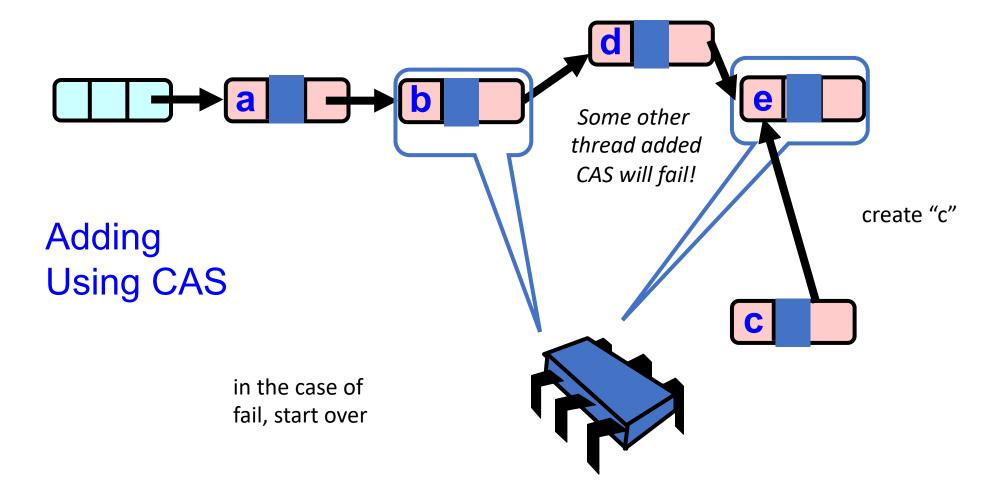


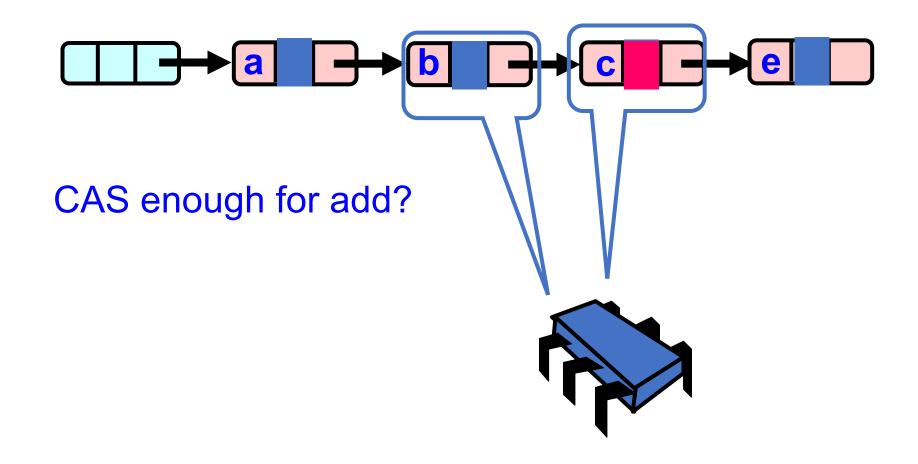
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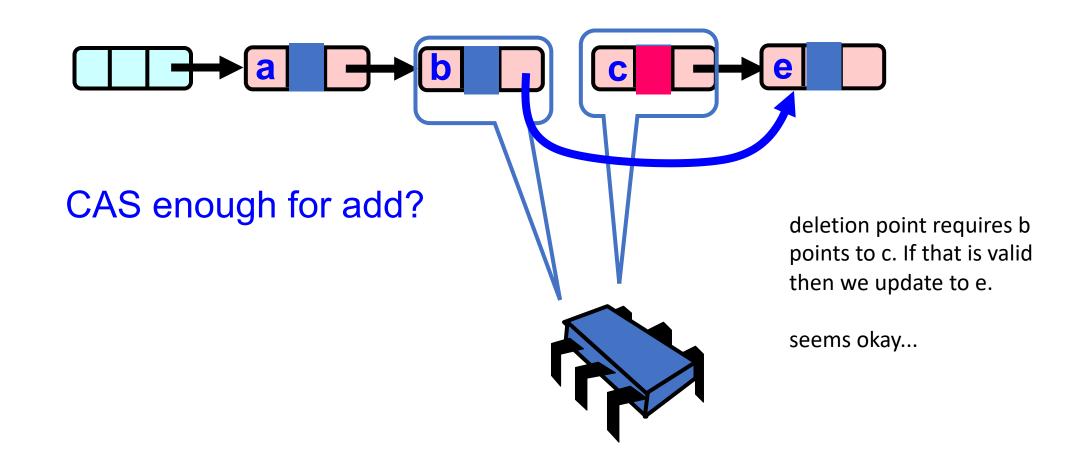
CAS(b.next, e, c);

Find the location Cache your insertion point!

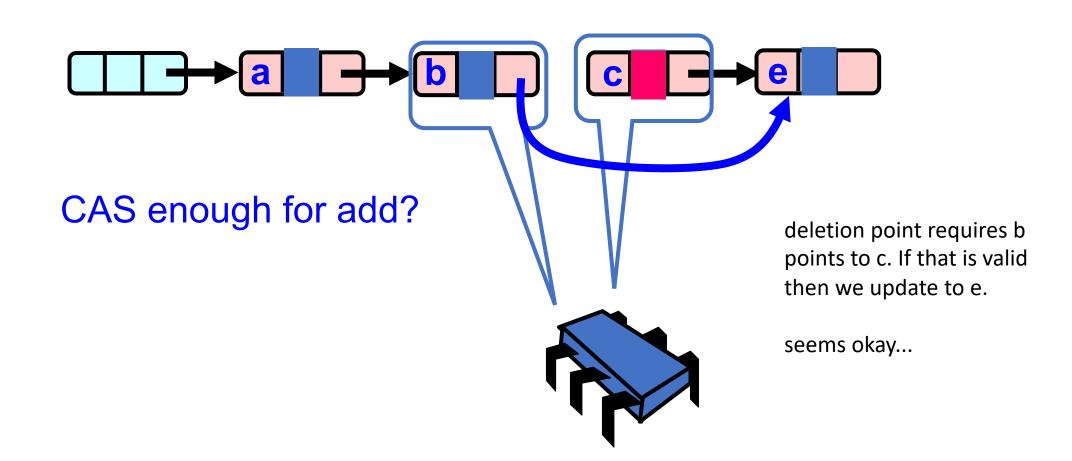
b.next == e



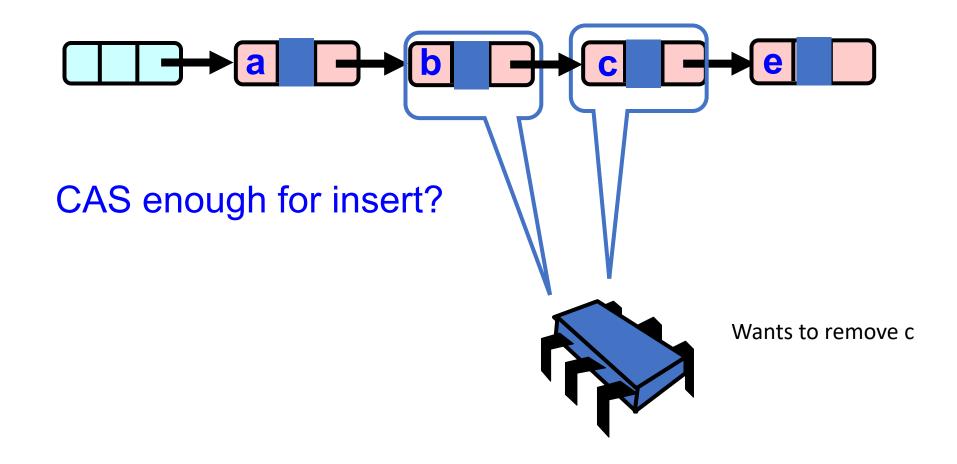


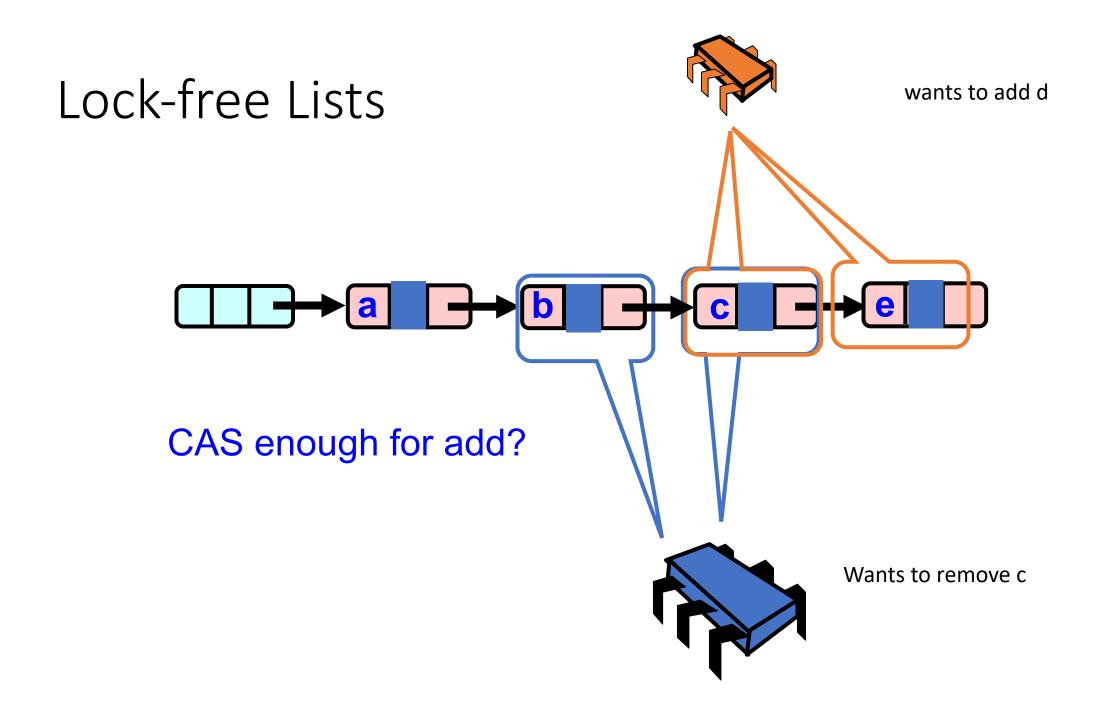


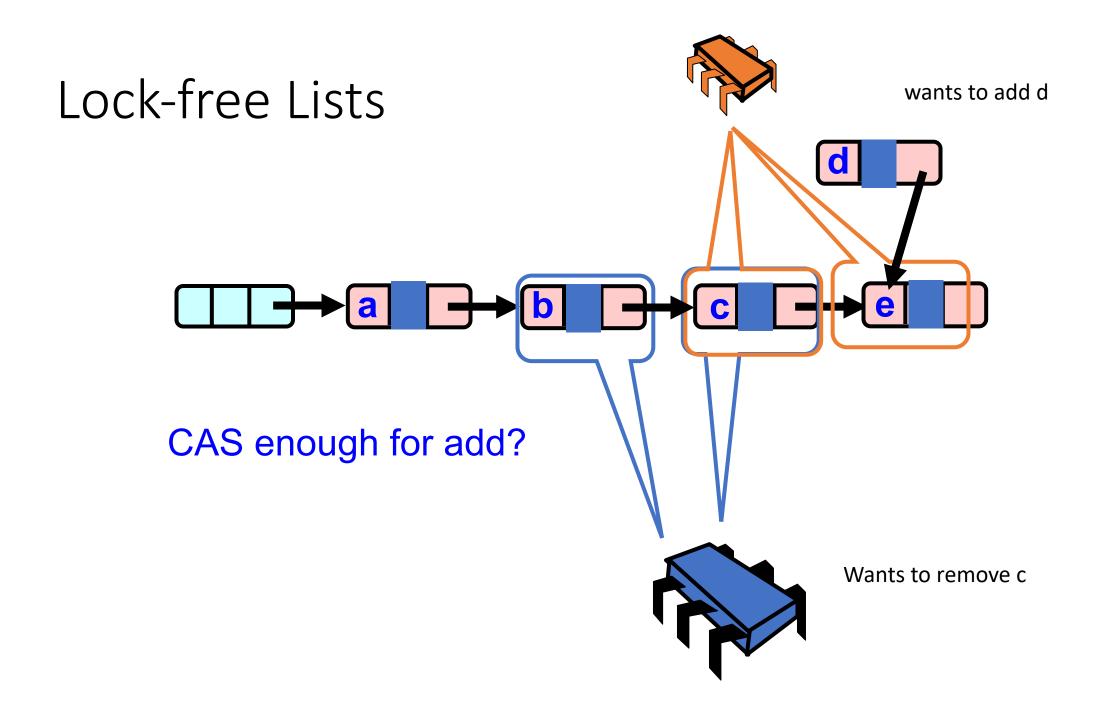
ensures that nobody has added a node between b and c

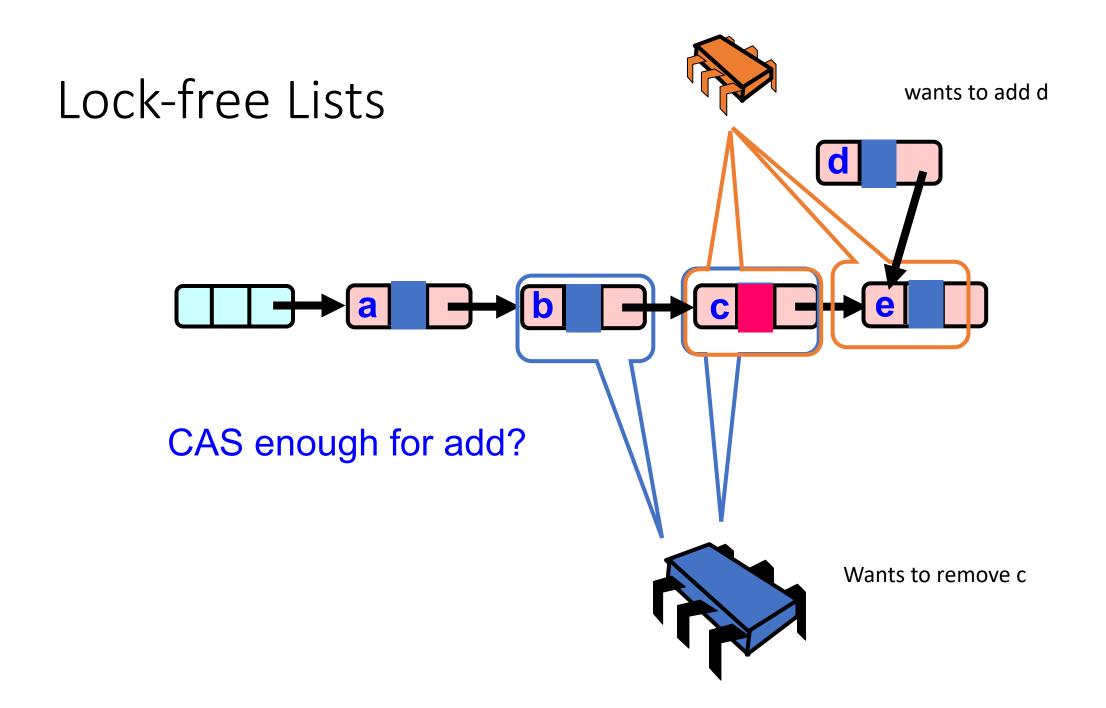


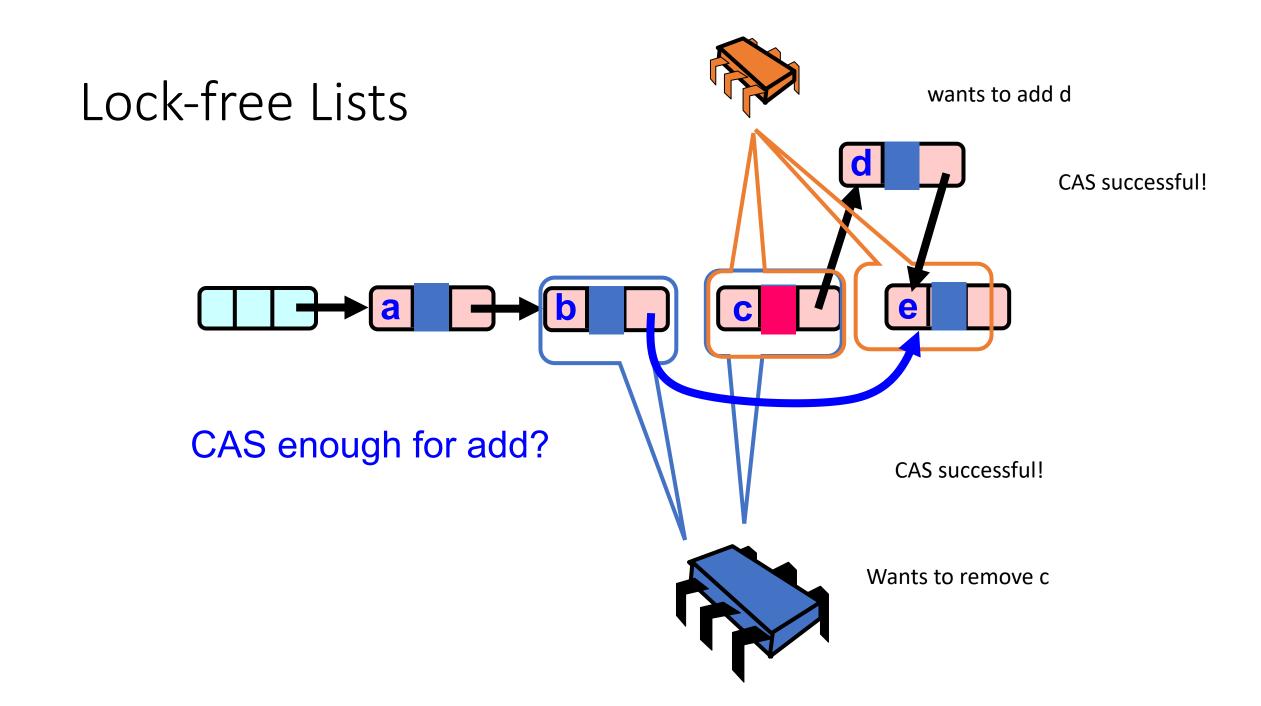
Rewind

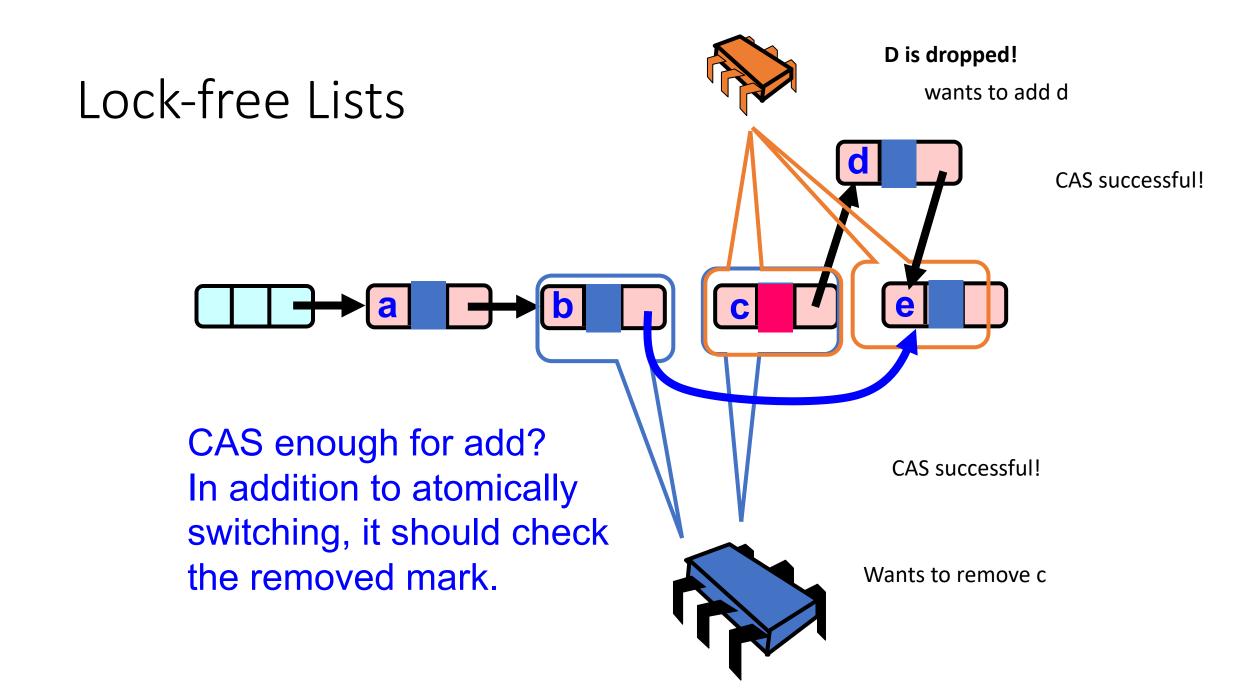






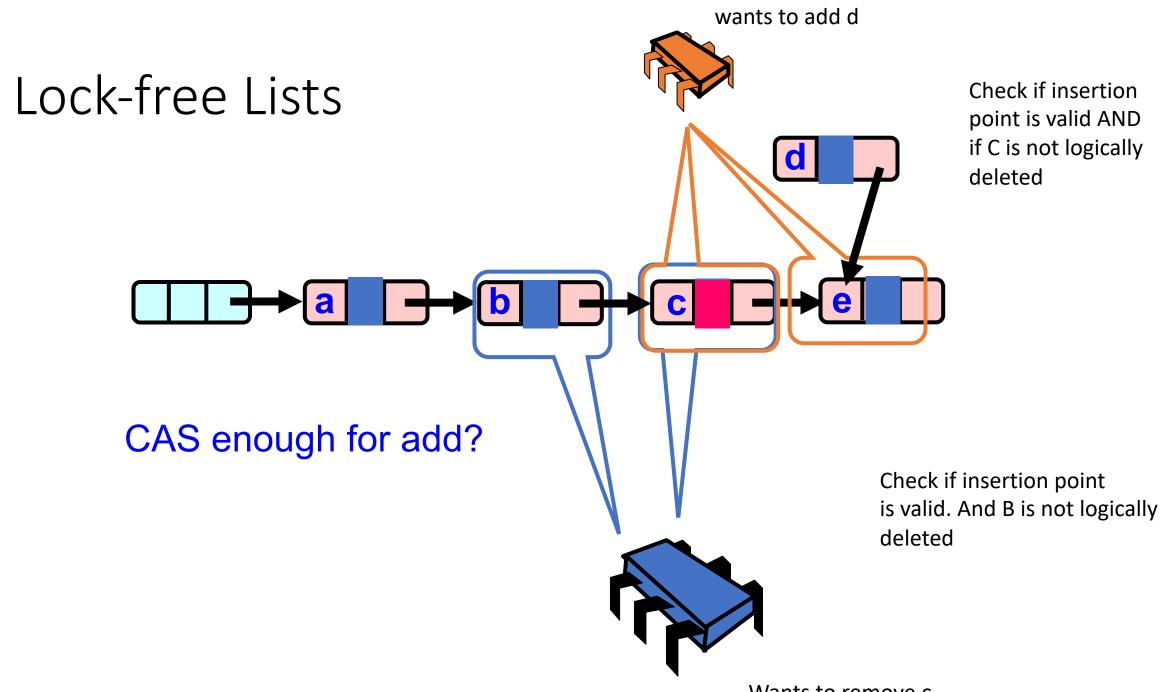






### Solution

- Use AtomicMarkableReference
- Atomic CAS that checks not only the address, but also a bit.
- We can say: update pointer if the insertion point is valid AND the node has not been logically removed.



Wants to remove c

# Marking a Node

- AtomicMarkableReference class
  - Java.util.concurrent.atomic package
  - But we're using a better<sup>™</sup> language (C++)

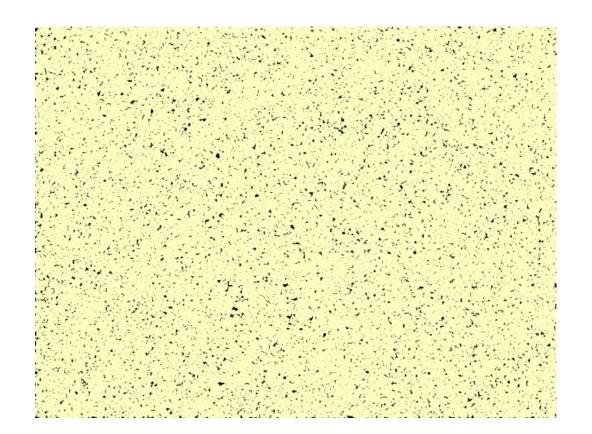


# This stuff is tricky

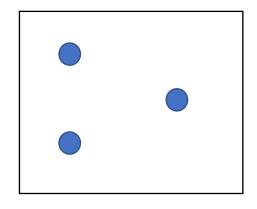
- Focus on understanding the concepts:
  - Locks are easiest, but can impede performance
  - Fine-grained locks are better, but more difficult
  - Optimistic concurrency can take you far. CAS is your friend
- When reasoning about correctness:
  - You have to consider all combination of adds/removes.
  - Thread sanitizer will help, but not as much as in mutexes. Other research tools can help.

- A barrier is a concurrent object (like a mutex):
  - Only one method: barrier (called await in the book)
- Separates computational phases

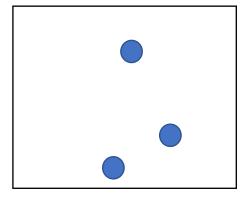
#### Particle simulation



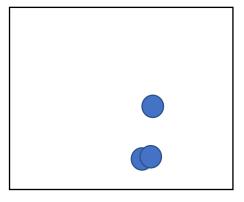
#### Particle simulation





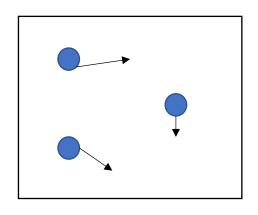


time = 1

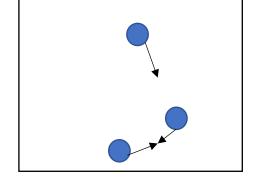


time = 2

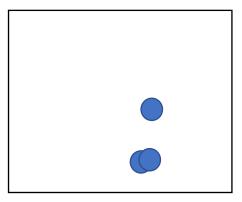
#### Particle simulation







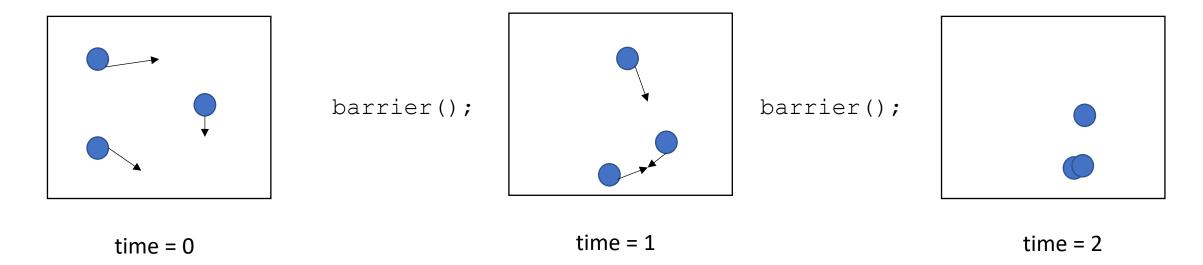
time = 1



time = 2

At each time, compute new positions for each particle (in parallel)

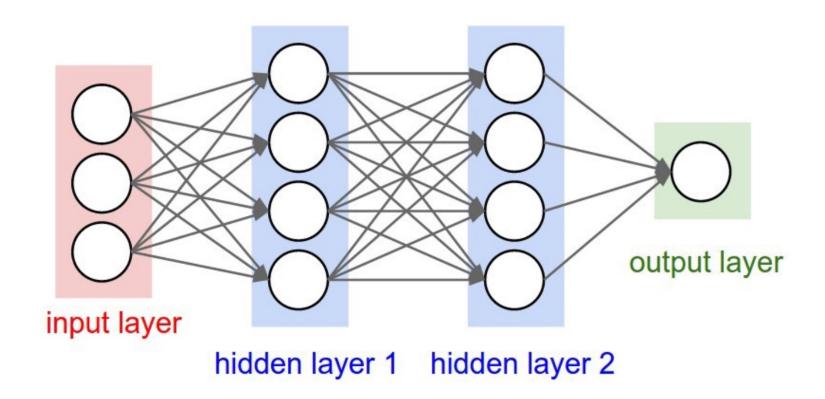
#### Particle simulation



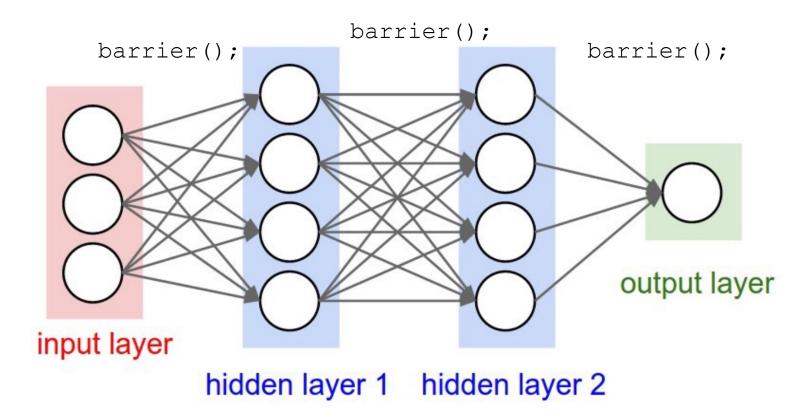
At each time, compute new positions for each particle (in parallel)

But you need to wait for all particles to be computed before starting the next time step

Deep neural networks



Deep neural networks

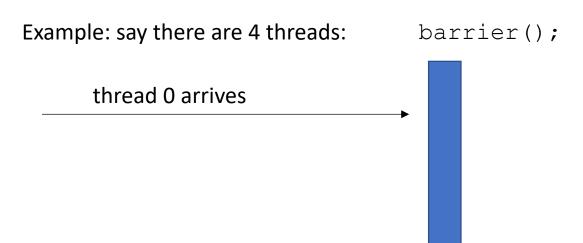


- Intuition: threads stop and wait for each other:
  - Threads *arrive* at the barrier
  - Threads wait at the barrier
  - Threads *leave* the barrier once all other threads have arrived

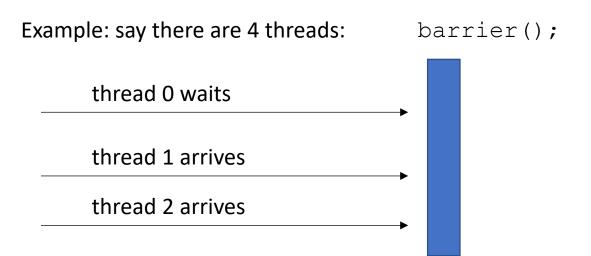
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Example: say there are 4 threads: barrier();

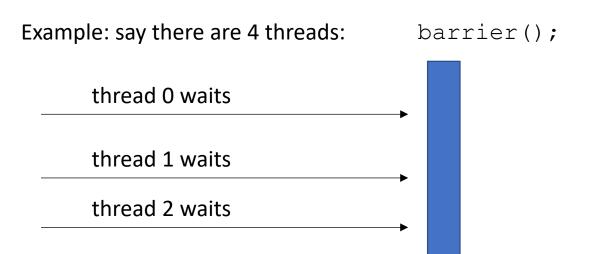
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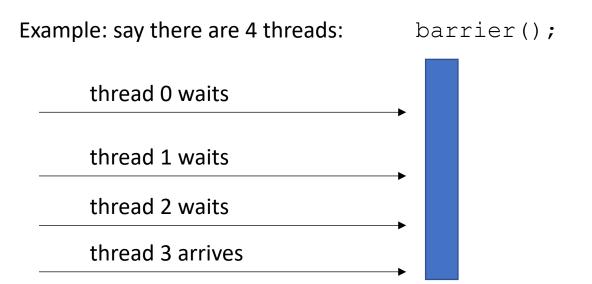
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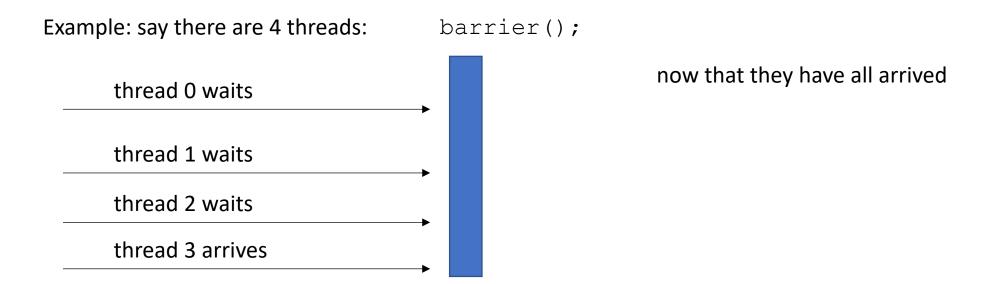
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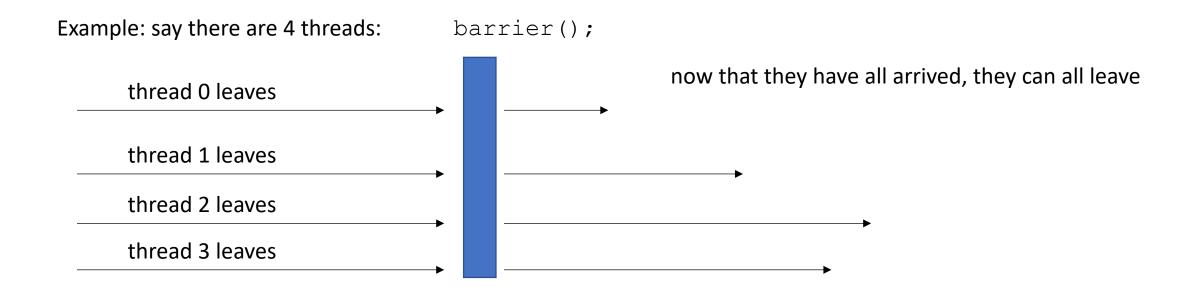
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```
A more formal specification
```

Given a global barrier  $\mathbb{B}$  and a global memory location x where initially \*x = 0;

First, what would we expect var to be after this program?

```
Thread 1:
B.barrier();
var = *x;
```

```
thread 0
```

Thread 0:

\*x = 1;

B.barrier();

```
thread 1 ----
```

```
A more formal specification
```

Given a global barrier  $\mathbb{B}$  and a global memory location x where initially \*x = 0;

```
Thread 1:
B.barrier();
var = *x:
```

gives an event: barrier arrive

```
thread 0 —
```

```
thread 1 barrier arrive
```

Thread 0:

```
*x = 1;
B.barrier();
```

#### A more formal specification

Given a global barrier  $\mathbb{B}$  and a global memory location x where initially \*x = 0;

```
<u>Thread 0:</u>
*x = 1;
B.barrier();
```

Thread 1:
B.barrier();
var = \*x;

gives an event: barrier arrive

barrier arrive needs to wait for all threads to arrive (similar to how a mutex request must wait for another to release)

thread 0

thread 1 — barrier arrive

```
A more formal specification
```

Given a global barrier  $\mathbb{B}$  and a global memory location x where initially \*x = 0;

```
Thread 0:
*x = 1;
B.barrier();
```

```
thread 0 *x = 1
```

thread 1 barrier arrive

A more formal specification

Given a global barrier  $\mathbb{B}$  and a global memory location x where initially \*x = 0;

```
Thread 0:
*x = 1;
B.barrier();
```

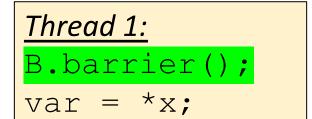


thread 1 barrier arrive

```
Thread 0:
    *x = 1;
    B.barrier();
```

#### A more formal specification

Given a global barrier  $\mathbb{B}$  and a global memory location x where initially \*x = 0;



now that all threads have arrived: They can leave (1 event at the same time)



```
A more formal specification
```

\*x = 1;

B.barrier();

Given a global barrier  $\mathbb{B}$  and a global memory location x where initially \*x = 0;

```
Thread 1:
B.barrier();
var = *x;
```

This finishes the barrier execution

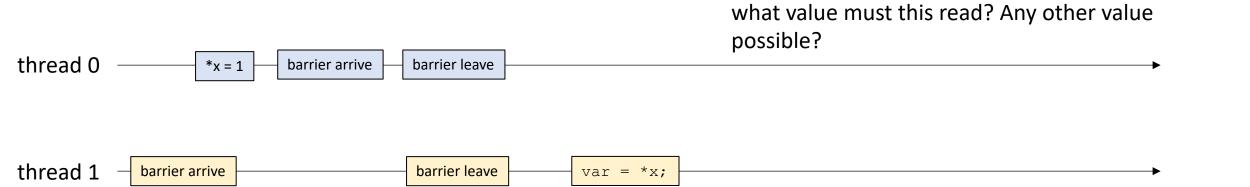
```
thread 0 *x = 1 barrier arrive barrier leave thread 1 barrier arrive barrier leave
```

```
A more formal specification
```

Given a global barrier  $\mathbb{B}$  and a global memory location x where initially \*x = 0;

```
Thread 0:
*x = 1;
B.barrier();
```

```
Thread 1:
B.barrier();
var = *x;
```



## Thread 0: \*x = 1; B.barrier();

```
<u>Thread 1:</u>
*y = 2;
B.barrier();
```

```
Thread 2:
B.barrier();
var = *x + *y;
```

```
thread 0

thread 1
```

# Thread 0: \*x = 1; B.barrier();

barrier arrive

thread 2

```
<u>Thread 1:</u>
*y = 2;
B.barrier();
```

```
Thread 2:
B.barrier();
var = *x + *y;
```

thread 0
thread 1

```
<u>Thread 0:</u>
*x = 1;
B.barrier();
```

barrier arrive

```
Thread 1:

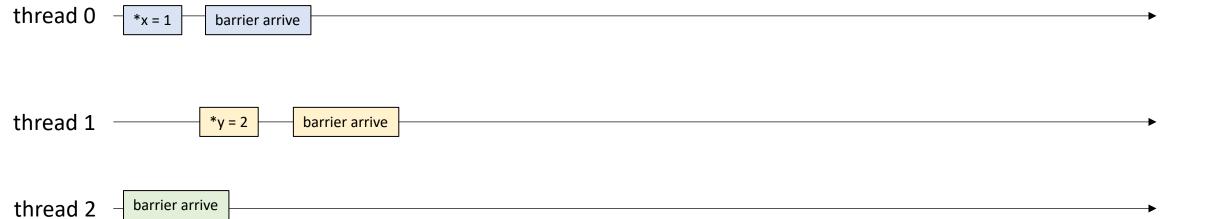
*y = 2;

B.barrier();
```

```
Thread 2:
B.barrier();
var = *x + *y;
```

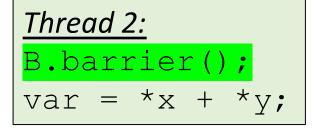
```
thread 0 *x = 1 
thread 1 *y = 2
```

# Thread 0: \*x = 1; B.barrier();

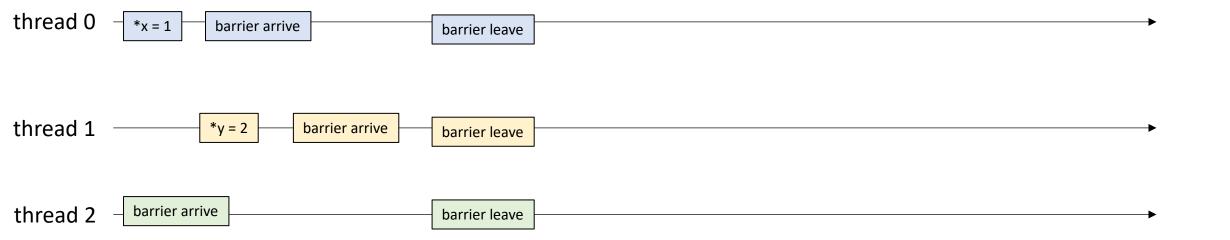


# Thread 0: \*x = 1; B.barrier();

```
Thread 1:
*y = 2;
B.barrier();
```

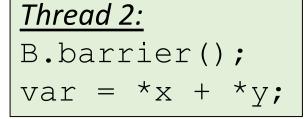


They've all arrived

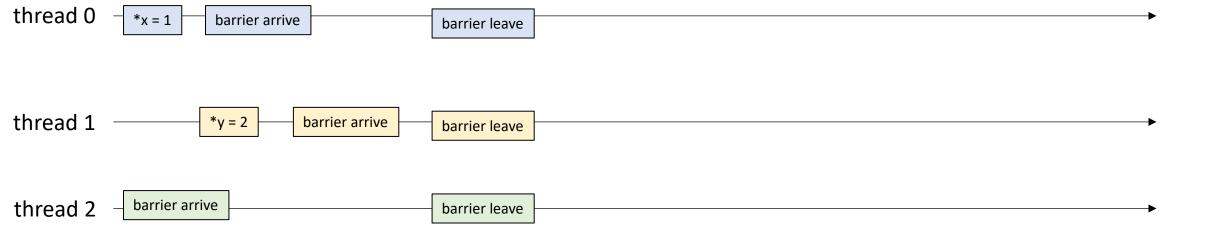


# Thread 0: \*x = 1; B.barrier();

```
<u>Thread 1:</u>
*y = 2;
B.barrier();
```



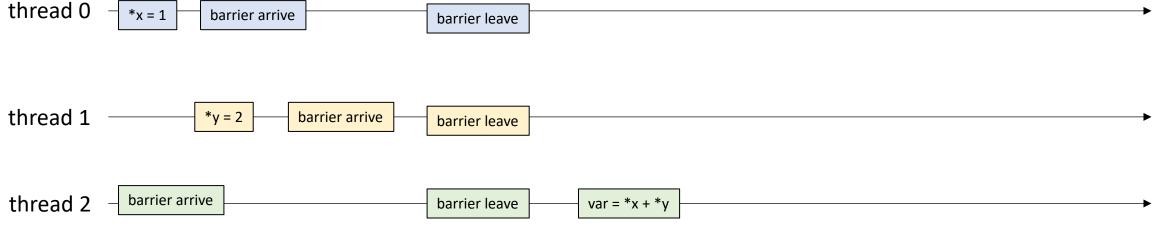
They've all arrived



# Thread 0: \*x = 1; B.barrier();

```
<u>Thread 1:</u>
*y = 2;
B.barrier();
```

```
<u>Thread 2:</u>
B.barrier();
var = *x + *y;
```

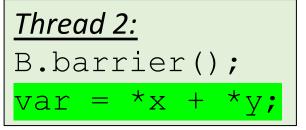


What is this guaranteed to be?

```
<u>Thread 0:</u>
*x = 1;
B.barrier();
```

thread 1

```
<u>Thread 1:</u>
*y = 2;
B.barrier();
```



Barrier Interval 1

sometimes called a phase

Barrier Interval 0

barrier arrive

\*y = 2

extending to the next barrier leave

thread 0 \*x = 1 barrier arrive barrier leave

thread 2 barrier arrive barrier leave var = \*x + \*y

barrier leave

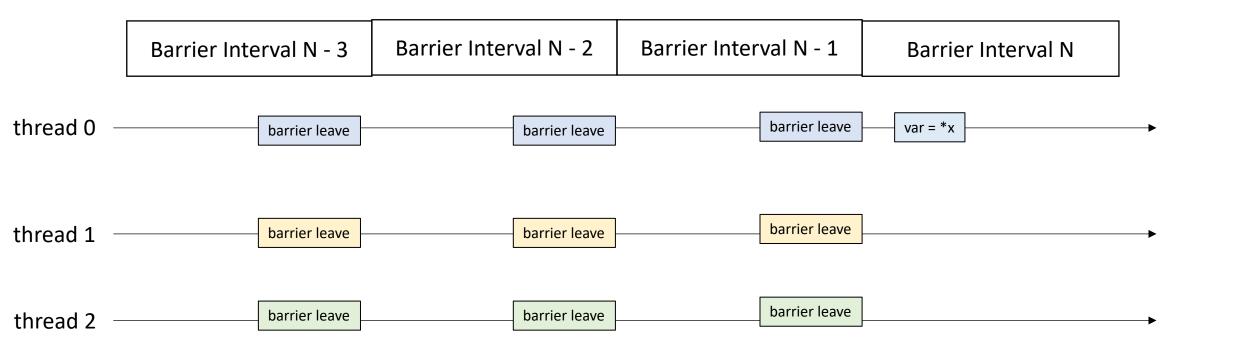
- Barrier Property:
  - If the only concurrent object you use in your program is a barrier (no mutexes, concurrent data-structures, atomic accesses)
  - If every barrier interval contains no data conflicts, then

your program will be deterministic (only 1 outcome allowed)

• much easier to reason about ©

Assume we are reading from x

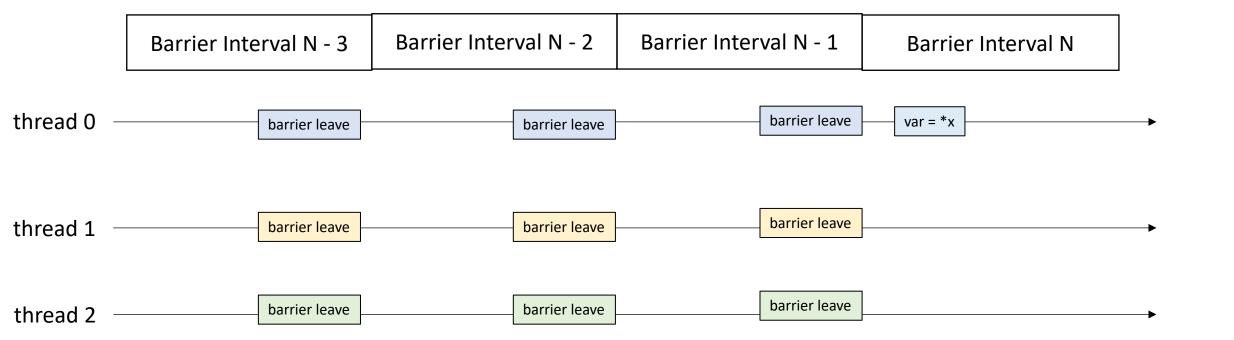
We are only allowed to return one possible value



no data conflicts means that x is written to at most once per barrier interval

Assume we are reading from x

We are only allowed to return one possible value



Assume we are reading no data conflicts means that x is written to at most once from x per barrier interval We are only allowed to return one possible not allowed value Barrier Interval N - 2 Barrier Interval N - 1 Barrier Interval N - 3 Barrier Interval N thread 0 barrier leave barrier leave var = \*x\*x = 2barrier leave barrier leave thread 1 barrier leave barrier leave \*x = 1 barrier leave barrier leave barrier leave thread 2

Assume we are reading no data conflicts means that x is written to at most once from x per barrier interval We are only allowed to we will read from the write return one possible from the most recent barrier interval value Barrier Interval N - 2 Barrier Interval N - 3 Barrier Interval N - 1 Barrier Interval N thread 0 barrier leave \*x = 2barrier leave var = \*xbarrier leave barrier leave \*x = 1thread 1 barrier leave barrier leave barrier leave barrier leave barrier leave thread 2

## Schedule

- Barriers
  - Specification
  - Implementation

First attempt at implementation

```
class Barrier {
 private:
    atomic int counter;
    int num threads;
 public:
    Barrier(int num threads) {
      counter = 0;
      this->num_threads = num_threads;
     void barrier() {
        // ??
```

```
class Barrier {
 private:
    atomic int counter;
    int num threads;
 public:
    Barrier(int num_threads) {
      counter = 0;
      this->num threads = num threads;
     void barrier() {
        int arrival_num = atomic_fetch_add(&counter, 1);
        // What next?
```

First handle the case where the thread is the last thread to arrive

```
class Barrier {
  private:
    atomic int counter;
    int num threads;
  public:
    Barrier(int num threads) {
      counter = 0;
      this->num threads = num threads;
     void barrier() {
        int arrival num = atomic fetch add(&counter, 1);
        if (arrival_num == num_threads - 1) {
           counter.store(0);
        // What next?
```

Spin while there is a thread waiting at the barrier

```
class Barrier {
  private:
    atomic int counter;
    int num threads;
  public:
    Barrier(int num threads) {
      counter = 0;
      this->num threads = num threads;
     void barrier() {
        int arrival num = atomic fetch add(&counter, 1);
        if (arrival_num == num_threads - 1) {
           counter.store(0);
        else {
          while (counter.load() != 0);
```

Spin while there is a thread waiting at the barrier

Does this work?

```
class Barrier {
  private:
    atomic int counter;
    int num threads;
  public:
    Barrier(int num threads) {
      counter = 0;
      this->num threads = num threads;
     void barrier() {
        int arrival num = atomic fetch add(&counter, 1);
        if (arrival_num == num_threads - 1) {
           counter.store(0);
        else {
          while (counter.load() != 0);
```

```
B.barrier();
B.barrier();
```

```
void barrier() {
    int arrival_num = atomic_fetch_add(&counter, 1);
    if (arrival_num == num_threads) {
        counter.store(0);
    }
    else {
        while (counter.load() != 0);
    }
}
```

### Thread 1:

B.barrier();
B.barrier();

thread 0

```
num threads == 2
```

```
Thread 0:
```

B.barrier();

B.barrier();

```
void barrier() {
    int arrival_num = atomic_fetch_add(&counter, 1);
    if (arrival_num == num_threads - 1) {
        counter.store(0);
    }
    else {
        while (counter.load() != 0);
    }
}
```

### Thread 1:

B.barrier();

B.barrier();

arrival\_num = 1

arrival\_num = 0

thread 0

```
num_threads == 2
counter == 2
```

B.barrier();

B.barrier();

```
void barrier() {
    int arrival_num = atomic_fetch_add(&counter, 1);
    if (arrival_num == num_threads - 1) {
        counter.store(0);
    }
    else {
        while (counter.load() != 0);
    }
}
```

### Thread 1:

B.barrier();

B.barrier();

arrival\_num = 1

arrival\_num = 0

thread 0

```
num_threads == 2
counter == 0
```

B.barrier();

B.barrier();

```
void barrier() {
    int arrival_num = atomic_fetch_add(&counter, 1);
    if (arrival_num == num_threads - 1) {
        counter.store(0);
    }
    else {
        while (counter.load() != 0);
    }
}
```

#### Thread 1:

B.barrier();

B.barrier();

arrival\_num = 1

arrival\_num = 0

thread 0

```
num_threads == 2
counter == 0
```

B.barrier();
B.barrier();

```
void barrier() {
    int arrival_num = atomic_fetch_add(&counter, 1);
    if (arrival_num == num_threads - 1) {
        counter.store(0);
    }
    else {
        while (counter.load() != 0);
    }
}
```

### Thread 1:

B.barrier();

B.barrier();

Leaves barrier

arrival\_num = 0

in a perfect world, thread 1 executes now and leaves the barrier

thread 0

```
num_threads == 2
counter == 0
```

```
Thread 0:
```

```
B.barrier();
B.barrier();
```

```
void barrier() {
    int arrival_num = atomic_fetch_add(&counter, 1);
    if (arrival_num == num_threads - 1) {
        counter.store(0);
    }
    else {
        while (counter.load() != 0);
    }
}
```

#### Thread 1:

B.barrier();
B.barrier();

Leaves barrier

arrival\_num = 0

in a perfect world, thread 1 executes now and leaves the barrier

but what if the OS preempted thread 1? Or it was asleep?

```
num_threads == 2
counter == 0
```

```
Thread 0:
```

B.barrier();
B.barrier();

```
void barrier() {
    int arrival_num = atomic_fetch_add(&counter, 1);
    if (arrival_num == num_threads - 1) {
        counter.store(0);
    }
    else {
        while (counter.load() != 0);
    }
}
```

#### Thread 1:

B.barrier();
B.barrier();

enters next barrier

arrival num = 0

in a perfect world, thread 1 executes now and leaves the barrier

but what if the OS preempted thread 1? Or it was asleep?

```
num_threads == 2
counter == 1
```

```
Thread 0:
```

B.barrier();
B.barrier();

```
void barrier() {
    int arrival_num = atomic_fetch_add(&counter, 1);
    if (arrival_num == num_threads - 1) {
        counter.store(0);
    }
    else {
        while (counter.load() != 0);
    }
}
```

#### Thread 1:

B.barrier();
B.barrier();

arrival\_num == 0

arrival\_num = 0

in a perfect world, thread 1 executes now and leaves the barrier

but what if the OS preempted thread 1? Or it was asleep?

```
num_threads == 2
counter == 1
```

```
Thread 0:
```

B.barrier();

arrival\_num == 0

```
void barrier() {
    int arrival_num = atomic_fetch_add(&counter, 1);
    if (arrival_num == num_threads - 1) {
        counter.store(0);
    }
    else {
        while (counter.load() != 0);
    }
}
```

### Thread 1:

B.barrier();

B.barrier();

Thread 1 wakes up! Doesn't think its missed anything

arrival num = 0

in a perfect world, thread 1 executes now and leaves the barrier

```
num threads == 2
counter == 1
```

```
Thread 0:
```

B.barrier(); B.barrier();

```
arrival_num == 0
```

```
void barrier() {
       int arrival num = atomic fetch add(&counter, 1);
       if (arrival num == num threads - 1) {
          counter.store(0);
       else {
         while (counter.load() != 0);
```

Thread 1:

B.barrier(); B.barrier();

Thread 1 wakes up! Doesn't think its missed anything

arrival num = 0

in a perfect world, thread 1 executes now and leaves the barrier

Both threads get stuck here!

```
B.barrier();
B.barrier();
```

```
void barrier() {
    int arrival_num = atomic_fetch_add(&counter, 1);
    if (arrival_num == num_threads - 1) {
        counter.store(0);
    }
    else {
        while (counter.load() != 0);
    }
}
```

### Thread 1:

```
B.barrier();
B.barrier();
```

Ideas for fixing?

```
B.barrier();
B.barrier();
```

```
void barrier() {
    int arrival_num = atomic_fetch_add(&counter, 1);
    if (arrival_num == num_threads - 1) {
        counter.store(0);
    }
    else {
        while (counter.load() != 0);
    }
}
```

### Ideas for fixing?

Two different barriers that alternate?

#### Thread 1:

```
B.barrier();
B.barrier();
```

```
B0.barrier();
B1.barrier();
```

```
void barrier() {
    int arrival_num = atomic_fetch_add(&counter, 1);
    if (arrival_num == num_threads - 1) {
        counter.store(0);
    }
    else {
        while (counter.load() != 0);
    }
}
```

#### Ideas for fixing?

Two different barriers that alternate?

Pros: simple to implement

Cons: user has to alternate barriers

#### Thread 1:

```
B0.barrier();
B1.barrier();
```

```
B0.barrier();
B1.barrier();
```

```
void barrier() {
    int arrival_num = atomic_fetch_add(&counter, 1);
    if (arrival_num == num_threads - 1) {
        counter.store(0);
    }
    else {
        while (counter.load() != 0);
    }
}
```

#### Thread 1:

```
B0.barrier();
B1.barrier();
```

Ideas for fixing?

Two different barriers that alternate?

Pros: simple to implement

Cons: user has to alternate barriers

```
B.barrier();
if (...) {
   B.barrier();
}
B.barrier();
```

How to alternate these calls?

# Sense Reversing Barrier

Alternating "sense" dynamically

```
Thread 0:

B.barrier();

B.barrier();
```

```
sync on sense = false
```

#### Thread 1:

```
B.barrier();
B.barrier();
```

# Sense Reversing Barrier

Alternating "sense" dynamically

```
Thread 0:

B.barrier();

B.barrier();
```

```
sync on sense = true
```

```
Thread 1:
B.barrier();
```

B.barrier();

```
class SenseBarrier {
 private:
   atomic int counter;
   int num threads;
   atomic bool sense;
   bool thread sense[num threads];
 public:
   Barrier(int num threads) {
      counter = 0;
     this->num threads = num threads;
     sense = false;
      thread sense = {true, ...};
    void barrier(int tid) {
        int arrival num = atomic fetch add(&counter, 1);
        if (arrival num == num threads) {
           counter.store(0);
           sense = thread sense[tid];
        else {
          while (sense != thread sense[tid]);
        thread sense[tid] = !thread sense[tid];
```

thread\_sense = true

```
num_threads == 2
counter == 0
sense = false
```

thread\_sense = true

```
Thread 0:
```

```
B.barrier();
B.barrier();
```

```
void barrier(int tid) {
    int arrival_num = atomic_fetch_add(&counter, 1);
    if (arrival_num == num_threads-1) {
        counter.store(0);
        sense = thread_sense[tid];
    }
    else {
        while (sense != thread_sense[tid]);
    }
    thread_sense[tid] = !thread_sense[tid];
}
```

#### Thread 1:

```
B.barrier();
B.barrier();
```

```
thread_sense = true
arrival_num = 1
```

```
Thread 0:

B.barrier();

B.barrier();
```

```
thread_sense = true
arrival_num = 0
```

```
Thread 1:
```

```
B.barrier();
B.barrier();
```

```
thread_sense = true
arrival_num = 1
```

```
Thread 0:

B.barrier();

B.barrier();
```

```
thread_sense = true
arrival_num = 0
```

```
Thread 1:
```

B.barrier();

```
thread_sense = false
arrival_num = 1
```

```
Thread 0:

B.barrier();

B.barrier();
```

```
thread_sense = true
arrival_num = 0
```

```
Thread 1:
B.barrier();
```

```
B.barrier();
```

```
thread_sense = false
arrival_num = ?
```

```
Thread O:

B.barrier();

B.barrier();
```

```
thread_sense = true
arrival_num = 0
hread 1:
```

```
Thread 1:
B.barrier();
B.barrier();
```

Remember the issue! Thread 1 went to sleep around this time and thread 0 went into the barrier again!

```
thread_sense = false
arrival_num = 0
```

```
Thread 0:
B.barrier();
B.barrier();
```

```
thread_sense = true
arrival_num = 0
```

```
Thread 1:
```

B.barrier();

```
thread_sense = false
arrival_num = 0
```

```
Thread 0:
B.barrier();
B.barrier();
```

```
thread_sense = true
arrival_num = 0
```

```
Thread 1:
B.barrier();
B.barrier();
```

both are waiting!, but thread 1 can leave

```
thread_sense = false
arrival_num = 0
```

```
Thread 0:

B.barrier();

B.barrier();
```

```
thread_sense = false
arrival_num = 0
```

```
Thread 1:
B.barrier();
B.barrier();
```

both are waiting!, but thread 1 can leave

```
thread_sense = false
arrival_num = 0
```

```
Thread 0:
B.barrier();
B.barrier();
```

```
thread_sense = false
   arrival_num = ?

Thread 1:
   B.barrier();
   B.barrier();
```

Thread 1 finishes the barrier

```
thread_sense = false
arrival_num = 0
```

```
Thread 0:

B.barrier();

B.barrier();
```

```
thread_sense = false
    arrival_num = ?

Thread 1:
    B.barrier();
    B.barrier();
```

```
thread_sense = false
arrival_num = 0
```

```
Thread 0:

B.barrier();

B.barrier();
```

```
thread_sense = false
arrival_num = 1

<u>Thread 1:</u>
B.barrier();
```

```
thread_sense = false
arrival_num = 0
```

```
Thread 0:

B.barrier();

B.barrier();
```

```
thread_sense = false
    arrival_num = 1

Thread 1:
    B.barrier();
```

```
thread_sense = false
arrival_num = 0
```

```
Thread 0:
B.barrier();
B.barrier();
```

```
thread_sense = false
arrival_num = 1

Thread 1:
```

```
Thread 1:
B.barrier();
B.barrier();
```

```
thread_sense = false
arrival_num = 0
```

```
Thread 0:

B.barrier();

B.barrier();
```

```
thread_sense = false
arrival_num = 1
```

```
Thread 1:
B.barrier();
B.barrier();
```

thread 0 can leave, thread 1 can leave and the barrier works as expected!