Package 'ETRep'

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Type Package

Title Analysis of Elliptical Tubes Under the Relative Curvature Condition

Version 1.2.2

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Description Analysis of elliptical tubes with applications in biological modeling. The package is based on the references: Taheri, M., Pizer, S. M., & Schulz, J. (2024) ``The Mean Shape under the Relative Curvature Condition." Journal of Computational and Graphical Statistics <doi:10.1080/10618600.2025.2535600> and arXiv <doi:10.48550/arXiv.2404.01043>. Mohsen Taheri Shalmani (2024) ``Shape Statistics via Skeletal Structures", PhD Thesis, University of Stavanger, Norway <doi:10.13140/RG.2.2.34500.23685>. Key features include constructing discrete elliptical tubes, calculating transformations, validating structures under the Relative Curvature Condition (RCC), computing means, and generating simulations. Supports intrinsic and non-intrinsic mean calculations and transformations, size estimation, plotting, and random sample generation based on a reference tube. The intrinsic approach relies on the interior path of the original non-convex space, incorporating the RCC, while the non-intrinsic approach uses a basic robotic arm transformation that disregards the RCC.

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URL https://github.com/MohsenTaheriShalmani/Elliptical_Tubes

Depends R (>= 4.0.0)

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Imports rgl, shapes, Morpho, matlib, RSpincalc, rotations, Rvcg, fields, truncnorm, htmlwidgets

RoxygenNote 7.3.3

NeedsCompilation no

Repository CRAN

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Contents

`.etrep_open3d` *Open an rgl device with fallback to WebGL*

Description

This function tries to open a native rgl window. If that fails (e.g. on macOS without OpenGL) it falls back to an off-screen device suitable for rendering with rglwidget().

Usage

```
.etrep_open3d(show_widget = TRUE, ...)
```

Arguments

`show_widget`	logical; if TRUE and native OpenGL is not available, a message is displayed suggesting to use etrep_show3d().
`...`	additional arguments passed to [rgl::open3d()].

Value

Device ID returned by [rgl::open3d()].

.etrep_show3d *Display current rgl scene in the browser*

Description

Saves the current rgl scene to a temporary HTML file and opens it in the system's default browser.

Usage

```
.etrep_show3d(width = 800, height = 600)
```

Arguments

width, height	size of the viewer in pixels.

Value

The path to the HTML file (invisible).

.onLoad *Package startup hook*

Description

This special function is called automatically when the ETRep package is loaded. It ensures that 'rgl' uses the off-screen WebGL device ('useNULL = TRUE') on macOS and other headless environments, so that package installation and examples do not fail with an OpenGL error.

Usage

```
.onLoad(libname, pkgname)
```

Arguments

libname	Character string; the path to the package library.
pkgname	Character string; the name of the package.
	If the user has not already set 'options(rgl.useNULL)', this function sets it to 'TRUE' to suppress the typical warning: *"rgl.init failed, will use the null device"*.

check_Tube_Legality *Check the Legality of an Elliptical Tube (ETRep)*

Description

Checks the validity of a given ETRep based on the Relative Curvature Condition (RCC) and principal radii such that forall i a_i>b_i.

Usage

```
check_Tube_Legality(tube)
```

Arguments

tube	List containing ETRep details.

Value

Logical value: TRUE if valid, FALSE otherwise.

References

Taheri, M., Pizer, S. M., & Schulz, J. (2024). "The Mean Shape under the Relative Curvature Condition." arXiv. doi:10.48550/arXiv.2404.01043

Taheri Shalmani, M. (2024). "Shape Statistics via Skeletal Structures." University of Stavanger. doi:10.13140/RG.2.2.34500.23685

Examples

```
# Load tube
data("colon3D")
check_Tube_Legality(tube = colon3D)
```

colon3D *Data*

Description

A colon sample as an elliptical tube.

Usage

```
colon3D
```

Format

A list containing the information of an e-tube

Source

Generated and stored in the package's 'data/' folder.

create_Elliptical_Tube *Create a Discrete Elliptical Tube (ETRep)*

Description

Constructs a discrete elliptical tube (ETRep) based on specified parameters.

Usage

```
create_Elliptical_Tube(
  numberOfFrames,
  method,
  materialFramesBasedOnParents = NA,
  initialFrame = diag(3),
  initialPoint = c(0, 0, 0),
  EulerAngles_Matrix = NA,
  ellipseResolution = 10,
  ellipseRadii_a,
  ellipseRadii_b,
  connectionsLengths,
  plotting = TRUE
)
```

Arguments

numberOfFrames	Integer, specifies the number of consecutive material frames.
method	String, either "basedOnEulerAngles" or "basedOnMaterialFrames", defines the material frames method.
materialFramesBasedOnParents	Array (3 x 3 x numberOfFrames) with pre-defined material frames.
initialFrame	Matrix 3 x 3 as the initial frame
initialPoint	Real vector with three elemets as the initial point
EulerAngles_Matrix	Matrix of dimensions numberOfFrames x 3 with Euler angles to define material frames.
ellipseResolution	Integer, resolution of elliptical cross-sections (default is 10).
ellipseRadii_a	Numeric vector for the primary radii of cross-sections.
ellipseRadii_b	Numeric vector for the secondary radii of cross-sections.
connectionsLengths	Numeric vector for lengths of spinal connection vectors.
plotting	Logical, enables plotting of the ETRep (default is TRUE).

Value

List containing tube details (orientation, radii, connection lengths, boundary points, etc.).

References

Taheri, M., Pizer, S. M., & Schulz, J. (2024). "The Mean Shape under the Relative Curvature Condition." arXiv. doi:10.48550/arXiv.2404.01043

Taheri Shalmani, M. (2024). "Shape Statistics via Skeletal Structures." University of Stavanger. doi:10.13140/RG.2.2.34500.23685

Examples

```
numberOfFrames<-15
EulerAngles_alpha<-c(rep(0,numberOfFrames))
EulerAngles_beta<-c(rep(-pi/20,numberOfFrames))
EulerAngles_gamma<-c(rep(0,numberOfFrames))
EulerAngles_Matrix<-cbind(EulerAngles_alpha,
                          EulerAngles_beta,
                          EulerAngles_gamma)
tube <- create_Elliptical_Tube(numberOfFrames = numberOfFrames,
                               method = "basedOnEulerAngles",
                               EulerAngles_Matrix = EulerAngles_Matrix,
                               ellipseResolution = 10,
                               ellipseRadii_a = rep(3, numberOfFrames),
                               ellipseRadii_b = rep(2, numberOfFrames),
                               connectionsLengths = rep(4, numberOfFrames),
                               plotting = FALSE)
# Plotting
## Not run:
 plot_Elliptical_Tube(tube = tube,plot_frames = FALSE,
                      plot_skeletal_sheet = TRUE,
                      plot_r_project = FALSE,
                      plot_r_max = FALSE,add = FALSE)

## End(Not run)
```

---

elliptical_Tube_Euclideanization

Convert an ETRep to a Matrix in the Convex Transformed Space.

Description

Convert an ETRep to a Matrix in the Convex Transformed Space.

Usage

```
elliptical_Tube_Euclideanization(tube)
```

Arguments

tube	A list containing the details of the ETRep.

Value

An n*6 matrix, where n is the number of spinal points, representing the ETRep in the transformed Euclidean convex space.

Examples

```
#Example
# Load tube
data("tube_A")
Euclideanized_Tube<- elliptical_Tube_Euclideanization(tube = tube_A)
```

`intrinsic_Distance_Between2tubes` *Calculating the intrinsic distance between two ETReps*

Description

Calculating the intrinsic distance between two ETReps

Usage

```
intrinsic_Distance_Between2tubes(tube1, tube2)
```

Arguments

`tube1`	List containing ETRep details.
`tube2`	List containing ETRep details.

Value

Numeric

References

Taheri, M., Pizer, S. M., & Schulz, J. (2024). "The Mean Shape under the Relative Curvature Condition." arXiv. doi:10.48550/arXiv.2404.01043

Taheri Shalmani, M. (2024). "Shape Statistics via Skeletal Structures." University of Stavanger. doi:10.13140/RG.2.2.34500.23685

Examples

```
# Load tubes
data("tube_A")
data("tube_B")
intrinsic_Distance_Between2tubes(tube1 = tube_A,tube2 = tube_B)
```

`intrinsic_mean_tube` *Calculate Intrinsic Mean of ETReps*

Description

Computes the intrinsic mean of a set of ETReps. The computation involves transforming the non-convex hypertrumpet space into a convex space, calculating the mean in this transformed space, and mapping the result back to the original hypertrumpet space.

Usage

```
intrinsic_mean_tube(tubes, type = "sizeAndShapeAnalysis", plotting = TRUE)
```

Arguments

`tubes`	List of ETReps.
`type`	String, "ShapeAnalysis" or "sizeAndShapeAnalysis" (default is "sizeAndShapeAnalysis").
`plotting`	Logical, enables visualization of the mean (default is TRUE).

Value

List representing the mean ETRep.

References

Taheri, M., Pizer, S. M., & Schulz, J. (2024). "The Mean Shape under the Relative Curvature Condition." arXiv. doi:10.48550/arXiv.2404.01043

Taheri Shalmani, M. (2024). "Shape Statistics via Skeletal Structures." University of Stavanger. doi:10.13140/RG.2.2.34500.23685

Examples

```
#Example 1
# Load tubes
data("tube_A")
data("tube_B")
intrinsic_mean<-
  intrinsic_mean_tube(tubes = list(tube_A,tube_B),
                      plotting = FALSE)
# Plotting
## Not run:
plot_Elliptical_Tube(tube = intrinsic_mean,
                     plot_frames = FALSE,
                     plot_skeletal_sheet = FALSE,
                     plot_r_project = FALSE,
                     plot_r_max = FALSE,
                     add = FALSE)

## End(Not run)

#Example 2
```

```
data("simulatedColons")
intrinsic_mean<-
  intrinsic_mean_tube(tubes = simulatedColons,
                      plotting = FALSE)
# Plotting
## Not run:
plot_Elliptical_Tube(tube = intrinsic_mean,
                     plot_frames = FALSE,
                     plot_skeletal_sheet = FALSE,
                     plot_r_project = FALSE,
                     plot_r_max = FALSE,
                     add = FALSE)

## End(Not run)
```

`intrinsic_Transformation_Elliptical_Tubes`
Intrinsic Transformation Between Two ETReps

Description

Performs an intrinsic transformation from one ETRep to another, preserving essential e-tube properties such as the Relative Curvature Condition (RCC) while avoiding local self-intersections.

Usage

```
intrinsic_Transformation_Elliptical_Tubes(
  tube1,
  tube2,
  type = "sizeAndShapeAnalysis",
  numberOfSteps = 5,
  plotting = TRUE,
  colorBoundary = "blue"
)
```

Arguments

`tube1`	List containing details of the first ETRep.
`tube2`	List containing details of the second ETRep.
`type`	String defining the type of analysis as sizeAndShapeAnalysis or shapeAnalysis
`numberOfSteps`	Integer, number of transformation steps.
`plotting`	Logical, enables visualization during transformation (default is TRUE).
`colorBoundary`	String defining the color of the e-tube

Value

List containing intermediate ETReps.

References

Taheri, M., Pizer, S. M., & Schulz, J. (2024). "The Mean Shape under the Relative Curvature Condition." arXiv. doi:10.48550/arXiv.2404.01043

Taheri Shalmani, M. (2024). "Shape Statistics via Skeletal Structures." University of Stavanger. doi:10.13140/RG.2.2.34500.23685

Examples

```
# Load tubes
data("tube_A")
data("tube_B")
numberOfSteps <- 10
transformation_Tubes<-
  intrinsic_Transformation_Elliptical_Tubes(
    tube1 = tube_A,tube2 = tube_B,
    numberOfSteps = numberOfSteps,
    plotting = FALSE)
# Plotting
## Not run:
for (i in 1:length(transformation_Tubes)) {
  plot_Elliptical_Tube(tube = transformation_Tubes[[i]],
  plot_frames = FALSE,plot_skeletal_sheet = FALSE
  ,plot_r_project = FALSE,
  plot_r_max = FALSE,
  add = FALSE)
}
##
## End(Not run)
```

---

nonIntrinsic_Distance_Between2tubes

Calculating the non-intrinsic distance between two ETReps

Description

Calculating the non-intrinsic distance between two ETReps

Usage

```
nonIntrinsic_Distance_Between2tubes(tube1, tube2)
```

Arguments

tube1	List containing ETRep details.
tube2	List containing ETRep details.

Value

Numeric

References

Taheri, M., Pizer, S. M., & Schulz, J. (2024). "The Mean Shape under the Relative Curvature Condition." arXiv. doi:10.48550/arXiv.2404.01043

Taheri Shalmani, M. (2024). "Shape Statistics via Skeletal Structures." University of Stavanger. doi:10.13140/RG.2.2.34500.23685

Examples

```
# Load tubes
data("tube_A")
data("tube_B")
intrinsic_Distance_Between2tubes(tube1 = tube_A,tube2 = tube_B)
```

`nonIntrinsic_mean_tube` *Compute Non-Intrinsic Mean of ETReps*

Description

Calculates the non-intrinsic mean of a set of ETReps. This method utilizes a non-intrinsic distance metric based on robotic arm non-intrinsic transformations.

Usage

```
nonIntrinsic_mean_tube(tubes, type = "sizeAndShapeAnalysis", plotting = TRUE)
```

Arguments

`tubes`	List of ETReps.
`type`	String, "ShapeAnalysis" or "sizeAndShapeAnalysis" (default is "sizeAndShapeAnalysis").
`plotting`	Logical, enables visualization of the mean (default is TRUE).

Value

List representing the mean ETRep.

Examples

```
#Example 1
# Load tubes
data("tube_A")
data("tube_B")
nonIntrinsic_mean<-
  nonIntrinsic_mean_tube(tubes = list(tube_A,tube_B),
                         plotting = FALSE)
# Plotting
## Not run:
plot_Elliptical_Tube(tube = nonIntrinsic_mean,
                     plot_frames = FALSE,
                     plot_skeletal_sheet = FALSE,
                     plot_r_project = FALSE,
```

```
                    plot_r_max = FALSE,
                    add = FALSE)

## End(Not run)

#Example 2
data("simulatedColons")
nonIntrinsic_mean<-
  nonIntrinsic_mean_tube(tubes = simulatedColons,
                         plotting = FALSE)
# Plotting
## Not run:
plot_Elliptical_Tube(tube = nonIntrinsic_mean,
                    plot_frames = FALSE,
                    plot_skeletal_sheet = FALSE,
                    plot_r_project = FALSE,
                    plot_r_max = FALSE,
                    add = FALSE)

## End(Not run)
```

`nonIntrinsic_Transformation_Elliptical_Tubes`
Non-Intrinsic Transformation Between Two ETReps

Description

Performs a non-intrinsic transformation from one ETRep to another. This approach is inspired by robotic arm transformations and does not account for the Relative Curvature Condition (RCC).

Usage

```
nonIntrinsic_Transformation_Elliptical_Tubes(
  tube1,
  tube2,
  type = "sizeAndShapeAnalysis",
  numberOfSteps = 4,
  plotting = TRUE,
  colorBoundary = "blue",
  add = FALSE
)
```

Arguments

`tube1`	List containing details of the first ETRep.
`tube2`	List containing details of the second ETRep.
`type`	String defining the type of analysis as sizeAndShapeAnalysis or shapeAnalysis
`numberOfSteps`	Integer, number of transformation steps.
`plotting`	Logical, enables visualization during transformation (default is TRUE).
`colorBoundary`	String defining the color of the e-tube
`add`	Logical, enables overlay plotting

Value

List containing intermediate ETReps.

References

Taheri, M., Pizer, S. M., & Schulz, J. (2024). "The Mean Shape under the Relative Curvature Condition." arXiv. doi:10.48550/arXiv.2404.01043

Taheri Shalmani, M. (2024). "Shape Statistics via Skeletal Structures." University of Stavanger. doi:10.13140/RG.2.2.34500.23685

Examples

```
# Load tubes
data("tube_A")
data("tube_B")
numberOfSteps <- 10
transformation_Tubes<-
  nonIntrinsic_Transformation_Elliptical_Tubes(
    tube1 = tube_A,tube2 = tube_B,
    numberOfSteps = numberOfSteps,
    plotting = FALSE)
# Plotting
## Not run:
for (i in 1:length(transformation_Tubes)) {
  plot_Elliptical_Tube(tube = transformation_Tubes[[i]],
  plot_frames = FALSE,plot_skeletal_sheet = FALSE
  ,plot_r_project = FALSE,
  plot_r_max = FALSE,
  add = FALSE)
}

## End(Not run)
```

---

plot_Elliptical_Tube *Plot an Elliptical Tube (ETRep)*

Description

Plots a given ETRep with options for boundary, material frames, and projection visualization.

Usage

```
plot_Elliptical_Tube(
  tube,
  plot_boundary = TRUE,
  plot_r_max = FALSE,
  plot_r_project = TRUE,
  plot_frames = TRUE,
  frameScaling = NA,
  plot_spine = TRUE,
  plot_normal_vec = FALSE,
```

```
  plot_skeletal_sheet = TRUE,
  decorate = TRUE,
  colSkeletalSheet = "blue",
  colorBoundary = "blue",
  add = FALSE
)
```

Arguments

tube	List containing ETRep details.
plot_boundary	Logical, enables plotting of the boundary (default is TRUE).
plot_r_max	Logical, enables plotting of max projection size (default is FALSE).
plot_r_project	Logical, enables plotting of projection along normals (default is TRUE).
plot_frames	Logical, enables plotting of the material frames (default is TRUE).
frameScaling	Numeric, scale factor for frames.
plot_spine	Logical, enables plotting of the spine.
plot_normal_vec	Logical, enables plotting of the normals.
plot_skeletal_sheet	Logical, enables plotting of the surface skeleton.
decorate	Logical, enables decorate the plot
colSkeletalSheet	String, defining the color of the surface skeleton
colorBoundary	String, defining the color of the e-tube
add	Logical, enables overlay plotting

Value

Graphical output.

Examples

```
# Load tube
data("colon3D")
## Not run:
plot_Elliptical_Tube(tube = colon3D,
                     plot_frames = FALSE)

## End(Not run)
```

---

simulatedColons *Data*

Description

Simulated samples of e-tubes, modeled after a reference structure resembling a colon.

Usage

```
simulatedColons
```

Format

Five simulated samples of elliptical tubes, modeled after a reference structure resembling a colon.

Source

Generated and stored in the package's 'data/' folder.

`simulate_etube` *Simulate Random Elliptical Tubes (ETReps)*

Description

Generates random samples of ETReps based on a reference tube with added variation.

Usage

```
simulate_etube(
  referenceTube,
  numberOfSimulation,
  sd_v = 10^-10,
  sd_psi = 10^-10,
  sd_x = 10^-10,
  sd_a = 10^-10,
  sd_b = 10^-10,
  rangeSdScale = c(1, 2),
  plotting = TRUE
)
```

Arguments

`referenceTube`	List containing ETRep information as the reference.
`numberOfSimulation`	Integer, number of random samples.
`sd_v`	Standard deviations for various parameters.
`sd_psi`	Standard deviations for various parameters.
`sd_x`	Standard deviations for various parameters.
`sd_a`	Standard deviations for various parameters.
`sd_b`	Standard deviations for various parameters.
`rangeSdScale`	Numeric range for random scaling.
`plotting`	Logical, enables visualization of samples (default is FALSE).

Value

List of random ETReps.

References

Taheri, M., Pizer, S. M., & Schulz, J. (2024). "The Mean Shape under the Relative Curvature Condition." arXiv. doi:10.48550/arXiv.2404.01043

Taheri Shalmani, M. (2024). "Shape Statistics via Skeletal Structures." University of Stavanger. doi:10.13140/RG.2.2.34500.23685

Examples

```
# Load tube
data("colon3D")
#Set Parameters
sd_v<-sd_psi<-1e-03
sd_x<-sd_a<-sd_b<-1e-04
numberOfSimulation<-4
random_Tubes<-
  simulate_etube(referenceTube = colon3D,
                 numberOfSimulation = numberOfSimulation,
                 sd_v = sd_v,
                 sd_psi = sd_psi,
                 sd_x = sd_x,
                 sd_a = sd_a,
                 sd_b = sd_b,
                 rangeSdScale = c(1, 2),
                 plotting = FALSE)
# Plotting
## Not run:
plot_Elliptical_Tube(random_Tubes[[1]], add = FALSE)
plot_Elliptical_Tube(random_Tubes[[2]], add = TRUE)
plot_Elliptical_Tube(random_Tubes[[3]], add = TRUE)
plot_Elliptical_Tube(random_Tubes[[4]], add = TRUE)

## End(Not run)
```

---

tube_A *Data*

Description

A tube with 204 elliptical cross-sections.

Usage

```
tube_A
```

Format

A list containing the information of an e-tube with 204 elliptical cross-sections

Source

Generated and stored in the package's 'data/' folder.

tube_B *Data*

Description

A tube with 204 elliptical cross-sections.

Usage

```
tube_B
```

Format

A list containing the information of an e-tube with 204 elliptical cross-sections

Source

Generated and stored in the package's 'data/' folder.

tube_Surface_Mesh *Create surface mesh of a tube*

Description

Create surface mesh of a tube

Usage

```
tube_Surface_Mesh(
  tube,
  meshType = "quadrilateral",
  plotMesh = TRUE,
  color = "blue",
  decorate = TRUE
)
```

Arguments

tube	List containing ETRep details.
meshType	String, either "quadrilateral" or "triangular" definig the type of mesh.
plotMesh	Logical, enables plotting of the mesh (default is TRUE).
color	String, defining the color of the mesh (default is 'blue').
decorate	Logical, enables decorating the plot (default is TRUE).

Value

An object from rgl::mesh3d class

Examples

```
## Not run:
quad_mesh<-tube_Surface_Mesh(tube = ETRep::tube_B,
                             meshType = "quadrilateral",
                             plotMesh = TRUE,
                             decorate = TRUE,
                             color = "orange")
# draw wireframe of the mesh
rgl::wire3d(quad_mesh, color = "black", lwd = 1)   # add wireframe
# Display in browser
ETRep:::.etrep_show3d(width = 800, height = 600)

tri_mesh<-tube_Surface_Mesh(tube = ETRep::tube_B,
                            meshType = "triangular",
                            plotMesh = TRUE,
                            decorate = TRUE,
                            color = "green")
# draw wireframe of the mesh
rgl::wire3d(tri_mesh, color = "black", lwd = 1)   # add wireframe
# Display in browser
ETRep:::.etrep_show3d(width = 800, height = 600)

## End(Not run)
```