

# Package ‘ETRep’

June 5, 2025

**Type** Package

**Title** Analysis of Elliptical Tubes Under the Relative Curvature Condition

**Version** 1.2.0

**Maintainer** Mohsen Taheri Shalmani <MohsenTaheriShalmani@gmail.com>

**Description** Analysis of elliptical tubes with applications in biological modeling. The package is based on the references: Taheri, M., Pizer, S. M., & Schulz, J. (2024) ``The Mean Shape under the Relative Curvature Condition." arXiv <[doi:10.48550/arXiv.2404.01043](https://doi.org/10.48550/arXiv.2404.01043)>. Mohsen Taheri Shalmani (2024) ``Shape Statistics via Skeletal Structures", PhD Thesis, University of Stavanger, Norway <[doi:10.13140/RG.2.2.34500.23685](https://doi.org/10.13140/RG.2.2.34500.23685)>. Key features include constructing discrete elliptical tubes, calculating transformations, validating structures under the Relative Curvature Condition (RCC), computing means, and generating simulations. Supports intrinsic and non-intrinsic mean calculations and transformations, size estimation, plotting, and random sample generation based on a reference tube. The intrinsic approach relies on the interior path of the original non-convex space, incorporating the RCC, while the non-intrinsic approach uses a basic robotic arm transformation that disregards the RCC.

**License** MIT + file LICENSE

**URL** [https://github.com/MohsenTaheriShalmani/Elliptical\\_Tubes](https://github.com/MohsenTaheriShalmani/Elliptical_Tubes)

**Depends** R (>= 4.0.0)

**Author** Mohsen Taheri Shalmani [aut, cre] (ORCID:  
<<https://orcid.org/0000-0003-4044-8507>>),  
Jörn Schulz [aut],  
Stephen M. Pizer [aut]

**Encoding** UTF-8

**LazyData** true

**Imports** rgl, shapes, Morpho, matlib, RSpincalc, rotations, Rvcg,  
fields, truncnorm

**RoxygenNote** 7.3.2

**NeedsCompilation** no

**Repository** CRAN

**Date/Publication** 2025-06-05 06:10:02 UTC

Contents

check_Tube_Legality . . . . .	2
colon3D . . . . .	3
create_Elliptical_Tube . . . . .	3
elliptical_Tube_Euclideanization . . . . .	5
intrinsic_Distance_Between2tubes . . . . .	5
intrinsic_mean_tube . . . . .	6
intrinsic_Transformation_Elliptical_Tubes . . . . .	7
nonIntrinsic_Distance_Between2tubes . . . . .	9
nonIntrinsic_mean_tube . . . . .	10
nonIntrinsic_Transformation_Elliptical_Tubes . . . . .	11
plot_Elliptical_Tube . . . . .	12
simulatedColons . . . . .	13
simulate_etube . . . . .	14
tube_A . . . . .	15
tube_B . . . . .	16
tube_Surface_Mesh . . . . .	16
<b>Index</b>	<b>18</b>

---

check_Tube_Legality	<i>Check the Legality of an Elliptical Tube (ETRep)</i>
---------------------	---

---

Description

Checks the validity of a given ETRep based on the Relative Curvature Condition (RCC) and principal radii such that forall  $i$   $a_i > b_i$ .

Usage

check\_Tube\_Legality(tube)

Arguments

tube                      List containing ETRep details.

Value

Logical value: TRUE if valid, FALSE otherwise.

References

Taheri, M., Pizer, S. M., & Schulz, J. (2024). "The Mean Shape under the Relative Curvature Condition." arXiv. doi:10.48550/arXiv.2404.01043

Taheri Shalmani, M. (2024). "Shape Statistics via Skeletal Structures." University of Stavanger. doi:10.13140/RG.2.2.34500.23685

**Examples**

```
# Load tube
data("colon3D")
check_Tube_Legality(tube = colon3D)
```

colon3D

*Data***Description**

A colon sample as an elliptical tube.

**Usage**

```
colon3D
```

**Format**

A list containing the information of an e-tube

**Source**

Generated and stored in the package's 'data/' folder.

create\_Elliptical\_Tube

*Create a Discrete Elliptical Tube (ETRep)***Description**

Constructs a discrete elliptical tube (ETRep) based on specified parameters.

**Usage**

```
create_Elliptical_Tube(
  numberOfFrames,
  method,
  materialFramesBasedOnParents = NA,
  initialFrame = diag(3),
  initialPoint = c(0, 0, 0),
  EulerAngles_Matrix = NA,
  ellipseResolution = 10,
  ellipseRadii_a,
  ellipseRadii_b,
  connectionsLengths,
  plotting = TRUE,
  add = FALSE
)
```

## Arguments

numberOfFrames	Integer, specifies the number of consecutive material frames.
method	String, either "basedOnEulerAngles" or "basedOnMaterialFrames", defines the material frames method.
materialFramesBasedOnParents	Array (3 x 3 x numberOfFrames) with pre-defined material frames.
initialFrame	Matrix 3 x 3 as the initial frame
initialPoint	Real vector with three elements as the initial point
EulerAngles_Matrix	Matrix of dimensions numberOfFrames x 3 with Euler angles to define material frames.
ellipseResolution	Integer, resolution of elliptical cross-sections (default is 10).
ellipseRadii_a	Numeric vector for the primary radii of cross-sections.
ellipseRadii_b	Numeric vector for the secondary radii of cross-sections.
connectionsLengths	Numeric vector for lengths of spinal connection vectors.
plotting	Logical, enables plotting of the ETRep (default is TRUE).
add	Logical, enables overlay plotting

## Value

List containing tube details (orientation, radii, connection lengths, boundary points, etc.).

## References

Taheri, M., Pizer, S. M., & Schulz, J. (2024). "The Mean Shape under the Relative Curvature Condition." arXiv. [doi:10.48550/arXiv.2404.01043](https://arxiv.org/abs/2404.01043)

Taheri Shalmani, M. (2024). "Shape Statistics via Skeletal Structures." University of Stavanger. [doi:10.13140/RG.2.2.34500.23685](https://arxiv.org/abs/2404.01043)

## Examples

```
numberOfFrames<-15
EulerAngles_alpha<-c(rep(0,numberOfFrames))
EulerAngles_beta<-c(rep(-pi/20,numberOfFrames))
EulerAngles_gamma<-c(rep(0,numberOfFrames))
EulerAngles_Matrix<-cbind(EulerAngles_alpha,
                           EulerAngles_beta,
                           EulerAngles_gamma)
tube <- create_Elliptical_Tube(numberOfFrames = numberOfFrames,
                              method = "basedOnEulerAngles",
                              EulerAngles_Matrix = EulerAngles_Matrix,
                              ellipseResolution = 10,
                              ellipseRadii_a = rep(3, numberOfFrames),
                              ellipseRadii_b = rep(2, numberOfFrames),
                              connectionsLengths = rep(4, numberOfFrames),
```

```

                                plotting = FALSE)
# Plotting
plot_Elliptical_Tube(tube = tube, plot_frames = FALSE,
                     plot_skeletal_sheet = TRUE,
                     plot_r_project = FALSE,
                     plot_r_max = FALSE, add = FALSE)

```

---

elliptical\_Tube\_Euclideanization

*Convert an ETRep to a Matrix in the Convex Transformed Space.*

---

### Description

Convert an ETRep to a Matrix in the Convex Transformed Space.

### Usage

```
elliptical_Tube_Euclideanization(tube)
```

### Arguments

tube                      A list containing the details of the ETRep.

### Value

An  $n \times 6$  matrix, where  $n$  is the number of spinal points, representing the ETRep in the transformed Euclidean convex space.

### Examples

```

#Example
# Load tube
data("tube_A")
Euclideanized_Tube<- elliptical_Tube_Euclideanization(tube = tube_A)

```

---

intrinsic\_Distance\_Between2tubes

*Calculating the intrinsic distance between two ETReps*

---

### Description

Calculating the intrinsic distance between two ETReps

### Usage

```
intrinsic_Distance_Between2tubes(tube1, tube2)
```

**Arguments**

tube1	List containing ETRep details.
tube2	List containing ETRep details.

**Value**

Numeric

**References**

Taheri, M., Pizer, S. M., & Schulz, J. (2024). "The Mean Shape under the Relative Curvature Condition." arXiv. [doi:10.48550/arXiv.2404.01043](https://doi.org/10.48550/arXiv.2404.01043)

Taheri Shalmani, M. (2024). "Shape Statistics via Skeletal Structures." University of Stavanger. [doi:10.13140/RG.2.2.34500.23685](https://doi.org/10.13140/RG.2.2.34500.23685)

**Examples**

```
# Load tubes
data("tube_A")
data("tube_B")
intrinsic_Distance_Between2tubes(tube1 = tube_A, tube2 = tube_B)
```

---

intrinsic_mean_tube	<i>Calculate Intrinsic Mean of ETReps</i>
---------------------	---

---

**Description**

Computes the intrinsic mean of a set of ETReps. The computation involves transforming the non-convex hypertrumpet space into a convex space, calculating the mean in this transformed space, and mapping the result back to the original hypertrumpet space.

**Usage**

```
intrinsic_mean_tube(tubes, type = "sizeAndShapeAnalysis", plotting = TRUE)
```

**Arguments**

tubes	List of ETReps.
type	String, "ShapeAnalysis" or "sizeAndShapeAnalysis" (default is "sizeAndShapeAnalysis").
plotting	Logical, enables visualization of the mean (default is TRUE).

**Value**

List representing the mean ETRep.

## References

Taheri, M., Pizer, S. M., & Schulz, J. (2024). "The Mean Shape under the Relative Curvature Condition." arXiv. doi:10.48550/arXiv.2404.01043

Taheri Shalmani, M. (2024). "Shape Statistics via Skeletal Structures." University of Stavanger. doi:10.13140/RG.2.2.34500.23685

## Examples

```
#Example 1
# Load tubes
data("tube_A")
data("tube_B")
intrinsic_mean<-
  intrinsic_mean_tube(tubes = list(tube_A,tube_B),
                      plotting = FALSE)

# Plotting
plot_Elliptical_Tube(tube = intrinsic_mean,
                     plot_frames = FALSE,
                     plot_skeletal_sheet = FALSE,
                     plot_r_project = FALSE,
                     plot_r_max = FALSE,
                     add = FALSE)

#Example 2
data("simulatedColons")
intrinsic_mean<-
  intrinsic_mean_tube(tubes = simulatedColons,
                      plotting = FALSE)

# Plotting
plot_Elliptical_Tube(tube = intrinsic_mean,
                     plot_frames = FALSE,
                     plot_skeletal_sheet = FALSE,
                     plot_r_project = FALSE,
                     plot_r_max = FALSE,
                     add = FALSE)
```

---

intrinsic\_Transformation\_Elliptical\_Tubes

*Intrinsic Transformation Between Two ETReps*

---

## Description

Performs an intrinsic transformation from one ETRep to another, preserving essential e-tube properties such as the Relative Curvature Condition (RCC) while avoiding local self-intersections.

**Usage**

```
intrinsic_Transformation_Elliptical_Tubes(
  tube1,
  tube2,
  type = "sizeAndShapeAnalysis",
  numberOfSteps = 5,
  plotting = TRUE,
  colorBoundary = "blue"
)
```

**Arguments**

tube1	List containing details of the first ETRep.
tube2	List containing details of the second ETRep.
type	String defining the type of analysis as sizeAndShapeAnalysis or shapeAnalysis
numberOfSteps	Integer, number of transformation steps.
plotting	Logical, enables visualization during transformation (default is TRUE).
colorBoundary	String defining the color of the e-tube

**Value**

List containing intermediate ETReps.

**References**

Taheri, M., Pizer, S. M., & Schulz, J. (2024). "The Mean Shape under the Relative Curvature Condition." arXiv. [doi:10.48550/arXiv.2404.01043](https://doi.org/10.48550/arXiv.2404.01043)

Taheri Shalmani, M. (2024). "Shape Statistics via Skeletal Structures." University of Stavanger. [doi:10.13140/RG.2.2.34500.23685](https://doi.org/10.13140/RG.2.2.34500.23685)

**Examples**

```
# Load tubes
data("tube_A")
data("tube_B")
numberOfSteps <- 10
transformation_Tubes<-
  intrinsic_Transformation_Elliptical_Tubes(
    tube1 = tube_A, tube2 = tube_B,
    numberOfSteps = numberOfSteps,
    plotting = FALSE)
# Plotting
for (i in 1:length(transformation_Tubes)) {
  plot_Elliptical_Tube(tube = transformation_Tubes[[i]],
    plot_frames = FALSE, plot_skeletal_sheet = FALSE
    , plot_r_project = FALSE,
    plot_r_max = FALSE,
    add = FALSE)
```



```
}
```

---

```
nonIntrinsic_Distance_Between2tubes
```

*Calculating the non-intrinsic distance between two ETReps*

---

## Description

Calculating the non-intrinsic distance between two ETReps

## Usage

```
nonIntrinsic_Distance_Between2tubes(tube1, tube2)
```

## Arguments

tube1	List containing ETRep details.
tube2	List containing ETRep details.

## Value

Numeric

## References

Taheri, M., Pizer, S. M., & Schulz, J. (2024). "The Mean Shape under the Relative Curvature Condition." arXiv. [doi:10.48550/arXiv.2404.01043](https://doi.org/10.48550/arXiv.2404.01043)

Taheri Shalmani, M. (2024). "Shape Statistics via Skeletal Structures." University of Stavanger. [doi:10.13140/RG.2.2.34500.23685](https://doi.org/10.13140/RG.2.2.34500.23685)

## Examples

```
# Load tubes
data("tube_A")
data("tube_B")
intrinsic_Distance_Between2tubes(tube1 = tube_A, tube2 = tube_B)
```

---

nonIntrinsic\_mean\_tube

*Compute Non-Intrinsic Mean of ETReps*


---

## Description

Calculates the non-intrinsic mean of a set of ETReps. This method utilizes a non-intrinsic distance metric based on robotic arm non-intrinsic transformations.

## Usage

```
nonIntrinsic_mean_tube(tubes, type = "sizeAndShapeAnalysis", plotting = TRUE)
```

## Arguments

tubes	List of ETReps.
type	String, "ShapeAnalysis" or "sizeAndShapeAnalysis" (default is "sizeAndShapeAnalysis").
plotting	Logical, enables visualization of the mean (default is TRUE).

## Value

List representing the mean ETRep.

## Examples

```
#Example 1
# Load tubes
data("tube_A")
data("tube_B")
nonIntrinsic_mean<-
  nonIntrinsic_mean_tube(tubes = list(tube_A,tube_B),
                        plotting = FALSE)

# Plotting
plot_Elliptical_Tube(tube = nonIntrinsic_mean,
                    plot_frames = FALSE,
                    plot_skeletal_sheet = FALSE,
                    plot_r_project = FALSE,
                    plot_r_max = FALSE,
                    add = FALSE)

#Example 2
data("simulatedColons")
nonIntrinsic_mean<-
  nonIntrinsic_mean_tube(tubes = simulatedColons,
                        plotting = FALSE)

# Plotting
plot_Elliptical_Tube(tube = nonIntrinsic_mean,
```

```

plot_frames = FALSE,
plot_skeletal_sheet = FALSE,
plot_r_project = FALSE,
plot_r_max = FALSE,
add = FALSE)

```

---

nonIntrinsic\_Transformation\_Elliptical\_Tubes

*Non-Intrinsic Transformation Between Two ETReps*


---

## Description

Performs a non-intrinsic transformation from one ETRep to another. This approach is inspired by robotic arm transformations and does not account for the Relative Curvature Condition (RCC).

## Usage

```

nonIntrinsic_Transformation_Elliptical_Tubes(
  tube1,
  tube2,
  type = "sizeAndShapeAnalysis",
  numberOfSteps = 4,
  plotting = TRUE,
  colorBoundary = "blue",
  add = FALSE
)

```

## Arguments

tube1	List containing details of the first ETRep.
tube2	List containing details of the second ETRep.
type	String defining the type of analysis as sizeAndShapeAnalysis or shapeAnalysis
numberOfSteps	Integer, number of transformation steps.
plotting	Logical, enables visualization during transformation (default is TRUE).
colorBoundary	String defining the color of the e-tube
add	Logical, enables overlay plotting

## Value

List containing intermediate ETReps.

## References

Taheri, M., Pizer, S. M., & Schulz, J. (2024). "The Mean Shape under the Relative Curvature Condition." arXiv. doi:10.48550/arXiv.2404.01043

Taheri Shalmani, M. (2024). "Shape Statistics via Skeletal Structures." University of Stavanger. doi:10.13140/RG.2.2.34500.23685

**Examples**

```
# Load tubes
data("tube_A")
data("tube_B")
numberOfSteps <- 10
transformation_Tubes<-
  nonIntrinsic_Transformation_Elliptical_Tubes(
    tube1 = tube_A,tube2 = tube_B,
    numberOfSteps = numberOfSteps,
    plotting = FALSE)
# Plotting
for (i in 1:length(transformation_Tubes)) {
  plot_Elliptical_Tube(tube = transformation_Tubes[[i]],
    plot_frames = FALSE,plot_skeletal_sheet = FALSE
    ,plot_r_project = FALSE,
    plot_r_max = FALSE,
    add = FALSE)
}
```

---

plot\_Elliptical\_Tube    *Plot an Elliptical Tube (ETRep)*

---

**Description**

Plots a given ETRep with options for boundary, material frames, and projection visualization.

**Usage**

```
plot_Elliptical_Tube(
  tube,
  plot_boundary = TRUE,
  plot_r_max = FALSE,
  plot_r_project = TRUE,
  plot_frames = TRUE,
  frameScaling = NA,
  plot_spine = TRUE,
  plot_normal_vec = FALSE,
  plot_skeletal_sheet = TRUE,
  decorate = TRUE,
  colSkeletalSheet = "blue",
  colorBoundary = "blue",
  add = FALSE
)
```

Arguments

tube	List containing ETRep details.
plot_boundary	Logical, enables plotting of the boundary (default is TRUE).
plot_r_max	Logical, enables plotting of max projection size (default is FALSE).
plot_r_project	Logical, enables plotting of projection along normals (default is TRUE).
plot_frames	Logical, enables plotting of the material frames (default is TRUE).
frameScaling	Numeric, scale factor for frames.
plot_spine	Logical, enables plotting of the spine.
plot_normal_vec	Logical, enables plotting of the normals.
plot_skeletal_sheet	Logical, enables plotting of the surface skeleton.
decorate	Logical, enables decorate the plot
colSkeletalSheet	String, defining the color of the surface skeleton
colorBoundary	String, defining the color of the e-tube
add	Logical, enables overlay plotting

Value

Graphical output.

Examples

```
# Load tube
data("colon3D")
plot_Elliptical_Tube(tube = colon3D,
                     plot_frames = FALSE,
                     add=FALSE)
```

---

simulatedColons	<i>Data</i>
-----------------	-------------

---

Description

Simulated samples of e-tubes, modeled after a reference structure resembling a colon.

Usage

simulatedColons

Format

Five simulated samples of elliptical tubes, modeled after a reference structure resembling a colon.

**Source**

Generated and stored in the package's 'data/' folder.

---

simulate_etube	<i>Simulate Random Elliptical Tubes (ETReps)</i>
----------------	--

---

**Description**

Generates random samples of ETReps based on a reference tube with added variation.

**Usage**

```
simulate_etube(
  referenceTube,
  numberOfSimulation,
  sd_v = 10^-10,
  sd_psi = 10^-10,
  sd_x = 10^-10,
  sd_a = 10^-10,
  sd_b = 10^-10,
  rangeSdScale = c(1, 2),
  plotting = TRUE
)
```

**Arguments**

referenceTube	List containing ETRep information as the reference.
numberOfSimulation	Integer, number of random samples.
sd_v	Standard deviations for various parameters.
sd_psi	Standard deviations for various parameters.
sd_x	Standard deviations for various parameters.
sd_a	Standard deviations for various parameters.
sd_b	Standard deviations for various parameters.
rangeSdScale	Numeric range for random scaling.
plotting	Logical, enables visualization of samples (default is FALSE).

**Value**

List of random ETReps.

References

Taheri, M., Pizer, S. M., & Schulz, J. (2024). "The Mean Shape under the Relative Curvature Condition." arXiv. doi:10.48550/arXiv.2404.01043

Taheri Shalmani, M. (2024). "Shape Statistics via Skeletal Structures." University of Stavanger. doi:10.13140/RG.2.2.34500.23685

Examples

```
# Load tube
data("colon3D")
#Set Parameters
sd_v<-sd_psi<-1e-03
sd_x<-sd_a<-sd_b<-1e-04
numberOfSimulation<-3
random_Tubes<-
  simulate_etube(referenceTube = colon3D,
                 numberOfSimulation = numberOfSimulation,
                 sd_v = sd_v,
                 sd_psi = sd_psi,
                 sd_x = sd_x,
                 sd_a = sd_a,
                 sd_b = sd_b,
                 rangeSdScale = c(1, 2),
                 plotting = FALSE)

# Plotting
rgl::open3d()
for (i in 1:numberOfSimulation) {
  plot_Elliptical_Tube(tube = random_Tubes[[i]],
                      plot_frames = FALSE,
                      plot_skeletal_sheet = FALSE,
                      plot_r_project = FALSE,
                      plot_r_max = FALSE,
                      add = TRUE)
}
```

---

tube_A	<i>Data</i>
--------	-------------

---

Description

A tube with 204 elliptical cross-sections.

Usage

tube\_A

Format

A list containing the information of an e-tube with 204 elliptical cross-sections

Source

Generated and stored in the package’s ‘data/’ folder.

---

tube_B	<i>Data</i>
--------	-------------

---

Description

A tube with 204 elliptical cross-sections.

Usage

tube\_B

Format

A list containing the information of an e-tube with 204 elliptical cross-sections

Source

Generated and stored in the package’s ‘data/’ folder.

---

tube_Surface_Mesh	<i>Create surface mesh of a tube</i>
-------------------	--------------------------------------

---

Description

Create surface mesh of a tube

Usage

```
tube_Surface_Mesh(  
  tube,  
  meshType = "quadrilateral",  
  plotMesh = TRUE,  
  color = "blue",  
  decorate = TRUE  
)
```

Arguments

- |          |  |
|----------|--|
| tube     | List containing ETRep details.   |
| meshType | String, either "quadrilateral" or "triangular" definig the type of mesh. |
| plotMesh | Logical, enables plotting of the mesh (default is TRUE).                 |
| color    | String, defining the color of the mesh (default is 'blue').              |
| decorate | Logical, enables decorating the plot (default is TRUE).                  |



**Value**

An object from `rgl::mesh3d` class

**Examples**

```
quad_mesh<-tube_Surface_Mesh(tube = ETRep::tube_B,  
                             meshType = "quadrilateral",  
                             plotMesh = TRUE,  
                             decorate = TRUE,  
                             color = "orange")  
tri_mesh<-tube_Surface_Mesh(tube = ETRep::tube_B,  
                             meshType = "triangular",  
                             plotMesh = TRUE,  
                             decorate = TRUE,  
                             color = "green")
```

# Index

## \* datasets

- colon3D, [3](#)
- simulatedColons, [13](#)
- tube\_A, [15](#)
- tube\_B, [16](#)

check\_Tube\_Legality, [2](#)  
colon3D, [3](#)  
create\_Elliptical\_Tube, [3](#)

elliptical\_Tube\_Euclideanization, [5](#)

intrinsic\_Distance\_Between2tubes, [5](#)  
intrinsic\_mean\_tube, [6](#)  
intrinsic\_Transformation\_Elliptical\_Tubes,  
[7](#)

nonIntrinsic\_Distance\_Between2tubes, [9](#)  
nonIntrinsic\_mean\_tube, [10](#)  
nonIntrinsic\_Transformation\_Elliptical\_Tubes,  
[11](#)

plot\_Elliptical\_Tube, [12](#)

simulate\_etube, [14](#)  
simulatedColons, [13](#)

tube\_A, [15](#)  
tube\_B, [16](#)  
tube\_Surface\_Mesh, [16](#)