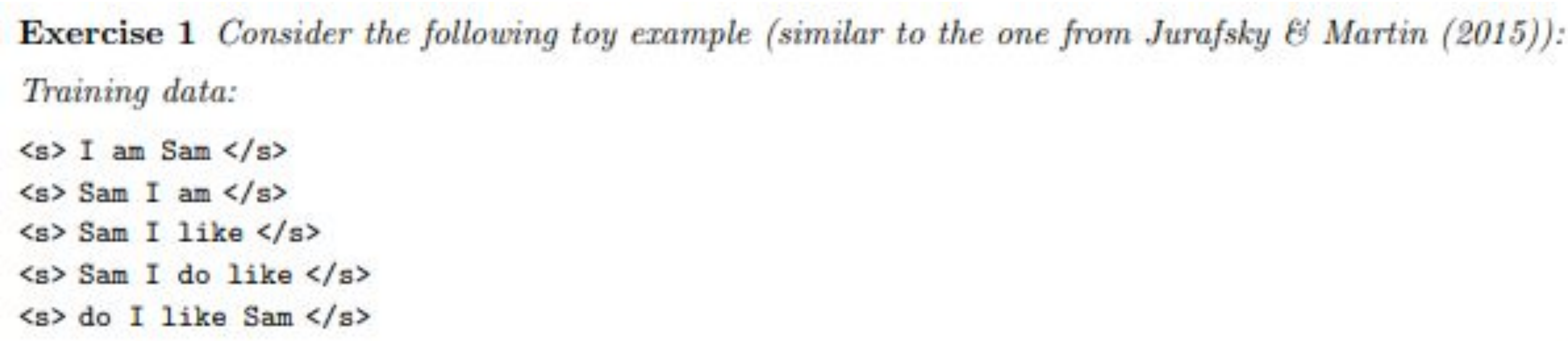
This is AI4001

GCR : t37g47w

N Gram Language Model

N gram

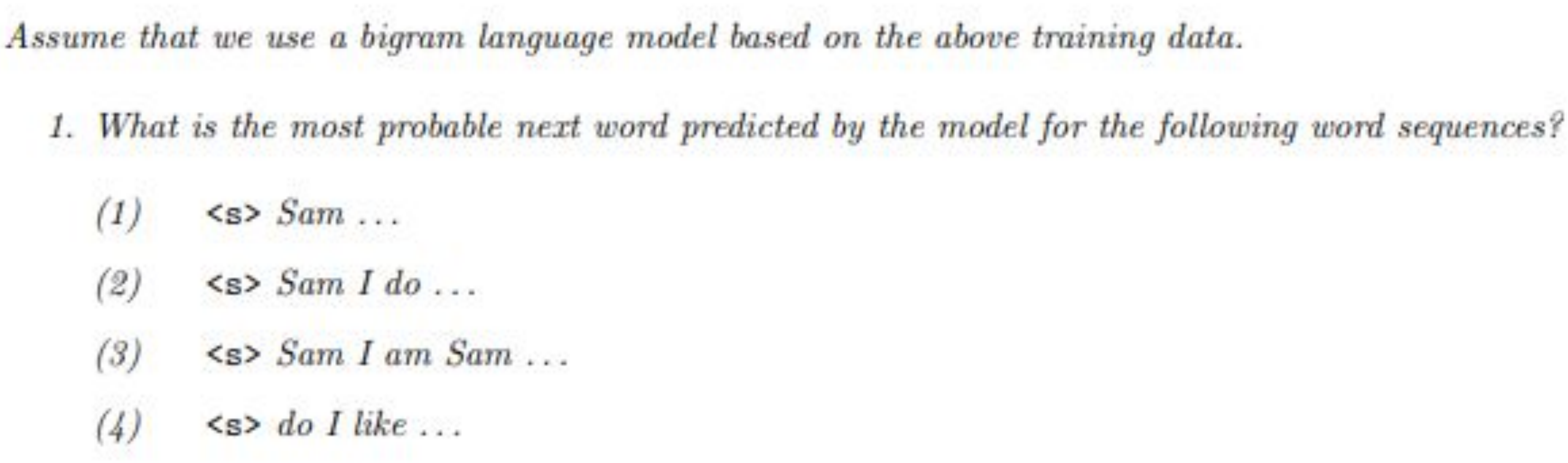


Exercise 1 *Consider the following toy example (similar to the one from Jurafsky & Martin (2015)):*

Training data:

```
<s> I am Sam </s>
<s> Sam I am </s>
<s> Sam I like </s>
<s> Sam I do like </s>
<s> do I like Sam </s>
```

N gram



Assume that we use a bigram language model based on the above training data.

1. *What is the most probable next word predicted by the model for the following word sequences?*

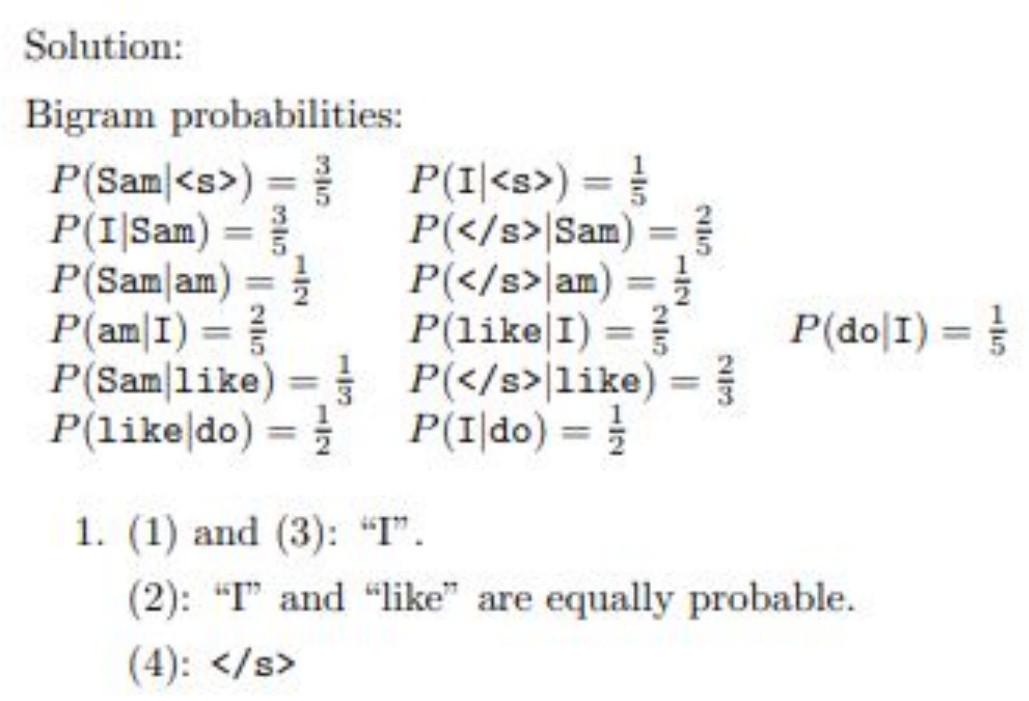
   (1) `<s>` *Sam ...*

   (2) `<s>` *Sam I do ...*

   (3) `<s>` *Sam I am Sam ...*

   (4) `<s>` *do I like ...*

N gram



Solution:

Bigram probabilities:

$P(\texttt{Sam}|\texttt{<s>}) = \frac{3}{5}$ $\quad P(\texttt{I}|\texttt{<s>}) = \frac{1}{5}$

$P(\texttt{I}|\texttt{Sam}) = \frac{3}{5}$ $\quad P(\texttt{</s>}|\texttt{Sam}) = \frac{2}{5}$

$P(\texttt{Sam}|\texttt{am}) = \frac{1}{2}$ $\quad P(\texttt{</s>}|\texttt{am}) = \frac{1}{2}$

$P(\texttt{am}|\texttt{I}) = \frac{2}{5}$ $\quad P(\texttt{like}|\texttt{I}) = \frac{2}{5}$ $\quad P(\texttt{do}|\texttt{I}) = \frac{1}{5}$

$P(\texttt{Sam}|\texttt{like}) = \frac{1}{3}$ $\quad P(\texttt{</s>}|\texttt{like}) = \frac{2}{3}$

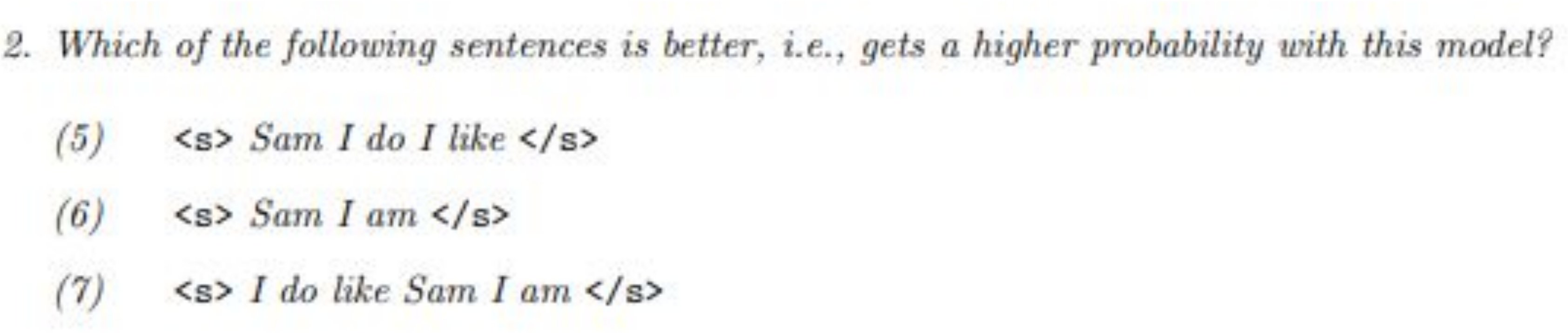
$P(\texttt{like}|\texttt{do}) = \frac{1}{2}$ $\quad P(\texttt{I}|\texttt{do}) = \frac{1}{2}$

1. (1) and (3): "I".

   (2): "I" and "like" are equally probable.

   (4): `</s>`

N gram



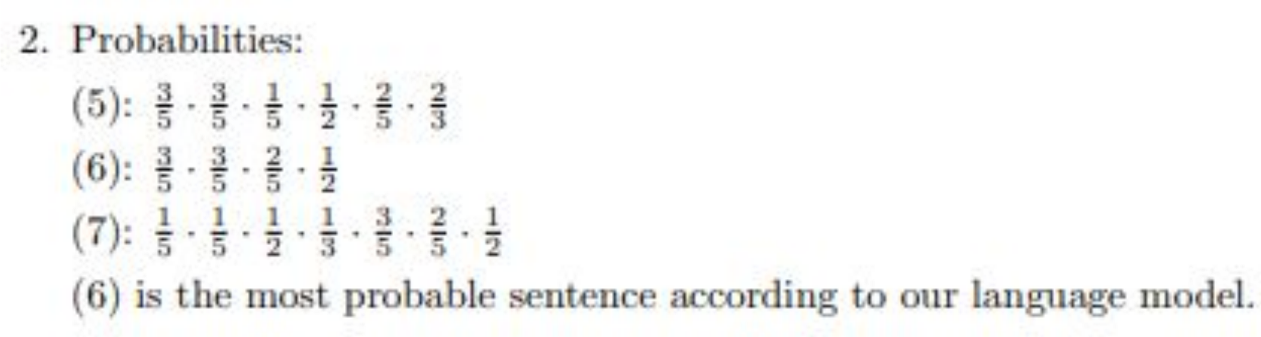
2. *Which of the following sentences is better, i.e., gets a higher probability with this model?*

(5) <s> *Sam I do I like* </s>

(6) <s> *Sam I am* </s>

(7) <s> *I do like Sam I am* </s>

N gram



2. Probabilities:

(5): $\frac{3}{5} \cdot \frac{3}{5} \cdot \frac{1}{5} \cdot \frac{1}{2} \cdot \frac{2}{5} \cdot \frac{2}{3}$

(6): $\frac{3}{5} \cdot \frac{3}{5} \cdot \frac{2}{5} \cdot \frac{1}{2}$

(7): $\frac{1}{5} \cdot \frac{1}{5} \cdot \frac{1}{2} \cdot \frac{1}{3} \cdot \frac{3}{5} \cdot \frac{2}{5} \cdot \frac{1}{2}$

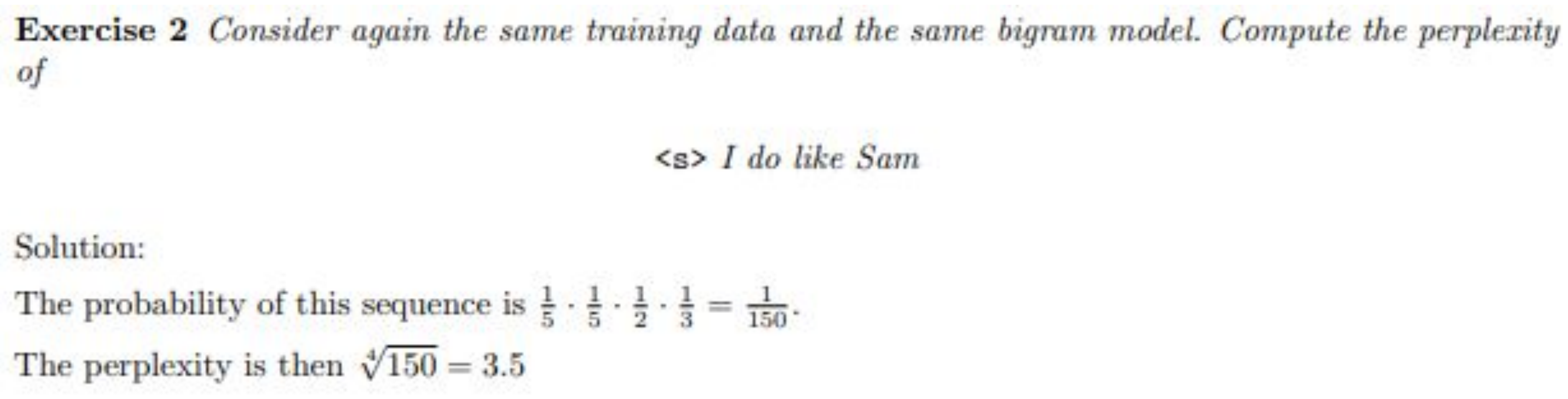
(6) is the most probable sentence according to our language model.

N Gram

Do exercise 1 and 2 for trigram.

$$P(W3|W1,W2)= \frac{Count(W1,W2)}{Count(W1,W2,W3)}$$

Perplexity



Exercise 2 *Consider again the same training data and the same bigram model. Compute the perplexity of*

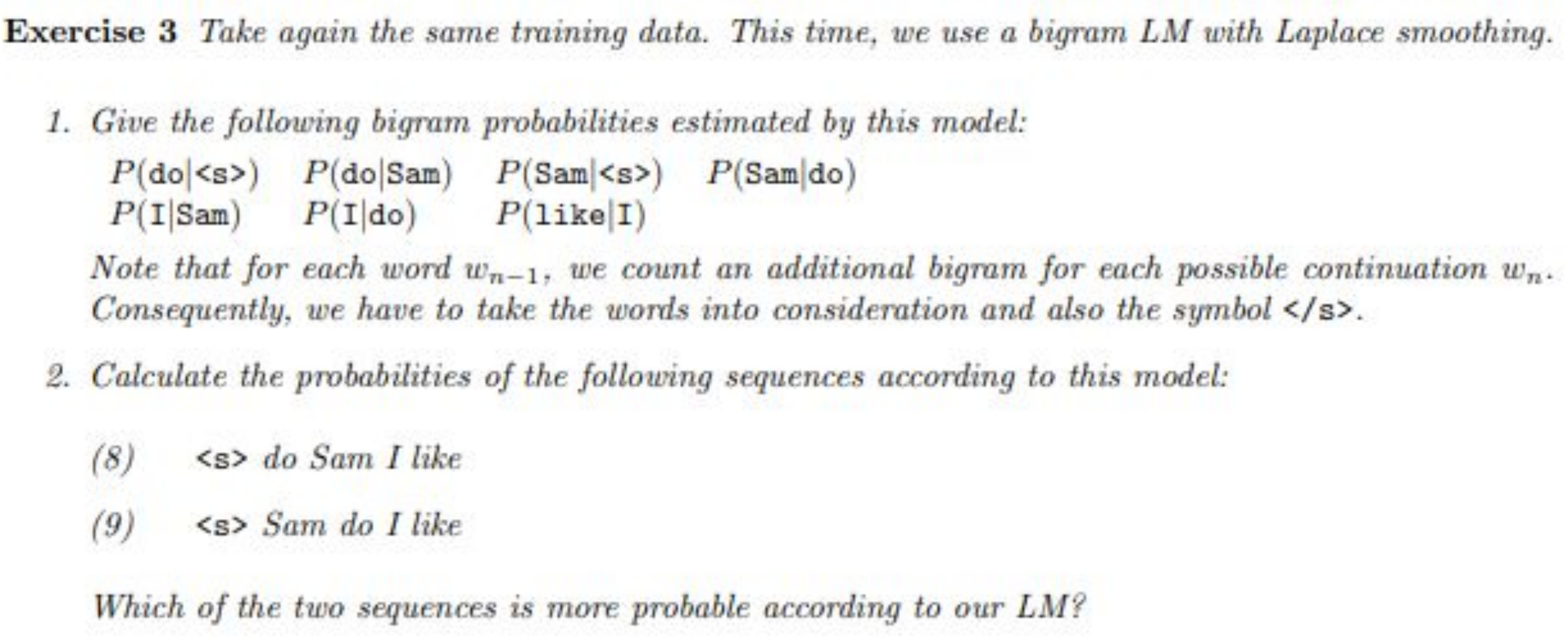
$$\texttt{<s>}\ \textit{I do like Sam}$$

Solution:

The probability of this sequence is $\frac{1}{5} \cdot \frac{1}{5} \cdot \frac{1}{2} \cdot \frac{1}{3} = \frac{1}{150}$.

The perplexity is then $\sqrt[4]{150} = 3.5$

N GRAM



Exercise 3 *Take again the same training data. This time, we use a bigram LM with Laplace smoothing.*

1. *Give the following bigram probabilities estimated by this model:*

   $P(\texttt{do}|\texttt{<s>})$ $P(\texttt{do}|\texttt{Sam})$ $P(\texttt{Sam}|\texttt{<s>})$ $P(\texttt{Sam}|\texttt{do})$
   $P(\texttt{I}|\texttt{Sam})$ $P(\texttt{I}|\texttt{do})$ $P(\texttt{like}|\texttt{I})$

   Note that for each word w_{n-1}, we count an additional bigram for each possible continuation w_n. Consequently, we have to take the words into consideration and also the symbol `</s>`.

2. *Calculate the probabilities of the following sequences according to this model:*

   (8) `<s>` *do Sam I like*

   (9) `<s>` *Sam do I like*

   Which of the two sequences is more probable according to our LM?

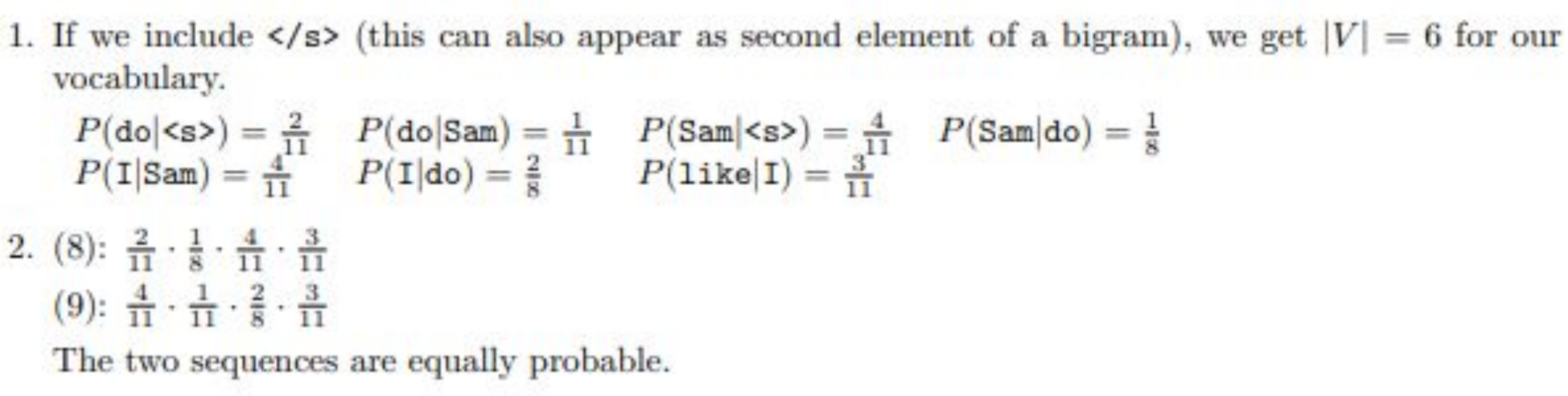
MLE estimate:

$$P_{MLE}(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})}$$

Add-1 estimate:

$$P_{Add-1}(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i) + 1}{c(w_{i-1}) + V}$$

N GRAM



1. If we include `</s>` (this can also appear as second element of a bigram), we get $|V| = 6$ for our vocabulary.

   $P(\texttt{do}|\texttt{<s>}) = \frac{2}{11}$ $P(\texttt{do}|\texttt{Sam}) = \frac{1}{11}$ $P(\texttt{Sam}|\texttt{<s>}) = \frac{4}{11}$ $P(\texttt{Sam}|\texttt{do}) = \frac{1}{8}$
   $P(\texttt{I}|\texttt{Sam}) = \frac{4}{11}$ $P(\texttt{I}|\texttt{do}) = \frac{2}{8}$ $P(\texttt{like}|\texttt{I}) = \frac{3}{11}$

2. (8): $\frac{2}{11} \cdot \frac{1}{8} \cdot \frac{4}{11} \cdot \frac{3}{11}$
   (9): $\frac{4}{11} \cdot \frac{1}{11} \cdot \frac{2}{8} \cdot \frac{3}{11}$
   The two sequences are equally probable.