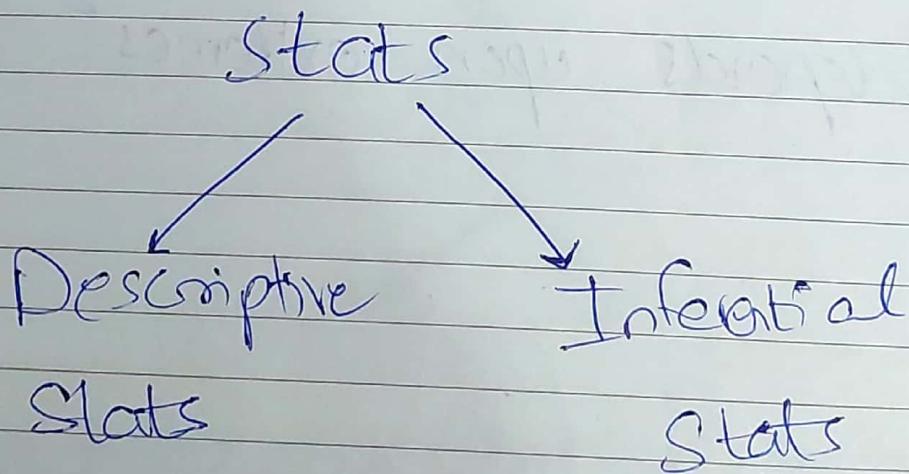


# Statistics

Date: \_\_\_\_\_

- ① collect data
- ② Summarize/organize
- ③ Analyze /Descriptive Stat
- ④ Inferential statistic

MSM



Chapter  
"Measure of central  
tendency?"

- ① Mean - average =  $\frac{\sum x_i}{n}$   
Data =  $\frac{\text{sum}}{\text{count}}$
- ② Median - Middle value
- ③ Mode -

## Mean

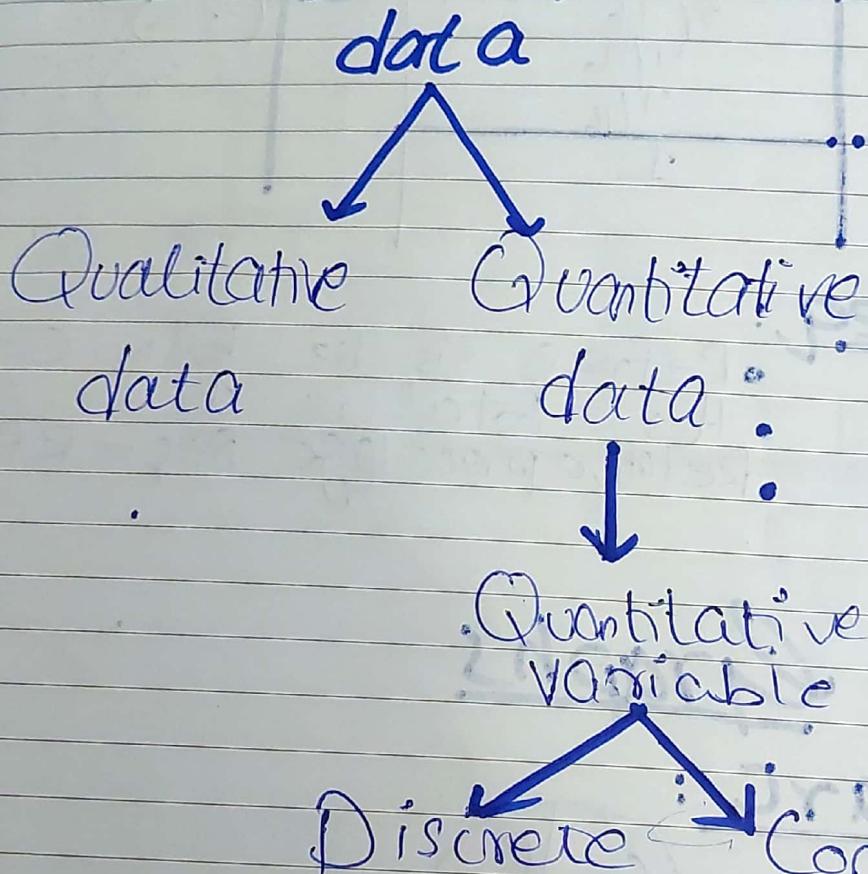
- data accumulate around point
- depends upon extremes
- 

## Median :

# Chapter 01

Date:

## Organizing and Summarizing data



Organizing qualitative data:

- tabular
- graphical

# Frequency Distribution:

Color	freq.	Relative freq.	freq. Total	Relative freq. Total	Percentage freq.
B	5	5/16			$(5/16) \times 100$
R	4	4/16			$(4/16) \times 100$
G	7	7/16			$(7/16) \times 100$
Total	16	1			

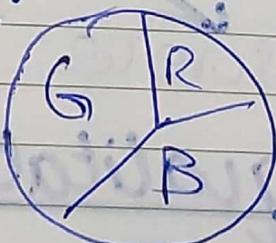
## Relative freq.:

- R-freq is lie b/w 0-1
- Its total is  $\frac{1}{1}$
- Relative percentage freq = RF  $\times 100\%$

## Graphs

### Pie Chart:

eg:-



### Formula:

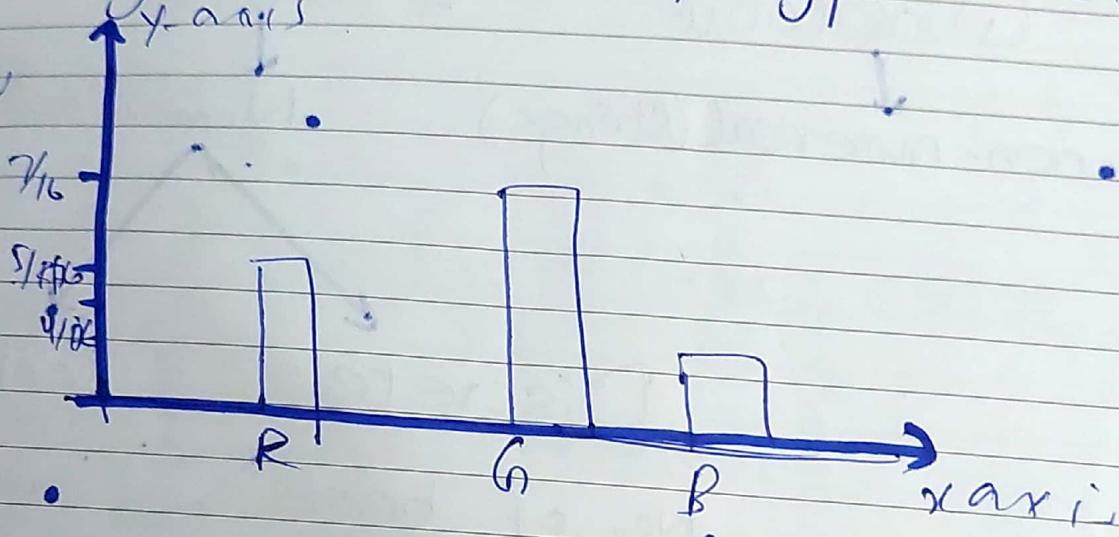
$$\frac{\text{freq}}{\text{Total freq.}} \times 360^\circ$$

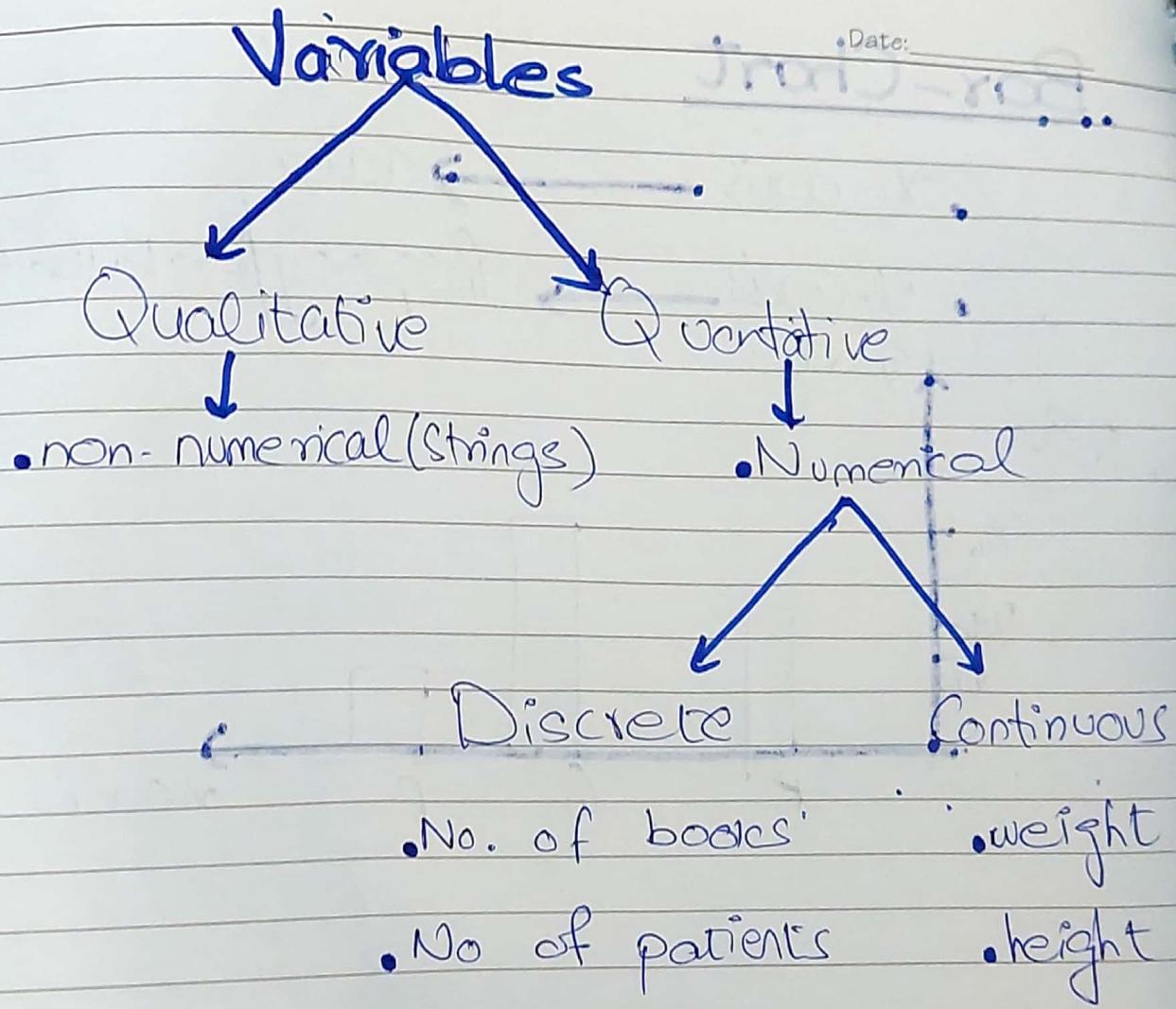
## Bar-Chart

• x-axis → data

• y-axis → Frequency / Relative freq

Relative freq





## Measurement of scales

- { **Nominal:** Non-numerical categorical  
eg: gender, religion.
- Ordinal:** Order, ranking

Interval:

- addition, subtract allowed
- Absolute zero not exists

Quantitative

Ratio:

- \* • +, -, \*, ÷

- Absolute zero exist

• Name: Quali - Norm

• Age: Quant - Ratio

• Gender: Quali - Norm

• City: Quali - Norm

• Weight: Quant - Norm Ratio

• Postal code: Quali - ~~Ratio~~ Norm

• Qualification: Quali - Norm

• Marital Status: Quali - Norm

# Dot-Plot

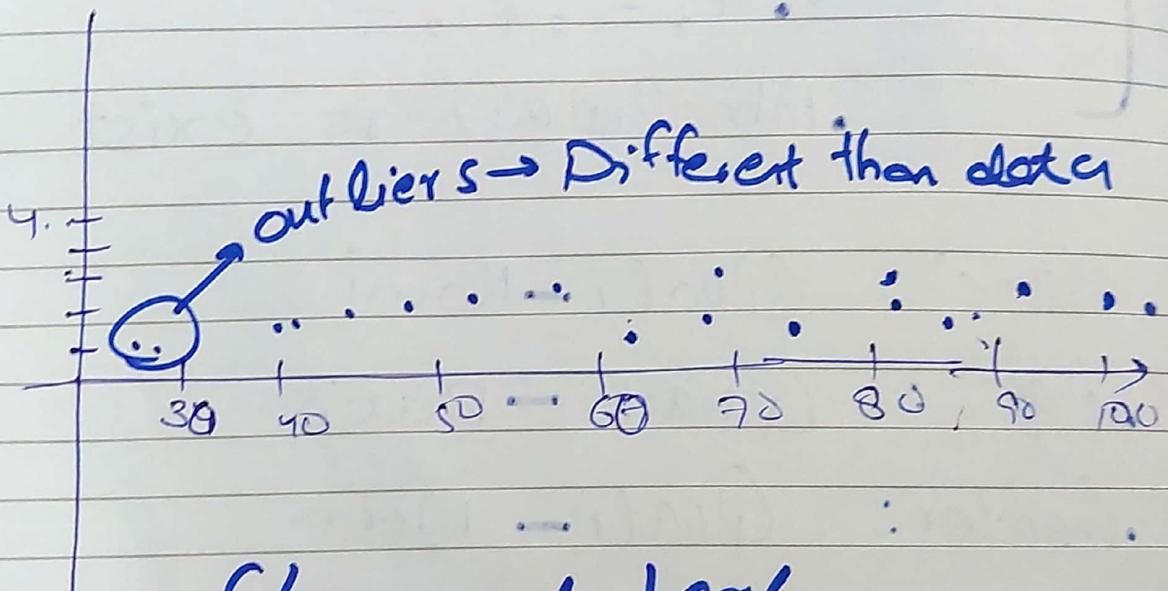
Date:

88 82 89 70 85

68 100 86 67 38

90 96 76 34 81

64 75 84 89 96



## Stem and leaf

Step	Leaves	f	Cf
3	9 4 9	3	30-60
4	.	2	61-69
5	.	2	70-
6	3 7	.	.
7	0 6	.	.
8	3 2 4 5 6 9 5 1	1	.
9	0 6 6	.	.
	0	.	.

CI	f	Midpoint	fx	C.F
30-39	3	34.5	103.5	4
40-49	8	44.5	356.0	12
50-59	10	54.5	545.0	22
60-69	7	64.5	451.5	39
70-79	7	74.5	521.5	36
80-89	4	84.5	338.0	40
89-98	3	94.5	283.5	
				2720.

$$\text{Mean} = 2, 4, 6$$

$$= \frac{2+4+6}{3} = 4$$

$$\text{Median} = \left( \frac{n+1}{2} \right)^{\text{th}} \Rightarrow 2^{\text{nd}} \text{ if } \left( \frac{n+1}{2} \right) = 2$$

1, 2, 3, 4.

$$\text{Median} = \frac{4+1}{2} = \frac{5}{2} = 2.5 \Rightarrow \text{take } \left( \frac{2^{\text{nd}} + 3}{2} \right)$$

Mod = Repetitive

$$\mu = \frac{\sum f(x)}{\sum f} = \frac{2720}{40} = 68$$

Short term investment

70	64	97	55	64	81	87	65
62	38	67	70	60	67	78	34
75	56	71	51	99	68	95	86
57	53	47	50	55	81	80	98
51	36	63	66	85	74	83	70

GROUP FREQUENCY DISTRIBUTION

Class interval	f	CF (<)	CF (>)	relative freq, CB
30 - 39	3	3	40	3/40 29.5 - 39.5
40 - 49	1	4	37	1/40 39.5 - 49.5
50 - 59	8	12	36	8/40
60 - 69	10	22	28	.
70 - 79	7	29	18	.
80 - 89	7	36	11	.
90 - 99	4	40	4	4/40 89.5 - 99.5

Total = 40 Mid point ( $x$ ) ( $\frac{a+b}{2}$ )

34.5

44.5

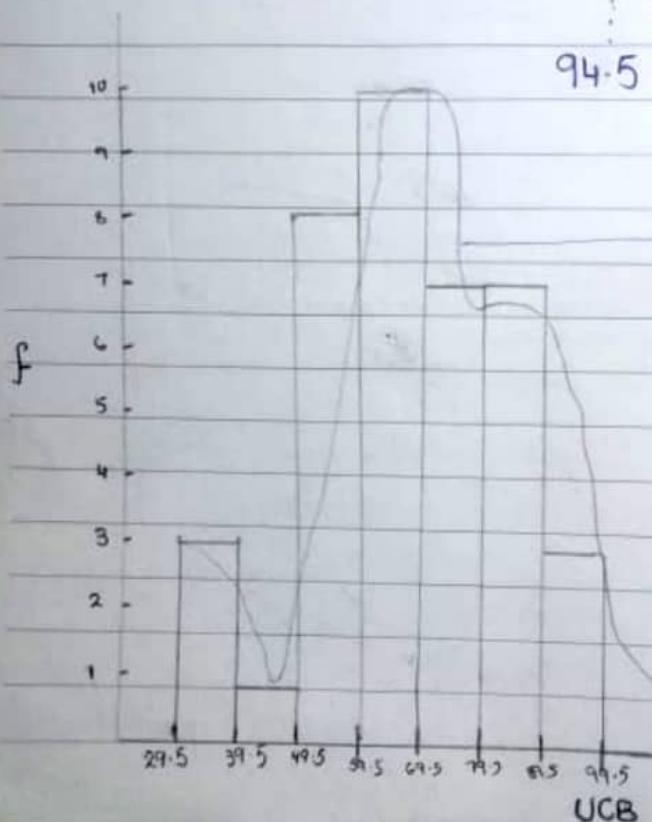
54.5

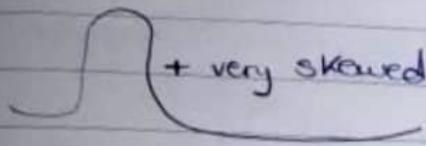
94.5

-bell shaped  
frequency polygon

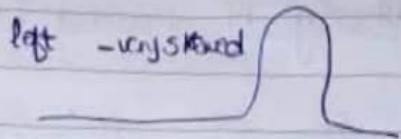
Mean = Median = Mode

-single peak  
-unimodal

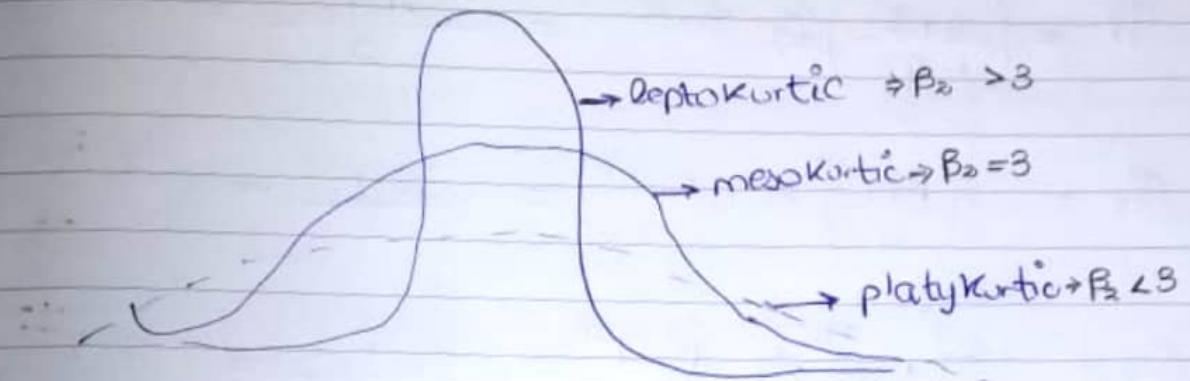




mean  $\rightarrow$  median  $\rightarrow$  mode



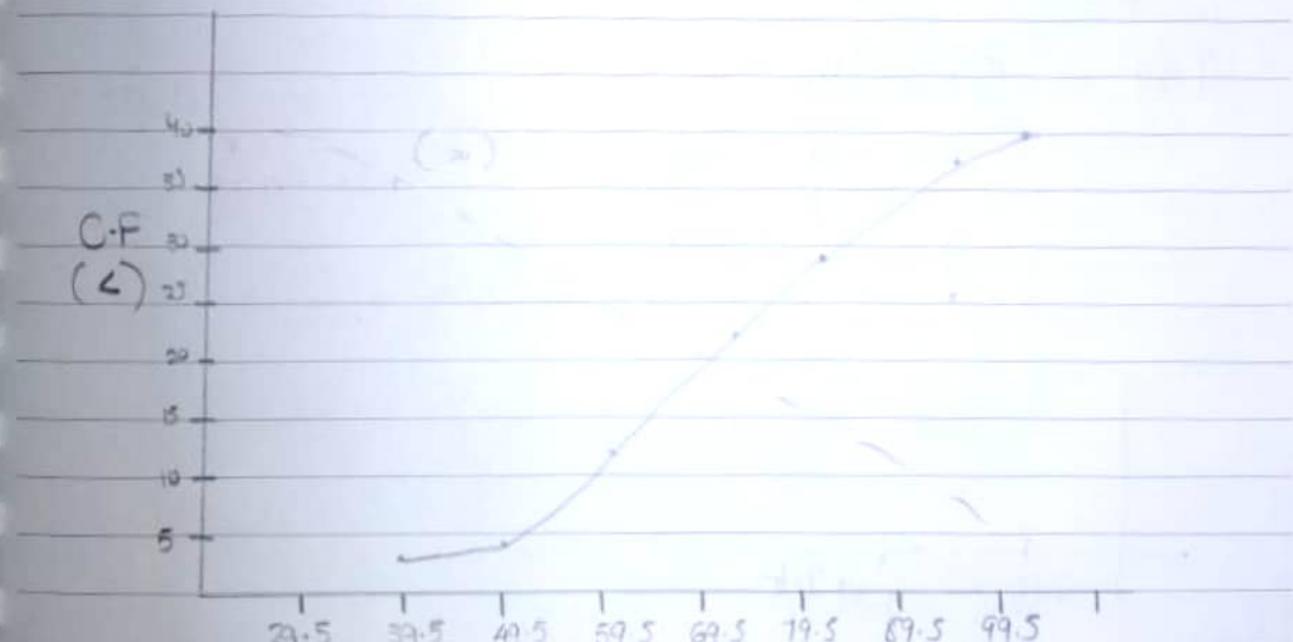
mode  $\rightarrow$  median  $\rightarrow$  mean



Outliers Sudden large or small values (eg 1, 2, 3, 20)

O.G.F.

Cumulative freq. graph



CB

$$\text{Median} = l + \frac{h}{f} \left( \frac{cf - cf}{2} \right)$$

Date: \_\_\_\_\_

~~Median =  $\frac{l + h}{2}$~~

$h \rightarrow \text{class size}$ .

$$\frac{cf}{2} = \frac{40}{2} = 20$$

$$\text{Median} = 59.5 + \frac{10}{10} \left[ \frac{40}{2} - 12 \right]$$

Mod = ~~l +  $\frac{f_m - f_1}{2f_m - f_1 - f_2}$~~ ,

$$= l + h \left[ \frac{f_m - f_1}{2f_m - f_1 - f_2} \right]$$

$$Q = Q_i + CB \text{ of Median}$$

$h = \text{Change}$

$f = \text{free}$

C.F = Proceday  
f.

$$Q_1 = l + \frac{h}{f} \left[ \frac{\Sigma f}{4} - C.F \right]$$

Q\_2 = Median

$$Q_3 = l + \frac{h}{f} \left[ \frac{3}{4} \Sigma f - C.F \right]$$

# Box-Plot

$$Q_1 = \left( \frac{n+1}{4} \right)^{\text{th}}$$

$$Q_2 = \left( \frac{n+1}{2} \right)^{\text{th}}$$

$$Q_3 = \frac{3(n+1)}{4}^{\text{th}}$$

$n$  = no. of terms

Example 17:

$$Q_1 = \left( \frac{n+1}{4} \right)^{\text{th}} = \left( \frac{20+1}{4} \right)^{\text{th}} = \frac{21}{4} = 5.3$$

$$\text{So, } \frac{21+25}{2} = 23, \text{ so } \left( \frac{5^{\text{th}} + 6^{\text{th}}}{2} \right) \text{ terms}$$

$$Q_2 = \left( \frac{n+1}{2} \right)^{\text{th}} = 10.5 = \frac{30+31}{2} = 30.5$$

$$Q_3 = \frac{3(n+1)}{4} = \frac{3(21)}{4}^{\text{th}} = 15.75 = \frac{35+36}{2} = 35.5$$

Date:

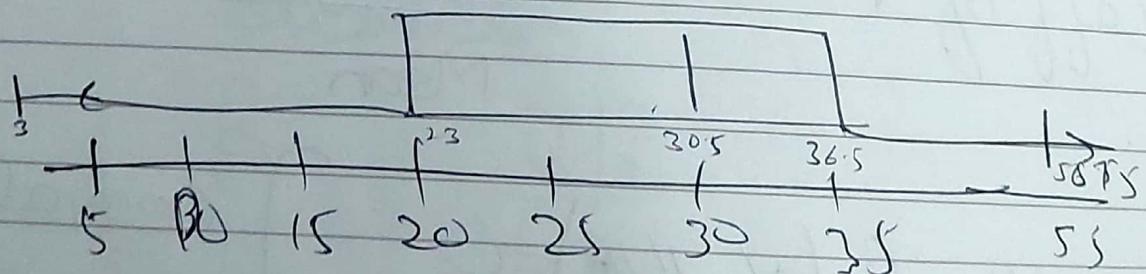
- $L = Q_1 - 1.5(\text{IQR})$
- $U = Q_3 + 1.5(\text{IQR})$
- $\text{IQR} = Q_3 - Q_1$

$$\text{IQR} = Q_3 - Q_1$$

$$\text{IQR} = 36.5 - \cancel{26.5} \cancel{23}$$

$$\textcircled{2} L = 2.75 \quad \left. \begin{array}{l} \text{outliers less than} \\ \text{outliers more than} \end{array} \right\}$$

$$U = 36.75 \quad \left. \begin{array}{l} \text{outliers more than} \\ \text{outliers less than} \end{array} \right\}$$



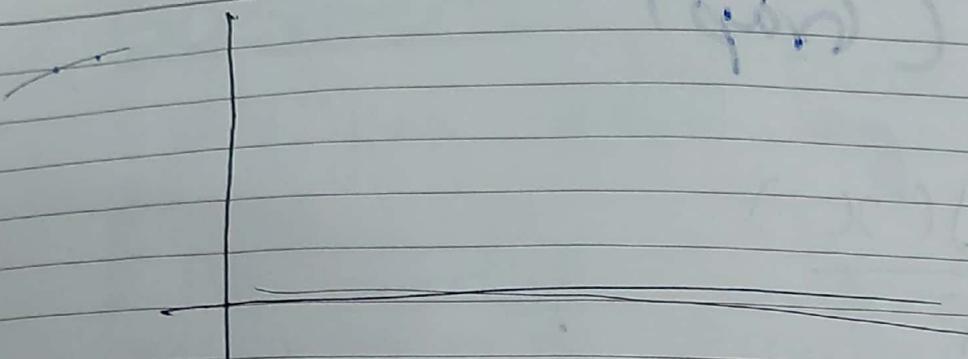
## Example 19:

### Variance

$$\begin{aligned}
 & \text{mean} \\
 & \text{u-mu} \\
 & \text{variance} \\
 & \text{sum} \\
 & = \frac{\sum (x - \bar{x})^2}{n} \Rightarrow \text{for ungroup} \\
 & = \sum f(x - \bar{x})^2 \Rightarrow \text{for group}
 \end{aligned}$$

$\Sigma$  Coff of variance =  $\frac{\text{standard deviation} \times 100}{\text{Mean}}$

$$\begin{aligned}
 \mu_1 &= E(x - \mu) = 0 && \text{central} \\
 \mu_2 &= E(x - \mu)^2 = 0 && \text{movement} \\
 \mu_3 &= E(x - \mu)^3 = 0 \\
 \mu_4 &= E(x - \mu)^4 = 0
 \end{aligned}$$



$$\text{Mean} = \bar{M} = \frac{\sum x}{n}$$

$$\text{Mean} = 193.125$$

## Standard Deviation

$$\sqrt{\sigma^2} = \sqrt{\text{Variance}}$$

## Skewness

$$\beta_1 = \frac{M_3^2}{M_2^2}$$

## Kurtosis

$$\beta_2 = \frac{M_4}{M_2^2}$$

Date:

# Media (Graph)

$$\frac{(\varepsilon_f)(x)}{\varepsilon_f}$$

nothing broken

223745/2

220705

## Experiment:

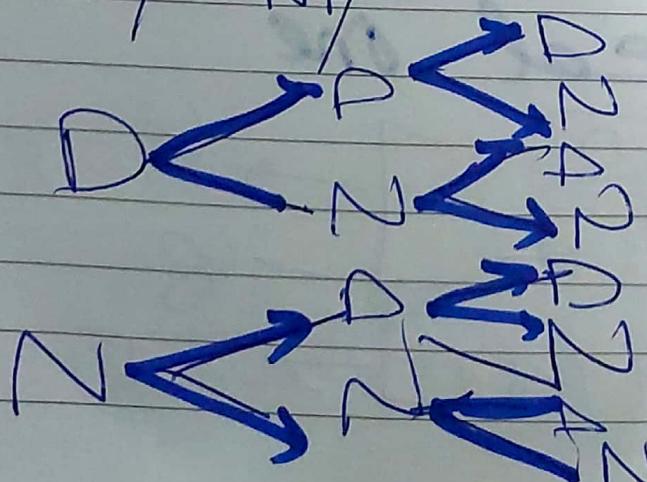
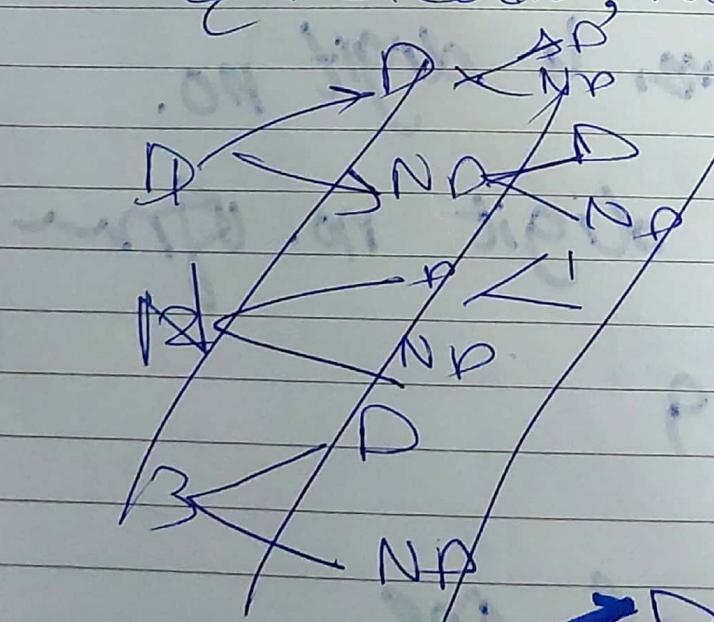
Any process or activity gives data. **eg:** Rolling dice

- All possible outcomes of experiment is sample space.

**eg:** Rolling dice =  $\{0, 1, 2, 3, 4, 5, 6\}$

Q: Suppose 3 items Defective  
Non-defective

$\Sigma$  Defective, Nondefective?



Mutually exclusive

Date: \_\_\_\_\_

AnB + φ

No. from 2, 4, 6, 8

i) Rep allowed

$$4 \times 4 \times 4 = 64$$

ii) Rep Not allowed

$$4 \times 3 \times 2 = 24$$

Q: How many even 4 digit no.

form from digit no. given

0, 1, 2, 5, 6, 9

i) Digit used one

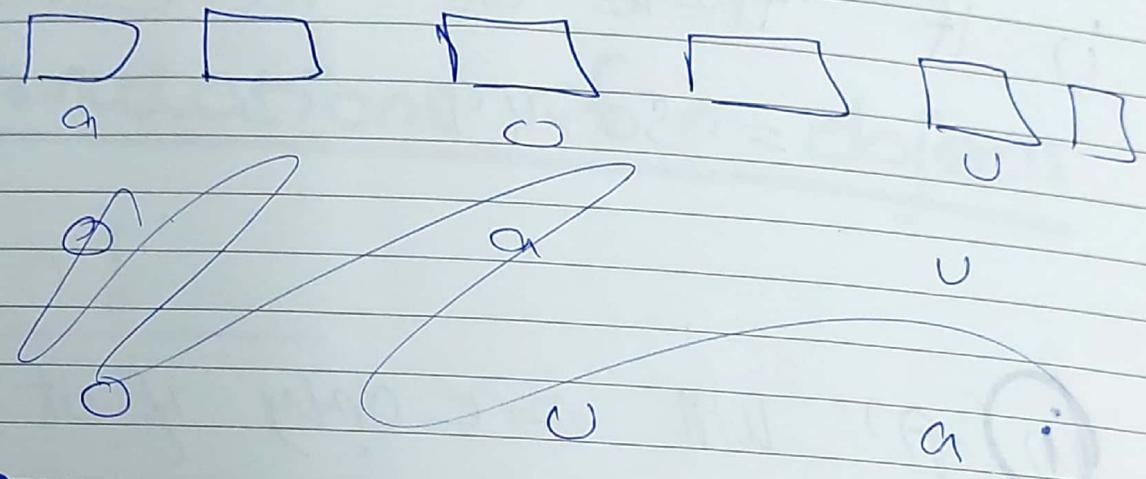
$$\boxed{5} \quad \boxed{4} \quad \boxed{3} \quad \boxed{0} \quad \boxed{1} \rightarrow 60$$

$$\boxed{4} \quad \boxed{5} \quad \boxed{3} \quad \boxed{6} \quad \boxed{0} \rightarrow 48$$

$$\boxed{5} \quad \boxed{4} \quad \boxed{3} \quad \boxed{6} \quad \boxed{1} \rightarrow ?$$

**Q** Favour Fanour Date: \_\_\_\_\_

So, vowels occupy even space



## Combination and Permutation

Arrangement

order does not matter

Arrangement

Order matters

**Q**

Stat Maths, Physics

$$\frac{n!}{(n-r)!} = \frac{n!}{r!(n-r)!}$$

$$= 3!$$

**Q**

If 2 books are even

$$\frac{n!}{(n-r)!} = \frac{3!}{(3-2)!} = 6$$

$${}^n C_r \cdot {}^n P_r = \frac{n!}{(n-r)!} \cdot \frac{n!}{r!} = \frac{n!}{(n-r)!r!}$$

No. of items = 50  
Chose = 2

i) If these are not restricted.  
 $= 50 \times 49$

(i) a) Will care only if it product  
involves A & B together.

b and c some together or not

$$2 \times 48 + 48 \times 47$$

=

D & E not some together

one tag = 2 #

$$\text{All} = 50 \times 49$$

$$\text{Not} = (50 \times 49) - 2 =$$

- If to be in circle  
fix  $(n-1)!$

## Permutations of $n$ objects

$$\frac{n!}{n_1! n_2! \cdots n_r!}$$

Total object =  ~~$\frac{n!}{n_1! n_2! \cdots n_r!}$~~

for  $\underbrace{9995}$ . No. of permutation =  $\frac{4!}{\text{set } 3! \text{ set } 2!}$

$$\frac{4!}{3! 2!}$$

↓      ↓  
Same    Same  
↓      ↓  
?      1

No. of permutation of Statistics =  $\frac{10!}{3! 3! 2!}$

In how many ways can  $2R, 3B, 6G$  be arranged?

So, no. ways color together = 91.

Date: 21/3/14

• 10.  $B, G$   
3    2

# Probability

Date: \_\_\_\_\_

Measurement of chance

↳

subjective

- personal experience
- judgments
- expertise

objective

- Classical approach

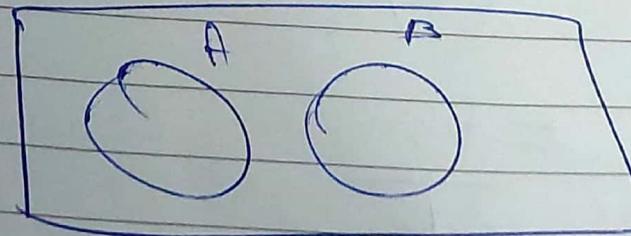
•  $P(E) = \frac{\text{Favourable outcome}}{\text{all probability}}$

$$0 \leq P(E) \leq 1$$

• Sum of possibilities =

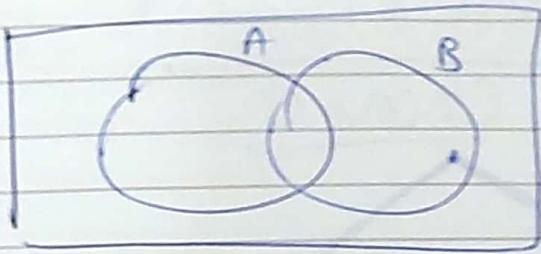
Mutually exclusive

$$\cdot P(A_1 \cup A_2) = P(A_1) + P(A_2)$$



## Non-Mutually Exclusive

$$P(A_1 \cup A_2) = P(A_1) + P(A_2) - P(A_1 \cap A_2)$$



Q1: A coin is tossed twice.  
What is probability of Head  
= HH, TH, HT, TT.

$$P(\text{At least 1 Head}) = \frac{3}{4}$$

$$P(1 \text{ Head}) = \frac{1}{2} = \frac{2}{4}$$

$$P(TT) = \frac{1}{4}$$

$$P(HH) = \frac{1}{4}$$

$$P(\text{Head}) = \frac{1}{2} = \frac{3}{6}$$

Date: 1, 2, 3, 3, 5, 6

Q2

An dice rolled once

$$P(\text{Even}) = \frac{3}{6}$$

$$P(4) = \frac{1}{6}$$

$$P(4 \text{ or higher}) = \frac{3}{6} = \frac{1}{2}$$

$$P(\text{odd}) = 0.$$

$$P(1 \text{ to } 6) = 1$$

Q3

A die is loaded such that over number is twice as likely to occur

- If  $E$  is event then no less than 4 occur.

$$\{1, 2, 3, 4, 5, 6\}$$

$$\omega, 2\omega, w, 2w, w, 2w \} \\ = \frac{1}{9}$$

$$P(E) = P(\tau < 6) = \frac{1}{9} + \frac{2}{9} + \frac{1}{9}$$

$$\frac{-4}{9}$$

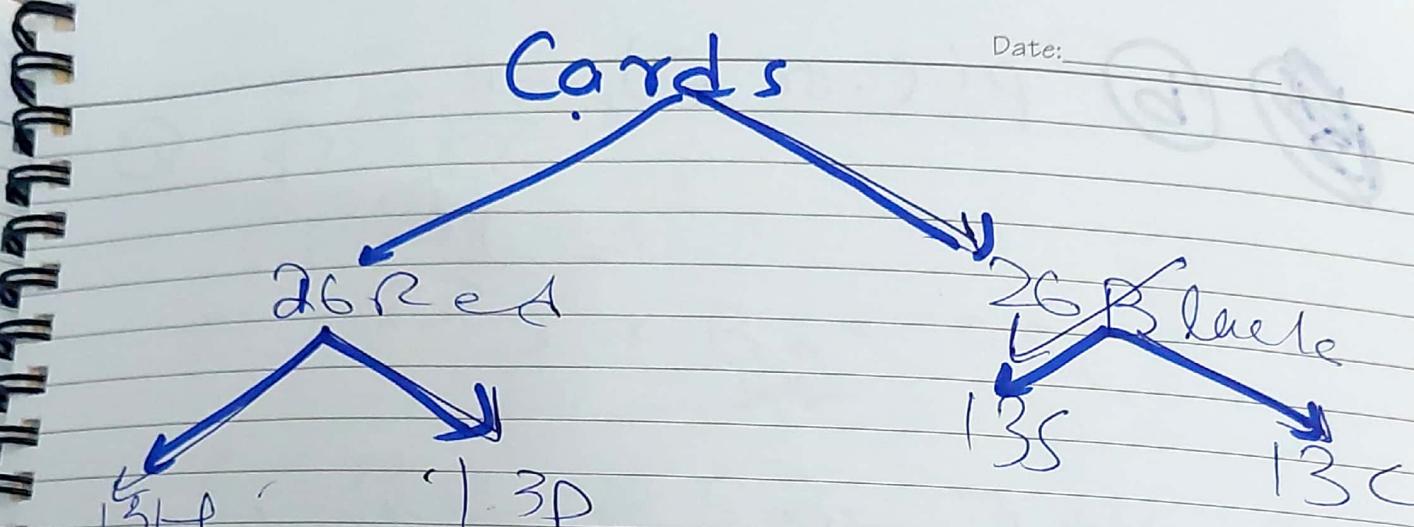
Q4 Two balanced dice are rolled once

$$\begin{aligned}
 S = \{ &(1,1), (1,2), (1,3), (1,4), (1,5), (1,6) \\
 &(2,1), (2,2), (2,3), (2,4), (2,5), (2,6) \\
 &(3,1), (3,2), (3,3), (3,4), (3,5), (3,6) \\
 &(4,1), (4,2), (4,3), (4,4), (4,5), (4,6) \\
 &(5,1), (5,2), (5,3), (5,4), (5,5), (5,6) \\
 &(6,1), (6,2), (6,3), (6,4), (6,5), (6,6)
 \}
 \end{aligned}$$

a)  $P(\text{sum of } 11) = \frac{2}{36}$

b)  $P(\text{sum of both dice} \leq 6) = \frac{6}{36}$

(sum of 13)  $\geq 0$



**Q** A card is drawn Random

(a)  $P(\text{Jack}) = \frac{4}{52}$

(b)  $P(\text{Not Jack}) = 1 - \frac{4}{52} = \frac{48}{52}$

**Q** 25 Indefinite 10 Matrix 10  
8 Chem

Total = 53.

(a)  $P(\text{Indefinite}) = \frac{25}{53}$

(b)  $P(C \text{ or } E) = \frac{8}{53} + \frac{10}{53}$   
 $= \frac{18}{53}$

Q Prob of getting a total of  
 ≥ 11 when a pair of dice is  
 rolled

$$P(7 \text{ or } 11) = \frac{8}{36} = \frac{4}{18} = \frac{2}{9}$$

Q  $P(\text{spec}) = 0.99$ .

$$P(\text{for large}) = \frac{1 - 0.99}{2}$$

$$P(\text{large than } 1990) = 1 - P(\text{small})$$

$$= 1 - 0.605$$

$$= 0.395$$

$$Q) P(S) = 7$$

$$P(B) = 4.$$

$$P(\text{either } S \text{ or } B \text{ or both}) = 0.8$$

$$\textcircled{a} \quad P(B \text{ or } S \text{ or both}) = 7 + 4 - P(A \cap B)$$

$$0.8 = 7 + 4 - A(A \cap B)$$

$$= 0.3.$$

$$\textcircled{b} \quad P(\sim \text{Both}) = 1 - 0.8.$$

$$\boxed{1 - 0.8 = 0.2}$$

**Q:**

$$P(\text{break defect}) = 0.25$$

$$P(\text{transistor}) = 0.12$$

$$P(\text{full sig}) = 0.17$$

$$P(\text{other}) = 0.40$$

\textcircled{a}

$$P(\text{Break or Full or Other}) = 0.40 + 0.15$$

$$= 0.27$$

# Product Rule

Date: \_\_\_\_\_

Independent Event  $= P(AB) = P(A)P(B)$

For dependent Event  $= \underline{P(A)P(B|A)}$

$$P(B|A) = \frac{P(B \cap A)}{P(A)}$$

Q

20-fuses

15 Defective fuses

SD

$$\leftarrow P(F_1 \cap F_2)$$

$$\leftarrow P(F_1 \cdot F_2 | F_1)$$

$\frac{B}{20} \cdot \frac{4}{19}$

Q:

$$\cancel{\frac{8}{82}}$$

$$= P(S_1, S_2)$$

$$= \left(\frac{13}{52}\right) \cdot \left(\frac{12}{51}\right)$$

=

Q

$$1, 2, 3, 4, 5, 6, 7, 8, 9 = 8$$

 $\downarrow 2$ 

$$= \boxed{\frac{5}{8} \times \frac{4}{7}}$$

Q

$$P(M) = 0.25$$

$$P(S) = 0.15$$

$$P(M \cap S) = 0.10$$

Q

$$P(M|S)$$

$$= \frac{P(M \cap S)}{P(S)}$$

$$= \frac{0.10}{0.15}$$