

Converting a given NFA to DFA:

Colors:

Red: Files

Purple: Python objects (variables, dicts, etc)

Orange: State elements

Green: Functions

Blue: Arguments to functions

Algorithm:

1. Read input from `input.json`.
2. Define a dict `out` to store the definition of DFA.
3. Define two dictionaries:
 - a. `dfa`: To hold the states of DFA
 - b. `nfa`: To hold the states of NFA
4. Add the given states (0 - `n-1`) to `nfa` and every subset of set of NFA states to `dfa`
5. Define the transitions of the states as:
 - a. The transitions from subsets of single elements (in DFA) will be given by the input transition function.
 - b. The transitions from subsets of multiple elements will be given by taking union of the transitions of subsets of single elements.
6. Define the transition function in the `out` dictionary.
7. Write the `out` dict to `output.json`.

Class defined:

The class `State` contains information and methods for a state.

It contains:

- (i) `name`: The name given to the state (In case of DFA, this will consist of the subset that the state is formed of).
- (ii) `bin`: The binary index of the state (For printing).
- (iii) `In`: States which can reach the concerned state consuming a single character from the alphabet.
- (iv) `Out`: States which can be reached from the concerned state consuming single character from the alphabet.
- (v) `transitions`: Defines the next state reached on consuming different characters from the alphabet on this state.
- (vi) `addTransitions(self, letter, output, automata)`: function that adds the transition of type:

`self --letter--> output`

It also adds the current state to `In` of `output` and `output` to `Out` of `self`.

If (`automata == 'dfa'`) The function works in the `dfa` dict, else it works in `nfa` dict. (By default, `automata = 'dfa'`)

Functions:

1. `fz(set)`:

Takes an int or a set as input and returns a frozenset. (This is needed because a set is unhashable but frozenset is hashable)

2. `union(states)`:

Takes input a list of states (or a set) and returns a frozenset of the union of set of each state.

If the list (or set) is empty, it returns `frozenset({'phi'})`.

If the union of sets is not present in the current list of states in `dfa`, it adds the state to `dfa`.

3. `trans_union(letter, states)`:

Takes an input character from alphabet and a list of states and returns a combination of transitions of every state in `states` on consuming `letter`.

It is used to define the transitions of subsets of more than one element in the DFA.

4. `get_bin(x)`:

Takes an int `x` and returns binary representation of `x`.

5. `findsubsets(s, n)`:

Takes in a set `s` and an int `n` and returns a list of all subsets of `s` with `n` elements.

6. `isfinal(state)`:

Adds `state` to the set of final states of DFA if any element of `state` is in set of final states of NFA.

7. `b_s(states)`:

Takes input a set `states` and returns a list of individual states in the set.

8. `State_construction()`:

- a. First it adds the state "phi" to `dfa`.
- b. A set is defined which consists of numbers 0 - `n`-1. These represent the states of the input NFA where `n` is the number of states of the NFA.
- c. All subsets of the set of size 1 - `n`-1 are added to `dfa` and states are added to `nfa` as well.
- d. Each added state is sent to `isfinal()` function.

9. `Transition_construction()`:

- i. Defines the transition from 'phi' on every letter.
- ii. Defines the transitions of rest of the states of the DFA starting from states with only one element (Directly from the input transition function) and uses them to define the transition of rest of the states.

- iii. Finally checks if transition on any letter is still undefined and defines such transitions as:

state --letter--> "phi"

10. `Generate_output(reduce)`:

Updates the out dict with all the defined transitions.

If (`reduce == true`), the DFA is simplified before updating

Additional functions:

1. `State_reduction()`:

Simplifies the DFA.

- i. Adds all states with no element in `In` to a queue.
- ii. Starts working on the queue and removes any state in the queue from `dfa` if their `In` is empty.
- iii. On removing a state, all states in the `Out` of that state are added to the queue.
- iv. When the queue empties, all useless states have been removed.

2. `Print_Table()`:

Prints the table of transitions of various states on consuming different characters from the alphabet.

3. `nfa_run(In, curr_state)`:

Runs the NFA on given input `In`.

4. `dfa_run(ln)`:

Runs the DFA on given input `ln`

5. `testNFA_DFA()`:

Asks for a number and runs the same number of inputs on both, NFA and the DFA giving the result of both.

It asks for the input before every run.