

STA-5007: Advanced Natural Language Processing

Lecture 2: Basics of Deep Learning



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Content



- Introduction
- Model
- Optimization
- Training
- Coding

Data Analyses



- To create a function to map an input X into an output Y, Y = f(X)
- Examples:

Input X	Output Y	<u>Task</u>
Text	Text in Other Language	Translation
Text	Response	Dialog
Text	Label	Text Classification
Text	Linguistic Structure	Language Analysis

- To create such a system, we can use
 - Manual creation of rules
 - Machine learning from paired data <X, Y>

Machine Learning



- Statistical approach
 - Generalized linear model, linear regression, logistic regression
 - Gaussian mixture models
 - Support vector machine (SVM)
 - Decision trees, random forests
- Deep learning approach
 - Modeling with different deep neural networks

Why didn't They Work Before?



- Datasets too small
 - For machine translation, not really better until you have 1M+ parallel sentences (and really need a lot more)
- Optimization not well understood
 - Good initialization
 - Momentum (Adagrad/Adam) work best out-of-the-box
- Other innovations
 - Word embedding
 - Dropout, layer normalization, residual connection
 - Large-scale computing system

Deep Learning



- Modeling with deep neural networks
- Optimized on big data
- Research Contributions
 - Resource: dataset for new tasks and existing tasks, toolkit, demo
 - Algorithm: training strategy, model structure, decoding algorithm, data selection
 - Theory: optimization, evaluation, analyses

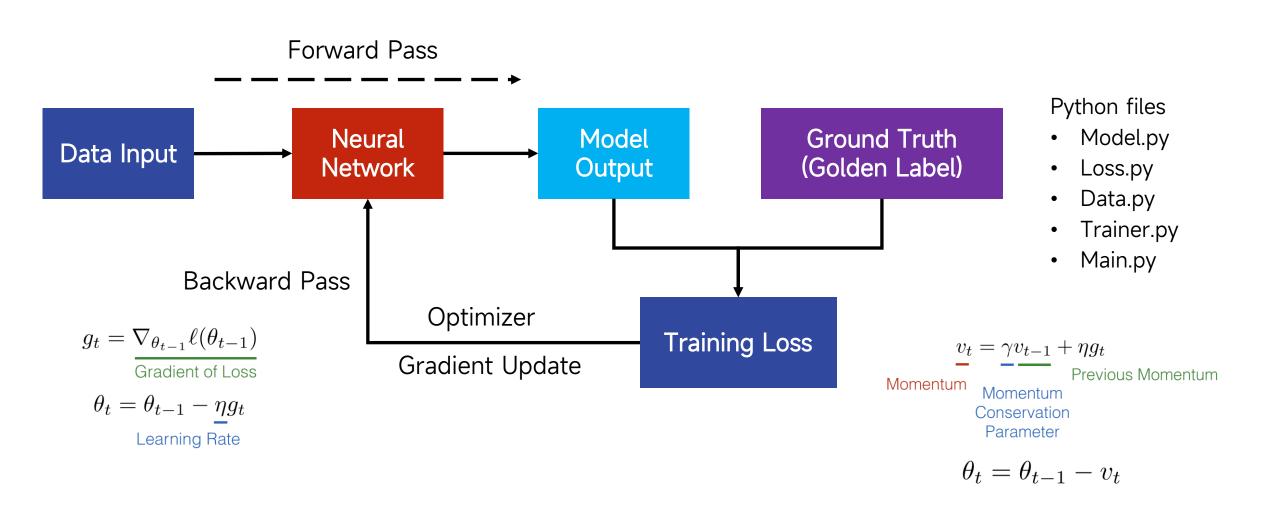
Deep Learning Algorithm Sketch



- Create a model and define a loss
- For each example
 - Forward process: calculate the result (prediction & loss) of that example
 - if training
 - Perform back propagation
 - Update parameters

Deep Learning Algorithm Sketch





Dataset Split

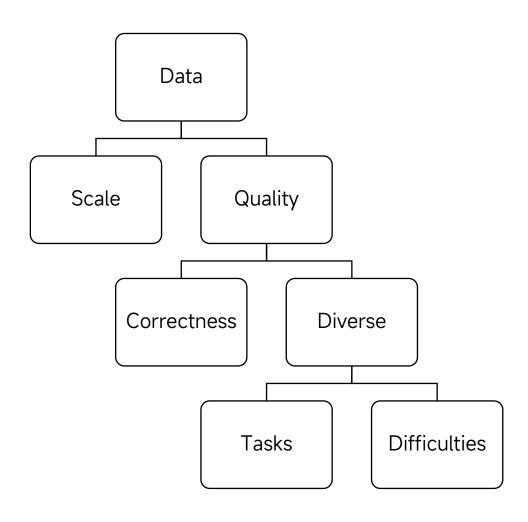


When creating a system, use three sets of data

- Training Set
 - Generally larger dataset, used during system design, creation, and learning of parameters.
- Development/validation Set
 - Smaller dataset for testing different design decisions ("hyper-parameters").
- Test Set
 - Dataset reflecting the final test scenario, do not use for making design decisions.

Data is Very Important





Deep Learning Algorithm Sketch

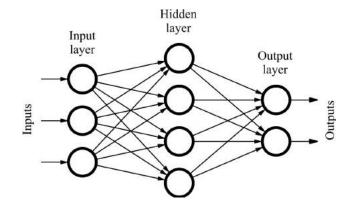


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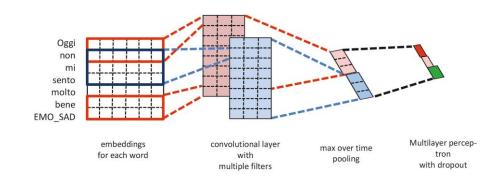
Different Model Structures



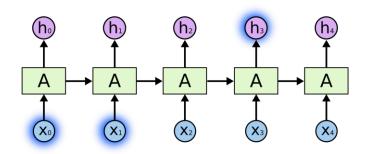
Feed-forward NNs

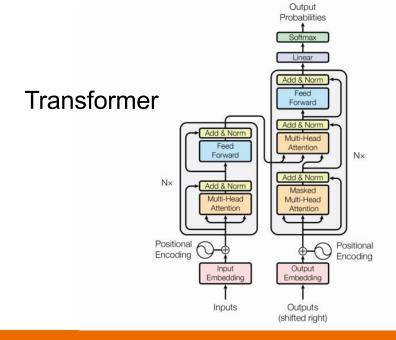


Convolutional NNs



Recurrent NNs

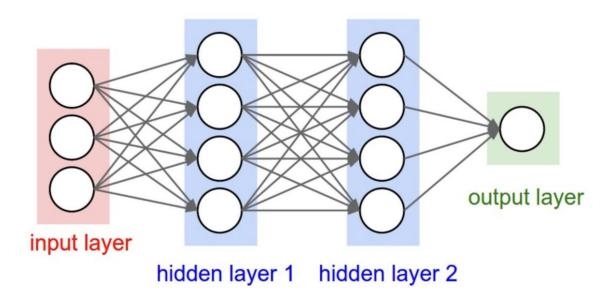




Feed-Forward Neural Network



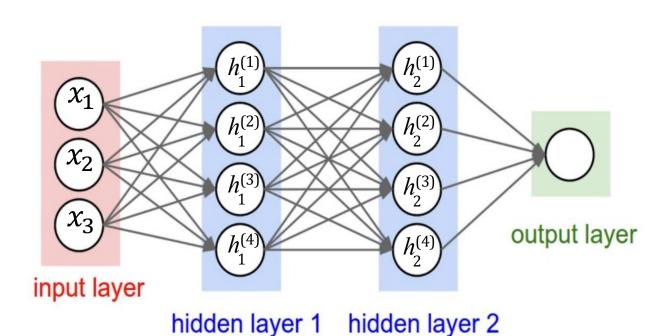
- The units are connected with no cycles
- The outputs from units in each layer are passed to units in the next higher layer
- No outputs are passed back to lower layers
- Fully-connected (FC) layers



```
import torch.nn as nn
     import torch.nn.functional as F
    class Net(nn.Module):
         def __init__(self):
             super(). init ()
             self.fc1 = nn.Linear(784, 128)
             self.fc2 = nn.Linear(128, 64)
             self.fc3 = nn.Linear(64, 10)
10
        def forward(self, x):
11
             x = F.relu(self.fc1(x))
12
13
            x = F.relu(self.fc2(x))
            x = self.fc3(x)
14
15
             return x
16
```

Feed-Forward Neural Network





• Input layer: $\mathbf{x} \in \mathbb{R}^d$

Hidden layer 1:

$$\mathbf{h}_1 = f(\mathbf{W}^{(1)}\mathbf{x} + \mathbf{b}^{(1)}) \in \mathbb{R}^{d_1}$$
$$\mathbf{W}^{(1)} \in \mathbb{R}^{d_1 \times d}, \mathbf{b}^{(1)} \in \mathbb{R}^{d_1}$$

• Hidden layer 2:

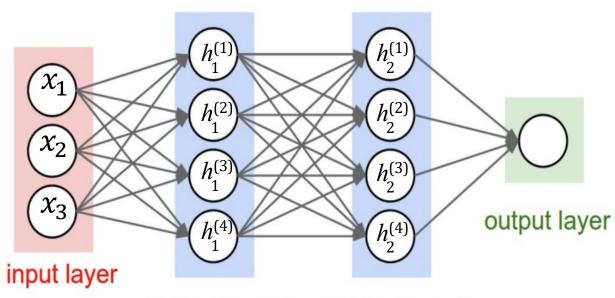
$$\mathbf{h}_2 = f(\mathbf{W}^{(2)}\mathbf{h}_1 + \mathbf{b}^{(2)}) \in \mathbb{R}^{d_2}$$
$$\mathbf{W}^{(2)} \in \mathbb{R}^{d_2 \times d_1}, \mathbf{b}^{(2)} \in \mathbb{R}^{d_2}$$

Output layer:

$$\mathbf{y} = \mathbf{W}^{(o)} \mathbf{h}_2, \mathbf{W}^{(o)} \in \mathbb{R}^{C \times d_2}$$

Feed-Forward Neural Network





$$h_1^{(1)} = f(w_{1,1}^{(1)}x_1 + w_{1,2}^{(1)}x_2 + w_{1,3}^{(1)}x_3)$$

$$h_2^{(3)} = f(w_{3,1}^{(2)}h_1^{(1)} + w_{3,2}^{(2)}h_1^{(2)} + w_{3,3}^{(2)}h_1^{(3)} + w_{3,4}^{(2)}h_1^{(4)})$$

hidden layer 1 hidden layer 2

Non-linearity (activation function) f: tanh or ReLU

Feed-Forward Neural Network for Classification



Use softmax to get the probability distribution

$$\mathbf{y} = \mathbf{W}^{(o)} \mathbf{h}_2, \mathbf{W}^{(o)} \in \mathbb{R}^{C \times d_2}$$

$$\hat{\mathbf{y}} = \operatorname{softmax}(\mathbf{y}) \qquad \operatorname{softmax}(\mathbf{y})_k = \frac{\exp(y_k)}{\sum_{j=1}^C \exp(y_j)} \quad \mathbf{y} = [y_1, y_2, ..., y_C]$$

Training loss:

min
$$-\sum_{\mathbf{W}^{(1)}, \mathbf{W}^{(2)}, \mathbf{W}^{(o)}} \log \hat{\mathbf{y}}_{y} - \sum_{(\mathbf{x}, y) \in D} \log \hat{\mathbf{y}}_{y}$$

$$\mathbf{h}^{(1)} = \text{ReLU}(\mathbf{W}^{(1)}\mathbf{x})$$

$$\mathbf{h}^{(2)} = \text{ReLU}(\mathbf{W}^{(2)}\mathbf{h}^{(1)})$$

$$\hat{\mathbf{y}} = \text{softmax}(\mathbf{W}^{(o)}\mathbf{h}^{(2)})$$

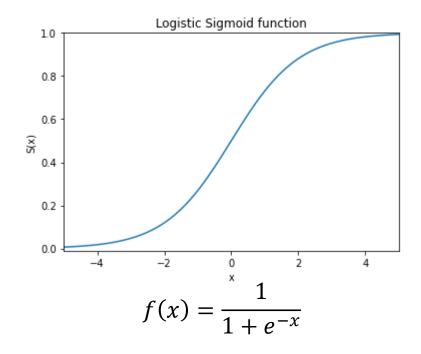
Neural networks are difficult to optimize. SGD can only converge to local minimum.

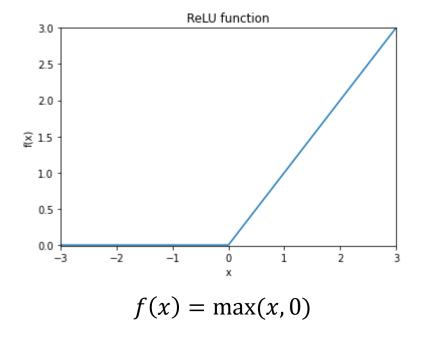
Initializations and optimizers matter a lot!

Activation Functions



- Add non-linearities into neural networks
- Allowing the neural networks to learn powerful operations





Activation Functions



- GeLU (Gaussian Error Linear Unit)
 - Used in GPT-3, BERT, and many other models

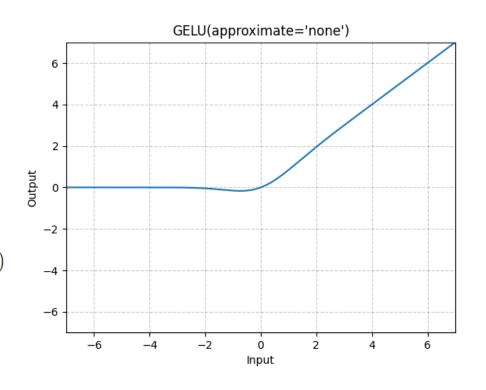
Applies the Gaussian Error Linear Units function:

$$GELU(x) = x * \Phi(x)$$

where $\Phi(x)$ is the Cumulative Distribution Function for Gaussian Distribution.

When the approximate argument is 'tanh', Gelu is estimated with:

$$\operatorname{GELU}(x) = 0.5 * x * (1 + \operatorname{Tanh}(\sqrt{(2/\pi)} * (x + 0.044715 * x^3)))$$



Loss Functions



• Given a labeled example (x, \hat{y}) , we use a neural network to estimate the conditional probability and predict the label as

$$\hat{y} = \operatorname{argmax} P_{\theta}(y|x)$$

- We compute how close our prediction w.r.t. the true label by a loss function
- Classification: Cross-Entropy

$$\mathcal{L}(x, y^*) = -\log P_{\theta}(y = y^*|x)$$

Regression: L1 loss, L2 loss (a.k.a. Mean Square Error)

$$\mathcal{L}(x, y^*) = ||f(x) - y^*||_1$$

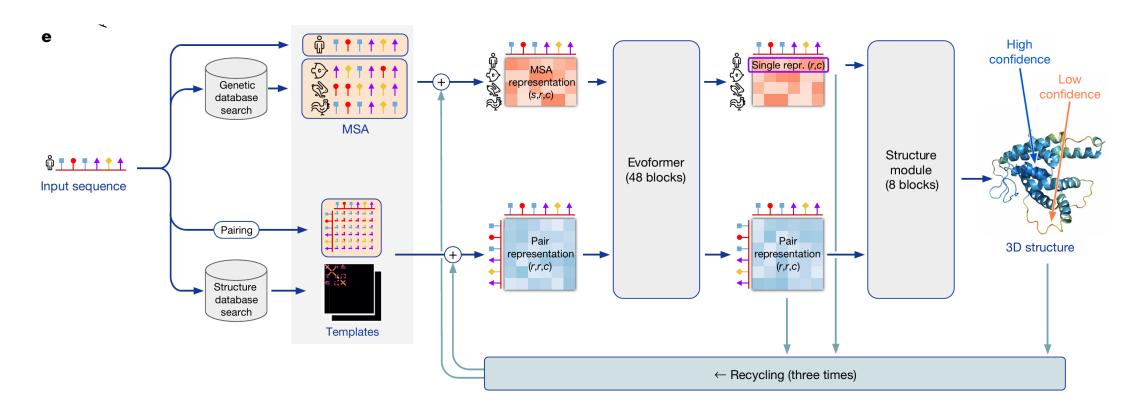
$$\mathcal{L}(x, y^*) = \|f(x) - y^*\|_2$$

Loss Functions



- AlphaFold-2
 - Use regression loss to close the difference between predictions and references

alphafold/alphafold/model/all_atom.py at main · google-deepmind/alphafold



Deep Learning Algorithm Sketch



- Create a model and define a loss (i.e., construct a computation graph)
- For each example
 - Forward process: calculate the result (prediction & loss) of that example
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Back-Propagation 反向传播算法



Forward propagation: from input to output layer

Forward step 1: Compute $h_1^{(1)}, h_2^{(1)}$

Forward step 2: Compute $h_1^{(2)}, h_2^{(2)}$

Forward step 3: Compute y_1, y_2, y_3 and $[\hat{y}_1, \hat{y}_2, \hat{y}_3] = \text{softmax}[y_1, y_2, y_3]$

Given: x_1, x_2, x_3 and the class label y (a single training example)

Forward step 4: Compute loss $L = -\log \hat{\mathbf{y}}_y$

Goal: $\frac{\partial L}{\partial W^{(1)}},$ $\frac{\partial L}{\partial W^{(2)}},$ $\frac{\partial L}{\partial W^{(o)}}$

Back step 4: Compute $\frac{\partial L}{\partial W^{(1)}}$

Back step 3: Compute $\frac{\partial L}{\partial h_1^{(1)}}, \frac{\partial L}{\partial h_2^{(1)}}, \frac{\partial L}{\partial W^{(2)}}$

Back step 2: Compute $\frac{\partial L}{\partial h_1^{(2)}}, \frac{\partial L}{\partial h_2^{(2)}}, \frac{\partial L}{\partial W^{(o)}}$

Back propagation: from output to input layer

Back step 1: Compute $\frac{\partial L}{\partial y_1}, \frac{\partial L}{\partial y_2}, \frac{\partial L}{\partial y_3}$

Back-Propagation in PyTorch



```
import torch.nn as nn
    import torch.nn.functional as F
    class Net(nn.Module):
        def __init__(self):
 5
             super().__init__()
             self.fc1 = nn.Linear(784, 128)
             self.fc2 = nn.Linear(128, 64)
             self.fc3 = nn.Linear(64, 10)
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        def forward(self, x):
            x = F.relu(self.fc1(x))
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            x = F.relu(self.fc2(x))
13
            x = self.fc3(x)
14
15
             return x
```

```
import torch.optim as optim

net = Net()
criterion = nn.CrossEntropyLoss()
optimizer = optim.SGD(net.parameters(), lr=0.001, momentum=0.9)
```

```
1  outputs = net(inputs)
2  loss = criterion(outputs, labels)
3  loss.backward()
4  optimizer.step()
```

PyTorch did back-propagation for you in this one line of code!

What if a function is not differentiable?

A toy pytorch example to train an NN model

Deep Learning Algorithm Sketch



- Create a model and define a loss (i.e., construct a computation graph)
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Optimizer Update



Most deep learning toolkits implement the parameter updates by calling optimizer.step() function

```
[59] # Before gradient update
    for name, param in model.named_parameters():
        print(name, param)

A Parameter containing:
    tensor([[-0.2267,  0.6521, -0.8193,  0.7723, -0.6456],
        [ 1.2410, -2.4380, -0.5612, -0.1144, -0.2687],
        [ 0.4792,  0.4543, -1.3530,  1.2934, -0.9943],
        [ 0.7565,  0.9449,  0.2796,  0.4703,  0.2926],
        [ 0.4143,  0.5891,  0.4370,  0.6060,  0.0161]]
    b Parameter containing:
    tensor([ 0.3592,  0.3455, -0.2517, -0.5678, -0.6016], :
        C Parameter containing:
        tensor([-1.5490], requires_grad=True)
```

Before optimizer update

After optimizer update

Can be updated with standard SGD or Adam optimizer

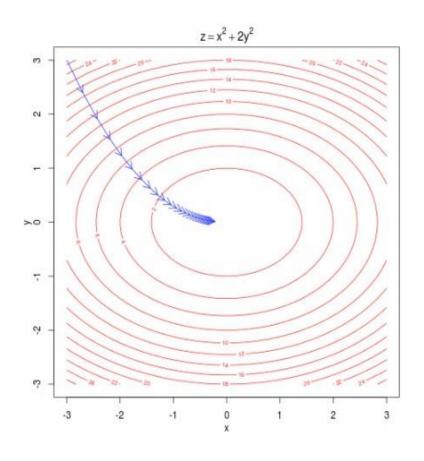
Standard SGD



• Standard stochastic gradient descent

$$g_t = rac{
abla_{ heta-1}\ell(heta_{t-1})}{ ext{Gradient of Loss}}$$
 $heta_t = heta_{t-1} - \underline{\eta}g_t$ Learning Rate

optimizer = torch.optim.SGD(model.parameters(), lr=learning_rate)



Adam Optimizer



- Most standard optimization option in NLP and beyond
- Considers rolling average of gradient g_t , and momentum m_t

$$m_t = \beta_1 m_{t-1} + (1-\beta_1) g_t \longrightarrow \text{Momentum}$$

$$v_t = \beta_2 v_{t-1} + (1-\beta_2) g_t \odot g_t \longrightarrow \text{Rolling Average of Gradient}$$

$$\hat{m}_t = \frac{m_t}{1 - (\beta_1)^t} \quad \hat{v}_t = \frac{v_t}{1 - (\beta_2)^t} \longrightarrow \text{Correction of bias}$$

Further reading: how to use the optimizer in Pytorch

$$\theta_t = \theta_{t-1} - \frac{\eta}{\sqrt{\hat{v}_t} + \epsilon} \hat{m}_t \longrightarrow \text{Final update the parameter}$$

optimizer = torch.optim.Adam(model.parameters(), lr=0.0005, betas=(0.99, 0.999))

Adam Optimizer



- Gradient descent | Khan Academy
- Intuition of Adam Optimizer
- Blog: An updated overview of recent gradient descent algorithms
- (paper) Convex Optimization: Algorithms and Complexity
- Course: Optimization for Machine Learning

Learning Rate



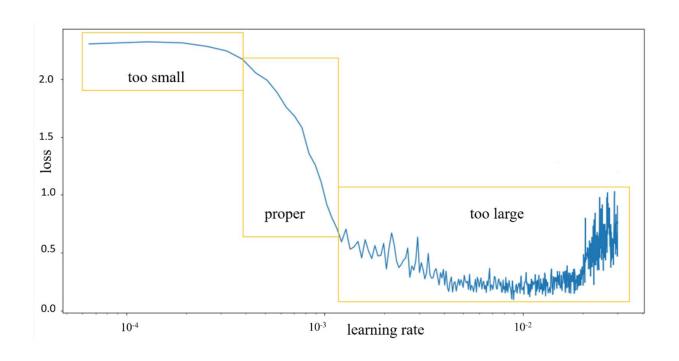


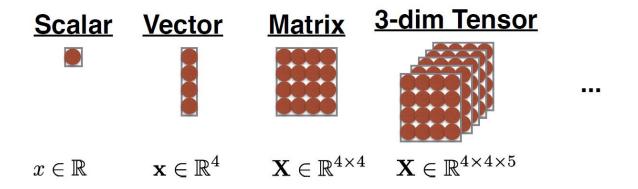
Figure 4: Effect of learning rate (adapted figure from: https://www.jeremyjordan.me/nn-learning-rate/)

<u>learning rate schedule [another link]</u>, warmup

Tensors



An n-dimensional array



- Widely used in neural networks
- Parameters in NNs consist of different shape of tensors, which store both their values and gradients (e.g., x, x.grad)

Tensor Operations



```
import numpy as np
x = torch.Tensor([[2, 3], [1, 2]])
x = torch.Tensor(np.array([[-1, 1], [2, 4]]))
x = torch.zeros([2, 3], dtype=torch.int32)
```

create tensors from list, numpy.array

```
import torch
    import torch.nn as nn
    x = torch.randn((4, 2))
    W = torch.randn((3, 4))
    print(x)
    print(W)
    tensor([[-1.5372, 0.0845],
            [ 0.5752, 0.7634],
            [0.4265, -0.1287],
            [-1.8629, -0.8520]])
    tensor([[-1.1272, -1.1810, 0.0867, 0.0676],
            [-0.1070, 3.2586, 0.7446, -1.2094],
            [-1.7670, 0.2900, -1.0881, -1.5555]]
[10] torch.matmul(W, x) # results in a [3,2] matrix
    tensor([[ 0.9646, -1.0656],
            [ 4.6092, 3.4132],
            [ 5.3167, 1.5373]])
```

matrix multiply

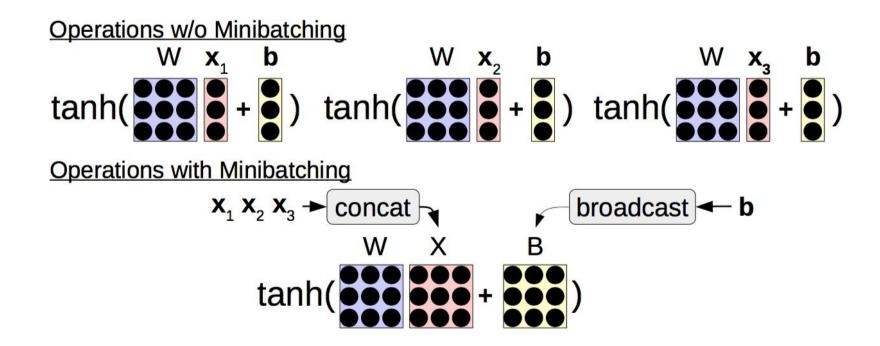
```
x = torch.randn((4,2))
    z = torch.randn((4,2))
    print(x)
    print(z)
 \Gamma tensor([[ 0.0762, 1.5145],
            [-0.4747, -0.9141],
            [ 0.7106, 0.4888],
            [0.6959, -0.5305]])
    tensor([[-0.1766, 0.6187],
            [0.9254, -0.5931],
            [-0.9162, 0.3209],
            [0.0216, -0.7116]])
[13] x * z # results in a [4,2] matrix
    tensor([[-0.0135, 0.9371],
            [-0.4392, 0.5421],
            [-0.6510, 0.1569],
            [0.0151, 0.3775]
```

Element-wise matrix multiply

Efficiency Tricks: Mini-batching

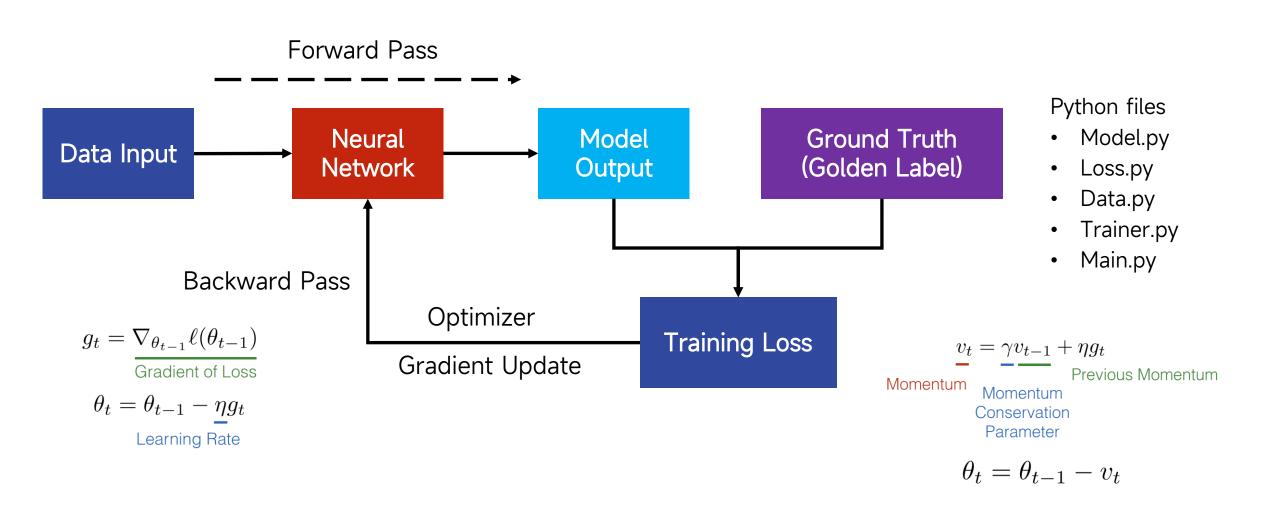


- On modern hardware 10 operations of size 1 is much slower than 1 operation of size 10
- Mini-batching combines together smaller operations into one big one
- About padding



Deep Learning Algorithm Sketch





Coding Practice



```
if args.model == 'Transformer':
179
180
                    output = model(data)
                     output = output.view(-1, ntokens)
181
182
                else:
183
                    hidden = repackage hidden(hidden)
184
                     output, hidden = model(data, hidden)
185
                loss = criterion(output, targets)
186
                loss.backward()
187
                # `clip grad norm` helps prevent the exploding gradient problem in RNNs / LSTMs.
188
                torch.nn.utils.clip grad norm (model.parameters(), args.clip)
189
190
                if args.use_optimizer:
191
                     optimizer.step()
                else:
192
                    for p in model.parameters():
193
194
                         p.data.add (p.grad, alpha=-lr)
10E
```

<u>examples/word_language_model/main.py at main · pytorch/examples</u>

Different Learnings



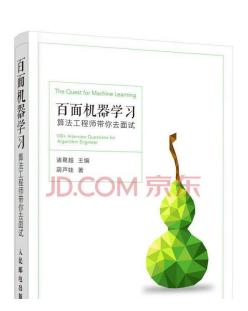
- Supervised/unsupervised learning
- Self-supervised learning
- Transfer learning
- Few-shot/zero-shot learning

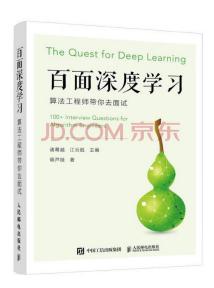
Stanford STATS214 / CS229M: Machine Learning Theory

Further Reading



- (book) Information Theory From Coding to Learning
- Neural Networks: Zero to Hero (Andrej Karpathy)
- Course: Introduction to Deep Learning
- Course: MIT Introduction to Deep Learning
- Github free resources for students







Thank you