

Decision problems

A **decision problem** has a yes/no answer

Different, but related to **optimization problem**,
where trying to maximize/minimize a value

Any decision problem Q can be viewed as
language: $L = \{x \in \{0,1\}^* : Q(x) = 1\}$

Q **decides** L : every string in L accepted by Q ,
every string not in L rejected

Example of a decision problem

PATH = $\{\langle G, u, v, k \rangle : G = (V, E) \text{ is an undirected graph, } u, v \in V, k \geq 0 \text{ is an integer, and } \exists \text{ a path from } u \text{ to } v \text{ in } G \text{ with } \leq k \text{ edges}\}$

Encoding of input $\langle G, u, v, k \rangle$ is important! We express running times as function of input size

Corresponding optimization problem is
SHORTEST-PATH