

Construct the truth table for the following statements:

i) $(\sim p \wedge q) \vee p$

p	q	$\sim p$	$\sim p \wedge q$	$(\sim p \wedge q) \vee p$
T	T	F	F	T
T	F	F	F	T
F	T	T	T	T
F	F	T	F	F

Contd.

Construct the truth table for the following statement:

$$\text{ii) } (p \rightarrow q) \leftrightarrow (\sim q \rightarrow \sim p)$$

p	q	$p \rightarrow q$	$\sim q$	$\sim p$	$\sim q \rightarrow \sim p$	$(p \rightarrow q) \leftrightarrow (\sim q \rightarrow \sim p)$
T	T	T	F	F	T	T
T	F	F	T	F	F	T
F	T	T	F	T	T	T
F	F	T	T	T	T	T

Contd.

Consider the statements

p: “I will study Discrete Mathematics”.

q: “I will go to a movie”.

r: “I am in a good mood”.

Write the following statements in terms of p,q,r and logical connectives. Construct the truth table for each of them.

a) *“If I am not in good mood then I will go to a movie else I will study Discrete Mathematics”.*

$$(\sim r \rightarrow q) \vee p$$

Contd.

b) *“If I am in a good mood then either I will study Discrete Mathematics or I will not go to a movie else I will go to a movie”.*

$$(r \rightarrow (p \vee \sim q)) \vee q$$

c) *“I will not go to a movie and I will study Discrete Mathematics iff I am in a good mood”.*

$$r \leftrightarrow (\sim q \wedge p)$$

Contd.

a) Truth table of $(\sim r \rightarrow q) \vee p$

p	q	r	$\sim r$	$\sim r \rightarrow q$	$(\sim r \rightarrow q) \vee p$
T	T	T	F	T	T
T	T	F	T	T	T
T	F	T	F	T	T
T	F	F	T	F	T
F	T	T	F	T	T
F	T	F	T	T	T
F	F	T	F	T	T
F	F	F	T	F	F

Contd.

b) Truth table of $(r \rightarrow (p \vee \sim q)) \vee q$

p	q	r	$\sim q$	$p \vee \sim q$	$r \rightarrow p \vee \sim q$	$(r \rightarrow (p \vee \sim q)) \vee q$
T	T	T	F	T	T	T
T	T	F	F	T	T	T
T	F	T	T	T	T	T
T	F	F	T	T	T	T
F	T	T	F	F	F	T
F	T	F	F	F	T	T
F	F	T	T	T	T	T
F	F	F	T	T	T	T

Contd.

Consider the following statements:

p: "The flood destroys my house."

q: "The fire destroys my house."

r: "My insurance company will pay me."

Write down the following statements in terms of p, q, r.

a) "If the flood destroys my house or the fire destroys my house then my insurance company will pay me."

Ans. $(p \vee q) \rightarrow r$

b) "If my insurance company pays me then the flood destroys my house or the fire destroys my house."

Ans. $r \rightarrow (p \vee q)$

Contd.

c) *“If neither the flood destroys my house nor the fire destroys my house then my insurance company will not pay me.”*

Ans. $(\sim p \wedge \sim q) \rightarrow \sim r$

d) *“If my insurance company does not pay me then the flood does not destroy my house or the fire does not destroy house.”*

Ans. $\sim r \rightarrow (\sim p \vee \sim q)$

e) *“If my insurance company does not pay me then the flood does not destroy my house and fire does not destroy my house.”*

Ans. $\sim r \rightarrow (\sim p \wedge \sim q)$