

# The Robotics Kinematics

— We need to declare the variables that we will use and include the libraries

```
#include <Keypad.h>
int L1=40,L2=45,CHECK;
float ANG1, ANG2, ANGL1, ANGL2, X,Y, ALLANG=50, INVANG;

#include <Servo.h>
Servo motor1;
Servo motor2;

char keys[4][3]=
{{'1','2','3'},{'4','5','6'},{'7','8','9'},{' ','9',' '}};

byte rows [4]={A2, A3, A4, A5};
byte cols [3]={B8, B9, B10};
Keypad userINPUTS = Keypad(makeKeymap(keys),rows,cols,4,3);

#include <LiquidCrystal.h>
// initialize the library with the numbers of the interface pins
LiquidCrystal lcd(12, 11, 5, 4, 3, 2);

void setup() {
  motor1.attach(7);
  motor2.attach(6);

  lcd.begin(16, 2);
  lcd.print("hello, world!");
}

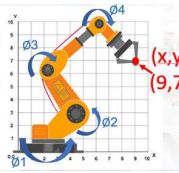
void loop() {
  // set the cursor to column 0, line 1
  // (note: line 1 is the second row, since counting begins with 0):
  lcd.setCursor(0, 1);
  // print the number of seconds since reset:
  lcd.print(millis() / 1000);
  lcd.clear(); //clear word on led
  CHECK=forwaORinver();
}
```

```
if (CHECK==1) {
  int ANGL11=ANGL12, ANGL1,
  ANGL21=ANGL22, ANGL2;

  lcd.clear();
  lcd.print("Enter angle 1");
  while (ANGL11==0) {ANGL11=userINPUTS.getKey();} //wait user to
  enter first number of Q1
  lcd.setCursor(0,1);
  ANGL11=ANGL1-48; // CONVERT THE Number From ASCII
  lcd.print(ANGL11);
  while (ANGL12==0) {ANGL12=userINPUTS.getKey();} //wait user to
  enter second number of Q1
  ANGL12=ANGL12-48;
  lcd.print (ANGL12);
  delay (500);
  ANGL1=ANGL11*10+ANGL12;
  lcd.clear();
  lcd.print("Enter angle 2");
  while (ANGL21==0)
  {ANGL21=userINPUTS.getKey();} //wait user to enter first number
  of Q1
  lcd.setCursor(0,1);
  ANGL21=ANGL21-48; // CONVERT THE Number From ASCII
  lcd.print(ANGL21);
  while (ANGL22==0) {ANGL22=userINPUTS.getKey();} //wait user to
  enter second number of Q1
  ANGL22=ANGL22-48;
  lcd.print (ANGL22);
  delay (500);
  ANGL2=ANGL21*10+ANGL22;
  forward(); // Calling forward function
}
else
{ int X11=0,X12=0,X
,Y11=0,Y12=0,Y,u;}
```

```
lcd.clear();
lcd.print("Enter value of X, position");
while (X11==0)
{X11=userINPUTS.getKey();}
X11=X11-48;
lcd.setCursor(0,1);
lcd.print (X11);
while (X12==0)
{X12=userINPUTS.getKey();}
X12=X12-48;
lcd.print (X12);
delay (500);
X=X11*10+X12;
lcd.clear();
lcd.print("Enter value of Y");
while (Y11==0)
{Y11=userINPUTS.getKey();}
Y11=Y11-48;
lcd.setCursor(0,1);
lcd.print (Y11);
while (Y12==0)
{Y12=userINPUTS.getKey();}
Y12=Y12-48;
lcd.print (Y12);
delay (500);
Y=Y11*10+Y12;
invers(); //call invers function
```

#We have two types :-  
1st/ Forward Kinematics :-



knowns  
the angles ( $\phi_1, \phi_2$ )  
the length of  
the arm. ( $L_1, L_2$ )

knowns  
the end effector  
position. ( $x, y$ )  
the angle of the end effector. ( $\theta$ ).

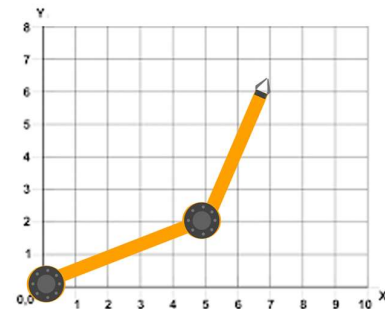
$$\cos \phi_1 = \frac{x_1}{L_1}$$

$$x_1 = \cos \phi_1 \cdot L_1$$

$$y_1 = \sin \phi_1 \cdot L_1$$

$$x_2 = (\cos \phi_1 + \phi_2) \cdot L_2$$

$$y_2 = \sin(\phi_1 + \phi_2) \cdot L_2$$



Lastly, we want to find the end effector position ( $x, y$ )

$$x = x_1 + x_2 = L_1 \cos \phi_1 + L_2 \cos(\phi_1 + \phi_2)$$

$$y = y_1 + y_2 = L_1 \sin \phi_1 + L_2 \sin(\phi_1 + \phi_2)$$

$\theta$  between  $x, y$  is  $\theta = \phi_1 + \phi_2$

We need to change these equations to code, as follow:

```
int forwaORinver()
{
  char IND=0;
  moto1.write(0);
  moto2.write(0);
  lcd.clear();
  lcd.print("Press 1 FOR forward");
  lcd.setCursor(0,1);
```

```

lcd.print ("or 2 FOR Inverse");
while (IND==0)
{ IND = userINPUTS.getKey();}
IND=IND-48;
if (IND==1) {
  lcd.clear();
  lcd.print ("Forward Kinematic");
  lcd.setCursor (0,1);
  lcd.print (1);
  delay (2000);
  return 1;
}
else if (IND==2) {
  lcd.clear();
  lcd.print ("Inverse Kinematic");
  lcd.setCursor (0,1);
  lcd.print (2);
  delay (2000);
  return 2;
}

void forward () {
  //this function to calculate Q1 & Q2
  moto1.write (ANGL1);
  moto2.write (ANGL2);
  lcd.clear();
  ANG1=ANGL1*PI/180; //Degree to radian
  ANG2=ANGL2*PI/180; //Degree to radian
  X=(L1*cos (ANG1) ) + (L2*cos (ANG1+ANG2));
  Y=(L1*sin (ANG1))+(L2*sin (ANG1+ANG2));
  lcd.print ("The position of the end effector");
  lcd.setCursor(5, 1);
  lcd.print("X:");
  lcd.setCursor(0, 1);
  lcd.print (X);
  lcd.setCursor(6, 1);
  lcd.print (Y);
  Serial.print ("ANG1");
  Serial.println(q1);
  Serial.print ("ANG2");
  Serial.println(q2);
  delay (7000);
}

```

## 2 / Inverse Kinematics :-

<p><b>Knowns</b></p> <ul style="list-style-type: none"> <li>the position of end effector end ang <math>\theta</math></li> <li>the length of the arm</li> </ul>	<p><b>Unknowns</b></p> <ul style="list-style-type: none"> <li>the angle of the first joint</li> <li>the angle of the second joint</li> </ul>
--	--

Triangle (1)

$$H^2 = X^2 + Y^2$$

Triangle (2)

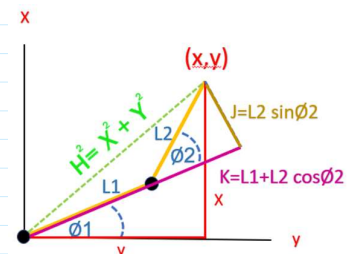
$$J = L_2 \sin \phi_2$$

$$K = L_1 + L_2 \cos \phi_2$$

$$H^2 = J^2 + K^2$$

$$\begin{aligned}
 \bullet \quad X^2 + Y^2 &= J^2 + K^2 \\
 &= (L_2 \sin \phi_2)^2 + (L_1 + L_2 \cos \phi_2)^2 \\
 &= \underline{L_2^2 \sin^2 \phi_2} + L_1^2 + \underline{L_2^2 \cos^2 \phi_2} + 2L_1L_2 \cos \phi_2 \\
 &= L_2^2 (\sin^2 \phi_2 + \cos^2 \phi_2) + L_1^2 + 2L_1L_2 \cos \phi_2 \\
 X^2 + Y^2 &= L_2^2 (1) + L_1^2 + 2L_1L_2 \cos \phi_2
 \end{aligned}$$

Lastly, To find the desired angle.



1 = L1 cos(θ1) + L2 cos(θ2)  
 Lastly, To find the desired angle.

$$\cos \theta_2 = (x^2 + y^2 - L_1^2 - L_2^2) / (2 L_1 L_2)$$

$$\theta_2 = \cos^{-1}((x^2 + y^2 - L_1^2 - L_2^2) / (2 L_1 L_2))$$

$$\theta_1 = \theta - \theta_2$$

We need to change these equations to the following code :-

```
void invers() {
  // this function to determine end effector of arm depending on value of x, y
  lcd.clear();
  INVANG = (pow(x, 2) + pow(y, 2) - pow(L1, 2) - pow(L2, 2)) / (2 * L1 * L2);
  ANGL2 = acos(INVANG);
  ANG2 = ANGL2 * 180 / PI;
  ANG1 = ALLANG - ANG2;
  lcd.print("Angle of Arm:");
  lcd.setCursor(0, 1);
  lcd.print("ANG1=");
  lcd.print(ANG1);
  cd.setCursor(0, 1);
  lcd.print("&");
  lcd.setCursor(9, 1);
  lcd.print("ANG2=");
  lcd.print(ANG2);
  Serial.print(ANG1);
  moto1.write(ANG1);
  moto2.write(ANG2);
  delay(7000);
}
```