

Exploring Computer Science Concepts

Via ACSL Competitions

Number Systems

- Decimal
 - base 10
- Binary
 - base 2
- Octal
 - base 8
- HexaDecimal
 - base 16

Digits per base

- Decimal
 - Ten digits
 - 0 1 2 3 4 5 6 7 8 9
- Binary
 - Two Digits
 - 0 1
- Octal
 - 8 digits
 - 0 1 2 3 4 5 6 7
- Hexadecimal
 - 16 digits
 - 0 1 2 3 4 5 6 7 8 9 A B C D E F

Counting in Decimal

- Increment the lowest place value (right most digit)

- When last digit is reached

- Set the current column to 0

- Increment the column on the left by 1

- Lets count with decimal

- 0 to 10

- 95 to105

- How frequently do we add a new digit ?

Decimal	Decimal
0	95
1	96
2	97
3	98
4	99
5	100
6	101
7	102
8	103
9	104
10	105

Counting in other bases

- Counting in binary
 - We add a new digit frequently
 - At 2, 4, 8, 16 ... decimal values
- Counting in Octal
 - We add a new digit at every
 - At 8, 64, 128 ...
- Counting in HexaDecimal
 - We add a new digit at every
 - At 16, 256 ... values

Decimal	Binary	Octal	HexaDecimal
0	0	0	1
1	1	1	1
2	10	2	2
3	11	3	3
4	100	4	4
5	101	5	5
6	110	6	6
7	111	7	7
8	1000	10	8
9	1001	11	9
10	1010	12	A
11	1011	13	B
12	1100	14	C
13	1101	15	D
14	1110	16	E
15	1111	17	F
16	10000	20	10

Place Values

- Decimal
 - We deal in power of 10s
 - $2452 = 2 * 1000 + 4 * 100 + 5 * 10 + 2 * 1$
 - $101 = 1 * 100 + 0 * 10 + 1 * 1$
- Binary
 - We deal in power of 2s
 - $111 = 1 * 4 + 1 * 2 + 1 * 1$
 - $1010 = 1 * 8 + 0 * 4 + 1 * 2 + 0 * 1$

Place values

Converting binary → decimal

Decimal	Binary
2452 → $2 \times 10^3 = 2000$ $4 \times 10^2 = 400$ $5 \times 10^1 = 50$ $2 \times 10^0 = 2$ = 2452	111 → $1 \times 2^2 = 1 \times 4 = 4$ $1 \times 2^1 = 1 \times 2 = 2$ $1 \times 2^0 = 1 \times 1 = 1$ = 7
101 → $1 \times 10^2 = 100$ $0 \times 10^1 = 0$ $1 \times 10^0 = 1$ = 101	1010 → $1 \times 2^3 = 1 \times 8 = 8$ $0 \times 2^2 = 0 \times 4 = 0$ $1 \times 2^1 = 0 \times 2 = 2$ $0 \times 2^0 = 0 \times 1 = 0$ = 10
756 →	1000 →

Converting Binary to Decimal

128	64	32	16	8	4	2	1
<hr/>							

$$1 \ 0 \ 0 \ 1 \ 0 \ 0 \ 1 = 64 + 16 + 1 = 81$$

$$1 \ 0 \ 0 \ 0 \ 0 \ 1 \ 1 \ 1 = 128 + 4 + 2 + 1 = 135$$

$$1 \ 1 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 = ?$$

Converting Decimal to Binary

128	64	32	16	8	4	2	1
<hr/>							

$$= 22$$

$$= 33$$

$$= 130$$

Exercises

- Convert following Decimal numbers to binary
 - 127_{10}
 - 128_{10}
 - 129_{10}
 - 255_{10}
 - 256_{10}
- Convert following Binary numbers to Decimal
 - 101101_2
 - 1110_2
 - 1111_2
 - 0110_2

Challenge

- How does binary addition and subtraction work ?

Place values

Converting octal,hexadecimal → decimal

Octal → Decimal	HexaDecimal → Decimal
777 → $7 \times 8^2 = 7 \times 64 = 448$ $7 \times 8^1 = 7 \times 8 = 56$ $7 \times 8^0 = 7 \times 1 = 7$ = 511	2AB → $2 \times 16^2 = 2 \times 256 = 512$ $A \times 16^1 = 10 \times 16 = 160$ $B \times 16^0 = 11 \times 1 = 11$ = 683
137 → $1 \times 8^2 = 1 \times 64 = 64$ $3 \times 8^1 = 3 \times 8 = 24$ $7 \times 8^0 = 7 \times 1 = 7$ = 95	101 → $1 \times 16^2 = 1 \times 256 = 256$ $0 \times 16^1 = 0 \times 16 = 0$ $1 \times 16^0 = 1 \times 1 = 1$ = 257
756 →	4A3 →

Converting Decimal to Octal

$$(312)_{10} \rightarrow (?)_8$$

$312 / 8 \rightarrow$ quotient : 39 , Remainder 0

$39 / 8 \rightarrow$ quotient : 4 , Remainder 7

$4 / 8 \rightarrow$ quotient : 0 , Remainder 4

(470)₈

$$(112)_{10} \rightarrow (?)_8$$

$112 / 8 \rightarrow$ quotient : 14 , Remainder 0

$14 / 8 \rightarrow$ quotient : 1 , Remainder 6

$1 / 8 \rightarrow$ quotient : 0 , Remainder 1

(160)₈

Exercises

- Convert following Decimal numbers to Octal
 - 111_{10}
 - 88_{10}
 - 511_{10}
 - 512_{10}
 - 513_{10}
- Convert following Octal numbers to Decimal
 - 45_8
 - 77_8
 - 100_8
 - 101_8

Converting Decimal to Hexadecimal

$$(312)_{10} \rightarrow (?)_8$$

$312 / 16 \rightarrow$ quotient : 19 , Remainder 8

$19 / 16 \rightarrow$ quotient : 1 , Remainder 3

$1 / 16 \rightarrow$ quotient : 0 , Remainder 1

$$(138)_{16}$$

$$(112)_{10} \rightarrow (?)_8$$

$112 / 16 \rightarrow$ quotient : 7 , Remainder 0

$7 / 16 \rightarrow$ quotient : 0 , Remainder 7

$$(70)_{16}$$

Hexadecimal → Octal

$(AC)_{16} \rightarrow (1010)_2 \times 16 + (1100)_2 \times 1$ // Replace hexa with binary
 $\rightarrow (1010\ 1100)_2$ // Convert to binary
 $\rightarrow (010\ 101\ 100)_2$ // group by 3s , added extra 0s in the front
 $\rightarrow (254)_8$ // Replace each group by octal value

$(1EF)_{16} \rightarrow (0001)_2 \times 256 + (1110)_2 \times 16 + (1111) \times 1$
 $\rightarrow (0001\ 1110\ 1111)_2$ // Convert to binary
 $\rightarrow (000\ 111\ 101\ 111)_2$ // group by 3 , removed 0s in the front
 $\rightarrow (757)_8$ // Replace each group by octal value

Octal → Hexadecimal

- $(\text{757})_8 \rightarrow (?)_{16}$
- $(\text{254})_8 \rightarrow (?)_{16}$

Exercises

- Convert following Decimal numbers to HexaDecimal/Octal
 - 255_{10}
 - 256_{10}
 - 257_{10}
- Convert following HexaDecimal numbers to Decimal, Octal
 - 99_{16}
 - 100_{16}
 - 101_{16}

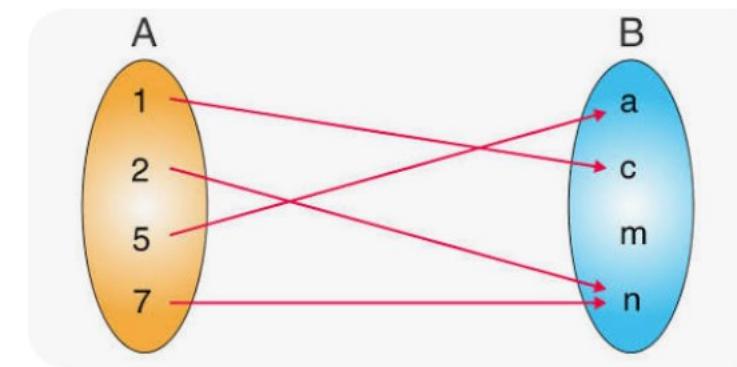
Recursion : programming

- Create factorial
 - $5! = 5 \times 4 \times 3 \times 2 \times 1 = 120$
 - $2! = 2$
- Provide sum of Fibonacci numbers using recursion
 - fibonacci(13)
 - $0 + 1 + 1 + 2 + 3 + 5 + 8 + 13 = 33$
 - fibonacci(3)
 - $0 + 1 + 1 + 2 + 3 = 7$

Relations

- A **relation** : connection/mapping between elements of two or more sets, Some characteristics ...

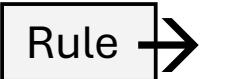
- It is a **mapping** as shown in figure
- Can be written as **Ordered pairs**
 - $\{(1,c), (2,n),(5,a),(7,n)\}$
- Not always unique
 - E.g. $y^2 = 4$ has multiple solutions (how many?)

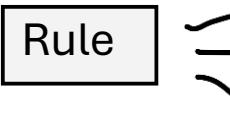


- Examples
 - Numerical relationship : $4+3 = 7$
 - Equation : $y = 2x+3$
 - Geometry : two congruent triangles
 - Set theory : A is a subset of B

Functions , mathematical kind

- A **relation** that gives exactly **one unique output for each input**

$x \rightarrow$  :this is a function as you always get one answer

$x \rightarrow$  :Not a function as you get multiple answers

- Representation
 - $f(x) = 2x+1$:this is a function
 - $g(x) = \pm 3x$:this is **not** a function , why?
- Follow up reading (optional): pg 11-13 : [functions](#)

Evaluating functions

- Solving
 - Substitute variables with numerals
 - Evaluate
 - Follow PEMDAS/BODMAS
- Solve for $x = 0, 1, 2, 3$
 - $f(x) = 3x + 1$
 - $g(x) = 2x^2 + 3$
 - $h(x) = x^2 + 2x + 1$

Recursive Functions

- Functions calling themselves

Fibonacci numbers	$fib: \mathbb{N} \rightarrow \mathbb{N}$ $fib(n) = \begin{cases} 0, & \text{if } n = 0 \\ 1, & \text{if } n = 1 \\ fib(n - 1) + fib(n - 2), & \text{if } n \geq 2. \end{cases}$
Factorial	$\mathbf{fact(n) = n * fact(n-1)}$ $\{\text{given, } fact(1) = fact(0) = 1\}$
Lucas numbers <i>(same rule as Fibonacci but with different starting values)</i>	$\mathbf{l(n) = l(n-1) + l(n-2)}$ $\{\text{given, } l(0) = 2, l(1) = 1\}$

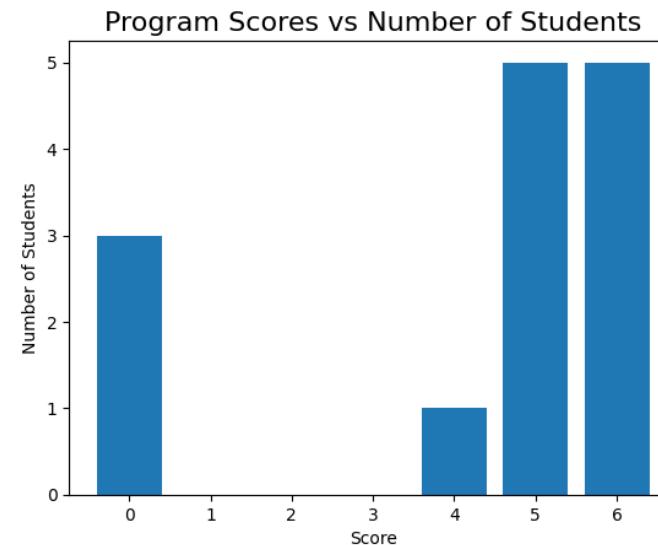
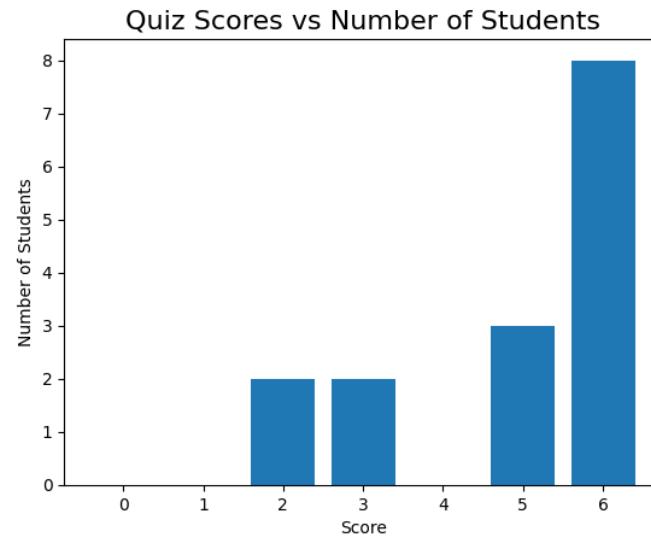
- Evaluate for ‘n’ = 2 , 4, 5, 6
- Follow up reading (optional): [nested functions visualized](#)

Programming, , Test #1

- Need to know
 - Data types
 - Conditionals : If/else
 - Loops : for
 - Arrays : 2 dimensional
- Practice
 - Arrays- DS (Hackerrank)
 - Do the 4 problems marked “easy”
 - Optional :“hard”, “medium” one are for extra challenge

Test 1, observations

- Great participation, nearly everyone attempted!
- Overall students did better in quiz
 - 8x full marks in quiz vs 5x full marks in programming
- **4 students got a zero in programming (with 1 not attempted)**



Test 2 , analysis

- The quizzes
 - seem to be easier for students to master
 - Success cause everyone attempted, next we figure out how to raise scores there
 - Suggestions ?
- Programming
 - It was amazing attempt
 - The codes generally worked
 - But 4/15 students had zeroes.
 - Suggestions ?
- Goal :We need raise scores for everyone and move some in attempted stage
 - Note
 - Compete with yourself , Do better than your last attempt
 - Ask for help
 - on what you don't know, to learn it.
 - And even on what you know , i.e. to master it

Topics for Test 2

- Mathematical expressions
 - Representations (infix, prefix, postfix)
 - Evaluation of expression
- Discrete Mathematics
 - Logical Operators (AND , OR , NOT, SHIFT,...)
 - Boolean logic
- Programming
 - char, string ,arrays
 - Loops
 - Conditionals
 - If/else
 - switch/case

Infix expressions

- Encounter them in grade maths. e.g.
 - $(11+14)/(9 - 3) + 2$
 - $3+7 / (4 * 5 - 6)$
 - $- 2 + 8 / 2$
- Can also be written using variables
 - $(a + b) / (c - d) + e$
 - $x + y / (g * h - k)$
- Evaluated using
 - PEMDAS / BODMAS

Expression : anatomy

- Expression is made of
 - Operators (+ , - , * , /)
 - Operands (numbers, variables)
- Unary operators : $- a$
 - <operator> <operand>
- Binary operators (infix) : $a + b$
 - < operand> <operator> <operand>

Prefix/Postfix expressions

- Benefits
 - Remove ambiguity(i.e. can forget PEMDAS, BODMAS)
 - Computer friendly
 - Works with both unary/binary
 - Faster evaluation
- Expression styles
 - Infix : operator in **middle** of operands
 - $(5+6)*3$
 - <**operand**> <*operator*> <**operand**>
 - Prefix : operator **before** operands
 - * + 5 6 3
 - <*operator*> <**operand**> <**operand**>
 - Postfix : operator **after** operands
 - 5 6 + 3 *
 - <**operand**> <**operand**> <*operator*>

Evaluating expression, *but first Stacks and Queues*

- What is a **Stack** ?
 - This is a sequential structure of **items**
 - That are **pushed at one end**
 - **Pulled via the same end**
 - **LIFO** : Last in First Out
 - Examples
 - Stack of plates
 - Your turned in paper assignments
- What is a **Queue**?
 - Another sequential structure of **items**
 - that are **pushed at one end**
 - **Pulled via the opposite end**
 - **FIFO** : First In First Out
 - Examples
 - Queue for buying tickets
 - Traffic in one way single lane

Evaluating prefix expression

- Infix : $(5+6)*3$
 - * + 5 6 3
 - - + 2 * 3 4 / 16 ^ 2 3
- Algorithm (harder way)
 - Scan from right to left
 - Anytime you find an operator
 - Evaluate the operation using the previous 2 operands
 - Replace the *operator* <ôřêšâñđ> with *sêşuł'tj* in the expression
 - Repeat the steps till only 1 operand is left

Evaluating postfix expression

- Evaluate
 - $2\ 3\ 1\ *\ +\ 9\ -$
 - $5\ 3\ +\ 6\ 2\ /\ *\ 3\ 5\ *\ +$
- *Algorithm to evaluate (use stack)*
 1. Push the operands in a stack
 2. When you encounter a operator
 - Pop 2 operands
 - Perform the operation on operands
 - Push the result in stack
 - Repeat from 1 until expression is parsed
 - The last item in stack is the answer
 - There would be only 1 item left when done correctly
- * prefix expr can also be evaluated in this way (*just in reverse*)

Evaluate

- Prefix
 - $- * 5 + - 4 2 2 / 6 3$
 - $- * + 3 5 7 + / 4 2 1$
 - $- + 10 * 2 3 + 4 / 5 5$
- Postfix
 - $1 2 + 3 4 + * 5 6 - / 7 +$
 - $8 2 / 3 4 + * 5 1 + 2 / -$
 - $9 8 4 2 1 ^ * / - 3 +$

Answers

- Prefix
 - $- * 5 + - 4 2 2 / 6 3$
 - Ans : 18
 - $- * + 3 5 7 + / 4 2 1$
 - Ans : 53
 - $- + 10 * 2 3 + 4 / 5 5$
 - Ans : 11
- Postfix
 - $1 2 + 3 4 + * 5 6 - / 7 +$
 - Ans : -14
 - $8 2 / 3 4 + * 5 1 + 2 / -$
 - Ans : 25
 - $9 8 4 2 1 ^ * / - 3 +$
 - Ans : 11

Practice: Programming

- Write a function that takes a string and checks if it is a palindrome
 - Returns true if palindrome is found else false
 - Hints: string indexing, loops, if , comparing characters
- Count the number of vowels, consonants in a sentence.
 - Vowels : a,e,i,o,u
 - Consonant : everything else other than vowels
 - Ignore : spaces (' ','), comma(,), dash(-),semicolon(;),colon(:)
- Find the most frequent word in a sentence
 - If more than 1 word has same frequency return the lexicographically smaller one.

Review Evaluating Prefix/Postfix

- From last week
 - Operator
 - Operand
 - Stack
 - Queue
- Evaluating Prefix/Postfix
 - <3 questions each>

Precedence and associativity

- Precedence (highest priority first)
 - ()
 - ^
 - / *
 - - +
- Associativity
 - Right to left : ^
 - Left to right : + , - , * , /
- Notes
 - () not categorized as associative, they represent grouping mechanism

Precedence and associativity

- Example
 - $10 + 20 / 2 * 3 - 5$
 - $\rightarrow 10 + ((20 / 2) * 3) - 5$ // added parenthesis for denoting precedence
 - $\rightarrow 10 + (10 * 3) - 5$ // interior most precedence first
 - $\rightarrow 10 + 30 - 5$
 - $\rightarrow 35$

Precedence and associativity (lets evaluate)

- $2 + 3 * 4 ^2$
- $2 ^3 ^2$
- $100 / 2 * 5 ^2 ^1$

Precedence and associativity (answers)

- $2 + 3 * 4 ^2$
 - $\rightarrow 2 + 3 * 16$
 - $\rightarrow 2 + 48$
 - $\rightarrow 50$
- $2 ^3 ^2$
 - $\rightarrow 2 ^9 //$ ^ is evaluated from right to left , so $3 ^2$ goes first
 - $\rightarrow 512$
 - ~~Not 64~~
- $100 / 2 * 5 ^2 ^1$
 - $\rightarrow 100 / 2 * 25 //$ Again $2 ^1$ goes first
 - $\rightarrow 50 \times 25$
 - $\rightarrow 1250$

Convert to Prefix/Postfix (examples)

- $B * C$
 - Prefix : *** B C**
 - Postfix : **B C ***
- $A + B * C$
 - Prefix : **+ A * B C**
 - Postfix : **A B C * +**
- $(5 + 6) * 3$
 - Prefix : *** + 5 6 3**
 - Postfix : **5 6 + 3 ***

Convert to Postfix

- How to convert!
 - Convert the highest precedence/priority first
 - (do paranthesize for mental ease)
- $(a + b) / (c - d) + e$
- $x + y / (g * h - k)$

Convert to Postfix

- How to convert!
 - Convert the highest priority first
 - (and paranthesize for mental ease)
- $(a + b) / (c - d) + e$
 - Prefix : **+ / + a b - c d e**
 - Postfix : **a b + c d - / e +**
- $x + y / (g * h - k)$
 - Prefix : **+ x / y - * g h k**
 - Postfix : **x y g h * k - / +**

Convert to Prefix and Postfix

- $a + b - c * d + e ^ f$
- $(a + b) * c - (d - e) * (f + g)$
- $((a + b) * (c + d) / (e - f)) + g$
- $a * (b + c) / (d - e)$
- $a - b / (c * d ^ e)$
- $(a + b) * (c + d) - e$

Convert to Prefix and Postfix (answers)

Infix	Prefix	Postfix
$a + b - c * d + e ^ f$	$+ - + a b * c d ^ e f$	$a b + c d * - e f ^ +$
$(a + b) * c - (d - e) * (f + g)$	$- * + a b c * - d e + f g$	$a b + c * d e - f g + * -$
$((a + b) * (c + d) / (e - f)) + g$	$+ / * + a b + c d - e f g$	$a b + c d + * e f - / g +$
$a * (b + c) / (d - e)$	$/ * a + b c - d e$	$a b c + * d e - /$
$a - b / (c * d ^ e)$	$- a / b * c ^ d e$	$a b c d e ^ * / -$
$(a + b) * (c + d) - e$	$- * + a b + c d e$	$a b + c d + * e -$

Logical operators (for bits/bytes)

- Bitwise
 - NOT, AND, XOR , OR
- Shift
 - Linear : LSHIFT, RSHIFT,
 - Circular : RCIRC, LCIRC
- Precedence
 - NOT,
 - SHIFT, CIRC,
 - AND ,
 - XOR,
 - OR

Truth Tables

X	NOT X
0	1
1	0

X	Y	X AND Y	X OR Y	X XOR Y
0	0	0	0	0
0	1	0	1	1
1	0	0	1	1
1	1	1	1	0

Truth Tables

- Linear shift , add 0s as padding (either left or right)
 - Shifting by word size (or more) would result in all 0s
- Circular shift just rolls over the bits (as per direction)
 - Shifting by the number of word size , same bit sequence would be produced

X	(LSHIFT-2 X)	(RSHIFT-3 X)	(LCIRC-3 X)	(RCIRC-1 X)
01101	10100	00001	01011	10110
10	00	00	01	01
1110	1000	0001	0111	0111
1011011	1101100	0001011	1011101	1101101

Operations (evaluate)

- 0110 AND 1011
- 1100 OR 0101
- 1010 XOR 1111
- 1010 AND 1100 OR 0001
- 0011 OR 1010 AND 0110
- (1100 XOR 1010) AND 0110

Operations (evaluate)

- 0110 AND 1011
- 1100 OR 0101
- 1010 XOR 1111
- 1010 AND 1100 OR 0001
- 0011 OR 1010 AND 0110
- (1100 XOR 1010) AND 0110

Operations : Shift (evaluate)

1. (LSHIFT-1 10101) AND (RSHIFT-2 11010)
2. (RCIRC-2 01111) OR (LSHIFT-3 10010)
3. (RSHIFT-1 11100) XOR (LCIRC-2 01011)
4. (LSHIFT-2 00110) OR (RCIRC-1 10101) AND (RSHIFT-3 11101)
5. (LCIRC-3 11001) AND (RSHIFT-2 10110)
6. (RCIRC-4 10011) OR (LSHIFT-1 01101)
7. (RSHIFT-3 11110) AND (LCIRC-1 00111) OR (LSHIFT-2 01010)
8. (LSHIFT-2 01101) OR (RCIRC-3 10110) AND (RSHIFT-1 11011)

Answers 1..3

1. (LSHIFT-1 10101) AND (RSHIFT-2 11010)
 - → 01010 AND 00110
 - → **00010**
2. (RCIRC-2 01111) OR (LSHIFT-3 10010)
 1. → 11011 OR 10000
 2. → **11011**
3. (RSHIFT-1 11100) XOR (LCIRC-2 01011)
 1. → 01110 XOR 01101
 2. → **00011**

Answers 4..6

4. (LSHIFT-2 00110) OR (RCIRC-1 10101) AND (RSHIFT-3 11101)
 - 11000 OR 11010 AND 00011 //*parenthesis evaluated first*
 - 11000 OR 00010 //*And has higher precedence so evaluated first*
 - **11010**
5. (LCIRC-3 11001) AND (RSHIFT-2 10110)
 - 01110 AND (RSHIFT-2 10110)
 - 01110 AND 00101
 - **00100**
6. (RCIRC-4 10011) OR (LSHIFT-1 01101)
 - 00111 OR 11010
 - **11111**

Answers 7..8

7. (RSHIFT-3 11110) AND (LCIRC-1 00111) OR (LSHIFT-2 01010)
 - 00011 AND 01110 OR (01000)
 - 00010 OR 01000
 - **01010**
8. (LSHIFT-2 01101) OR (RCIRC-3 10110) AND (RSHIFT-1 11011)
 - 11010 OR 11010 AND 01101
 - 11010 OR 01000
 - **11010**

What does this Program do ? Q1.

```
num = 72
for i = 2 to 6
    count = 0
    while num % i == 0
        num = num / i
        count = count + 1
    end while
    if count > 0 then
        output i, count
    end if
```

What does this Program do ? A1.

- i = 2
 - num = 72
 - $72 \% 2 == 0 \rightarrow$ yes
 - num = 36, count = 1
 - $36 \% 2 == 0 \rightarrow$ yes
 - num = 18, count = 2
 - $18 \% 2 == 0 \rightarrow$ yes
 - num = 9, count = 3
 - $9 \% 2 != 0 \rightarrow$ stop
 - output $\rightarrow 2\ 3$
- I=3
 - output $\rightarrow 3\ 2$
- I = 4 ,5, 6
 - num = 1 (not divisible by any)
 - no output

```
num = 72
for i = 2 to 6
    count = 0
    while num % i == 0
        num = num / i
        count = count + 1
    end while
    if count > 0 then
        output i, count
    end if
```

What does this Program do ? Q2.

```
sum = 0
for i = 1 to 5
    for j = 1 to i
        sum = sum + j
    next j
next i
output sum
```

What does this Program do ? A2.

- Nested loop sum : 35

i	j	Added	sum
1	1	1	1
2	1+2	3	4
3	1+2+3	6	10
4	1+2+3+4	10	20
5	1+2+3+4+5	15	35

```
sum = 0
for i = 1 to 5
    for j = 1 to i
        sum = sum + j
    next j
next i
output sum
```

What does this Program do ? Q3

```
x = 0
for i = 10 to 20
    if i % 3 == 0 and i % 4 != 0 then
        x = x + i
    end if
next i
output x
```

What does this Program do ? A3

- We want
 - Divisible by 3
 - NOT divisible by 4
- $15 + 18 = 33$

i	%3	%4	Include?
12	Y	Y	No
15	Y	N	Yes
18	Y	N	Yes

```
x = 0
for i = 10 to 20
    if i % 3 == 0 and i % 4 != 0 then
        x = x + i
    end if
next i
output x
```

What does this Program do ? Q4

```
n = 2468
count = 0
while n > 0
    digit = n % 10
    if digit % 2 == 0 then
        count = count + 1
    end if
    n = n / 10
end while
output count
```

What does this Program do ? A4

- Output 4

Step	digit	even?	count
8	yes	1	1
6	yes	2	2
4	yes	3	3
2	yes	4	4

```
n = 2468
count = 0
while n > 0
    digit = n % 10
    if digit % 2 == 0 then
        count = count + 1
    end if
    n = n / 10
end while
output count
```

What does this Program do ? Q5

```
A = [3, 6, 9, 12, 15]
for i = 0 to 4
    if A[i] % 3 == 0 then
        A[i] = A[i] / 3
    end if
next i
output A
```

What does this Program do ? A5

- Divide every element by 3
- Output 1,2,3,4,5

Index	Original	New
0	3	1
1	6	2
2	9	3
3	12	4
4	15	5

```
A = [3, 6, 9, 12, 15]
for i = 0 to 4
    if A[i] % 3 == 0 then
        A[i] = A[i] / 3
    end if
next i
output A
```

What does this Program do ? Q6

```
A = [5, 1, 4, 2]
for i = 0 to 2
    if A[i] > A[i+1] then
        temp = A[i]
        A[i] = A[i+1]
        A[i+1] = temp
    end if
next i
output A
```

What does this Program do ? A6

- Single pass swap
 - Output : 1,4,2,5
 - **Note : not sorted**
- i = 0
 - $5 > 1 \rightarrow$ swap $\rightarrow [1, 5, 4, 2]$
- i = 1
 - $5 > 4 \rightarrow$ swap $\rightarrow [1, 4, 5, 2]$
- i = 2
 - $5 > 2 \rightarrow$ swap $\rightarrow [1, 4, 2, 5]$

```
A = [5, 1, 4, 2]
for i = 0 to 2
    if A[i] > A[i+1] then
        temp = A[i]
        A[i] = A[i+1]
        A[i+1] = temp
    end if
next i
output A
```

What does this Program do ? Q7

```
n = 5
result = 1
for i = 1 to n
    result = result * i
    if result > 50 then
        output i
        break
    end if
next i
```

What does this Program do ? A7

- Output 5

<u>Step i</u>		<u>result</u>	<u>action</u>
1	1	1	result < 50 continue
2	2	2	result < 50 continue
3	3	6	result < 50 continue
4	4	24	result < 50 continue
5	5	120	result > 50 break

```
n = 5  
  
result = 1  
  
for i = 1 to n  
    result = result * i  
    if result > 50 then  
        output i  
        break  
    end if  
  
next i
```

Boolean Logic/Algebra

- The inputs are : 0,1 {only}
- The outputs are : 0,1 {only}
- Operators
 - ()
 - NOT $\rightarrow \bar{A}$
 - AND $\rightarrow A \cdot B$
 - XOR $\rightarrow A \oplus B$
 - XNOR $\rightarrow \overline{A \oplus B}$
 - OR $\rightarrow A + B$

Truth Tables (same as bitwise operations → easy)

X	\bar{X}
0	1
1	0

X	Y	$X \cdot Y$	$X + Y$	$X \oplus Y$
0	0	0	0	0
0	1	0	1	1
1	0	0	1	1
1	1	1	1	0

Some expressions

- Evaluate for $A = 1$, $B = 0$, $C = 0$

- $A \cdot (B + C)$
- $\bar{A} \cdot (B + C)$
- $A \cdot (\bar{B} + C)$
- $(A + B)(A + C)$
- $A + \bar{A} \cdot B$
- $A + AB$

Rules/Discovery

- Identity
 - $A + 0 = A$
 - $A \cdot 1 = A$
 - $A + 1 = 1$
 - $A \cdot 0 = 0$
- Idempotent
 - $A + A = ?$
 - $A \cdot A = ?$
- Complement
 - $A + \bar{A} = ?$
 - $A \cdot \bar{A} = ?$

Some more rules

- Double Negation
 - $\bar{\bar{A}} = A$
- Absorption law
 - $A + A \cdot B = A$
 - $A \cdot (A + B) = A$

Do it yourself

- Hint : These may be actual theorems

- $\overline{A \cdot B} = ?$

- $\overline{A + B} = ?$

- $(A + B) \cdot (\bar{A} + C) = ?$

- $A(\bar{A} + B) = ?$

- $A + \bar{A}B = ?$