

**PRACTICE QUESTIONS**  
**MATHEMATICS Compulsory Part**  
**Question-Answer Book**

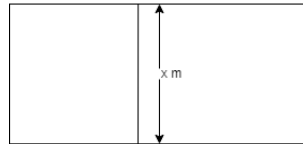
**Instructions**

1. This paper must be answered in English.
2. Unless otherwise specified, all working must be clearly shown.
3. Unless otherwise specified, numerical answers must be exact.
4. This paper is for **internal use** only.
5. All questions are collected from AL/CE/DSE past papers, reference site:  
<https://www.dse.life/ppindex/m2/>

- 
- This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

- 
- This image shows a single page of white paper with horizontal blue or grey ruling lines. The lines are evenly spaced and run across the width of the page, leaving small margins at the top and bottom. There are no vertical margin lines, text, or other markings on the page.

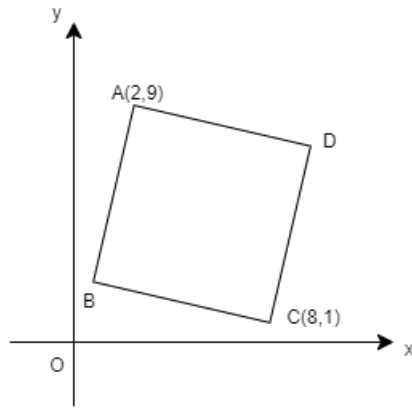
3. (a) Let  $f(x) = 36x - x^2$ . Using the method of completing the square, find the coordinates of the vertex of the graph of  $y = f(x)$ .
- (b) The length of a piece of string is 108m. A guard cuts the string into two pieces. One piece is used to enclose a rectangular restricted zone of area  $A \text{ m}^2$ . The other piece is used to divide this restricted zone into two rectangular regions as shown in the figure.



- Express  $A$  in terms of  $x$ .
- The guard claims that the area of this restricted zone can be greater than  $500 \text{ m}^2$ . Do you agree? Explain your answer.

This image shows a blank sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.





- (a) Find
  - i. the coordinates of  $E$ ,
  - ii. the equation of  $BD$ .
- (b) It is given that the equation of  $AD$  is  $x + 7y - 65 = 0$ . Find
  - i. the equation of  $BC$ ,
  - ii. the length of  $AB$ .

[illegible]









- [illegible]

- [illegible]

8. Factorize

(a)  $x^3 + x^2y - 7x^2$ .

(b)  $x^3 + x^2y - 7x^2 - x - y + 7$ .

---

---

---

---

---

---

---

---

---

---

---

---

9. Factorize

(a)  $4m^2 - 9$ .

(b)  $2m^2n + 7mn - 15n$ .

(c)  $4m^2 - 9 - 2m^2n - 7mn + 15n$

---

---

---

---

---

---

---

---

---

---

---

---

- 
- This image shows a blank sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

11. If  $3x^2 - kx - 2$  is divisible by  $x - k$ , find the two values of  $k$ .

[illegible]

- 
- This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

[illegible]

13. Simplify and express the following with positive indices

(a)  $\frac{x^3y^2}{x^{-3}y}$ .

(b)  $x(\frac{x^{-1}}{y^2})^{-3}$ .

(c)  $\frac{(m^5n^{-2})^6}{m^4n^{-3}}$ .

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



[illegible]

[illegible]

16. Let  $\log 2 = x, \log 3 = y$ . Express the following in terms of  $x$  and  $y$ .

- (a)  $\log 18$ .  
(b)  $\log 15$ .  
(c)  $\log \sqrt{12}$ .

This image shows a blank sheet of white paper with horizontal ruling lines. The lines are evenly spaced and extend across the width of the page. There are no margins, text, or other markings on the paper.

17. Solve the following without using calculator:

- (a)  $3^x = \frac{1}{\sqrt{27}}$ ;  
(b)  $\log x + 2 \log 4 = \log 48$ .

[illegible]

18. A researcher defined Scale  $A$  and Scale  $B$  to represent the magnitude of an explosion as shown in the table:

Scale	Formula
$A$	$M = \log_4 E$
$B$	$N = \log_8 E$

It is given that  $M$  and  $N$  are the magnitudes of an explosion on Scale  $A$  and Scale  $B$  respectively, while  $E$  is the relative energy released by the explosion. If the magnitude of an explosion is 6.4 on Scale  $B$ , find the magnitude of the explosion on Scale  $A$ .

[illegible]

19. Let  $a$  and  $b$  be constants. Denote the graph of  $y = a + \log_b x$  by  $G$ . The x-intercept of  $G$  is 9 and  $G$  passes through the point  $(243, 3)$ . Express  $x$  in terms of  $y$ .

[illegible]

20. Solve the following:

(a)  $\begin{cases} 4^{x-y} = 4 \\ 4^{x+y} = 16 \end{cases}$ , find  $x$  and  $y$ .

(b)  $3^{2x} + 3^x - 2 = 0$ , find  $x$ .

(c)  $\log_3(x - 3) + \log_3(x + 3) = 3$ , find  $x$ .

This image shows a blank sheet of white paper with horizontal ruling lines. The lines are evenly spaced and extend across the width of the page. There are no margins, text, or other markings on the paper.

21. If  $2\log_{10} x - \log_{10} y = 0$ . Show that  $y = x^2$ .

[illegible]

22. Solve the following equations:

(a)  $1 - 2x = \sqrt{2 - x}$ .

(b)  $x - \sqrt{x + 1} = 5$ .

(c)  $x - 5\sqrt{x} - 6 = 0$ .

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

23. Find the range of values of  $k$  for which the equation  $2x^2 + x + 5 = k(x + 1)^2$  has no real roots.

---

---

---

---

---

---

---

---

---

---

24. The quadratic equations  $x^2 - 6x + 2k = 0$  and  $x^2 - 5x + k$  have a common root  $\alpha$ . (i.e.  $\alpha$  is a root of both equations.) Show that  $\alpha = k$  and hence find the value(s) of  $k$ .

---

---

---

---

---

---

---

---

---

---

This image shows a single sheet of white paper with horizontal blue ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



26. If  $\frac{1}{m} + \frac{1}{n} = \frac{1}{a}$  and  $m + n = b$ , express the following in terms of  $a$  and  $b$

(a)  $mn$ ,

(b)  $m^2 + n^2$ .

---

---

---

---

---

---

---

---

---

---

27. Suppose  $\alpha$  and  $\beta$  are roots of the equation  $kx^2 - 4x + 2k = 0$ , where  $k$  ( $k \neq 0$ ) is a constant. Express the following in terms of  $k$ :

(a)  $\alpha^2 + \beta^2$ ,

(b)  $\frac{\alpha}{\beta} + \frac{\beta}{\alpha}$ .

---

---

---

---

---

---

---

---

---

---

28. Express  $\frac{1}{1+2i}$  in the form of  $a+bi$ , where  $a$  and  $b$  are real numbers.

---

---

---

---

---

---

---

---

---

---

---

---

29. If  $a:b=3:4$  and  $a:c=2:5$ , find

- (a)  $a:b:c$ ,  
(b) the value of  $\frac{ac}{a^2+b^2}$ .

---

---

---

---

---

---

---

---

---

---

---

---

- [illegible]

- [illegible]

32. A variable quantity  $y$  is the sum of two parts. The first part varies directly as another variable  $x$ , while the second part varies directly as  $x^2$ . When  $x = 1$ ,  $y = -5$ ; when  $x = 2$ ,  $y = -8$ .

- Express  $y$  in terms of  $x$ .
- Hence, find the value of  $y$  when  $x = 6$ .

[illegible]

- 
- This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

- Find  $h(x)$ .
- Solve the equation  $h(x) = 3x^2$ .

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

35. Simplify the following:

(a)  $\frac{1 - \cos^2 x}{\sin x}$ .

(b)  $\frac{\sin(180^\circ - \theta)}{\sin(90^\circ + \theta)}$ .

(c)  $\sin^2(180^\circ - \phi) + \sin^2(270^\circ + \phi)$ .

---

---

---

---

---

---

---

---

---

---

36. Solve the following with  $0^\circ \leq \theta < 360^\circ$ . Give your answer in 3 significant figures if needed.

(a)  $\sin^2 \theta + 7 \sin \theta = 5 \cos^2 \theta$ .

(b)  $\sin^2 \theta - 3 \cos \theta - 1 = 0$ .

---

---

---

---

---

---

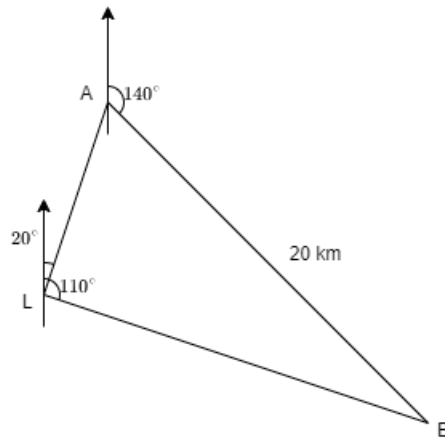
---

---

---

---

37. In the figure, the bearings of two ships  $A$  and  $B$  from a light house  $L$  are  $020^\circ$  and  $110^\circ$  respectively.  $B$  is 20 km and at a bearing of  $140^\circ$  from  $A$ .



Find

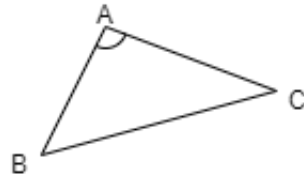
- the distance of  $L$  from  $B$ ,
- the bearing of  $L$  from  $B$ .

[illegible]



This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

38. In the figure,  $AB = 4$ ,  $AC = 5$  and  $BC = 7$ . Calculate  $\angle A$  to the nearest degree.



---

---

---

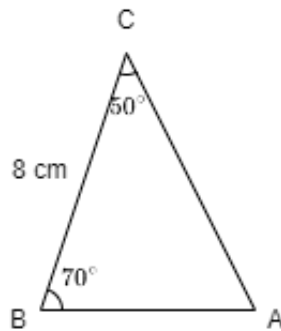
---

---

---

---

39. In the figure, find  $AB$  and the area of  $\triangle ABC$ .



---

---

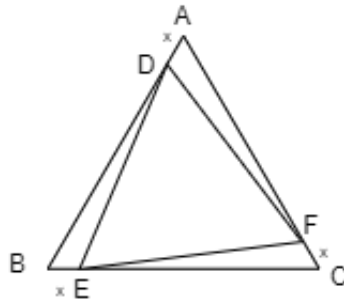
---

---

---

---

---



- By using the cosine formula or otherwise, express  $DE^2$  in terms of  $x$ .
- Show that the area of  $\triangle DEF = \frac{\sqrt{3}}{4}(3x^2 - 6x + 4)$ .

[illegible]

[illegible]