



The Container Stacking Problem

-

Final Presentation

Daniel Monteiro & Rafael Ribeiro

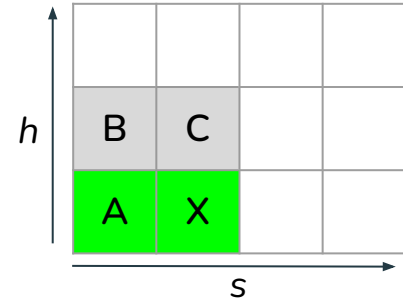
Previously on...

Problem definition

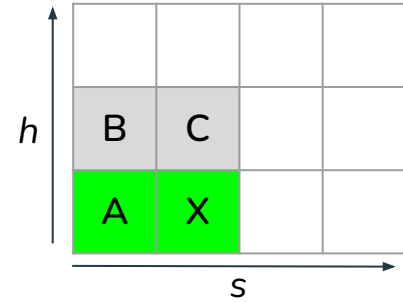
Given:

- The starting positions of the containers
- The number of stacks (s)
- The maximum height of the stacks (h)
- The maximum number of operations (t)
- A list of the containers we wish to remove (A and X, in this case)

Minimize the number of operations necessary to remove the desired containers



Three possible operations



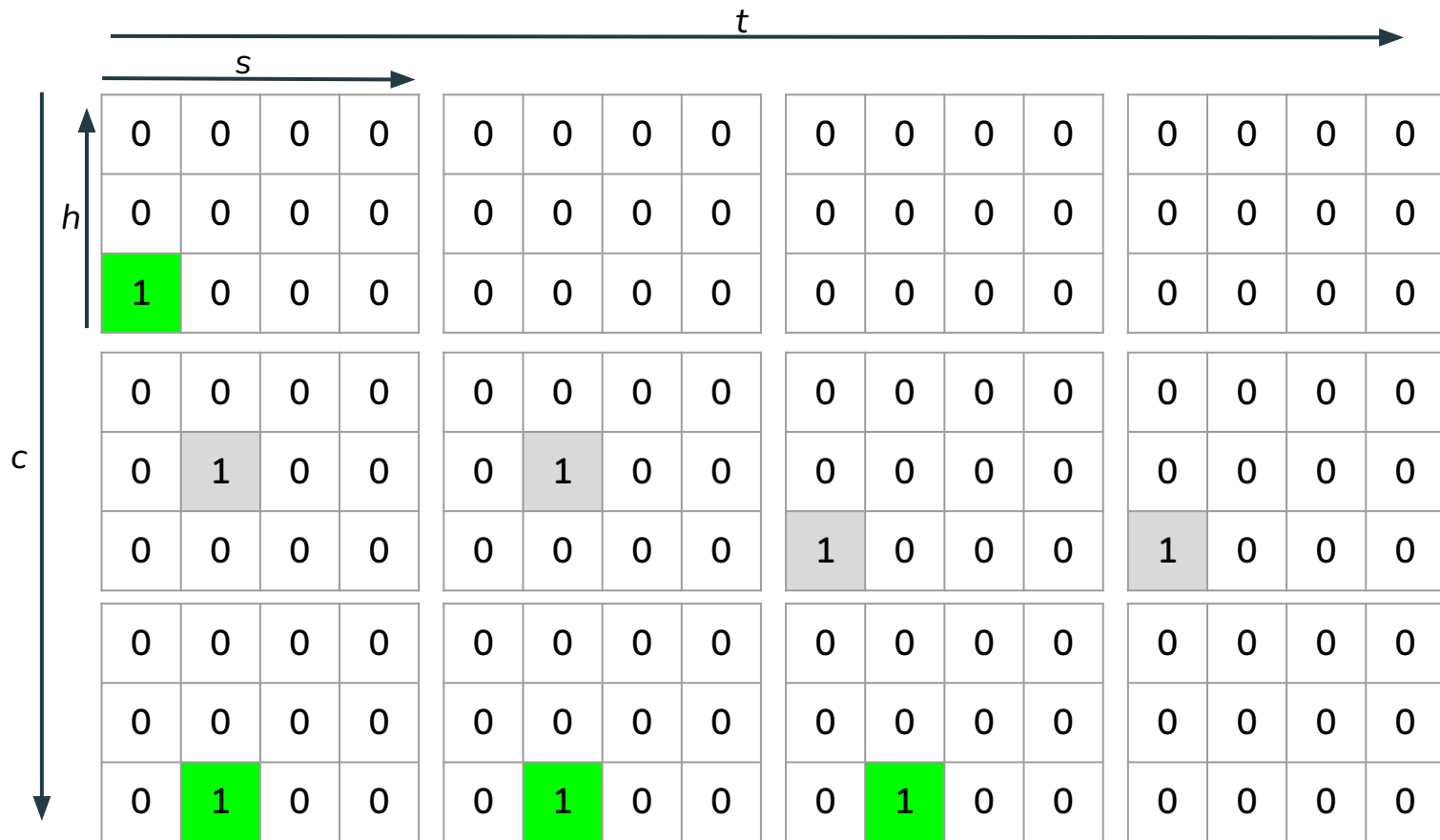
1. Move top container from stack a to stack b
2. Remove container from stack a
3. Idle (leave all the containers untouched)

	C		
A	X		

	C		
	X		

C	X		

C			



Previously on...

Time
↑
Container
↑
M[t][c][s][h]
↓ ↓
Stack Height

	t=0	t=1	t=2	t=3
A	1	0	0	0
C	1	1	1	1
X	1	1	1	0

Lifetimes

	op1	op2	op3
Emplace	0	1	0
Idle	0	0	0
Remove	1	0	1

Operations

In	0	0	0	0
	0	0	0	0
	0	0	0	0
Out	0	0	0	0
	0	0	0	0
	1	0	0	0



Here's what's new

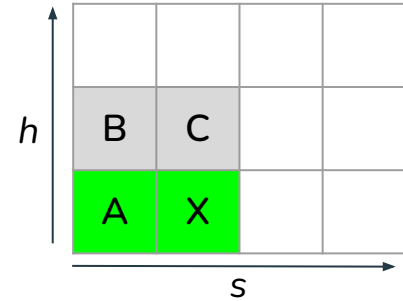


Problem definition

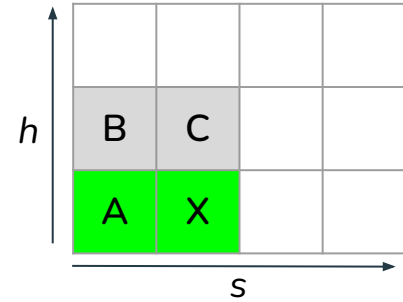
Given:

- The starting positions of the containers
- The weight of the containers (lighter containers on top of the heavier)
- The number of stacks (s)
- The maximum height of the stacks (h)
- The list of shipments and for how long they are docked
 - Each shipment can add or remove some containers to the problem

Minimize the number of operations necessary to remove the desired containers



Four possible operations



1. Move top container from stack a to stack b
2. Remove container from stack a
3. Idle (leave all the containers untouched)
4. Insert container to stack a

Example of a problem instance

```
{
  "containers" : [
    ["X", 0, 0],
    ["Y", 1, 0]
  ],
  "dimensions" : [4, 3],
  "shipments" : [
    {
      "in": ["A", "B", "C", "D", "E", "F", "G"],
      "out": [],
      "duration": 10,
    },
    {
      "duration": 5,
    },
    {
      "in": ["1", "2", "3"],
      "out": ["B", "D", "G"],
      "duration": 10,
    },
    ...
  ],
  "weights" : {
    "A" : 2,
    "1" : 2
  }
}
```



Feature highlight: shipments



Feature highlight: shipments

- Shipment 0
 - Duration: 5 | In: **[A, B]** | Out: []
- Gap
 - Duration: 3
- Shipment 1
 - Duration: 3 | In: **[C]** | Out: **[A]**
- Shipment 2
 - Duration: 4 | In: [] | Out: **[B]**
- Gap
 - Duration: 2

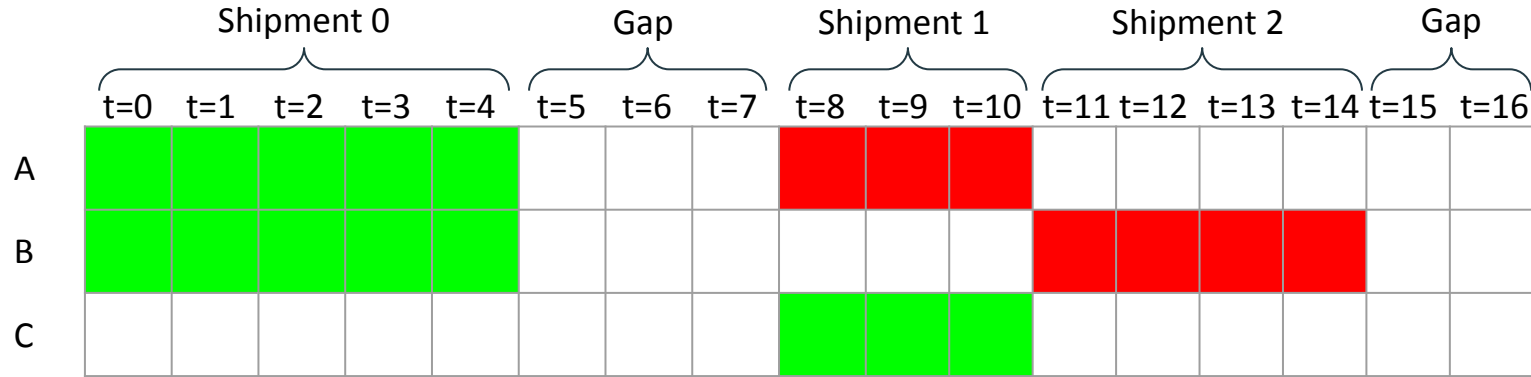
$$\text{Dimension T} = 5 + 3 + 3 + 4 + 2 = 17$$

Feature highlight: shipments

	Shipment 0					Gap			Shipment 1			Shipment 2				Gap	
	t=0	t=1	t=2	t=3	t=4	t=5	t=6	t=7	t=8	t=9	t=10	t=11	t=12	t=13	t=14	t=15	t=16
A																	
B																	
C																	

Lifetimes

Feature highlight: shipments



Lifetimes

Feature highlight: shipments

	Shipment 0					Gap			Shipment 1			Shipment 2				Gap	
	t=0	t=1	t=2	t=3	t=4	t=5	t=6	t=7	t=8	t=9	t=10	t=11	t=12	t=13	t=14	t=15	t=16
A						1	1	1				0	0	0	0	0	0
B						1	1	1	1	1	1					0	0
C	0	0	0	0	0	0	0	0				1	1	1	1	1	1

Lifetimes

Feature highlight: shipments

	Shipment 0					Gap			Shipment 1			Shipment 2				Gap	
	t=0	t=1	t=2	t=3	t=4	t=5	t=6	t=7	t=8	t=9	t=10	t=11	t=12	t=13	t=14	t=15	t=16
A						1	1	1				0	0	0	0	0	0
B						1	1	1	1	1	1					0	0
C	0	0	0	0	0	0	0	0				1	1	1	1	1	1

Lifetimes

The spaces in blank are left as an exercise to the reader cplex...



Feature highlight: weight restrictions



Feature highlight: weight restrictions

For every possible container location:

- if container exists:

- enforce lighter containers not being able to be placed below it

```
def enforce_weight_restrictions(model : Model, matrix : ContainerMatrix, weights : dict, index_lookup):  
    weight_array = [0] * len(index_lookup)
```

```
    for c, weight in weights.items():  
        weight_array[index_lookup[c]] = weight
```

```
    for t in range(matrix.t):
```

```
        for s in range(matrix.s):
```

```
            for h in range(matrix.h):
```

```
                for c in range(matrix.c):
```

```
                    container_is_here = model.NewBoolVar('b')
```

```
                    model.AddIf(matrix.get(t, c, s, h) == 1, container_is_here)
```

```
                    model.AddIf(matrix.get(t, c, s, h) == 0, model.Not(container_is_here))
```

} For every possible container location

```
    for container in range(matrix.c):
```

```
        for height in range(matrix.h):
```

```
            if container != c and height < h and weight_array[container] < weight_array[c]:
```

```
                model.AddIf(matrix.get(t, container, s, height) == 0, container_is_here)
```

} Don't

If container is lower and lighter



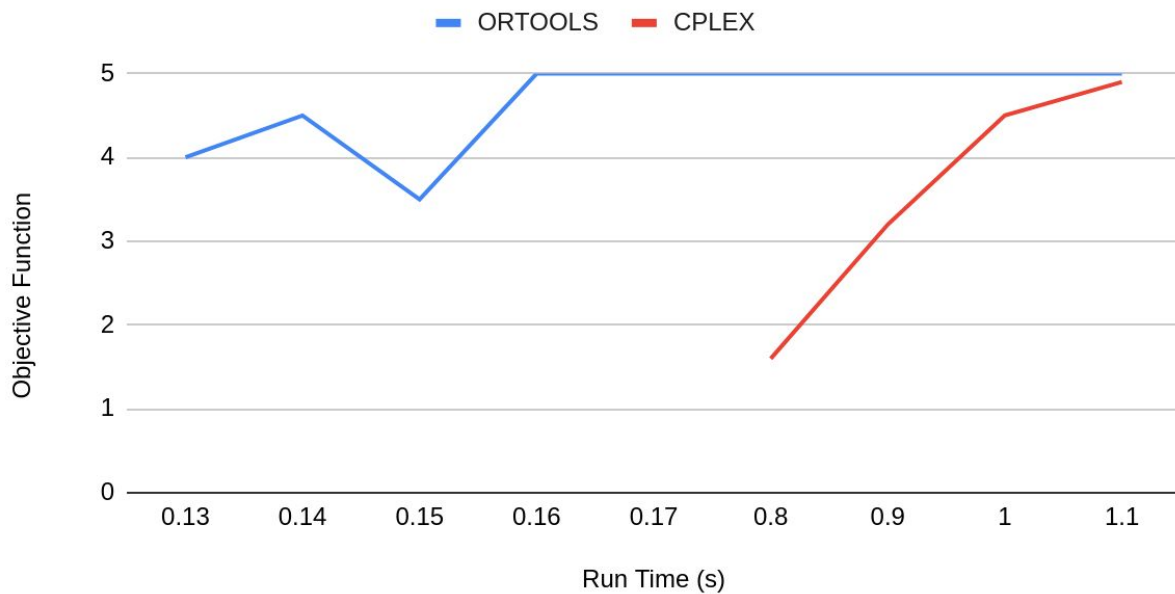
Performance analysis: Intermediate version



```
{  
  "containers" : [  
    ["A", 0, 0],  
    ["B", 0, 1],  
    ["C", 1, 1],  
    ["X", 1, 0]  
  ],  
  "dimensions" : [10, 4, 3],  
  "remove" : ["A", "X"]  
}
```

Implementation performance

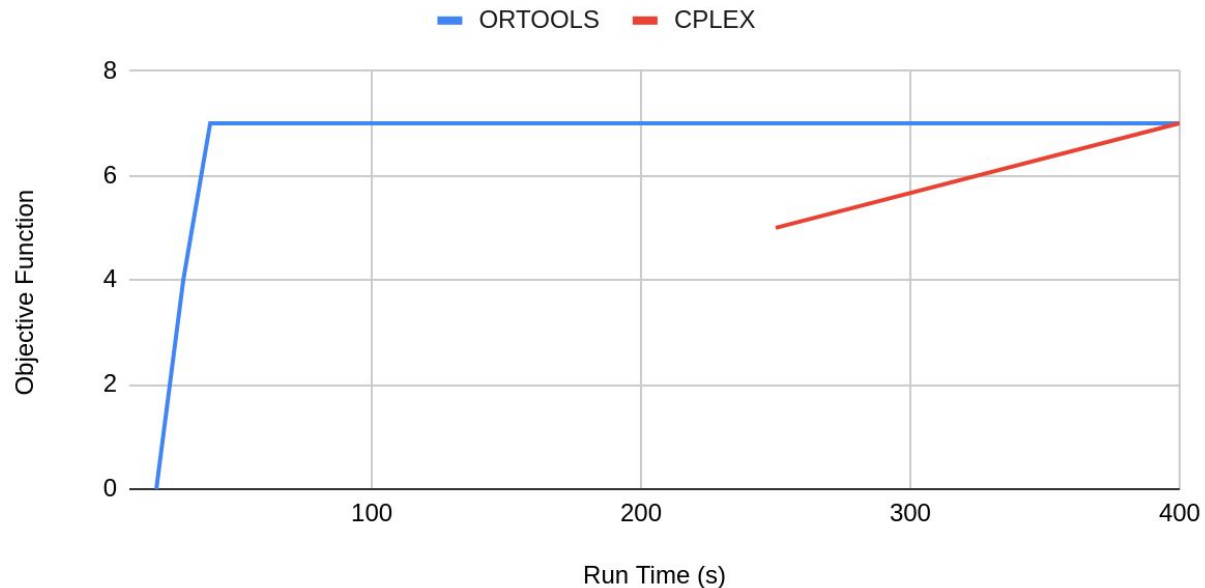
input.json



```
{  
  "containers" : [  
    ["A", 0, 0],  
    ["W", 0, 1],  
    ["B", 0, 2],  
    ["C", 0, 3],  
    ["X", 0, 4],  
    ["D", 0, 5],  
    ["E", 1, 0],  
    ["Y", 1, 1],  
    ["F", 1, 2],  
    ["G", 1, 3],  
    ["Z", 2, 0],  
    ["H", 2, 1],  
    ["I", 2, 2],  
    ["J", 2, 3]  
  ],  
  "dimensions" : [20, 4, 6],  
  "remove" : ["W", "X", "Y", "Z"]  
}
```

Implementation performance

suboptimal.json





Performance analysis: Final version



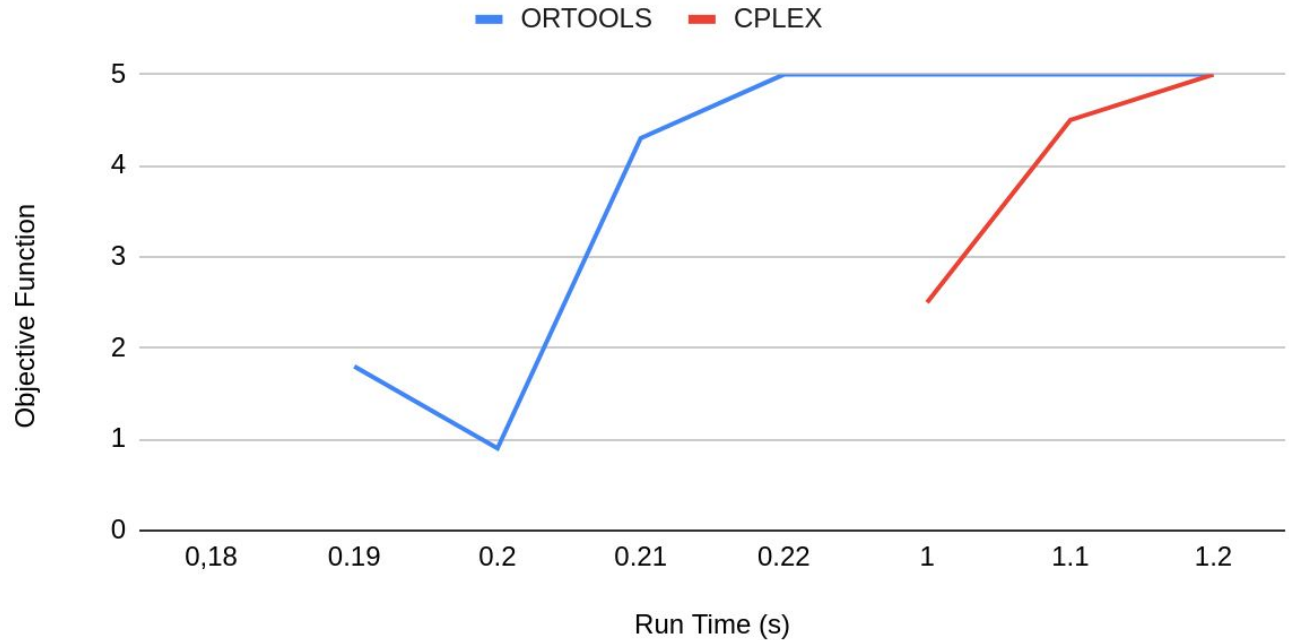
```

{
  "containers" : [
    ["A", 0, 0],
    ["B", 0, 1],
    ["C", 1, 1],
    ["X", 1, 0]
  ],
  "dimensions" : [4, 3],
  "shipments": [
    {
      "duration": 1
    },
    {
      "in": [],
      "out": [
        "A", "B", "C", "X"
      ],
      "duration": 10
    }
  ],
  "weights" : {
    "A" : 2,
    "B" : 2,
    "C" : 2,
    "X" : 2
  }
}

```

Implementation performance

input.json



```
{
  "containers" : [
    ["9", 0, 0],
    ["8", 0, 1],
    ["7", 0, 2],
    ["6", 0, 3],
    ["5", 0, 4],
    ["4", 0, 5],
    ["3", 0, 6]
  ],
  "dimensions" : [3, 7],
  "shipments" : [
    {
      "duration" : 33
    },
    {
      "in": [],
      "out": ["9"],
      "duration" : 2
    }
  ],
  "weights" : {
    "9" : 9,
    "8" : 8,
    "7" : 7,
    "6" : 6,
    "5" : 5,
    "4" : 4,
    "3" : 3
  }
}
```

Implementation performance

hanoi.json

