

2) a) plano horizontal que es tangente

$$Z = x^2 - 4xy - 2y^2 + 12x - 12y - 1$$

$$Z_x = 2x - 4y + 12$$

$$Z_y = -4x - 4y - 12$$

$$\nabla Z_{(x_0, y_0)} = (2x_0 - 4y_0 + 12, -4x_0 - 4y_0 - 12)$$

Para que sea horizontal

$$(0, 0) = (2x_0 - 4y_0 + 12, -4x_0 - 4y_0 - 12)$$

$$\bullet 0 = 2x_0 - 4y_0 + 12$$

$$\bullet 0 = -4x_0 - 4y_0 - 12$$

$$4y_0 = 2x_0 + 12$$

$$0 = -4x_0 - 2x_0 - 12 - 12$$

$$4y_0 = 2 \cdot (-4) + 12$$

$$\frac{24}{-6} = x_0$$

$$\boxed{y_0 = 1}$$

$$\boxed{x_0 = -4}$$

• Ecuación del plano tangente

$$p = (x-a)f_x(a,b) + (y-b)f_y(a,b) + f(a,b)$$

$$p = (x+4) \cdot (2 \cdot (-4) - 4 \cdot 1 + 12) + (y-1)(-4 \cdot (-4) - 4 \cdot 1 - 12) + \dots$$

$$\dots + ((-4)^2 - 4 \cdot (-4) \cdot 1 - 2 \cdot 1^2 + 12 \cdot (-4) - 12 \cdot 1 - 1)$$

$$= 0 + 0 + (16 + 16 - 2 - 48 - 12 - 1)$$

$$\boxed{p = -31}$$

Rta: la ecuación de plano horizontal que es tangente es:  $\boxed{p = -31}$

y el punto es  $(x_0, y_0) = (-4, 1)$

$$2) \quad b) \quad z = \text{Sen}(x^2 y) \quad x = st^2 \quad y = s^2 + 1/t$$

$$\frac{\partial z}{\partial s}(s, t) \quad \frac{\partial z}{\partial t}(s, t) \quad \bullet (s, t) = (1, 1)$$

$$z_x = \cos(x^2 y) \cdot 2xy \quad z_y = \cos(x^2 y) \cdot x^2$$

$$x_s = t^2$$

$$y_s = 2s$$

$$x_t = 2st$$

$$y_t = -\frac{1}{t^2}$$

$$z_s = \cos(s^2 t^4 \cdot (s^2 + 1/t)) \cdot 2st^2(s^2 + 1/t)t^2 + \cos(s^2 t^4 \cdot (s^2 + 1/t)) \cdot s^2 t^4 \cdot 2s$$

$$= \cos(s^4 t^4 + s^2 t^3) (2s^3 t^4 + 2st^3) + \cos(s^4 t^4 + s^2 t^3) 2s^3 t^4$$

$$= \cos(s^4 t^4 + s^2 t^3) \cdot (2s^3 t^4 + 2st^3 + 2s^3 t^4)$$

$$= \cos(s^4 t^4 + s^2 t^3) \cdot (4s^3 t^4 + 2st^3)$$

$$z_t = \cos(s^2 t^4 \cdot (s^2 + 1/t)) \cdot 2st^2(s^2 + 1/t) \cdot 2st + \cos(s^2 t^4 \cdot (s^2 + 1/t)) \cdot s^2 t^4 \cdot \frac{(-1)}{t^2}$$

$$= \cos(s^4 t^4 + s^2 t^3) \cdot (4s^4 t^3 + 4s^2 t^2) + \cos(s^4 t^4 + s^2 t^3) \cdot (-s^2 t^2)$$

$$= \cos(s^4 t^4 + s^2 t^3) (4s^4 t^3 + 4s^2 t^2 - s^2 t^2)$$

$$= \cos(s^4 t^4 + s^2 t^3) (4s^4 t^3 + 3s^2 t^2)$$

$$z_s(1, 1) = \cos(1 + 1) \cdot (4 \cdot 1 + 2 \cdot 1)$$

$$= 6 \cos(2)$$

$$z_t(1, 1) = \cos(1 + 1) \cdot (4 \cdot 1 + 3 \cdot 1)$$

$$= 7 \cos(2)$$

