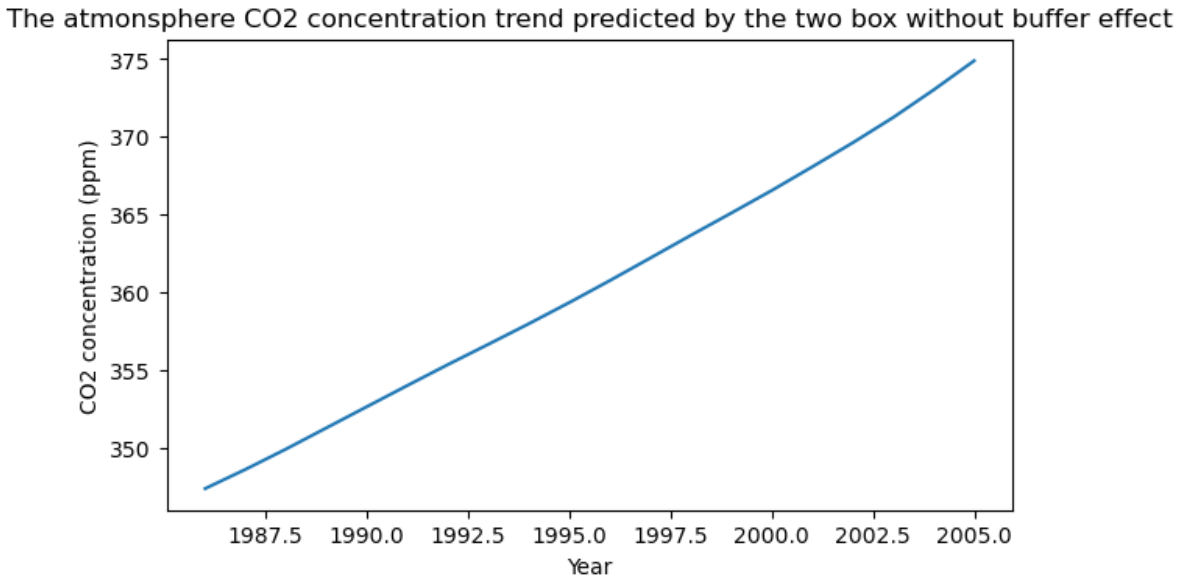
In [1]:
```
import numpy as np
import pandas as pd
from scipy.integrate import odeint
from scipy.interpolate import UnivariateSpline
import matplotlib.pyplot as plt

# fossil fuel unit is million metric tons 1e12 gram C
# unit PgC is 1e15 gram C
# 1ppm CO2 is 2.13 PgC/GtC
gamma_pd =pd.read_csv('global.1751_2014.csv',index_col= ['Year'])

# Spline interpolation
gamma = UnivariateSpline(gamma_pd.index, gamma_pd['Total carbon emissions from foss
gamma.set_smoothing_factor(0.5)
```

method to solve ODE questions

In [2]:
```
def dmove(Point,t,sets):

    k12,k21,gamma = sets
    gamma_t =gamma(t+1986)*1e-3
    n1,n2 = Point
    return np.array([ -k12*n1+k21*n2+gamma_t, k12*n1-k21*n2])

def move(Point,t,sets):

    k12,k21,gamma,sita,n02 = sets
    gamma_t =gamma(t+1986)*1e-3
    n1,n2 = Point
    return np.array([ -k12*n1+k21*(n02+sita*(n2-n02))+gamma_t, k12*n1-k21*(n02+sita

# from 1986 to 2007
t = np.arange(0,20,1)
```

plot Q1

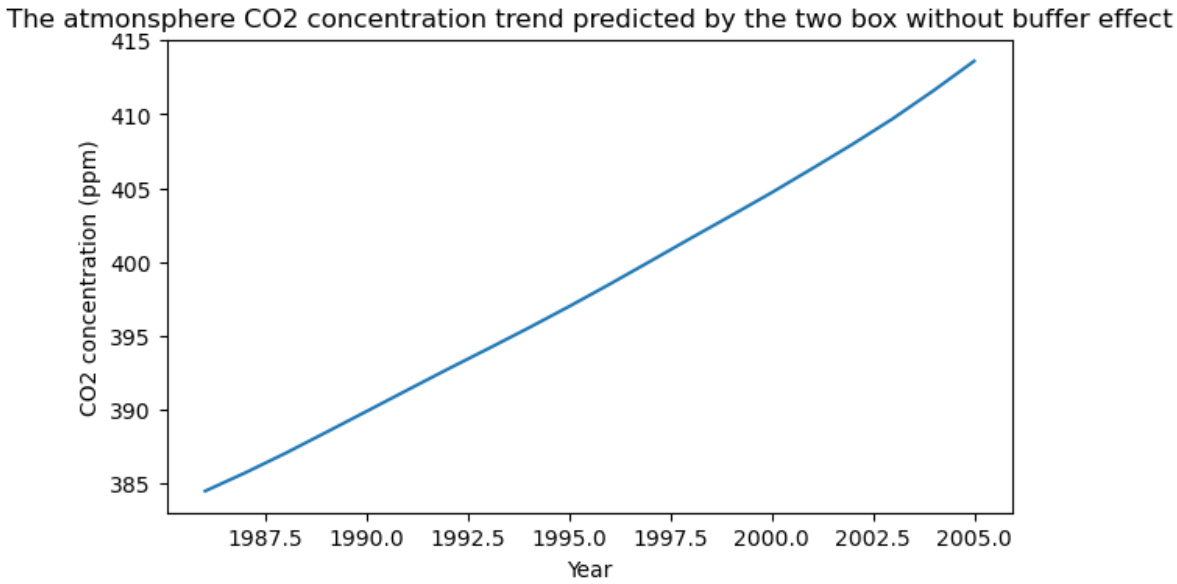
In [3]:
```
P1 = odeint(dmove,(740,900),t,args = ([105/740,102/900,gamma],))[:,0]/2.13

# plot
fig =plt.figure(figsize=(7,4),dpi =100)
plt.plot(t+1986,P1)
plt.title('The atmonsphere CO2 concentration trend predicted by the two box without
plt.ylabel('CO2 concentration (ppm)')
plt.xlabel('Year')
plt.show()
```



plot Q2

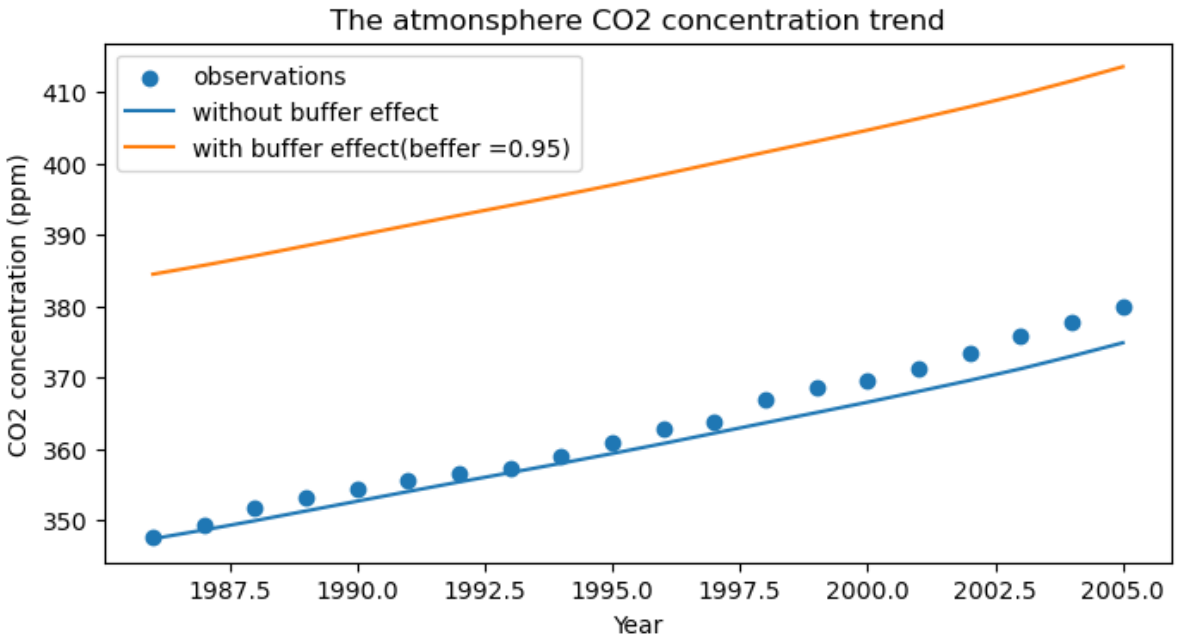
set buffer effect as 0.95

In [4]:
```
buff =0.95
P2 = odeint(move,(740+79,900-79),t,args = ([105/(740+79),102/(900-79),gamma,buff,82

# plot
fig =plt.figure(figsize=(7,4),dpi =100)
plt.plot(t+1986,P2)
plt.title('The atmonsphere CO2 concentration trend predicted by the two box without
plt.ylabel('CO2 concentration (ppm)')
plt.xlabel('Year')
plt.show()
```



plot Q3

In [5]:
```
obs =pd.read_csv('co2_annmean_mlo.csv', nrows= 20)

# plot
fig =plt.figure(figsize=(8,4),dpi =100)
plt.scatter(obs.year, obs.Mean, label ='observations')
plt.plot(t+1986,P1, label ='without buffer effect')
plt.plot(t+1986,P2, label ='with buffer effect(beffer =0.95)')
plt.title('The atmonsphere CO2 concentration trend')
plt.ylabel('CO2 concentration (ppm)')
plt.xlabel('Year')
plt.legend()
plt.show()
```



Q4

cannot find σ dataset(emission rate to the atmonsphere by changes in land use)

In [6]:
```
def sevenBox(Point,t,sets):

    k12,k21,k23,k24,k32,k34,k43,k45,k51,k67,k71, n02,f,sigma,sita,gamma = sets
    gamma_t =gamma(t+1751)*1e-3
    n1,n2,n3,n4,n5,n6,n7 = Point
    return np.array([ -k12*n1+k21*(n02+sita*(n2-n02))+gamma_t-f+sigma+k51*n5+k71*n7
                      k12*n1-k21*(n02+sita*(n2-n02))-k23*n2+k32*n3-k24*n2,
                      k23*n2-k32*n3-k34*n3+k43*n4,
                      k34*n3-k43*n4+k24*n2-k45*n4,
                      k45*n4-k51*n5,
                      f-k67*n6-2*sigma,
                      k67*n6-k71*n7+sigma
                      ])

t2 =np.arange(0,260,1)
```

In [7]:
```
P3 = odeint(sevenBox,
            (615,842,9744,26280,90000000,731,1238),
            t2,
            args = ([60/615, 60/842, 9/842, 43/842, 52/9744, 162/9744, 205/26280, 0
                     842,62, 0.7,0.38, gamma,],)
            )[:,0]/2.13

P4 = odeint(sevenBox,
            (615,842,9744,26280,90000000,731,1238),
            t2,
            args = ([60/615, 60/842, 9/842, 43/842, 52/9744, 162/9744, 205/26280, 0
                     842,62, 0.8,0.5, gamma,],)
            )[:,0]/2.13
```

In [8]:
```
fig =plt.figure(figsize=(8,4),dpi =100)
plt.plot(t2+1751,P3, label ='with buffer effect(buffer =0.38')
plt.plot(t2+1751,P4, label ='with buffer effect(beffer =0.50)')
plt.title('The atmonsphere CO2 concentration trend')
plt.ylabel('CO2 concentration (ppm)')
plt.xlabel('Year')
plt.legend()
plt.show()
```