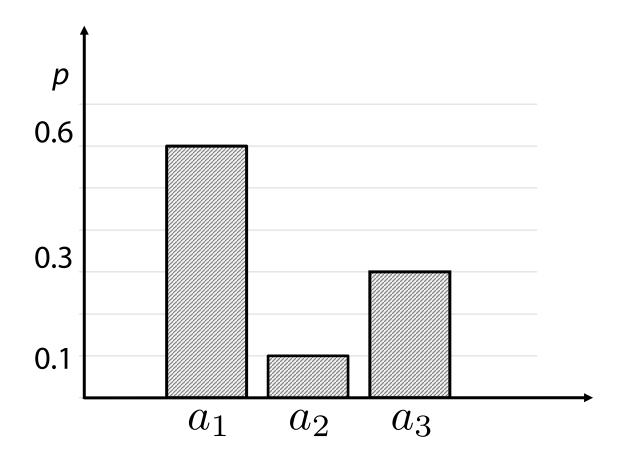
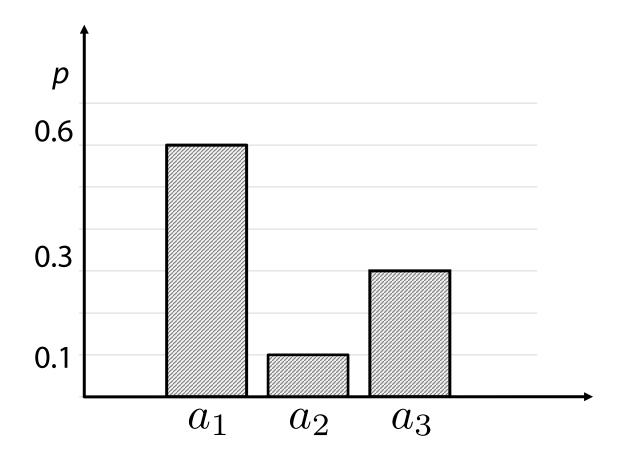
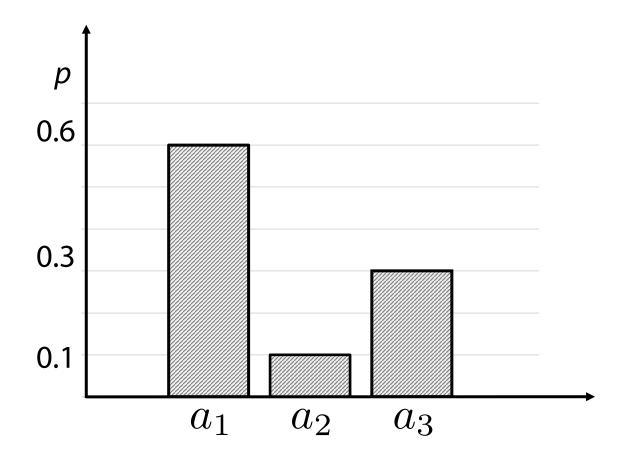
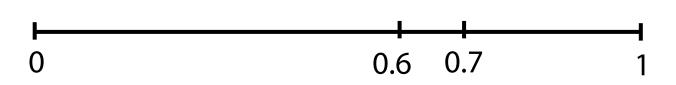
Sampling from 1d distributions

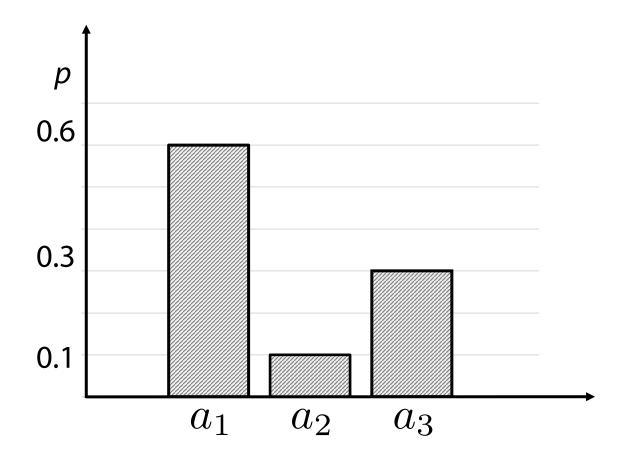


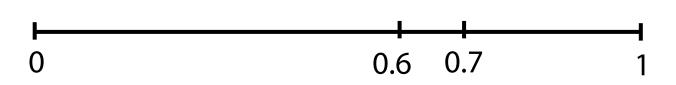


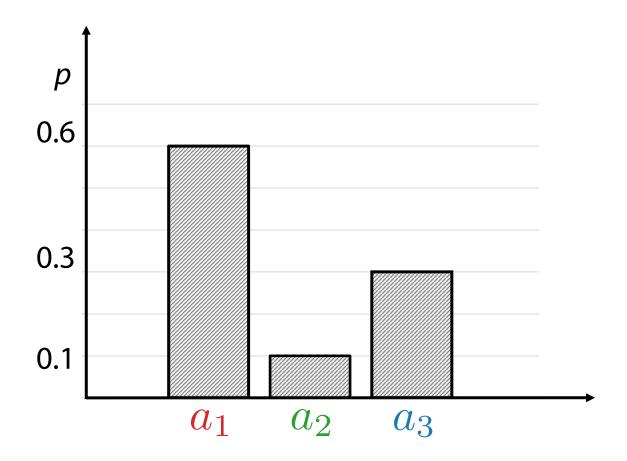
We can always sample from uniform $\,\mathcal{U}[0,1]$



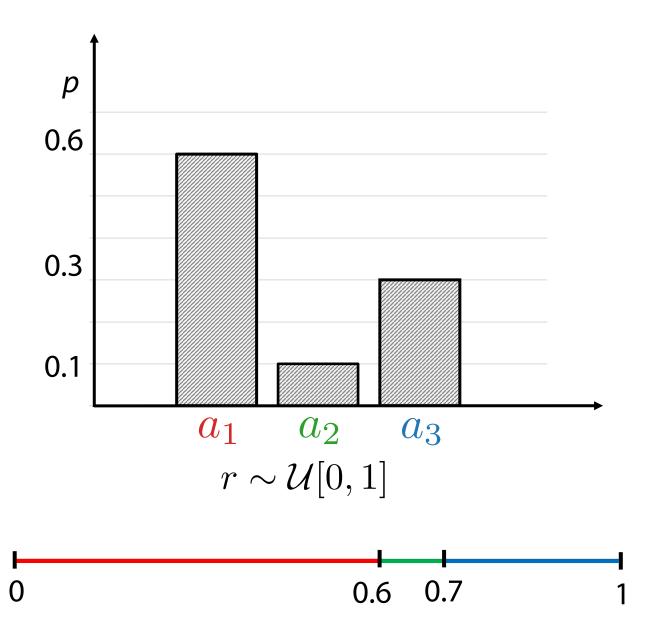


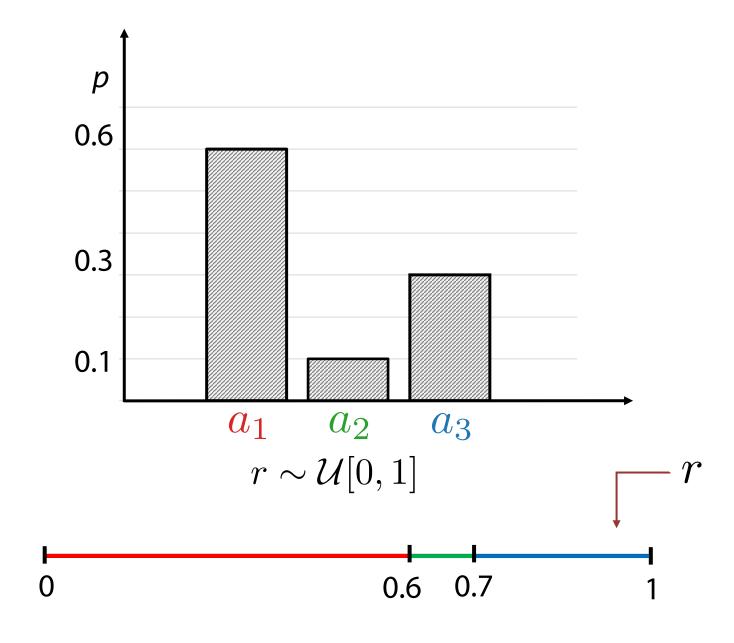














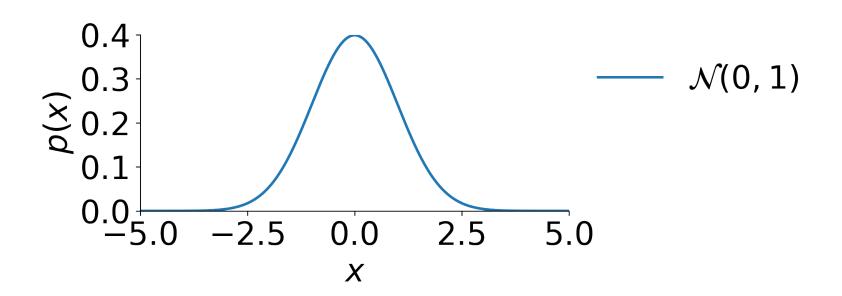
1d discrete distributions with finite number of values are easy

1d discrete distributions with finite number of values are easy

At least then number of values is < 100 000

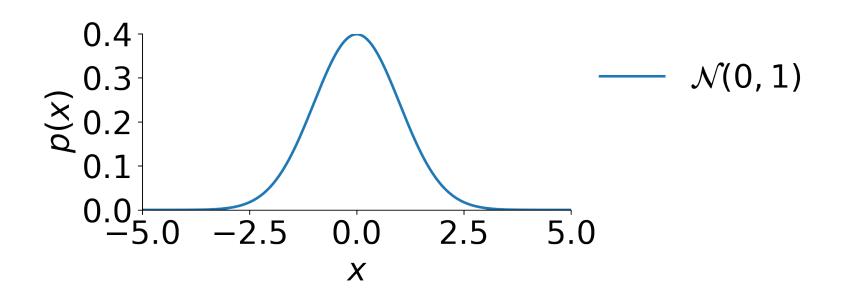
Continuous sampling

Sampling from Gaussian distribution



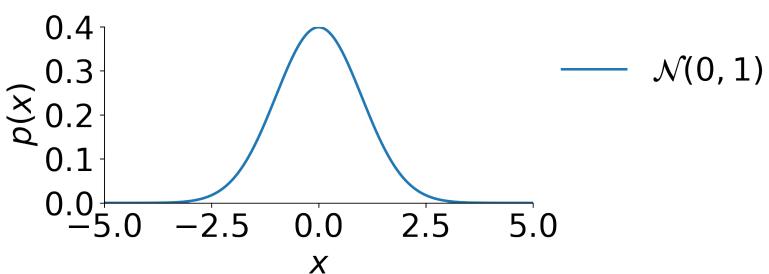
Sampling from Gaussian distribution

$$z = \sum_{i=1}^{12} x_i - 6, \quad x_i \sim \mathcal{U}[0, 1]$$



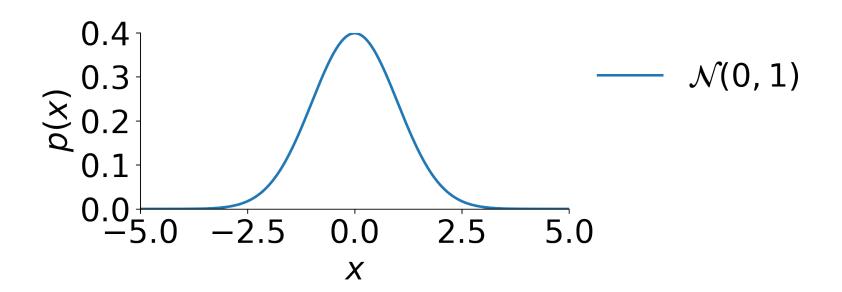
Sampling from Gaussian distribution

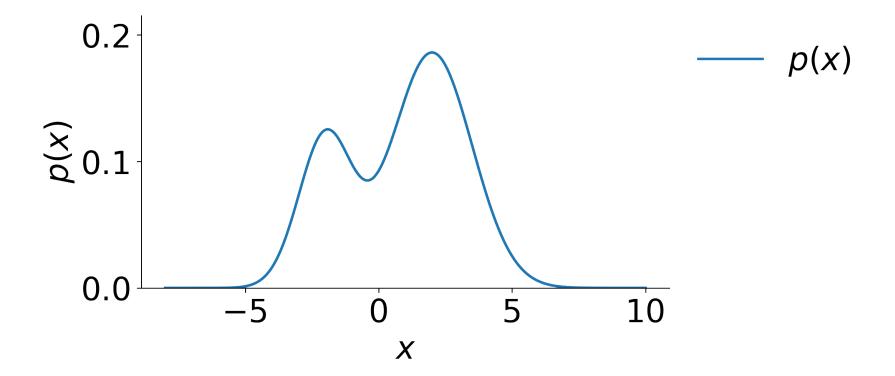
$$z = \sum_{i=1}^{12} x_i - 6, \quad x_i \sim \mathcal{U}[0, 1]$$
$$p(z) \approx \mathcal{N}(0, 1)$$

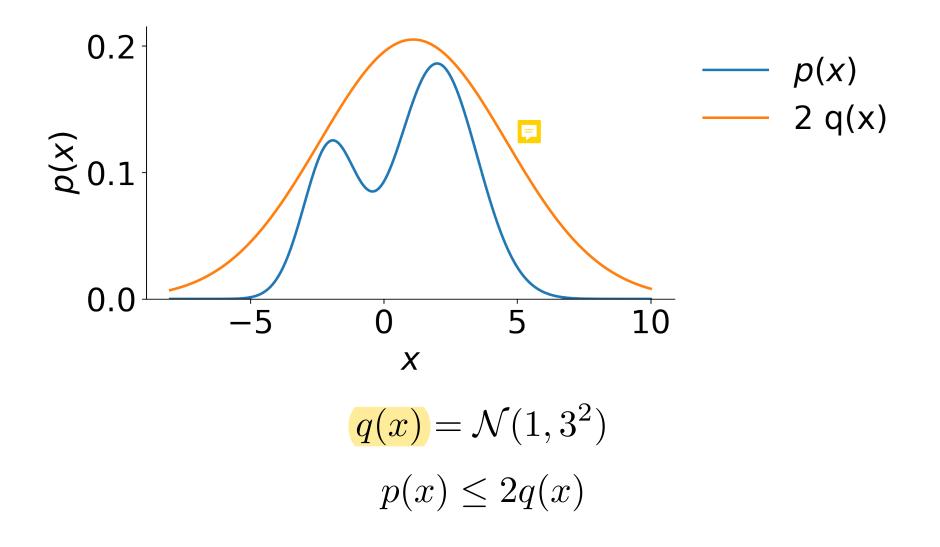


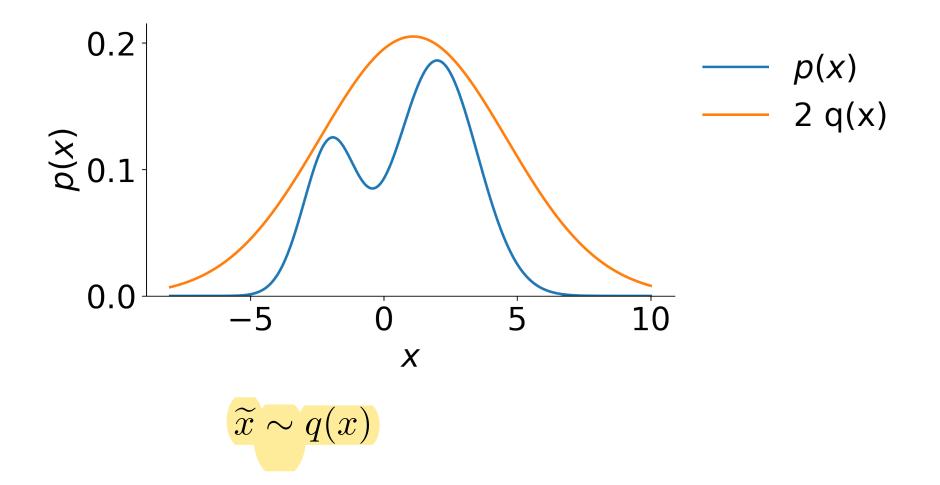
Sampling from Gaussian distribution

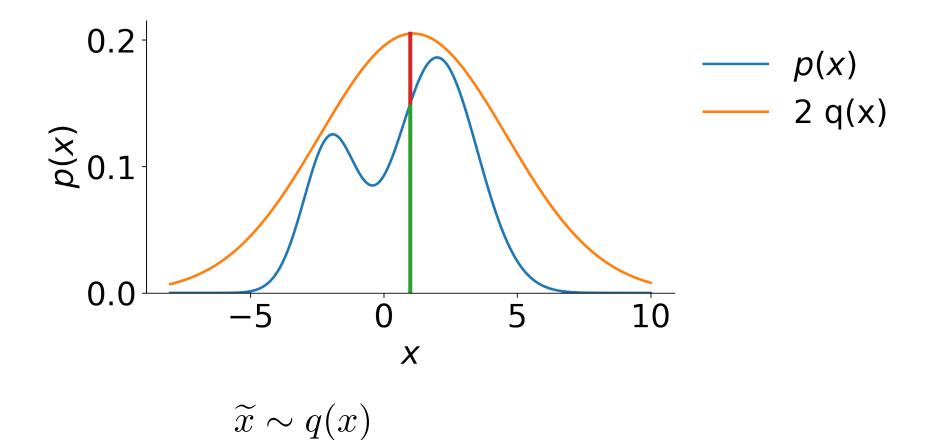
Or call library function © z = numpy.random.randn()

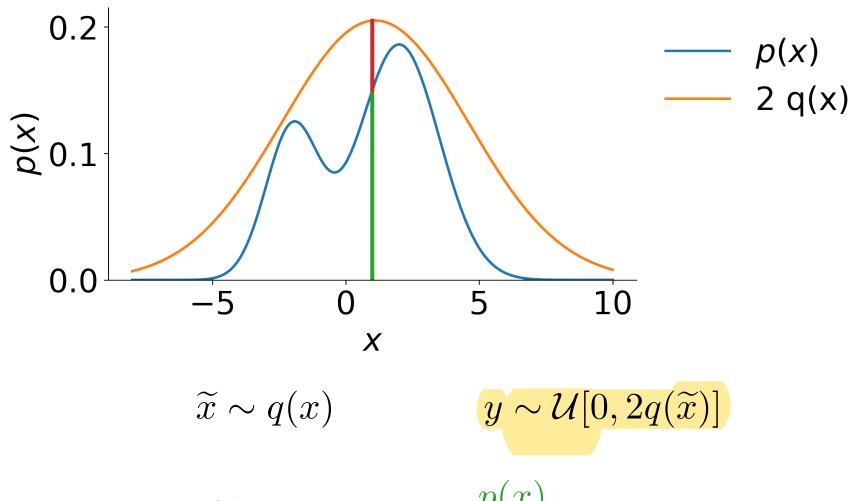




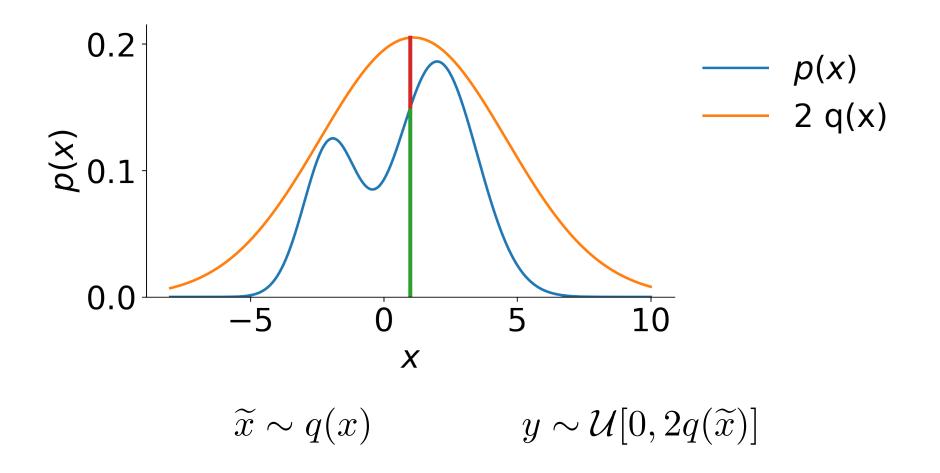




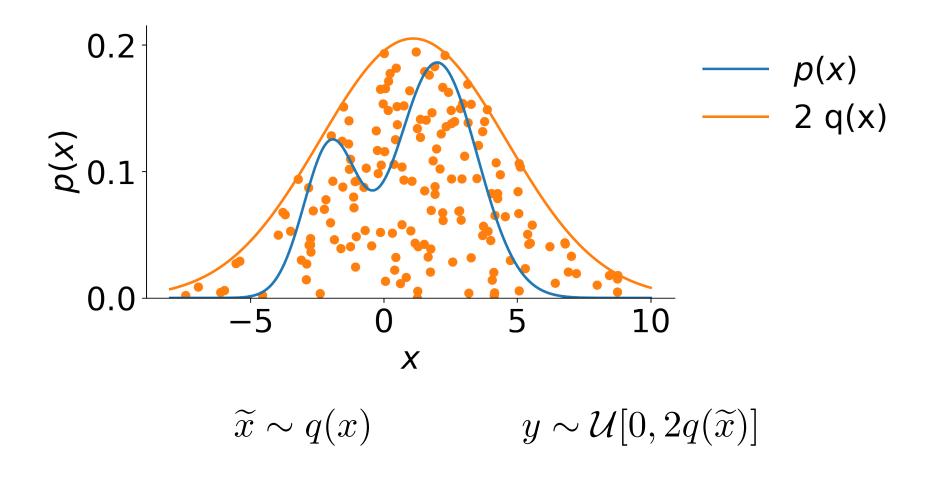




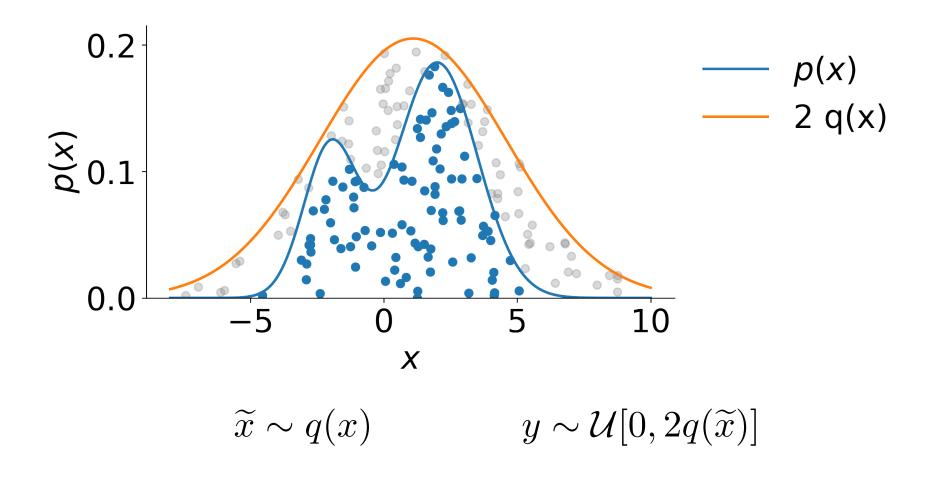
Accept \widetilde{x} with probability $\frac{p(x)}{2q(x)}$



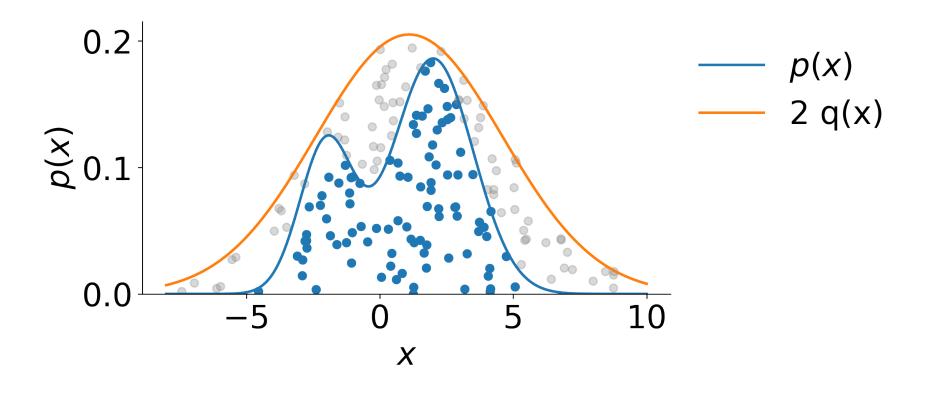
Accept
$$\widetilde{\mathcal{X}}$$
 with probability $\frac{p(x)}{2q(x)}\colon$ if $y\leq p(x)$



Accept
$$\widetilde{\mathcal{X}}$$
 with probability $\frac{p(x)}{2q(x)}\colon$ if $y\leq p(x)$

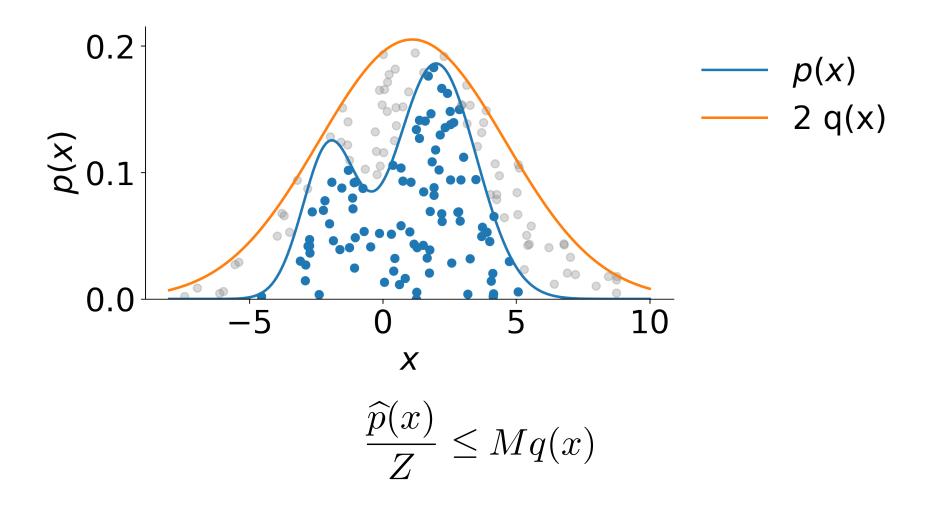


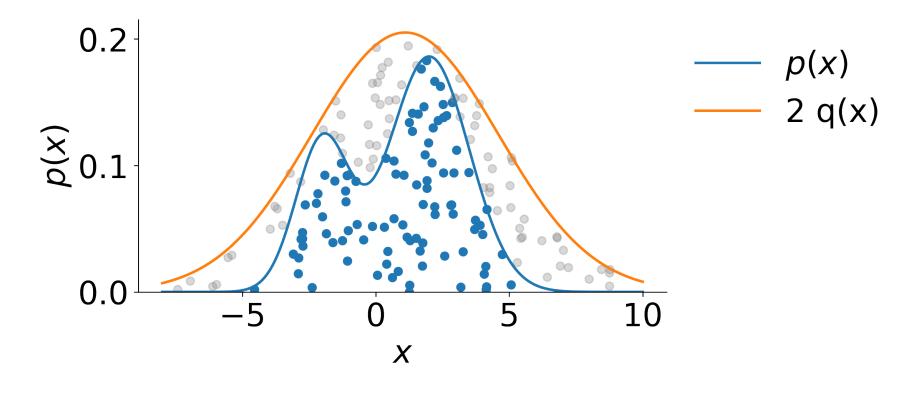
Accept
$$\widetilde{\mathcal{X}}$$
 with probability $\frac{p(x)}{2q(x)}\colon$ if $y\leq p(x)$



$$p(x) \le Mq(x)$$

Accepts
$$\frac{1}{M}$$
 points on average





$$\widehat{p}(x) \leq \underbrace{ZM}_{\widetilde{M}} q(x)$$

Pros:

Works for most distributions (even unnormalized)

Pros:

Works for most distributions (even unnormalized)

Cons:

• If q and p are too different (M is large), rejects most of the points

Pros:

Works for most distributions (even unnormalized)

Cons:

- If q and p are too different (M is large), rejects most of the points
- M is large for d-dimensional distributions