

# Nonparametric methods



# Parametric methods

1. Define parametric model:

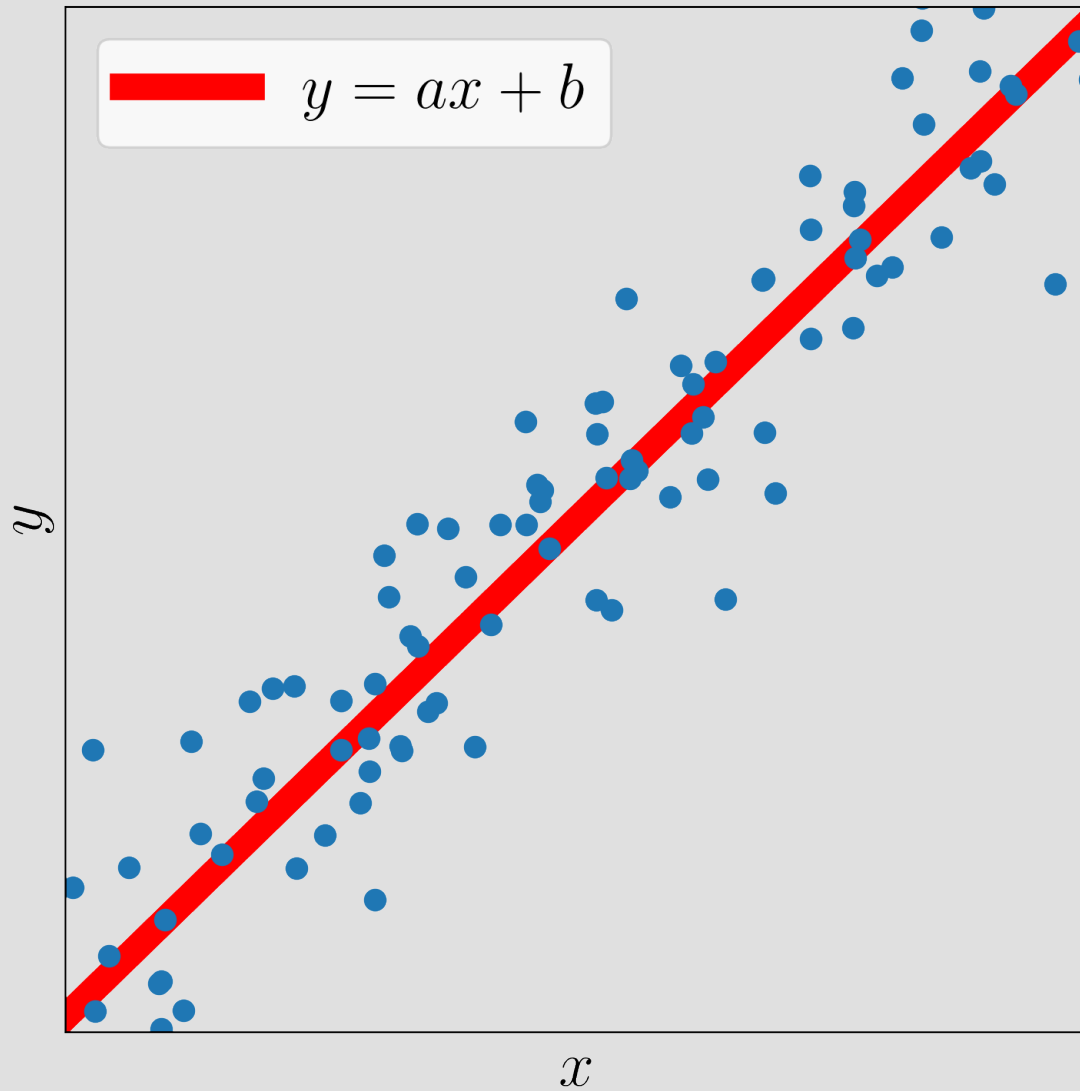
$$p(y|X, \theta)$$

2. Find best parameters using MAP estimation:

$$p(\theta|y, X) \rightarrow \max_{\theta}$$



# Parametric methods

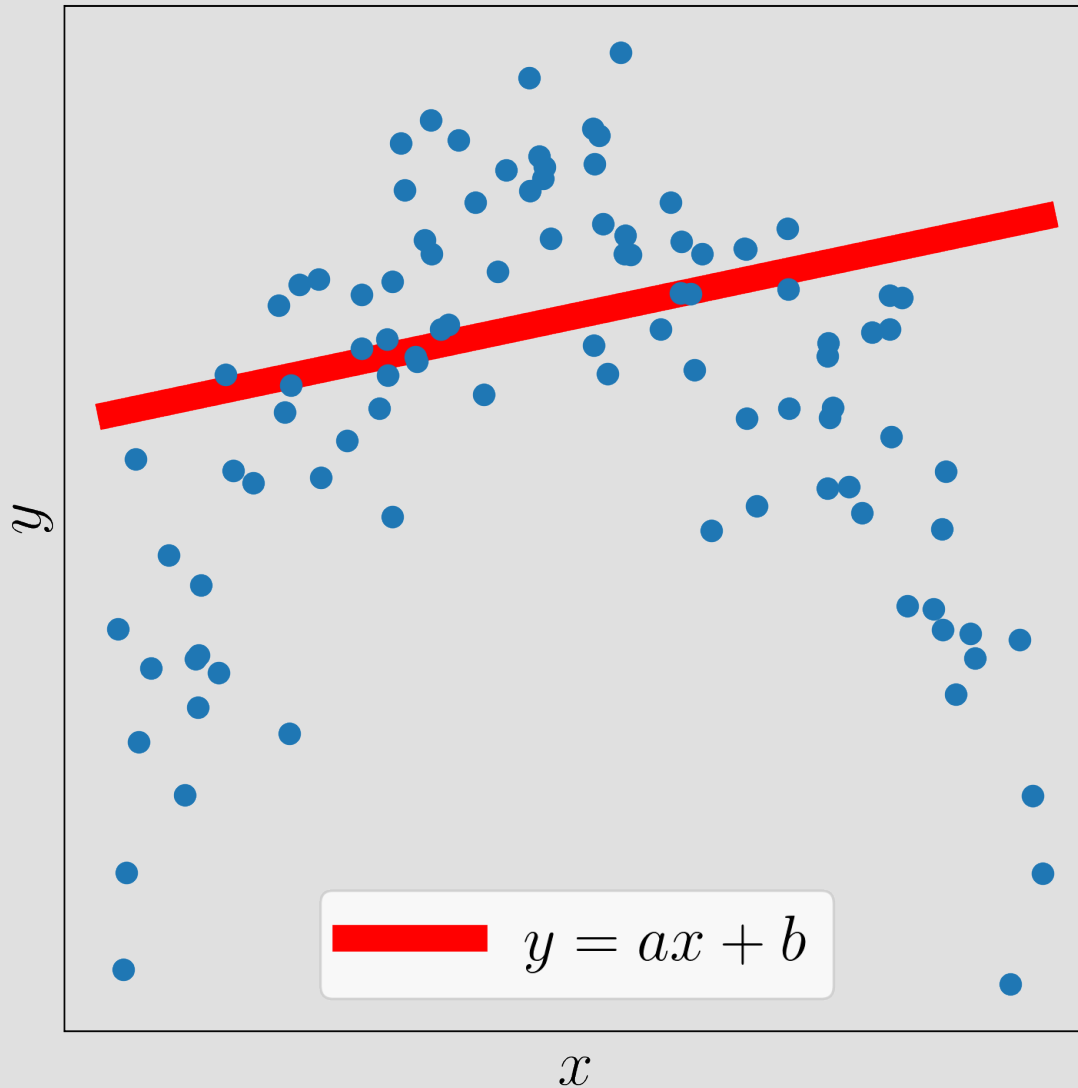


Parameters:

$$\theta = \{a, b\}$$



# Parametric methods

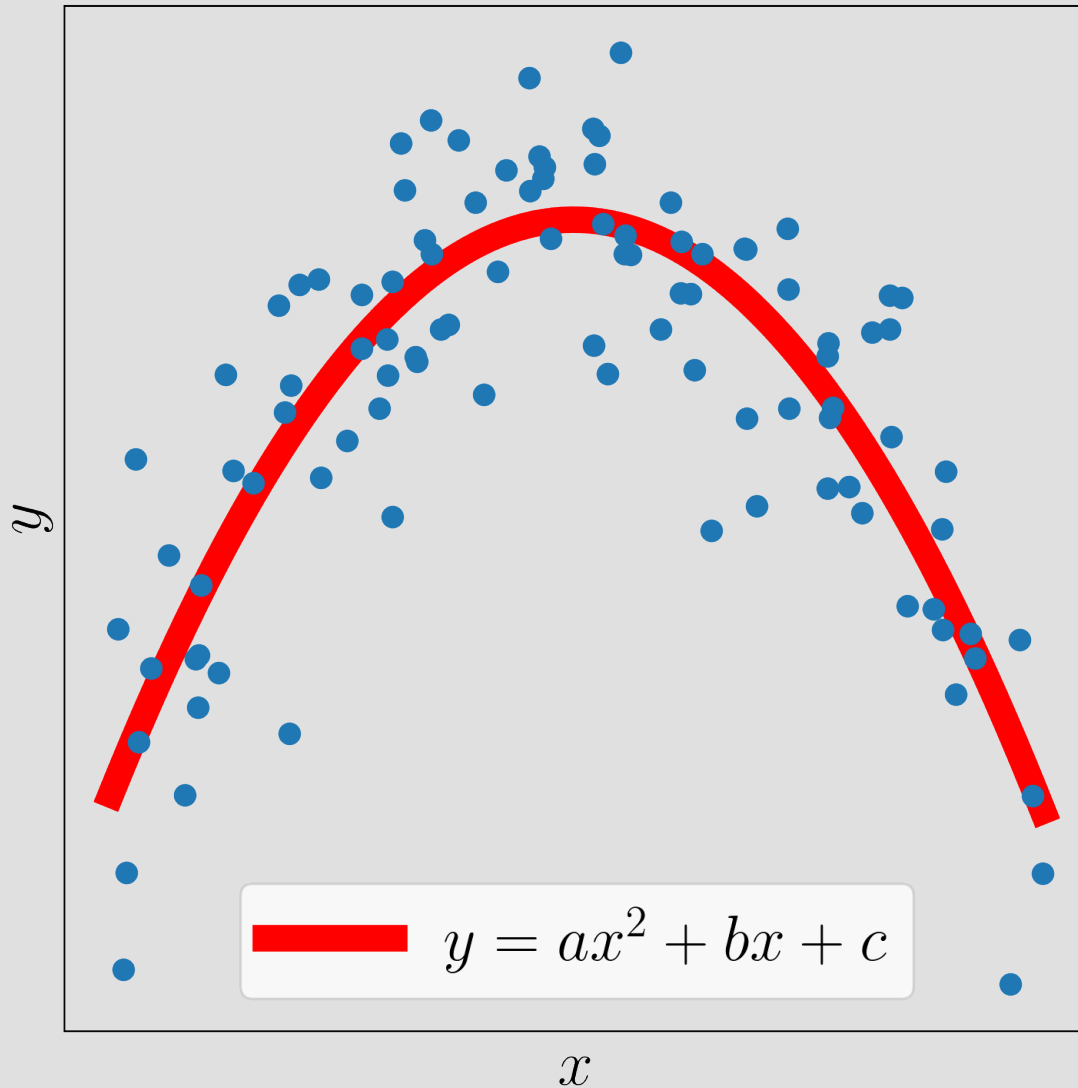


Parameters:

$$\theta = \{a, b\}$$



# Parametric methods

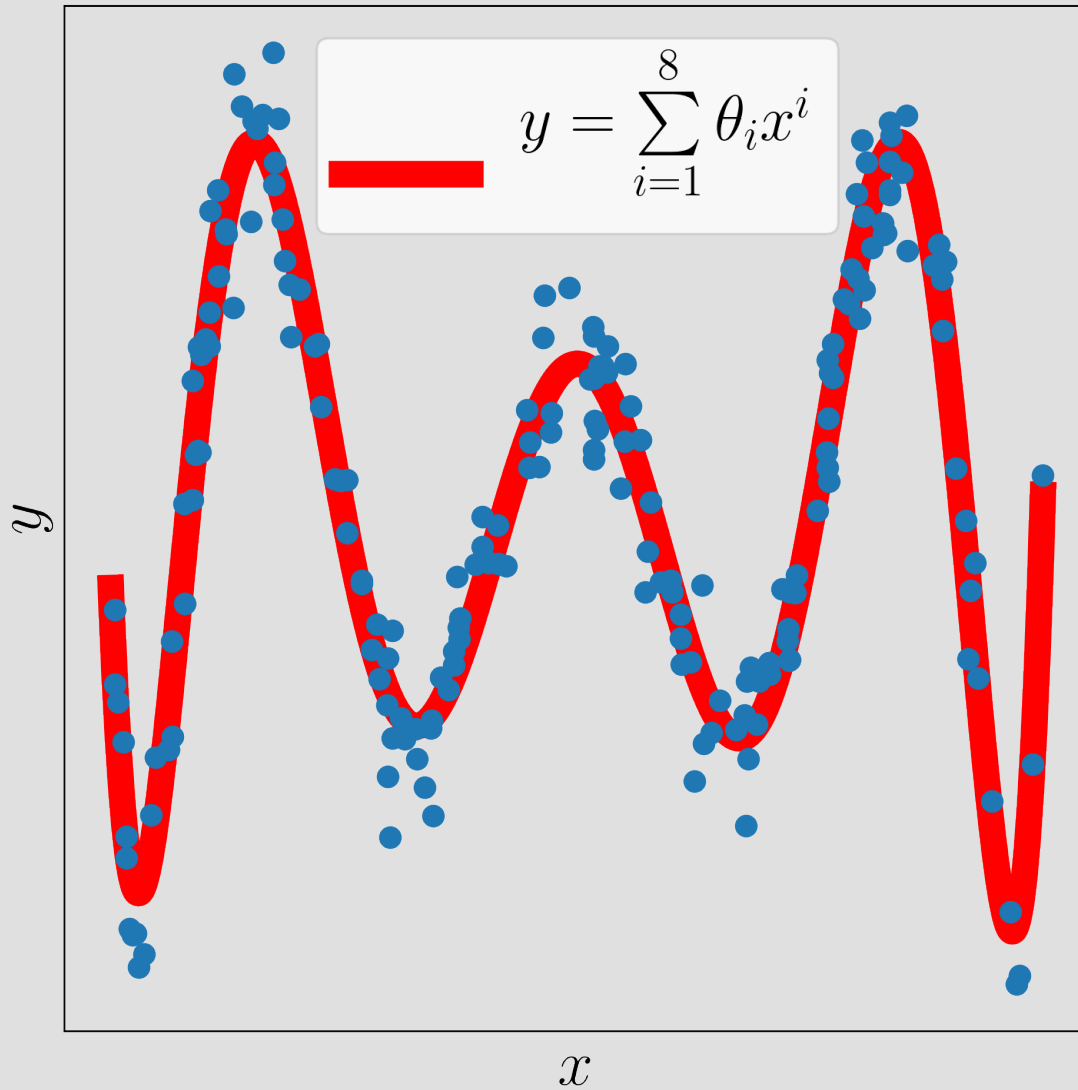


Parameters:

$$\theta = \{a, b, c\}$$



# Parametric methods



Parameters:

$$\theta = \{\theta_1, \theta_2, \dots, \theta_8\}$$



# Non-parametric methods

Parametric methods:

- Fixed number of parameters

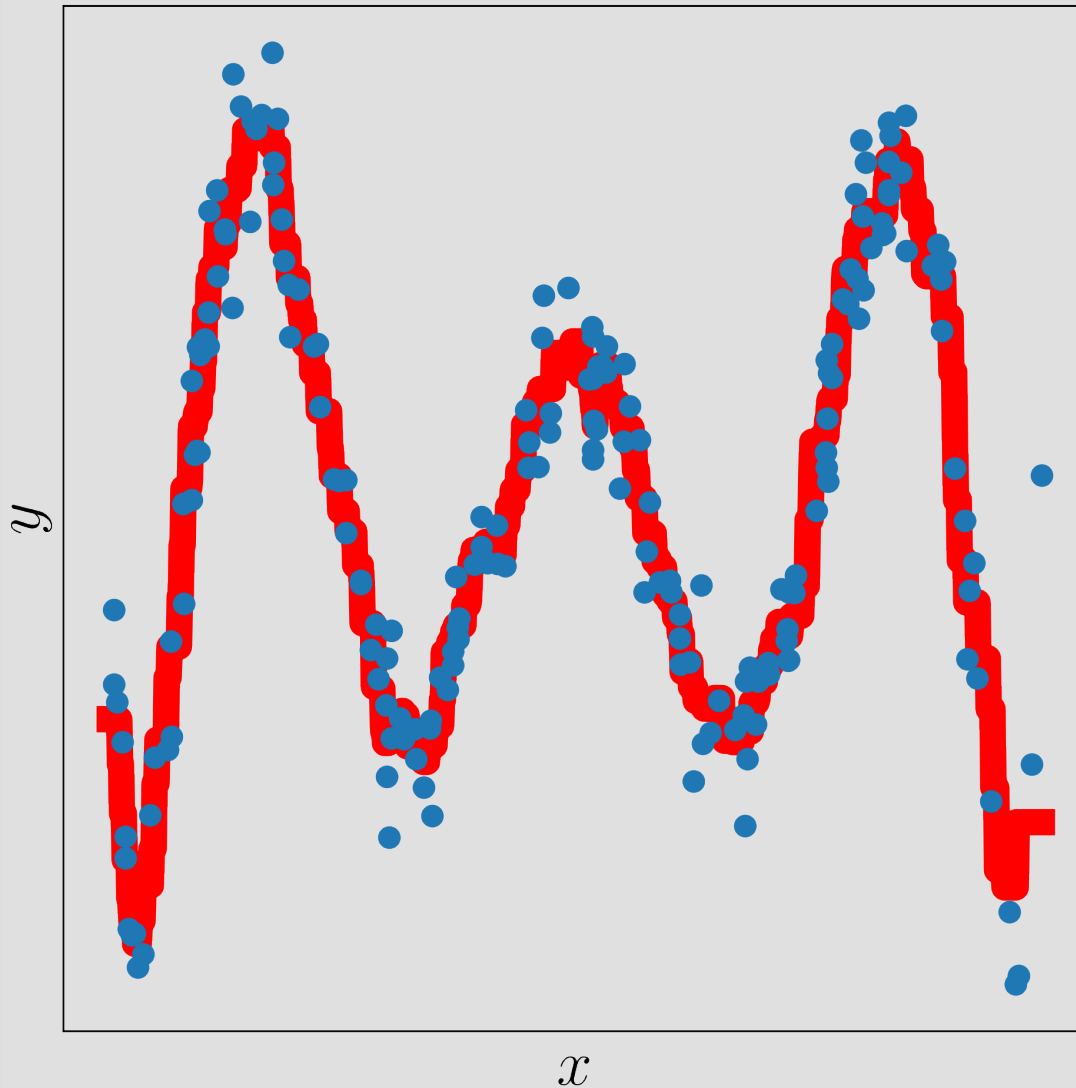
Non-parametric:

- Number of parameters depends on dataset size



# Non-parametric methods

kNN



K-nearest neighbors:

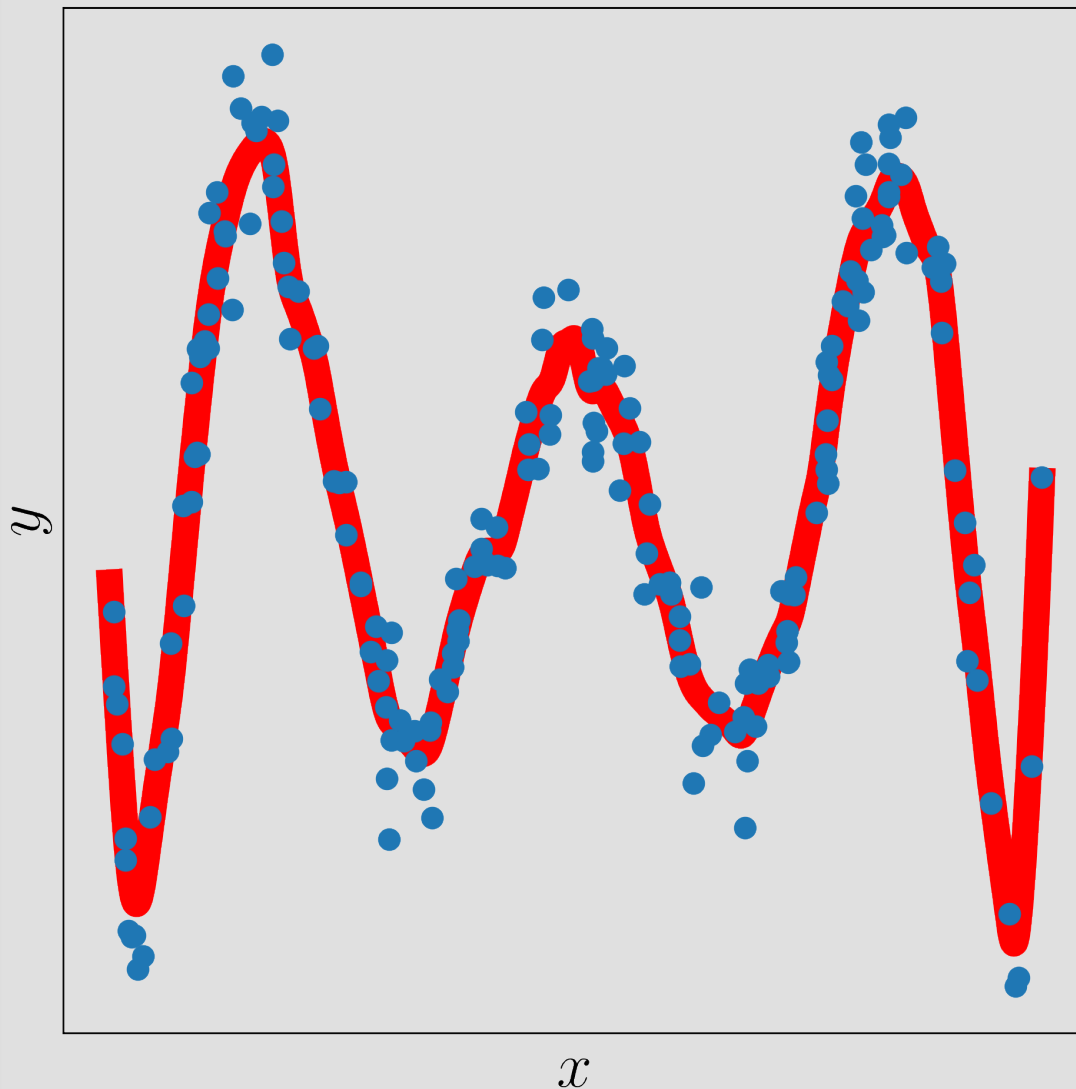
$$y = \frac{1}{5} \sum_{i=1}^5 y_{(i)}$$





# Non-parametric methods

## Nadaraya-Watson



K-nearest neighbors:

$$y = \frac{1}{5} \sum_{i=1}^5 y_{(i)}$$

Nadaraya-Watson:

$$y(x) = \sum_{i=1}^N w_i(x) y_i$$

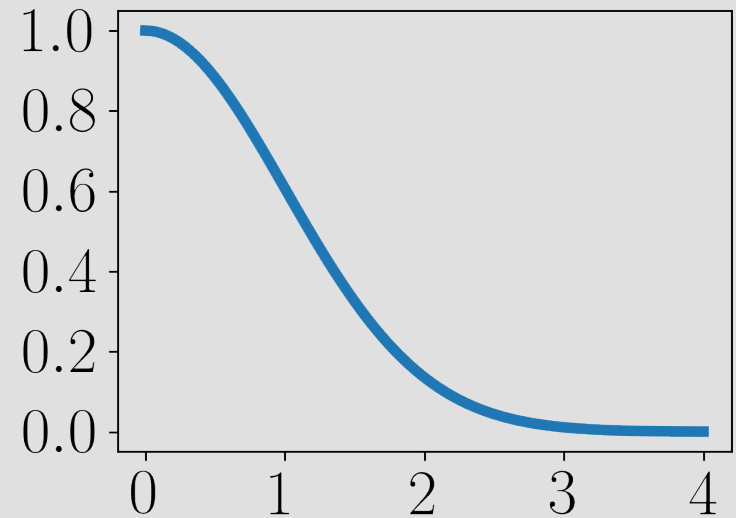
$$w_i(x) = \frac{K(x, x_i)}{\sum_{j=1}^N K(x, x_j)}$$



# Some kernels

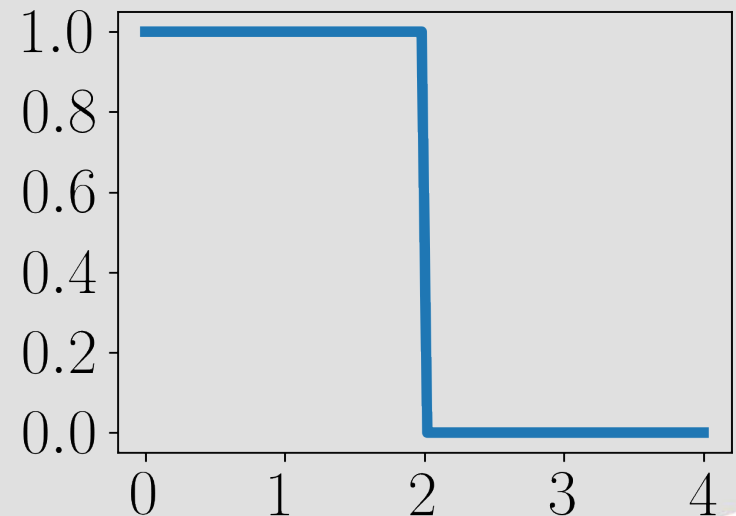
Gaussian

$$K(x_1, x_2) = e^{-\frac{1}{2\sigma^2} \|x_1 - x_2\|^2}$$



Uniform

$$K(x_1, x_2) = \mathbb{I}[\|x_1 - x_2\| < h]$$



# Parametric vs Non-parametric

## Parametric:

- Limited complexity
- Faster inference
- Slow learning

## Non-parametric:

- Arbitrary complex
- Need to process all data for prediction
- Learning: remember all data



# Gaussian Processes

Can estimate uncertainty of predictions

