Very unrigorous maths

by Monado

October 15, 2021

Let: r = critrate, d = critdamage, x = r/d, v = 2r + d. We want to approximate 1+rd for values of x close to 1/2. Clearly $r=\frac{(v-d)}{2}=xd$, so $d=\frac{v}{2(x+\frac{1}{2})}$

Clearly
$$r = \frac{(v-d)}{2} = xd$$
, so $d = \frac{v}{2(x+\frac{1}{2})}$

$$1 + rd = 1 + xd^2 = 1 + \frac{xv^2}{4(x + \frac{1}{2})^2}$$

Now suppose $x = \frac{1}{2} + \epsilon$, then:

$$1 + \frac{xv^2}{4(x + \frac{1}{2})^2} = 1 + \frac{(\frac{1}{2} + \epsilon)v^2}{4(1 + \epsilon)^2} = 1 + \frac{(\frac{1}{2} + \epsilon)v^2}{4(1 + 2\epsilon + \epsilon^2)}$$

For small ϵ ,

$$\frac{\frac{1}{2}+\epsilon}{1+2\epsilon+\epsilon^2}\approx\frac{1}{2}$$

So we have the approximation

$$1 + rd \approx 1 + \frac{v^2}{8} \tag{1}$$

for $x = \frac{r}{d} \approx \frac{1}{2}$.

As for why 0.7v seems to be a good approximation, notice that most players probably have between 2 and 4 crit value (0.5 crit rate, 1 crit damage to 1 crit rate, 2 crit damage), so we can try Taylor expanding (1) around v = a where a is somewhere between 2 and 4, then we have

$$1 + \frac{(a+v-a)^2}{8} \approx 1 + \frac{a^2 + 2(v-a)a}{8} = 1 + \frac{-a^2}{8} + \frac{av}{4}$$

We want the constant term to cancel out so $a = 2\sqrt{2}$, which gives $\frac{a}{4} = \frac{\sqrt{2}}{2}$, which is close to 0.7.