### **Preamble**

```
#include <bits/stdc++.h>

using namespace std;

#define int long long
#define REP(i, a, b) for (int i = a; i < (b); ++i)

signed main() {
    cin.tie(NULL)->sync_with_stdio(false);
}
```

### **Debug Memory Usage**

```
long long get_memory_usage() {
   struct rusage usage;
   getrusage(RUSAGE_SELF, &usage);
   return usage.ru_maxrss; // Maximum resident set size (in kilobytes on Linux, bytes on macOS)
}
```

## Output

```
// Fixed precision.
cout << fixed << setprecision(6) << lf << '\n';
// Binary output
cout << format("{:06b}", b) << "fixed length binary";
cout << format("{:b}", b) << "variable length binary";</pre>
```

# Linear Algebra

### Gauss-Jordan

### Partial Pivot RREF - Rectangular

```
const double EPSILON = 1e-10;
typedef double T:
typedef vector<T> VT:
typedef vector<VT> VVT;
tuple<int,double> rref(VVT &a) {
  int n = a.size();
 int m = a[0].size();
  int r = 0:
 double det = 1.;
 for (int c = 0; c < m && r < n; c++) {
 int j = r;
    for (int i = r + 1; i < n; i++)
    if (fabs(a[i][c]) > fabs(a[j][c])) j = i;
    if (fabs(a[j][c]) < EPSILON) continue;</pre>
 swap(a[j], a[r]);
 if (j != r) det *= -1.;
 det *= a[r][c];
   T s = 1.0 / a[r][c];
 for (int j = 0; j < m; j++) a[r][j] *= s;
   for (int i = 0; i < n; i++) if (i != r) {
    T t = a[i][c];
      for (int j = 0; j < m; j++) a[i][j] -= t * a[r][j];
    r++;
  return {r,det};
```

### Full Pivot - Inverse, Square, Solving $(n \times n) \cdot (n \times m) = (n. \times m)$

- Solving systems of linear equations (AX = B)
- Inverting matrices (AX = I)
- Computing determinants of square matrices

Runs in  $\mathcal{O}(n^3)$ 

### Output:

- X stored in b
- $A^{-1}$  stored in a

```
const double EPS = 1e-10;
typedef vector<int> VI;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
```

```
T GaussJordan(VVT &a, VVT &b) {
  const int n = a.size();
  const int m = b[0].size();
  VI irow(n), icol(n), ipiv(n);
  T \det = 1:
  for (int i = 0; i < n; i++) {</pre>
    int pj = -1, pk = -1;
   for (int j = 0; j < n; j++) if (!ipiv[j])</pre>
      for (int k = 0; k < n; k++) if (!ipiv[k])
  if (pj == -1 || fabs(a[j][k]) > fabs(a[pj][pk])) { pj = j; pk =
    if (fabs(a[pj][pk]) < EPS) { cerr << "Matrix is singular." <<</pre>
    endl; exit(0); }
    ipiv[pk]++;
    swap(a[pj], a[pk]);
   swap(b[pj], b[pk]);
    if (pj != pk) det *= -1;
   irow[i] = pj;
    icol[i] = pk;
   T c = 1.0 / a[pk][pk];
    det *= a[pk][pk];
    a[pk][pk] = 1.0;
    for (int p = 0; p < n; p++) a[pk][p] *= c;
    for (int p = 0; p < m; p++) b[pk][p] *= c;
    for (int p = 0; p < n; p++) if (p != pk) {
   c = a[p][pk];
     a[p][pk] = 0;
    for (int q = 0; q < n; q++) a[p][q] -= a[pk][q] * c;
      for (int q = 0; q < m; q++) b[p][q] -= b[pk][q] * c;
  }
  for (int p = n-1; p >= 0; p--) if (irow[p] != icol[p]) {
    for (int k = 0; k < n; k++) swap(a[k][irow[p]], a[k][icol[p]]);
  return det;
```

### **XOR Basis**

Small vectors

```
vector<int> basis;
void add(int x) {
  for (int i = 0; i < basis.size(); i++) { // reduce x using the current basis vectors
    x = min(x, x ^ basis[i]);
  }
  if (x != 0) { basis.push_back(x); }
}</pre>
```

Arbitrarily large vectors

```
bool non_zero(const vector<uint64_t>& x) {
  bool non zero = false;
  for(const auto& a : x) {
    non_zero |= (a != (uint64_t) 0);
  return non_zero;
}
struct Basis {
  vector<vector<uint64_t>> basis;
  vector<uint64_t> reduce(vector<uint64_t> x) {
    for(int i = 0; i < basis.size(); i++) {</pre>
      int state = 0;
      for(int j = 0; j < x.size(); j++) {</pre>
        int cur = basis[i][j] ^ x[j];
       if (state == 0 and cur < x[j]) state = -1;
        if (state == 0 and cur > x[j]) state = 1;
       if (state \leftarrow 0) x[j] = cur;
    return x;
  void add(vector<uint64_t> x) {
x = reduce(x);
    if (non_zero(x)) basis.push_back(x);
```

```
bool equal(const Basis& other) {
  if (other.basis.size() != basis.size()) return false;
  bool ans = true;
  for(const auto & v : other.basis) {
    ans &= !non_zero(reduce(v));
  }
  return ans;
}
};
```

# **Number Theory**

# **Extended Euclidean Algorithm**

Finds x and y for which  $ax + by = \gcd(a, b)$ . **Time:**  $\mathcal{O}(\log n)$ 

```
// Returns {x,y,gcd} where xa + yb = gcd
array<int,3> gcd_ext(int a,int b) {
    auto oa=a,ob=b;
    int x=0,y=1,u=1,v=0;
    while(a!=0) {
        auto q=b/a,r=b%a;
        auto m=x-u*q,n=y-v*q;
        b=a, a=r, x=u,y=v,u=m,v=n;
    }
    assert(oa*x+ob*y==b);
    return {x,y,b};
}
```

#### **Modular Inverse**

Finds x such that  $ax = 1 \mod m$ .

Time:  $\mathcal{O}(\log n)$ 

```
int inv(int a, int m) {
    auto [x,y,g] = gcd_ext(a, m);
    if (g != 1) {
        // No solution!!!
        return -1;
    }
    else {
            // Inverse
            return (x % m + m) % m;
    }
}
```

TODO: All modular inverses in  $\mathcal{O}(m)$ : https://cp-algorithms.com/algebra/module-inverse html

### **Linear Congruence Equation**

Time:  $\mathcal{O}(\log n)$ 

```
// Returns {solution, modulo}
pair<int,int> linear_congruence(int a, int b, int n) {
   int d;
   if ((d = gcd(a,n)) != 1) {
        // No solution
        if (b % d != 0) return {-1, -1};
        a /= d; b /= d; n /= d;
   }
   int i = inv(a, n);
   return {(b * i) % n, n};
}
```

# Linear Prime Sieve

This calculates the minimum prime factor pr[j] for all all j up to n. From this, we can calculate the prime factorisation of all these numbers.

Time:  $\mathcal{O}(n)$ 

```
const int N = 10000000;
vector<int> lp(N+1);
vector<int> pr;
for (int i=2; i <= N; ++i) {
   if (lp[i] == 0) { lp[i] = i; pr.push_back(i); }
   for (int j = 0; i * pr[j] <= N; ++j) {
        lp[i * pr[j]] = pr[j];
}</pre>
```

```
if (pr[j] == lp[i]) break;
}
```

#### **Extended Chinese Remainder Theorem**

Works for non-coprime moduli

```
struct ChineseRemainder {
  int a=0,m=0;
  void add(int b, int n) {
    b=(b%n+n)%n;
    if(m==-1) return;
    if(m==0) { a=b; m=n; return; }
    auto [u,v,g] = gcd_ext(m,n);
    if((a-b)%g!=0) { m=-1; return; }
    int lam = (a-b)/g;
    m=m/g*n;
    a = b + (lam*v)%m*n;
    a = (a%m+m)%m;
  }
  int get(int x) {return a+m*x;}
};
```

### **Fast Fourier Transform**

Useful for multiplying polynomials, or computing convolutions.  $c[k] = \sum_i a[i]b[k-i]$ . For sliding element-wise multiplication, reverse one of the arrays. Rounding is safe if  $\left(\sum a_i^2 + \sum b_i^2\right)\log_2 N < 9\cdot 10^{14}$ . (N=|A|+|B|. In practice, with random inputs, bound is  $10^{16}$ ).

Time:  $\mathcal{O}(N \log N)$ 

```
#define SZ(x) (int)(x).size()
#define ALL(x) begin(x), end(x)
typedef vector<int> vi;
typedef complex<double> C;
typedef vector<double> vd;
void fft(vector<C> &a) {
int n = SZ(a), L = 31 - __builtin_clz(n);
  static vector<complex<long double>> R(2, 1);
  static vector<C> rt(2, 1); // (^ 10% faster i f double )
  for (static int k = 2; k < n; k *= 2) {
  R.resize(n);
    rt.resize(n):
   auto x = polar(1.0L, acos(-1.0L) / k);
    REP(i, k, 2 * k) rt[i] = R[i] = i & 1 ? R[i / 2] * x : R[i / 2];
  vi rev(n);
  REP(i, 0, n) rev[i] = (rev[i / 2] | (i & 1) << L) / 2;
  REP(i, 0, n) if (i < rev[i]) swap(a[i], a[rev[i]]);</pre>
  for (int k = 1; k < n; k *= 2)
    for (int i = 0; i < n; i += 2 * k) REP(j, 0, k) {
     Cz = rt[j + k] *
        a[i + j + k]; // (25% faster i f hand-r o l l e d )
     a[i + j + k] = a[i + j] - z;
      a[i + j] += z;
vd conv(const vd &a, const vd &b) {
  if (a.empty() || b.empty()) return {};
  vd res(SZ(a) + SZ(b) - 1);
  int L = 32 - __builtin_clz(SZ(res)), n = 1 << L;</pre>
  vector<C> in(n), out(n);
  copy(ALL(a), begin(in));
  REP(i, 0, SZ(b)) in[i].imag(b[i]);
  fft(in);
  for (C &x : in) x *= x;
  REP(i, 0, n) out[i] = in[-i \& (n - 1)] - conj(in[i]);
  fft(out);
  REP(i, 0, SZ(res)) res[i] = imag(out[i]) / (4 * n);
  return res;
}
```

## Geometry

### Preamble

This gives us vector addition, scalar and complex multiplication, angle arg(), and polar form initialisation cis().

```
typedef complex<double> C;
```

#### Dot Product

```
double dotp(C a , C b){return (conj(a)*b).real();}
double dist2(C a, C b){return dotp(a-b, a-b);}
```

```
a_0b_0 + a_1b_1 = |a||b|\cos(\theta)
```

### **Cross Product**

```
double crossp(C a , C b){return (conj(a)*b).imag();}
double orient(C a, C b, C c){return crossp(b-c,b-a);}
```

```
a_0b_1-a_1b_0=|a\|b|\cos(\theta)
```

### **Ordering By Orientation**

```
bool topHalf(C a) {
  return (a.imag() > 0) || (a.imag() == 0 && a.real() >= 0);
}
bool cmp(const C &a, const C &b) {
  bool ha = topHalf(a);
  bool hb = topHalf(b);
  if (ha != hb) return ha;
  return orient(a, {0,0}, b) > 0;
}
```

# **String Matching**

### **Z-Algorithm**

```
vector<int> z_algo(const string& s) {
  int n = s.size();
  vector<int> z(n);
  int l = 0, r = 0;
  for(int i = 1; i < n; i++) {
    if(i < r) z[i] = min(r - i, z[i - l]);
    while(i + z[i] < n && s[z[i]] == s[i + z[i]]) z[i]++;
    if(i + z[i] > r) { l = i; r = i + z[i]; }
  }
  return z;
}
```

# Aho-Curasick

Aho-Corasick automaton, used for multiple pattern matching. Initialize with Aho-Corasick ac(patterns); the automaton start node will be at index 0. find(word) returns for each position the index of the longest word that ends there, or –1 if none. findAll(—, word) finds all words (up to  $N\sqrt{N}$  many if no duplicate patterns) that start at each position (shortest first). Duplicate patterns are allowed; empty patterns are not. To find the longest words that start at each position, reverse all input. For large alphabets, split each symbol into chunks, with sentinel bits for symbol boundaries. Time: construction takes O(26N), where N= sum of length of patterns. find(x) is O(N), where N = length of x. findAll is O(NM).

```
struct AhoCorasick {
  enum {alpha = 26, first = 'A'}; // change this!
 struct Node {
    // (nmatches is optional)
   int back, next[alpha], start = -1, end = -1, nmatches = 0;
    Node(int v) { memset(next, v, sizeof(next)); }
  vector<Node> N:
  vector<int> backp;
  void insert(string& s, int j) {
   assert(!s.empty());
    int n = 0;
    for (char c : s) {
      int& m = N[n].next[c - first];
    if (m == -1) { n = m = N.size(); N.emplace_back(-1); }
      else n = m;
    if (N[n].end == -1) N[n].start = j;
    backp.push_back(N[n].end);
```

```
N[n].end = j;
    N[n].nmatches++;
  AhoCorasick(vector<string>\& pat) : N(1, -1) {
    REP(i,0,pat.size()) insert(pat[i], i);
    N[0].back = N.size();
    N.emplace_back(0);
    queue<int> q;
    for (q.push(0); !q.empty(); q.pop()) {
      int n = q.front(), prev = N[n].back;
      REP(i,0,alpha) {
        int &ed = N[n].next[i], y = N[prev].next[i];
        if (ed == -1) ed = y;
        else {
          N[ed].back = y;
          (N[ed].end == -1 ? N[ed].end : backp[N[ed].start])
            = N[y].end;
          N[ed].nmatches += N[y].nmatches;
          q.push(ed);
      }
    }
  }
  vector<int> find(string word) {
    int n = 0;
    vector<int> res; // ll count = \theta;
    for (char c : word) {
     n = N[n].next[c - first];
      res.push_back(N[n].end);
     // count += N[n].nmatches;
    }
   return res;
  }
  vector<vector<int>>> findAll(vector<string>& pat, string word) {
    vector<int> r = find(word);
    vector<vector<int>>> res(word.size());
    REP(i,0,word.size()) {
     int ind = r[i];
      while (ind != -1) {
      res[i - pat[ind].size() + 1].push back(ind);
        ind = backp[ind];
    }
    return res;
  }
};
```

### Ukkonen's

Linear time suffix tree construction. Useful for string matching.

```
const int MAXN = 8000005;
string s;
int n;
struct Node {
  int l, r, par, link;
  vector<pair<char, int>> next;
  Node(int l = 0, int r = 0, int par = -1) : l(l), r(r), par(par),
  link(-1) {}
  int len() { return r - l; }
  // More space efficient than map, can use alternatively.
  int& get(char c) {
   for (auto& [a, b] : next)
      if (a == c) return b;
    next.push_back({c, -1});
    return next.back().second;
};
Node t[MAXN]:
int sz;
struct State {
 State(int v, int pos) : v(v), pos(pos) {}
}:
State ptr(0, 0);
```

```
State go(State st, int l, int r) {
 while (l < r)
    if (st.pos == t[st.v].len()) {
    st = State(t[st.v].get(s[l]), 0);
      if (st.v == -1) return st;
      if (s[t[st.v].l + st.pos] != s[l]) return State(-1, -1);
     if (r - l < t[st.v].len() - st.pos)</pre>
        return State(st.v. st.pos + r - l);
     l += t[st.v].len() - st.pos;
      st.pos = t[st.v].len();
 return st;
int split(State st) {
 if (st.pos == t[st.v].len()) return st.v;
 if (st.pos == 0) return t[st.v].par;
  Node v = t[st.v];
  int id = sz++;
  t[id] = Node(v.l, v.l + st.pos, v.par);
  t[v.par].get(s[v.l]) = id;
  t[id].get(s[v.l + st.pos]) = st.v;
  t[st.v].par = id;
 t[st.v].l += st.pos;
 return id:
int get_link(int v) {
 if (t[v].link != -1) return t[v].link;
  if (t[v].par == -1) return 0;
int to = get_link(t[v].par);
  return t[v].link = split(go(State(to, t[to].len()), t[v].l +
  (t[v].par == 0), t[v].r));
void tree_extend(int pos) {
for (;;) {
    State nptr = go(ptr, pos, pos + 1);
   if (nptr.v != -1) {
     ptr = nptr;
     return;
   }
 int mid = split(ptr);
    int leaf = sz++;
   t[leaf] = Node(pos, n, mid);
    t[mid].get(s[pos]) = leaf;
   ptr.v = get link(mid);
 ptr.pos = t[ptr.v].len();
    if (!mid) break;
 }
}
void build_tree() {
sz = 1;
  for (int i = 0; i < n; ++i) tree_extend(i);
```

# **Segment Trees!!!**

### Rasic

```
struct BasicSegmentTree {
  using Value = int:
  Value identity = INT_MAX;
  Value binop(Value a, Value b) {return min(a, b);}
  vector<Value> arr;
  BasicSegmentTree(int n) : arr(4*n + 2,identity), size(n) {};
  void update(int cur, int i, Value v, int l, int r) {
 if (l == r) {arr[cur] = v; return; }
    int mid = midpoint(l, r):
    if (i <= mid) update(2*cur, i, v, l, mid);</pre>
    else update(2*cur + 1, i, v, mid + 1, r);
   arr[cur] = binop(arr[2*cur],arr[2*cur + 1]);
void update(int i, int v) {update(1,i,v,0,size - 1);}
```

```
Value query(int cur, int ql, int qr, int l, int r) {
  if (l == ql and r == qr) return arr[cur];
  int mid = midpoint(l,r);
  Value val = identity;
  if (ql <= mid) val = binop(val,</pre>
  querv(2*cur.al.min(mid.ar).l.mid));
  if (qr > mid) val = binop(val,query(2*cur + 1,max(mid +
 1,ql),qr,mid+1,r));
  return val;
Value query(int ql, int qr) {return query(1,ql,qr,0,size - 1);}
```

# Lazy Update

```
struct LazyUpdateTree {
  using Value = int;
  using Update = int;
  Value identity = LLONG_MIN;
  Value def = 0;
  Update idUpdate = 0;
  Value binop(Value a, Value b) { return max(a, b); }
  Value applyUpdate(Update a, Value u, int l, int r) { return u +
  Update mergeUpdate(Update old, Update nw) { return old + nw; }
  vector<Value> arr;
  vector<Update> lazy;
  int size:
  LazyUpdateTree(int n) : arr(4 * n + 2, def), lazy(4 * n + 2, def)
  idUpdate), size(n) {};
  void push(int cur, int l, int r) {
  if (l != r) {
      int mid = midpoint(l, r);
     update(2 * cur, l, mid, lazy[cur], l, mid);
      update(2 * cur + 1, mid + 1, r, lazy[cur], mid + 1, r);
    lazy[cur] = idUpdate;
  void update(int cur, int ql, int qr, Update u, int l, int r) {
  if (l == ql and r == qr) {
      lazy[cur] = mergeUpdate(lazy[cur], u);
     arr[cur] = applyUpdate(u, arr[cur], l, r);
      return;
   }
    push(cur, l, r);
    int mid = midpoint(l, r);
    if (ql <= mid) update(2 * cur, ql, min(mid, qr), u, l, mid);</pre>
    if (qr > mid) update(2 * cur + 1, max(mid + 1, ql), qr, u, mid + 1
 1, r);
    arr[cur] = binop(arr[2 * cur], arr[2 * cur + 1]):
  void update(int ql, int qr, Update u) { update(1, ql, qr, u, 0,
  size - 1); }
  Value query(int cur, int ql, int qr, int l, int r) {
    if (l == ql and r == qr) return arr[cur];
    push(cur, l, r);
    int mid = midpoint(l, r);
    Value val = identity;
    if (ql <= mid) val = binop(val, query(2 * cur, ql, min(mid, qr),</pre>
    l, mid));
   if (qr > mid) val = binop(val, query(2 * cur + 1, max(mid + 1,
    ql), qr, mid + 1, r));
    return val:
  Value query(int ql, int qr) { return query(1, ql, qr, 0, size -
  1); }
```

## **Lazy Create Segment Tree**

```
struct LazyCreateNode {
  using Value = int;
  static const Value identity = 0;
  Value binop(Value a, Value b) { return a + b; }
  Value val = identity;
  LazyCreateNode *lt = NULL, *rt = NULL;
  LazyCreateNode() {};
```

```
void create_children() {
   if (lt != NULL) return;
    lt = new LazyCreateNode();
    rt = new LazyCreateNode();
 }
void update(int i, Value v, int l, int r) {
    if (l == r) { val = v; return; }
  create_children();
    int mid = midpoint(l, r);
   if (i <= mid) lt->update(i,v,l,mid);
    else rt->update(i,v,mid+1,r);
   val = binop(lt->val,rt->val);
 }
 Value query(int ql, int qr, int l, int r) {
    if (l == ql and r == qr) return val;
 create_children();
    int mid = midpoint(l, r);
   Value val = identity;
    if (ql <= mid) val = lt->query(ql,min(mid, qr), l, mid);
    if (qr > mid) val = binop(val, rt->query(max(mid + 1, ql), qr,
 mid + 1, r));
    return val;
 }
};
```

# **DP Optimisations**

### **Line Container**

Container where you can add lines of the form kx+m, and query maximum values at points x. Useful for dynamic programming convex hull trick.  $\mathcal{O}(\log n)$ .

```
struct Line {
  mutable ll k, m, p;
  bool operator<(const Line& o) const { return k < o.k; }</pre>
  bool operator<(ll x) const { return p < x; }</pre>
struct LineContainer : multiset<Line, less<>> {
 // (for doubles, use \inf = 1/.0, \operatorname{div}(a,b) = a/b)
 static const ll inf = LLONG_MAX;
  ll div(ll a, ll b) { // floored division
   return a / b - ((a ^ b) < 0 && a % b); }
  bool isect(iterator x, iterator y) {
  if (y == end()) return x -> p = inf, 0;
    if (x->k == y->k) x->p = x->m > y->m ? inf : -inf;
  else x-p = div(y-m - x-m, x-k - y-k);
    return x \rightarrow p >= y \rightarrow p;
}
 void add(ll k, ll m) {
   auto z = insert(\{k, m, 0\}), y = z++, x = y;
    while (isect(y, z)) z = erase(z);
   if (x != begin() \&\& isect(--x, y)) isect(x, y = erase(y));
    while ((y = x) != begin() && (--x)->p >= y->p)
     isect(x, erase(y));
 }
ll query(ll x) {
    assert(!empty());
  auto l = *lower_bound(x);
    return l.k * x + l.m;
```

### Divide and Conquer

```
// Inclusive, inclusive, 0-indexed
auto cost = [&](int i, int j) -> double {
    return 0;
};
vector<double> dpbefore(n, 1./0.);
vector<double> dpafter(n, 1./0.);
auto compute = [&](const auto& self, int l, int r, int optl, int optr) -> void {
    if (l > r) return;
    int mid = midpoint(l,r);
    pair<double, int> best = {1./0., -1};
```

```
REP(k, optl, min(mid,optr) + 1) {
   double cur = (k ? dpbefore[k - 1] : 0) + cost(k, mid);
   best = min(best, {cur,k});
}
dpafter[mid] = best.first;
self(self, l, mid - 1, optl, best.second);
self(self, mid + 1, r, best.second, optr);
};
REP(a,0,k) {
   compute(compute, 0, n - 1, 0, n - 1);
   swap(dpbefore, dpafter);
}
cout << dpbefore.back();</pre>
```

### **Flow**

### **Push Relabel**

 $\mathcal{O}(V^3)$ 

```
struct PushRelabel {
  struct Edge {
   int dest. back:
    ll f, c;
  vector<vector<Edge>> g;
  vector<ll> ec:
  vector<Edge*> cur;
  vector<vi> hs; vi H;
  PushRelabel(int n) : g(n), ec(n), cur(n), hs(2*n), H(n) {}
  void addEdge(int s, int t, ll cap, ll rcap=0) {
  if (s == t) return;
    g[s].push_back({t, sz(g[t]), 0, cap});
    g[t].push_back({s, sz(g[s])-1, 0, rcap});
  }
  void addFlow(Edge& e, ll f) {
    Edge &back = g[e.dest][e.back];
    if (!ec[e.dest] && f) hs[H[e.dest]].push_back(e.dest);
    e.f \leftarrow f; e.c \leftarrow f; ec[e.dest] \leftarrow f;
    back.f -= f; back.c += f; ec[back.dest] -= f;
  ll calc(int s, int t) {
   int v = sz(g); H[s] = v; ec[t] = 1;
    vi co(2*v); co[0] = v-1;
    rep(i,0,v) cur[i] = g[i].data();
    for (Edge& e : g[s]) addFlow(e, e.c);
    for (int hi = 0::) {
     while (hs[hi].empty()) if (!hi--) return -ec[s];
      int u = hs[hi].back(); hs[hi].pop_back();
      while (ec[u] > 0) // discharge u
        if (cur[u] == g[u].data() + sz(g[u])) {
          H[u] = 1e9;
          for (Edge\& e : g[u]) if (e.c \&\& H[u] > H[e.dest]+1)
           H[u] = H[e.dest]+1, cur[u] = \&e;
          if (++co[H[u]], !--co[hi] && hi < v)
           rep(i,0,v) if (hi < H[i] \&\& H[i] < v)
               --co[H[i]], H[i] = v + 1;
          hi = H[u];
        } else if (cur[u]->c \&\& H[u] == H[cur[u]->dest]+1)
          addFlow(*cur[u], min(ec[u], cur[u]->c));
        else ++cur[u];
  }
 bool leftOfMinCut(int a) { return H[a] >= sz(g); }
```