

## DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING

### MID SEMESTER EXAMINATION-II

Course Title with code	Introduction to Machine Learning, 18CSE751	Maximum Marks	30 Marks
Date and Time	24-12-21, 2:30pm to 3:30pm	No. of Hours	1.0
Course Instructor(s)	Dr. Vani V		
Instructions to Students			
1. Answer any <b>two full questions</b> . 2. Any missing data may assume suitably.			

Q. No	Question	MAX MARKS	C O	B L	PO/PSO																																																																	
1. a	<p>For the following 2 test instances, determine the class using <b>Naïve Bayes Classifier</b> with the training instances as given in <b>Table 1.a</b>.</p> <p>Y1 = [eyecolour = brown, married = yes, sex = female, hairlength = long] Y2 = [eyecolour = blue, married = no, sex = male, hairlength = short]</p> <p><b>Table 1.a Sports Club Dataset</b></p> <table><tr><th>eyecolour</th><th>married</th><th>sex</th><th>hairlength</th><th>class</th></tr><tr><td>brown</td><td>yes</td><td>male</td><td>long</td><td>football</td></tr><tr><td>blue</td><td>yes</td><td>male</td><td>short</td><td>football</td></tr><tr><td>brown</td><td>yes</td><td>male</td><td>long</td><td>football</td></tr><tr><td>brown</td><td>no</td><td>female</td><td>long</td><td>netball</td></tr><tr><td>brown</td><td>no</td><td>female</td><td>long</td><td>netball</td></tr><tr><td>blue</td><td>no</td><td>male</td><td>long</td><td>football</td></tr><tr><td>brown</td><td>no</td><td>female</td><td>long</td><td>netball</td></tr><tr><td>brown</td><td>no</td><td>male</td><td>short</td><td>football</td></tr><tr><td>brown</td><td>yes</td><td>female</td><td>short</td><td>netball</td></tr><tr><td>brown</td><td>no</td><td>female</td><td>long</td><td>netball</td></tr><tr><td>blue</td><td>no</td><td>male</td><td>long</td><td>football</td></tr><tr><td>blue</td><td>no</td><td>male</td><td>short</td><td>football</td></tr></table>	eyecolour	married	sex	hairlength	class	brown	yes	male	long	football	blue	yes	male	short	football	brown	yes	male	long	football	brown	no	female	long	netball	brown	no	female	long	netball	blue	no	male	long	football	brown	no	female	long	netball	brown	no	male	short	football	brown	yes	female	short	netball	brown	no	female	long	netball	blue	no	male	long	football	blue	no	male	short	football	8	3	3	1,2, 3/2
eyecolour	married	sex	hairlength	class																																																																		
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blue	no	male	long	football																																																																		
blue	no	male	short	football																																																																		

**Solution:**

$P(\text{eyecolour} = \text{brown}|\text{class}=\text{football})= 0.43$   
 $P(\text{eyecolour} = \text{blue}|\text{class}=\text{football})= 0.57$   
 $P(\text{eyecolour} = \text{brown}|\text{class}=\text{netball})=1$   
 $P(\text{eyecolour} = \text{blue}|\text{class}=\text{netball})=0$

$P(\text{married} = \text{yes} \mid \text{class} = \text{football}) = 0.43$   
 $P(\text{married} = \text{no} \mid \text{class} = \text{football}) = 0.57$   
 $P(\text{married} = \text{yes} \mid \text{class} = \text{netball}) = 0.2$   
 $P(\text{married} = \text{no} \mid \text{class} = \text{netball}) = 0.8$

$P(\text{sex} = \text{male} \mid \text{class} = \text{football}) = 1$   
 $P(\text{sex} = \text{female} \mid \text{class} = \text{football}) = 0$   
 $P(\text{sex} = \text{female} \mid \text{class} = \text{netball}) = 1$   
 $P(\text{sex} = \text{male} \mid \text{class} = \text{netball}) = 0$

$P(\text{hairlength} = \text{long} \mid \text{class} = \text{football}) = 0.57$   
 $P(\text{hairlength} = \text{short} \mid \text{class} = \text{football}) = 0.43$   
 $P(\text{hairlength} = \text{long} \mid \text{class} = \text{netball}) = 0.8$   
 $P(\text{hairlength} = \text{short} \mid \text{class} = \text{netball}) = 0.2$

	<p><math>P(Y1 Class=football) = 0</math> <math>P(Y1 Class = netball) = 0.16 * 0.42= 0.067</math> <b>Y1 = [eyecolour = brown, married = yes, sex = female, hairlength = long] =&gt; netball</b></p> <p><math>P(Y2 Class = football) = 0.14 * 0.58 =0.0812</math> <math>P(Y2 Class = netball) =0</math> <b>Y2 = [eyecolour = blue, married = no, sex = male, hairlength = short] =&gt; football</b></p> <p><b>Marking Scheme:</b> For each object classification :4 marks 4x 2 = 8 marks</p>																																																																																				
1. b	<p>Determine the class for the following objects</p> <p>1. y = [1,22] &amp; 2. y = [1,3]</p> <p>using the 3-NN classifier and the 5-NN classifier, both using training samples from the <b>Table 1.c</b> . Justify, why the two classifiers differ in their classification behavior.</p> <p style="text-align: center;"><b>Table 1.c Training Samples</b></p> <table><tr><td>X1</td><td>1</td><td>1</td><td>1</td><td>2</td><td>3</td><td>3</td><td>3</td><td>4</td><td>5</td></tr><tr><td>X2</td><td>1</td><td>2</td><td>4</td><td>3</td><td>0</td><td>2</td><td>5</td><td>4</td><td>3</td></tr><tr><td>Class</td><td>+</td><td>-</td><td>-</td><td>+</td><td>+</td><td>+</td><td>-</td><td>-</td><td>-</td></tr></table> <p><b>Solution:</b></p> <table><tr><td>X1</td><td>1</td><td>1</td><td>1</td><td>2</td><td>3</td><td>3</td><td>3</td><td>4</td><td>5</td></tr><tr><td>X2</td><td>1</td><td>2</td><td>4</td><td>3</td><td>0</td><td>2</td><td>5</td><td>4</td><td>3</td></tr><tr><td>Class</td><td>+</td><td>-</td><td>-</td><td>+</td><td>+</td><td>+</td><td>-</td><td>-</td><td>-</td></tr><tr><td>Distance y1</td><td>21</td><td>20</td><td>18</td><td>19.03</td><td>22.09</td><td>20.099</td><td>17.12</td><td>18.25</td><td>19.42</td></tr><tr><td>Distance y2</td><td>2</td><td>1</td><td>1</td><td>1</td><td>3.61</td><td>2.24</td><td>2.83</td><td>3.16</td><td>4</td></tr></table> <p>y1=[1,22]    y2=[1,3]</p> <p>1NN    y2 =&gt; -    y2 /+    3NN =&gt; -    5NN    y2=&gt;+</p> <p>1NN    y1 =&gt;    y1=&gt; -    3NN -    5NN    y1=&gt; -</p> <p>KNN -&gt; lazy learning algorithm, Change the value from low to high as a process of parameter tuning to achieve best performance. According to the research history, <math>K = \sqrt{n}</math> could be perfect number of nearest neighbors that can be considered for classification. However, in the given problem for classification of y2 sample, the prediction differs when we consider larger K. To avoid these problems, we can use Weighted KNN.</p> <p><b>Marking Scheme:</b></p>	X1	1	1	1	2	3	3	3	4	5	X2	1	2	4	3	0	2	5	4	3	Class	+	-	-	+	+	+	-	-	-	X1	1	1	1	2	3	3	3	4	5	X2	1	2	4	3	0	2	5	4	3	Class	+	-	-	+	+	+	-	-	-	Distance y1	21	20	18	19.03	22.09	20.099	17.12	18.25	19.42	Distance y2	2	1	1	1	3.61	2.24	2.83	3.16	4	7	3	3	1,2, 3/2
X1	1	1	1	2	3	3	3	4	5																																																																												
X2	1	2	4	3	0	2	5	4	3																																																																												
Class	+	-	-	+	+	+	-	-	-																																																																												
X1	1	1	1	2	3	3	3	4	5																																																																												
X2	1	2	4	3	0	2	5	4	3																																																																												
Class	+	-	-	+	+	+	-	-	-																																																																												
Distance y1	21	20	18	19.03	22.09	20.099	17.12	18.25	19.42																																																																												
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	For each classification :1.5 marks 4x 1.5 = 6 marks  1 mark for justification																									
2. a	Generate the decision rules for the decision tree in <b>Figure 2.a</b> <div><div><div><div><div>eyecolour</div><div><div>brown</div><div>blue</div></div><div><div>married</div><div>football (4)</div></div><div><div>yes</div><div>no</div></div><div><div>hairlength</div><div>hairlength</div></div><div><div><div>long</div><div>short</div></div><div><div>short</div><div>long</div></div></div><div><div>football (2)</div><div>netball (1)</div><div>football (1)</div><div>netball (4)</div></div></div></div></div><div>Figure 2.a Decision Tree</div><div><b>Solution:</b>  R1 : If eyecolour = blue then class=football R2: If eyecolour = brown AND married = yes AND hairlength = long then class=football R3: If eyecolour = brown AND married = yes AND hairlength = short then class=netball R4: If eyecolour = brown AND married = no AND hairlength = long then class=netball R5: If eyecolour = brown AND married = no AND hairlength = short then class=football</div></div> <td>5</td> <td>4</td> <td>3</td> <td>1,2, 3/2</td>	5	4	3	1,2, 3/2																					
2. b	Can another decision tree with a smaller number of predictors be identified for the given dataset in <b>Table 1.a</b> on determining who joins which club? If so, draw that decision tree with necessary reasoning. <div><b>Solution:</b><div><div><div>Sex</div><div><div>Female</div><div>Male</div></div><div><div>Netball</div><div>Football</div></div></div></div></div>	3	4	3	1,2, 3/2																					
2. c	Determine the best attribute split by calculating the information gain of <i>sex</i> , <i>eyecolour</i> , <i>married</i> , and <i>hairlength</i> attributes with the given dataset in <b>Table 1.a</b> <div><b>Solution:</b><table><tr><td></td><td colspan="2"><u>Sex</u></td></tr><tr><td><u>Class</u></td><td><u>Male</u></td><td><u>Female</u></td></tr><tr><td>Football</td><td>7</td><td>0</td></tr><tr><td>Netball</td><td>0</td><td>5</td></tr></table> <table><tr><td></td><td colspan="2"><u>Eyecolour</u></td></tr><tr><td><u>Class</u></td><td><u>Brown</u></td><td><u>Blue</u></td></tr><tr><td>Football</td><td>3</td><td>4</td></tr></table></div>		<u>Sex</u>		<u>Class</u>	<u>Male</u>	<u>Female</u>	Football	7	0	Netball	0	5		<u>Eyecolour</u>		<u>Class</u>	<u>Brown</u>	<u>Blue</u>	Football	3	4	7	4	3	1,2, 3/2
	<u>Sex</u>																									
<u>Class</u>	<u>Male</u>	<u>Female</u>																								
Football	7	0																								
Netball	0	5																								
	<u>Eyecolour</u>																									
<u>Class</u>	<u>Brown</u>	<u>Blue</u>																								
Football	3	4																								

Netball	5	0
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	<u>Married</u>	
<u>Class</u>	<u>Yes</u>	<u>No</u>
Football	3	4
Netball	1	4

	<u>HairLength</u>	
<u>Class</u>	<u>Short</u>	<u>Long</u>
Football	3	4
Netball	1	4

$$\begin{aligned}
 E(\text{Class}) &= \text{Entropy}(5,7) \\
 &= \text{Entropy}(5/12, 7/12) \\
 &= -7/12 \log(7/12) - 5/12 \log(5/12) \\
 &= -0.5833 * 0.777 - 0.4167 * (-1.263) \\
 &= 0.45357 + 0.52625 \\
 &= 0.9798
 \end{aligned}$$

$$\begin{aligned}
 E(\text{Sex}) &= 7/12 * E(\text{Sex} = \text{male}) + 5/12 * E(\text{Sex} = \text{female}) \\
 &= 7/12 * 0 + 5/12 * 0 = 0
 \end{aligned}$$

$$\begin{aligned}
 E(\text{EyeColour}) &= 8/12 * E(\text{eyecolour} = \text{brown}) + 4/12 * E(\text{eyecolour} = \text{blue}) \\
 &= 8/12 * (-3/8 * \log(3/8) - 5/8 * \log(5/8)) + 4/12 * (-4/4 * \log(4/4) - 0/4 * \log(0/4)) \\
 &= 0.63627
 \end{aligned}$$

$$\begin{aligned}
 E(\text{married}) &= 4/12 * E(\text{married} = \text{yes}) + 8/12 * E(\text{married} = \text{no}) \\
 &= 4/12 * (-3/4 * \log(3/4) - 1/4 * \log(1/4)) + 8/12 * (-4/8 * \log(4/8) - 4/8 * \log(4/8)) \\
 &= 4/12 * (-0.75 * -0.415 - 0.25 * -2) + 8/12 * (-.5 * -1 - 0.5 * -1) \\
 &= 4/12 * 0.811 + 8/12 * 1 = 0.9370
 \end{aligned}$$

$$E(\text{hairlength}) = E(\text{married}) = 0.9370$$

$$\text{Infogain}(\text{Sex}) = E(\text{Class}) - E(\text{Sex}) = 0.9798 - 0 = 0.9798$$

$$\text{Infogain}(\text{eyecolour}) = 0.9798 - 0.63627 = 0.34353$$

$$\text{Infogain}(\text{married}) = \text{Infogain}(\text{hairlength}) = 0.0428$$

0.9799 3 sex

0.3436 1 eyecolour

0.0428 2 married

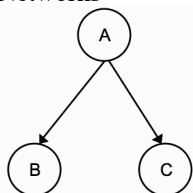
0.0428 4 hairlength

### Marking Scheme:

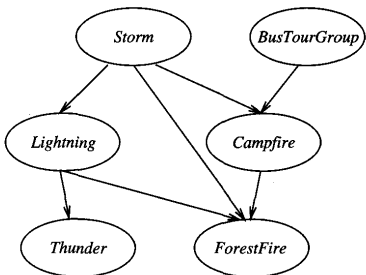
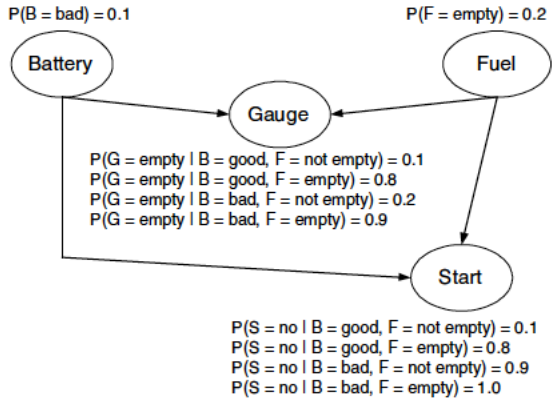
Overall Entropy Calculation: 1 Mark

Each info gain  $1.5 \times 4 = 6$  marks

3. a Illustrate with suitable example the term “conditional independence” in Bayesian Networks



where C is not directly linked to B, but there is a link through A.

	<p>C is conditionally independent of B, given A.</p>  <p>In the above Bayesian Belief Network, <b>Thunder is conditionally independent of other variables given Lightning.</b></p> <p>In contrast to the naive Bayes classifier, which assumes that all the variables are conditionally independent given the value of the target variable, Bayesian belief networks allow stating conditional independence assumptions that apply to subsets of the variables. Thus, Bayesian belief networks provide an intermediate approach that is less constraining than the global assumption of conditional independence made by the naive Bayes classifier, but more tractable than avoiding conditional independence assumptions altogether</p>				
3. b	<p>Given the Bayesian network shown in <b>Figure 3.b</b>, compute the following probabilities.</p> <p>(a) <math>P(B = \text{good}, F = \text{empty}, G = \text{empty}, S = \text{yes})</math>.</p> <p>(b) <math>P(B = \text{bad}, F = \text{empty}, G = \text{not empty}, S = \text{no})</math>.</p> <p>(c) Given that the battery is bad, compute the probability that the car will start.</p>  <p><b>Figure 3.b Bayesian Belief Network</b></p> $  \begin{aligned}  &P(B = \text{good}, F = \text{empty}, G = \text{empty}, S = \text{yes}) \\  &= P(B = \text{good}) \times P(F = \text{empty}) \times P(G = \text{empty}   B = \text{good}, F = \text{empty}) \\  &\quad \times P(S = \text{yes}   B = \text{good}, F = \text{empty}) \\  &= 0.9 \times 0.2 \times 0.8 \times 0.2 = 0.0288. \\  &P(B = \text{bad}, F = \text{empty}, G = \text{not empty}, S = \text{no}) \\  &= P(B = \text{bad}) \times P(F = \text{empty}) \times P(G = \text{not empty}   B = \text{bad}, F = \text{empty}) \\  &\quad \times P(S = \text{no}   B = \text{bad}, F = \text{empty}) \\  &= 0.1 \times 0.2 \times 0.1 \times 1.0 = 0.002. \\  &P(S = \text{yes}   B = \text{bad}) \\  &= \sum_{\alpha} P(S = \text{yes}   B = \text{bad}, F = \alpha) P(F = \alpha) P(B = \text{bad}) \\  &= 0.1 \times 0.1 \times 0.8 \\  &= 0.008  \end{aligned}  $ <p><b>Marking Scheme:</b> For each question :2 marks 3x 2 = 6 marks      <math>P(F=\alpha) = 1-0.2 = 0.8</math></p>	6	3	3	1,2, 3/2
3. c	<p>Consider the dataset in <b>Table 1.a</b>. Use the Modified Value Difference Metrics (MVDm) measure to compute the distance between every pair of attribute values for the <i>sex</i>, <i>eyecolour</i>, <i>married</i>, and <i>hairlength</i> attributes.</p>	6	4	3	1,2, 3/2

	$d(\text{sex}=\text{female}, \text{sex}=\text{male}) = 2$ $d(\text{eyecolour}=\text{blue}, \text{eyecolour}=\text{brown}) = 1.25$ $d(\text{married}=\text{yes}, \text{married}=\text{no}) = 0.5$ $d(\text{hairlength}=\text{long}, \text{hairlength}=\text{short}) = 0.625$ <b>Marking Scheme:</b> For each pair : 1.5 marks $4 \times 1.5 = 6$ marks				
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Faculty Signature	Course Co-Ordinator/Mentor Signature	HoD Signature