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IT - I

ML ASSIGNMENT - I

Unit -4 Probabilistic graphical models.

1) Naive Bayes Algorithm:

The naive bayes algorithm is a classification technique based on bayes theorem. It assumes that all features are conditionally independent given class label

$$P(C|x) = \frac{P(x|C) \cdot P(C)}{P(x)}$$

where,

$C \rightarrow$ class

$x \rightarrow$ feature vector

Since $P(x)$ is constant the decision is based on maximizing $P(x|C) \cdot P(C)$

Applications:

- * spam detection
- * Medical diagnosis
- * Sentiment analysis.

2) Bayesian Belief network (BBN):-

A Bayesian Belief network (BBN) also known as a Bayesian network, is a graphical model that represents probabilistic relationships among a set of random variables.

It is represented as a directed acyclic graph (DAG).

- > Node represent random variables.
- > Edge represents conditional dependency.
- > Each node has conditional probability table (CPT) that quantifies effect of parent nodes.

example:-

consider medical diagnosis network:

Node1: blue

Node2: fever

Node3: cough

Here fever and cough depends on blue.

The network completely encodes other dependencies.

Advantages:-

- => Capture causal relationship.
- => Handle incomplete data
- => Support both inference (predict unknown) and learning (update probabilities)

Application:-

- => medical diagnosis (disease & symptoms)
- => Fault detection in engineering system
- => Decision support system.

3) Hidden markov model (HMM):-

A hidden markov model (HMM) is a statistical model for system that evolve over time but whose underlying states are hidden. Instead, we observe actions generated probabilistic from hidden states.

Components:-

- a) Hidden states (S)
- b) Observation (O)
- c) Transition probabilities (A)
- d) Emission probabilities (B)
- e) Initial state distribution (π)

key problems solved by HMM;

=> evaluation : compute probability of observation sequence given model.

=> decoding : determine most likely sequence of hidden states (viterbi algorithm)

=> learning : estimate parameters.

Application:-

=> speech recognition

=> natural language processing

=> bio information...

4) Bayesian Inference:-

Bayesian inference is a method of statistical inference where probability is used to represent uncertainty about parameters. Unlike frequentist methods, Bayesian methods update beliefs based on new evidence.

$$P(H|D) = \frac{P(D|H) \cdot P(H)}{P(D)}$$

where,

H → Hypothesis

D → observed data.

advantages:-

- => Incorporates prior knowledge
- => Naturally handles uncertainty
- => produces full probability distribution.

problem based on naive bayes:-

A spam filter uses naive bayes algorithm consider the word "offer" appear in emails.

$$P(\text{spam}) = 0.4$$

$$P(\text{not spam}) = 0.6$$

$$P(\text{offer} | \text{spam}) = 0.8$$

$$P(\text{offer} | \text{not spam}) = 0.2$$

If email contain word "offer", clarify it as spam or not spam.

solution:-

$$P(\text{spam} | \text{offer}) = \frac{P(\text{offer} | \text{spam}) P(\text{spam})}{P(\text{offer})}$$

$$\begin{aligned} P(\text{offer}) &= P(\text{offer} | \text{spam}) + P(\text{offer} | \text{not spam}) P(\text{not spam}) \\ &= (0.8)(0.4) + (0.2)(0.6) \\ &= 0.32 + 0.12 \\ &= 0.44 \end{aligned}$$

Now,

$$P(\text{spam} | \text{offer}) = \frac{(0.8 \times 0.4)}{0.44} = 0.727$$

$$P(\text{not spam} | \text{offer}) = \frac{0.2 \times 0.6}{0.44} = 0.273$$

∴ Since the email is classified as "spam".