Name : Batch:

MATH LECTURE - 05

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PART I: CLASS PRACTICE

GROUP 1: SPEED, DISTANCE, TIME

1.	A bus went 300 mile on the way back if it	s average spee	d for the whole trip	was 100 mph?	·	
	a. 120 mph	b. 125 mph	c. 133 ¹ mp	h d. 137 ¹ m	ph e. 150 m	iph
2.	Ahnaf started walkir miles per hour. He 3:15 the same after	ig at 2:25 pm. H waited 10 minut	e walked down the es for a bus there	e road for half an h , which brought hir	our at an average	e speed of 3
	a. 1.5 miles per h d. 6 miles per hou		o. 3 miles per hour e. 9 miles per hour		5 miles per hour	
3.	A motorboat travels spends half an hou the entire trip. What	r for unloading,	and returns to its	original port empty		
	a. 3.75 mph	b. 4 mph	c. 7.5 mph	d. 8 mph	e. None	of these
4.	One third of a certai km per hour and the journey?					
	a. 28 km/hr	b. 30 km/hr	c. $33\frac{1}{3}$ km/l	nr d. 40 km/h	r e. None	of these
5.	A hiker walked up a station by the same speed for the desce station, what was the	e route. His ave ent was 4 miles	rage speed for the per hour. If the ol	ascent was 2 mil eservation point is	es per hour, and exactly 3 miles fi	his average
	a. $2\frac{2}{5}$	b. $2\frac{2}{3}$	c. 3	d. $3\frac{1}{3}$	e. $3\frac{3}{5}$	
6.	Trisha walks 15 bloomile, how long does			e of 2 miles per ho	our. If there are 20) blocks in a
	a. 12.5 minutes	b. 15 minutes	c. 22.5 minu	tes d. 37.5 mir	utes e. 45 mi	nutes
7.	A certain 90-mile trip trip took 1/5 of the trip?					
	a. 12 mph	b. 30 mph	c. 45 mph	d. 60 mph	e. 75 mp	oh
	Γ	GROUP 2: R	OWING BOAT,	CURRENT & SP	EED	
8	A man rowed 3 mile:	s unstream in 90) minutes. If the riv	er flowed with a cu	rrent of 2 miles o	er hour how
٠.	long did the man's r	eturn trip take?			·	·
	a. 20 minutes	b. 30 minutes	c. 45 minute	s d. 60 minu	tes e. 80 mi	nutes
9.	A certain river has a two points as it doe boat in still water?					
	a. 3 mph	b. 6 mph	c. 9 mph	d. 12 mph	e. Cannot be det	ermined
10). A boat sailing agai the time taken would a. 3 km/hr			the speed of curre		
	a. o KIII/III	D. Z.O KIII/III	C. Z KIII/III	d. 1 km/hr	e. None o	เ แเซอซ

	for three hours with rs. What is the boa			ns the same o	distance against the
a. 18 mph	b. 21 mph	c. 24 mph	d. 27 mph	e. 30 mpl	า
	an airplane travel d the velocity of the		seven hours. Aga	inst the winc	I, however, it takes
a. 20 mph	b. 140 mph	c. 12 mph	d. 10 mph	e. 160 mj	oh
	w 5 km/h in still wa o a place and back			ning at 1 km/l	h. If it takes him 75
a. 3 km	b. 2.5 km	c. 4 km	d. 5 km	е	. None of these
	vhose speed is 15 30 minutes. The sp			ownstream ar	nd comes back in a
a. 4	b. 5	c. 6	d. 10	е	. None
		ROUP 3: TRAI	N & SDEED		
		SKOUP 3. IKAI	N & SPEED		
15. A train running of the train?	at the speed of 45	km/hr took 12 sed	conds to pass a co	ertain point. V	Vhat was the length
a. 90 m	b. 120 m	c. 150 m	d. 540 n	n e	. None of these
16. A train 100 me is the bridge?	ters long, travelling	at 48 km/h, com	pletely crosses a	bridge in 30	seconds. How long
a. 100 m	b. 150 m	c. 200 m	d. 300 m	e. 50	00 m
	running on the sa ur earlier, how long				our. If the first train
a. 5 hrs	b. 4 hrs	c. 3 hrs	d. 2 hrs	•	. None of these
	ters long is moving te direction at a spe		km/hr. How long v	vill it take to c	cross a man coming
a. 36 sec	b. 32 sec	c. 28 sec	d. 24 se	ec e	. 16 sec
19. A motorist trave a. x/(y+60z)	els x miles in y hou b. (60y+z)/x	rs and z minutes. c. 60x/(y+:		•	niles per hour? 1 none of these
	ning in the same di				ss one another in 1 train?
a. 125 m	b. 150 m	c. 200 m	d. 175 n	n e	. 133 m
21. Two trains are running on parallel lines in the same direction at a speed of 50 km/hr and 30 km/hr respectively. The faster train crosses a man sitting in the slower train in 18 seconds. What is the length of the faster train?					
a. 170 m	b. 100 m	c. 98 m	d. 85 m	е	. 64 m
	GROUP 5: C	OMPARING TR	RAVELED DIST	ANCES	
a speed of 600	miles per hour. At	4:00 the same a	fternoon, plane <i>B</i>	leaves the f	ard the other city at irst city, traveling in vers represents the

- actual result?
 - a. Plane A arrives first, by exactly an hour
 - b. Plane A arrives first, by less than an hour
 - c. The two planes arrive at exactly the same time
 - d. Plane A arrives after plane B, by less than an hour
 - e. Plane A arrives first, by more than an hour

- 23. Rokon can travel 120 miles in either of two ways. He can travel at a constant rate of 40 miles per hour, or he can travel half way at 50 miles per hour, then slow down to 30 miles per hour for the second half. Which way is faster, and by how much?
 - a. The constant rate is faster by 10 minutes or more
 - b. The constant rate is faster by less than 10 minutes
 - c. The two ways take exactly the same time
 - d. The constant rate is slower by less than 10 minutes
 - e. The constant rate is slower by 10 minutes or more
- 24. Arefin and Hussham agreed to race across a 50-foot pool and back again. They started together, but Arefin finished 10 feet ahead of Hussham. If their rates were constant, and Arefin finished the race in 27 seconds, how long did Hussham take to finish it?
 - a. 28 seconds
- b. 30 seconds
- c. 33 seconds
- d. 35 seconds
- e. 37 seconds
- 25. One hour after Turab started walking from Dhaka to Narayanganj, a distance of 45 miles, Saif started walking along the same road from Narayanganj to Dhaka. If Turab speed was 3 miles per hour and Saif was 4 miles per hour, how many miles had Turab walked when they met?
 - a. 24
- b. 23
- c. 22
- d. 21
- e. 19.5

PART II: TAKE-HOME ASSIGNMENT

1.		e trip from P to Q			of 2 miles. If she average in trip, what was her aver	
	a. $2\frac{2}{9}$ mph	b. 4 mph	c. $4\frac{4}{9}$ mph	d. $4\frac{1}{2}$ mph	e. 5 mph	
2.	A certain 90-mile trip	took 2 hours. Exa	ctly $\frac{1}{3}$ of the d	istance traveled w	as by rail, and this part of	the
	2	avel time. What wa	as the average	rate, in miles per	nour, of the rail portion of	the
	trip? a. 24 mph	b. 30 mph	c. 45 mph	d. 60 mph	e. 75 mph	
3.					one hour to walk home foutes will the trip take?	rom
	a. 36	b. 48	c. 54	d. 72	e. 96	
4.	A man travels for 8 h miles per hour, then				speed for the whole trip is	80
	a. 8 hours	b. 9 hours	c. 10 hours	d. 12 hours	e. 15 hours	
5.	Mahmud walks a disat an average rate of				nour, and returns on a bicy him?	ycle
	a. 3 hours	b. 4 hours	c. 5 hours	d. 6 hours	e. 7 hours	
6.	A man travels for 6 haverage speed for the		0 miles per hou	ır. His return trip ta	akes him 9 hours. What is	his
	a. 35.5 mph	b. 40 mph	c. 44.44 mpł	d. 45 mph	e. 50 mph	
7.	In one hour, a boat g boat in still water (in		g the stream an	id 5 km/hr against	the stream. The speed of	the
	a. 3 km/hr	o. 5 km/hr c	. 8 km/hr	d. 9 km/hr	e. None of these	
8.	A boat can travel with time taken by the bo			r. If the speed of the	ne stream is 4 km/hr, find	the
	a. 2 hours	b. 3 hours	c. 4 hours	d. 5 hours	e. 6 hours	
9.	A boatman goes 2 kr long will it take to go			d goes 1 km with th	ne current in 10 minutes. F	dow
	a. 45 minute	b. 1 hour	c. 1 hr 15 mi	n d. 1 hr 30 r	nin e. None	
10	•				ver is 4 km/h. Moving with the same time going aga	
	a. 60 km	b. 80 km	c. 100 km	d. 120 km	e. 180 km	
11	. A train crosses a 4 length of the train?	00 meter long fly-	over in 1 minut	e and a lamp pos	t in 10 seconds. What is	the
	a. 50 m	o. 60 m c	. 80 m	d. 100 m	e. Cannot be determined	
12		on the track parall	el to the first tra	ain but it travels at	urs later, another train lea 100 miles per hour. How	
	a. 100 miles	b. 150 miles	c. 200 miles	d. 300 miles	e. 500 miles	
13	s. A faster train with a from the opposite dir				eed of 72 km/h in 15 seco s?	nds
	a. 150 m	o. 350 m — c	. 400 m	d. 750 m	e. Cannot be determined	

14. A train traveling at 72 km/h crosses a platform in 30 seconds and a man standing on the platform in 18 seconds. What is the length of the platform in meters?					
a. 240 m	b. 360 m	c. 420 m	d. 600 m	e. None of these	
15. A train 100 meter the opposite direct				120 meters long coming from rain?	
a. 132 km/hr	b. 82 km/hr	c. 60 km/hr	d. 50 km/h	r e. 40 km/hr	
was waiting. They	boarded the helic	opter and flew to	o Vietnam at an av	an airport where a helicopter verage speed of 60 mph. The e distance from the airport to	
a. 30 miles	b. 60 miles	c. 90 miles	d. 120 mile	es e. None of these	
			mph. How long aft	is 45 miles long. One cyclist is er they begin will they meet? tes e. None of these	
				nd returns to Uttara at a speed entire journey in km/hour? e. 36	
				and 9 minutes respectively. If was the distance between A	
a. 6	b. 4.6	c. 4	d. 3	e. None of these	
				hour. It takes him 10 minutes ce (in km) between his house	
and office?					
and office? a. 7	b. 6	c. 5	d. 4	e. None of these	
a. 7 21. A tub is shaped li	ke a rectangular s an output of 2 cub	olid, with internal ic feet of water po	measurements of er minute pour wat	e. None of these 2 feet x 2 feet x 5 feet. If two er into the tub simultaneously,	
a. 7 21. A tub is shaped li faucets, each with how many minutes a. Less than 3 m b. Less than 4 m c. Less than 5 m	ke a rectangular so an output of 2 cub does it take to fill inutes inutes, but not less inutes, but not less inutes but not less	olid, with internal ic feet of water po the tub complete s than 3 s than 4	measurements of er minute pour wat	2 feet x 2 feet x 5 feet. If two	
a. 7 21. A tub is shaped li faucets, each with how many minutes a. Less than 3 m b. Less than 4 m c. Less than 5 m d. Less than 6 m e. More than 6 n	ke a rectangular so an output of 2 cub does it take to fill inutes inutes, but not less inutes, but not less inutes but not less ninutes	olid, with internal ic feet of water po the tub complete s than 3 s than 4 s than 5	measurements of er minute pour wat ly?	2 feet x 2 feet x 5 feet. If two	
a. 7 21. A tub is shaped li faucets, each with how many minutes a. Less than 3 m b. Less than 4 m c. Less than 5 m d. Less than 6 m e. More than 6 n	ke a rectangular so an output of 2 cub does it take to fill inutes inutes, but not less inutes, but not less inutes but not less ninutes	olid, with internal ic feet of water po the tub complete s than 3 s than 4 s than 5	measurements of er minute pour wat ly?	2 feet x 2 feet x 5 feet. If two er into the tub simultaneously, hour. If they start at the same	
a. 7 21. A tub is shaped li faucets, each with how many minutes a. Less than 3 m b. Less than 4 m c. Less than 5 m d. Less than 6 m e. More than 6 n 22. Naabil can run 10 time from the same a.1 mile 23. On a certain trip,	ke a rectangular so an output of 2 cub does it take to fill inutes inutes, but not less inutes but not less inutes but not less ninutes miles per hour, whe point, and run in b. 2 miles a motorist drove 1	olid, with internal ic feet of water pot the tub complete is than 3 is than 4 is than 5 inile Samer can ruopposite direction c. 3 miles in miles at 30 miles	measurements of er minute pour wat ly? In only 8 miles per n, how far apart wil d. 4 miles les per hour, 10 m	2 feet x 2 feet x 5 feet. If two er into the tub simultaneously, hour. If they start at the same I they be after 10 minutes?	
a. 7 21. A tub is shaped li faucets, each with how many minutes a. Less than 3 m b. Less than 4 m c. Less than 5 m d. Less than 6 m e. More than 6 m 22. Naabil can run 10 time from the same a.1 mile 23. On a certain trip, 10 miles at 50 mil	ke a rectangular so an output of 2 cub does it take to fill inutes inutes, but not less inutes, but not less inutes but not less inutes miles per hour, whe e point, and run in b. 2 miles a motorist drove 1 es per hour. What	olid, with internal ic feet of water potential the tub complete is than 3 is than 4 is than 5 in the Samer can ruopposite direction c. 3 miles it portion of her to	measurements of er minute pour wat ly? In only 8 miles per n, how far apart wil d. 4 miles les per hour, 10 m	2 feet x 2 feet x 5 feet. If two er into the tub simultaneously, hour. If they start at the same I they be after 10 minutes? e. 5 miles iles at 40 miles per hour, and as spent driving 50 miles per	
a. 7 21. A tub is shaped lifaucets, each with how many minutes a. Less than 3 m b. Less than 4 m c. Less than 5 m d. Less than 6 m e. More than 6 m 22. Naabil can run 10 time from the same a.1 mile 23. On a certain trip, 10 miles at 50 mill hour? a. $\frac{5}{7}$ 24. Town A & B are	ke a rectangular so an output of 2 cub does it take to fill inutes, but not less inutes, but not less inutes but not less inutes but not less inutes miles per hour, whe point, and run in b. 2 miles a motorist drove 1 es per hour. What b. $\frac{5}{12}$	olid, with internal ic feet of water potential the tub complete is than 3 is than 4 is than 5 in the Samer can ruopposite direction c. 3 miles 0 miles at 30 mit portion of her to c. $\frac{1}{3}$ a train leaves A	measurements of er minute pour wat ly? In only 8 miles per n, how far apart wil d. 4 miles les per hour, 10 motal driving time where $\frac{13}{51}$ in the direction of	2 feet x 2 feet x 5 feet. If two er into the tub simultaneously, hour. If they start at the same I they be after 10 minutes? e. 5 miles iles at 40 miles per hour, and as spent driving 50 miles per	
a. 7 21. A tub is shaped lifaucets, each with how many minutes a. Less than 3 mb. Less than 4 mc. Less than 5 md. Less than 6 me. More than 6 me. More than 6 me. More than 6 me. More than 6 me. The same a.1 mile 23. On a certain trip, 10 miles at 50 miles	ke a rectangular so an output of 2 cub does it take to fill inutes, but not less inutes, but not less inutes but not less inutes but not less inutes miles per hour, whe point, and run in b. 2 miles a motorist drove 1 es per hour. What b. $\frac{5}{12}$	olid, with internal ic feet of water potential the tub complete is than 3 is than 4 is than 5 in the Samer can ruopposite direction c. 3 miles 0 miles at 30 mit portion of her to c. $\frac{1}{3}$ a train leaves A	measurements of er minute pour wat ly? In only 8 miles per n, how far apart wil d. 4 miles les per hour, 10 motal driving time with d. $\frac{13}{51}$ in the direction of going from B to $\frac{13}{51}$	2 feet x 2 feet x 5 feet. If two er into the tub simultaneously, hour. If they start at the same I they be after 10 minutes? e. 5 miles iles at 40 miles per hour, and as spent driving 50 miles per e. $\frac{12}{47}$ B, at 50 miles per hour, how	
a. 7 21. A tub is shaped lifaucets, each with how many minutes a. Less than 3 mb. Less than 4 mc. Less than 5 md. Less than 6 me. More than 6	ke a rectangular so an output of 2 cub does it take to fill does it take to fill does in the solution of less in the point of less does not does does does does does does does does	olid, with internal ic feet of water pot the tub complete is than 3 is than 4 is than 5 inile Samer can ruopposite direction c. 3 miles it portion of her to c. $\frac{1}{3}$ a train leaves A ets another train, c. 5 hours	measurements of er minute pour wat ly? In only 8 miles per n, how far apart wil d. 4 miles les per hour, 10 motal driving time where $\frac{13}{51}$ in the direction of going from B to $\frac{13}{51}$ d. 5.67	2 feet x 2 feet x 5 feet. If two er into the tub simultaneously, hour. If they start at the same I they be after 10 minutes? e. 5 miles iles at 40 miles per hour, and as spent driving 50 miles per e. $\frac{12}{47}$ B, at 50 miles per hour, how A, at a speed of 30 miles per	

PART III: REVIEW LESSON FOR THE NEXT LECTURE

Finding a Specific Value

Example: If a fence is 120 feet long and post are set 5 feet apart, how many posts are needed?

Solution: Divide the length by the distance between two posts, i.e. 120/5 = 24,

Then add 1 with that, i.e. 24+1 = 25 posts

Note: If the fence is open on both sides, you have to add 1 with the division result.

Example: If a triangular garden has a perimeter of 120 feet and has a fence around it, how many post are required if they are set 5 feet apart?

Solution: Divide the perimeter of the garden by the distance between two posts, i.e. 120/5 = 24 posts, It's the answer in this case.

Note: If the fence is around an enclosed area, like: triangular/ circular/ rectangular garden, you don't need to add anything with the division result.

Different Rate Problems:

Rate Problems concern a special type of relationship which is very common.

 $Rate \times Input = Output$. This results from the definition of rate as the ratio between output and input. In these problems, input may represent any type of "investment," but the most frequent quantities used as inputs are time, work, and money. Output is usually distance traveled, work done, or money spent.

Note: The word "per", as used in rates, signifies a ratio. Thus, a rate of 25 taka per hour signifies the ratio between an output of 25 taka and an input of 1 hour. Frequently, the word "per" will be represented by the fraction sign.

Example: Sayem earns 25 taka in 1 hour from his work for the first 4 hours and 30 taka for each additional hour. How many hours did he work if he earned taka 160 altogether in a particular day? **Solution:** For first 4 hours of work, he got $(25 \times 4 = 100 \text{ taka})$. Excess amount he earned = 160-100 = 60 taka. So his additional hour of work is, 60/30 = 2 hr. Altogether on that day he worked, 4+2=6 hours.

Set Problems:

Set is one of the most fundamental concepts of mathematics and you can expect some questions in the Admission test that test your knowledge of sets. Set is a mathematical way to describe a collection of distinct objects, such as a list of numbers, a group of students studying the same subject etc. The individual objects in a set are referred to as elements or members of the set. The elements or members of a set can be anything: numbers, people, letters of the alphabet, other sets and so on. Sets are conventionally denoted with capital letters.

Unions:

When you combine the elements of two or more sets, you are finding the union of the sets. The symbol for union is U.

Intersections:

When you find the elements that two or more sets have in common, you are finding the intersection of the set. The symbol for intersection is \cap .

Formula for finding out the number of elements in the intersection or union of more than two sets:

If the number of elements in set A, set B, intersection of sets A & B and union of sets A & B are denoted by n(A), n(B), $n(A\cap B)$ and $n(A\cup B)$ respectively, then

$$n (AUB) = n (A) + n (B) - n (A \cap B)$$

Example:

In a summer camp, there are a total of 28 students out of which 7 play hockey, 20 play tennis and 6 students play neither tennis nor hockey. How many students play both tennis and hockey?

Solution: Here,

n(A) = Number of students who play hockey = 7

n(B) = Number of students who play tennis = 20

n(AUB) = Number of total students – Number of students who play neither tennis nor hockey = 28 - 6 = 22

Therefore, $22 = 7 + 20 - \mathbf{n}(\mathbf{A} \cap \mathbf{B})$ $\Rightarrow \mathbf{n}(\mathbf{A} \cap \mathbf{B}) = 5$

Permutation and Combination:

Counting problems involve figuring out how many ways you select or arrange members of groups, such as letter of the alphabet, numbers, or menu selections.

Fundamental Counting Principle:

The Fundamental Counting Principle is the guiding rule for finding the number of ways to accomplish two tasks.

If there are m ways to do one thing, and n ways to do another, then there are m×n ways of doing both. For example:

- Let's say that you want to flip a coin and roll a dice. There are 2 ways that you can flip a coin and 6 ways that you can roll a dice. There are then 2x6=12 ways that you can flip a coin *and* roll a dice
- If you want to draw 2 cards from a standard deck of 52 cards without replacing them, then there are 52 ways to draw the first and 51 ways to draw the second, so there are a total of 52×51 = 2652 ways to draw the two cards.

Sample Spaces:

A listing of all the possible outcomes is called the sample space and is denoted by the capital letter S. The sample space for the experiments of flipping a coin and rolling a dice are S = {H1, H2, H3, H4, H5, H6, T1, T2, T3, T4, T5, T6}. Sure enough, there are twelve possible ways. The fundamental counting principle allows us to figure out that there are twelve ways without having to list them all out.

Permutations:

A permutation is an arrangement of objects, without repetition, and order being important. Another definition of permutation is the number of such arrangements that are possible.

$${}^{n}P_{r} = P(n, r) = \frac{n!}{(n-r)!}$$

Since a permutation is the number of ways you can arrange objects, it will always be a whole number. The denominator in the formula will always divide evenly into the numerator. The n value is the total number of objects to choose from. The r is the number of objects you are actually using.

The two key things to notice about permutations are that:

- i. Repetition of objects is not allowed.
- ii. Order / arrangement is important.

Example 1: List all permutations of the letters A, B, C, D

ABDC	BADC	CADB	DACB
ABCD	BACD	CABD	DABC

Now, if you didn't actually need a listing of all the permutations, you could use the formula for the number of permutations. There are 4 objects and you're taking 4 at a time. ${}^4P_4 = \frac{4!}{(4-4)!} = \frac{4!}{0!} = \frac{24}{1} = 24$.

This also gives us another definition of permutations. A permutation when you include all n objects is n!. That is, P(n,n) = n!

Combinations:

A combination is an arrangement of objects, without repetition, and order not being important. Another definition of combination is the number of such arrangements that are possible.

$${}^{n}C_{r} = C(n, r) = \frac{n!}{(n-r)! r!}$$

The n and r in the formula stand for the total number of objects to choose from and the number of objects in the arrangement, respectively.

The two key things to notice about combinations are that:

- i. Repetition of objects is not allowed.
- ii. Order / arrangement is not important.

Example 1: List all combinations of the letters A, B, C, D in groups of 3

There are only four combinations (ABC, ABD, ACD, and BCD). Listed below each of those combinations are the six permutations that are equivalent as combinations.

ABC	ABD	ACD	BCD
ABC ACB	ABD ADB	ACD ADC	BCD BDC

Probability

Probability indicates the chance that a particular event will occur. Probabilities are expressed as fractions.

The value of the probability has a range between 0 and 1. If an event is certain to occur, its probability is 1. If an event is certain *not* to occur, its probability is 0.

Example: If a box contains 9 white marbles, 5 green marbles and 3 black marbles, what is the probability of selecting a green marble from the box without looking?

Solution: Here, probability =
$$\frac{\text{number of green marbles}}{\text{total number of marbles}}$$
$$= \frac{5}{9+5+3}$$
$$= \frac{5}{17}$$

Therefore, the probability of selecting a green marble from the box is $\frac{5}{17}$

Independent Events:

If two events occur simultaneously and the first event does not affect the probability of the second event, then the events are said to be independent of each other. For two independent events A and B, the probability of A and B both occurring is the product of the probability of A and the probability of B, that is, $P(A \text{ and } B) = P(A) \times P(B)$

Example: If someone draws a card at random from a deck, and then, without replacing the first card, draws a second card, what is the probability that both cards will be aces?

Solution: In a deck, there are 52 cards. Among them, 4 are aces. The probability that the first card is an

ace is P(A) =
$$\frac{4}{52}$$

Since the first ace has been drawn, there are now 3 aces in a deck of 51 cards. Thus, the probability that the second card is an ace is $P(B) = \frac{3}{51}$

Therefore, the probability that both cards are aces is $P(A \text{ and } B) = P(A) \times P(B)$

$$=\frac{4}{52}\times\frac{3}{51}=\frac{1}{13}\times\frac{1}{17}=\frac{1}{221}$$

Mutually Exclusive Events:

Two events are said to be mutually exclusive, if it is impossible for both to occur simultaneously. For example, boys cannot be chosen from a group of girls and girls cannot be chosen from a group of boys. Hence, choosing boys and choosing girls are said to be mutually exclusive.

For two mutually exclusive events A or B, the probability that either of them will occur is P(A or B) = P(A) + P(B)

Example: What is the probability of rolling a dice and getting either a 1 or 6?

Solution: Since it is impossible to get both a 1 and a 6, these two events are mutually exclusive.

Therefore,

P (1 or 6) = P(1) + P(6) =
$$\frac{1}{6} + \frac{1}{6} = \frac{1}{3}$$

Note that, the probability of happening an event + the probability of not happening that event = 1

Work-Done Problems

Example: Jack can chop down 20 trees in 1 hour, while it takes Ted $1\frac{1}{2}$ hours to chop down 18 trees. If the two of them work together, how long will it take both of them together to chop down 48 trees?

Rate × Time = Work

	trees/hr.	Hours	Trees
1. Jack	20	1	20
2. Ted	12	$1\frac{1}{2}$	18
3. Jack	20		
4. Ted	12		

We represent the time that it takes Jack by x in line 3. Since we have the relationship that Rate \times Time = Work, we see that in line 3 the work done is 20x. Since the two boys work together (therefore, for the same amount of time), the time in line 4 must be x and the work must be 12x. Now, we see that the total work is 48 trees. From lines 3 and 4, 20x + 12x = 48. Solving for x gives us $x = 1\frac{1}{2}$. We are asked to find the number of hours needed by the boys to chop down the 48 trees together, and we see that this time is x, or $1\frac{1}{2}$ hours.

	.		
Name	Review Test or 10 Marks, 10		Batch
1. How many pounds of a \$2.40 pound mixture to produce a mix			ounds of a \$1.80 per
a. 10 b. 20	c. 30	d. 35	e. 40
2. A 30% solution of barium chloric grams of the original solution did		ams of water to form a 209	% solution. How many
a. 10 b. 15	c. 20	d. 25	e. 30
3. Elizabeth and Scott each receinstallments. If the amount paid Scott in the first nine months, we Elizabeth's prize? a. 1:3 b. 3:1	I to Elizabeth in the fir	st three months is equal	to the amount paid to
4. If it takes Adrito twice as long Adrito's pay per hour to Mezbah a. 2:1 b. 3:1		d. 3:4	u, what is the ratio of e. 4:3
5. If one star equals four circles			
diamond?	·	·	is the ratio of star to
a. 3:16 b. 1:3	c. 3:5	d. 3:1	e. 16:3
6. The average of the first 3 of 4 numbers is 13, what is the last r	number?		
a. 6 b. 5	c. 8	d. 4	e. 3
7. If 6 workers can complete 9 ide such jobs?	entical jobs in 3 days,	how long will it take 4 wo	orkers to complete 10
a. 3 days b. 4 days	s c. 5 days	d. 6 days	e. 8 days
8. Afifa puts taka 2000 into a bank years, what will be her balance?			
a. Tk. 2200 b. Tk. 2440			None of these
9. Which of the following CANNOT a. 1 b. 2	• • • • • • • • • • • • • • • • • • • •		e even integers? 12
10. At a certain firm, "d" gallons of will supply "t" trucks for how mar		ay for each truck. At this r	rate, "g" gallons of fuel
a. $\frac{dt}{d}$ b. $\frac{gt}{d}$	c. dgt	d. $\frac{t}{dq}$	e. $\frac{g}{dt}$
g d	3	dg	dt
Answer Sheet			
1			
3.		SCORE	
4.		3331,2111111	
5.			
6.		REMARK	S
7.			
8.			
9.			
10.			