

### CSC 424 Homework 3

3.

Source Code:

```
library(CCA)
library(psych)
library(CCP)
ds <- read.csv("/Users/Yiyang/Documents/CSC
424/Datasets/data_marsh_cleaned_homework2.csv", sep = ",", header = TRUE)
```

```
#x: water, y: soil
X <- ds[-1, 2: 6]
x <- apply(X, 2, as.numeric)
```

```
Y <- ds[-1, 7: 9]
y <- apply(Y, 2, as.numeric)
```

1)

a.

#a. combine all

```
c <- matcor(x, y)
cross <- c$XYcor[1:5, 6:8]
round(cross, 2)
```

#Corr test

```
p <- corr.p(cross, nrow(x))
p
```

#Canonical correlation

```
cc1 <- cc(x, y)
```

```
wilks1 <- ccaWilks(X, Y, cc1)
```

```
wilks1
```

```
round(wilks1, 2)
```

Output:

```
> wilks1 <- ccaWilks(X, Y, cc1)
> wilks1
      WilksL      F df1      df2      p
[1,] 0.6963021 4.051995 15 433.8093 6.185853e-07
[2,] 0.8179043 4.176302  8 316.0000 9.094796e-05
[3,] 0.9284064 4.087068  3 159.0000 7.921523e-03
> round(wilks1, 2)
      WilksL      F df1      df2      p
[1,]  0.70 4.05 15 433.81 0.00
[2,]  0.82 4.18  8 316.00 0.00
[3,]  0.93 4.09  3 159.00 0.01
```

b).

Source Code:

```
Y2 <- Y[, 2: 3]
y2 <- y[, 2: 3]
y2
cc2 <- cc(x, y2)
cc2
```

```
wilks2 <- ccaWilks(X, Y2, cc2)
wilks2
round(wilks2, 2)
```

Ouput:

```
> wilks2 <- ccaWilks(X, Y2, cc2)
> wilks2
      WilksL      F df1 df2      p
[1,] 0.7800982 4.177702  10 316 1.892668e-05
[2,] 0.9019218 4.322556   4 159 2.400337e-03
> round(wilks2, 2)
      WilksL      F df1 df2 p
[1,]   0.78 4.18  10 316 0
[2,]   0.90 4.32   4 159 0
```

c).

Source Code:

```
#c
Y3 <- data.frame(TPRSDFB = Y$TPRSDFB)
Y3
y3 <- as.matrix(y[, 3])
y3
cc3 <- cc(x, y3)
cc3
```

```
wilks3 <- ccaWilks(X, Y3, cc3)
wilks3
round(wilks3, 2)
```

Output:

```
> wilks3 <- ccaWilks(X, Y3, cc3)
> wilks3
      WilksL      F df1 df2      p
[1,] 0.888069 4.008028   5 159 0.00188145
> round(wilks3, 2)
      WilksL      F df1 df2 p
[1,]   0.89 4.01   5 159 0
```

d).

For the first one the correlations are 0.3855843, 0.3449978, 0.2675698.

For the second one the correlations are 0.3675203, 0.3131744.  
For the third one the correlation is 0.3345609.

e).

Since all the three correlations have small p value, it means we need to reject null hypothesis, which means the correlations are not equal to zero.

2.

Output:

```
$xcoef
      [,1]      [,2]      [,3]
MEHGSWB  0.720571333 -0.613310304  0.442819677
TURB      0.014902006  0.003947628  0.046585662
DOCSWD   -0.122898091 -0.045649299 -0.038307498
SRPRSWFB -15.972715690 77.864165952 -98.959103678
THGFSFC   0.004124619 -0.009849176 -0.009493841

$ycoef
      [,1]      [,2]      [,3]
THGSDFC  0.011415578 -0.010169482 -0.014106076
TCSDFB   -0.077556675 -0.037720634  0.072787341
TPRSDFB  -0.002969355  0.002268621 -0.004222605
```

a).

Soil variates and water variables

$$V1 = 0.720571333\text{MEHGSWB} + 0.014902006\text{TURB} - 0.122898091\text{DOCSWD} - 15.972715690\text{SRPRSWFB} + 0.004124619\text{THGFSFC}$$

$$V2 = -0.613310304\text{MEHGSWB} + 0.003947628\text{TURB} - 0.045649299\text{DOCSWD} + 77.864165952\text{SRPRSWFB} - 0.009849176\text{THGFSFC}$$

$$V3 = 0.442819677\text{MEHGSWB} + 0.46585662\text{TURB} - 0.038307498\text{DOCSWD} - 98.959103678\text{SRPRSWFB} - 0.009493841\text{THGFSFC}$$

$$V1 = 0.011415578\text{THGSDFC} - 0.077556675\text{TCSDFB} - 0.002969355\text{TPRSDFB}$$

$$V2 = -0.010169482\text{THGSDFC} - 0.037720634\text{TCSDFB} + 0.002268621\text{TPRSDFB}$$

$$V3 = -0.014106076\text{THGSDFC} + 0.072787341\text{TCSDFB} - 0.004222605\text{TPRSDFB}$$

b).

```
$scores$corr.X.xscores
      [,1]      [,2]      [,3]
MEHGSWB -0.2138288 -0.5442426  0.05580913
TURB     -0.1207027 -0.03435814  0.49853147
DOCSWD   -0.8920181 -0.39006177  0.02464817
SRPRSWFB -0.1719363  0.58138401 -0.63983875
THGFSFC   0.4914315 -0.62009828 -0.52589688

$scores$corr.Y.xscores
      [,1]      [,2]      [,3]
THGSDFC -0.003665011 -0.30485575 -0.12523874
TCSDFB   -0.246423901 -0.26504660  0.00980968
TPRSDFB  -0.275332457  0.05094524 -0.18310544

$scores$corr.X.ycores
      [,1]      [,2]      [,3]
MEHGSWB -0.08244902 -0.18776307  0.014932836
TURB     -0.04654108 -0.01185348  0.133391950
DOCSWD   -0.34394820 -0.13457045  0.006595106
SRPRSWFB -0.06629592  0.20057620 -0.171201505
THGFSFC   0.18948827 -0.21393254 -0.140714106

$scores$corr.Y.ycores
      [,1]      [,2]      [,3]
THGSDFC -0.009505083 -0.8836455 -0.46806012
TCSDFB   -0.639092107 -0.7682559  0.03666214
TPRSDFB  -0.714065477  0.1476683 -0.68432782
```

Soil variates and soil variables

$$V1 = -0.009505083\text{THGSDFC} - 0.0639092107\text{TCSDFB} - 0.714065477\text{TPRSDFB}$$

$$V2 = -0.8836455\text{THGSDFC} - 0.7682559\text{TCSDFB} + 0.1476683\text{TPRSDFB}$$

$$V3 = -0.46806012\text{THGSDFC} + 0.03666214\text{TCSDFB} - 0.68432782\text{TPRSDFB}$$

Water variates and water variables

$V1 = -0.2138288MEHGSWB - 0.1207027TURB - 0.8920181DOCSWD - 0.1719363SRPRSWFB + 0.4914315THGFSFC$   
 $V2 = -0.54424426MEHGSWB - 0.03435814TURB - 0.39006177DOCSWD - 0.58138401SPRSWFB - 0.62009828THGFSFC$   
 $V3 = 0.05580913MEHGSWB + 0.49853147TURB + 0.02464817DOCSWD - 0.63983875SRPRSWFB - 0.52589688THGFSFC$

c).

The correlations between Soil variates and water variables are similar with the one between soil variates and water variables.

4.

Source Code:

```

smoking <- read.csv("/Users/Yiyang/Documents/CSC 424/Smoking.csv", sep = ',', header = TRUE)
colnames(smoking) <- c("Staff Group", "None", "Light", "Medium", "Heavy", "Row Total")
cSmoking = ca(smoking[1:5, 2:5])
plot(cSmoking, mass = T, contrib = "absolute", map = "rowgreen", arrows = c(F, T))

```

a).

Output:

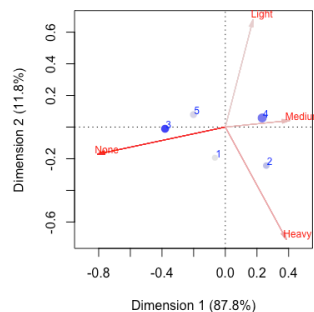
```

Principal inertias (eigenvalues):
      1      2      3
Value  0.074759 0.010017 0.000414
Percentage 87.76% 11.76% 0.49%

Rows:
      1      2      3      4      5
Mass  0.056995 0.093264 0.264249 0.455959 0.129534
ChiDist 0.216559 0.356021 0.380779 0.240025 0.216169
Inertia 0.002673 0.011881 0.038314 0.026269 0.006053
Dim. 1 -0.240539 0.947105 -1.391973 0.851989 -0.735456
Dim. 2 -1.935708 -2.430958 -0.106508 0.576944 0.788435

Columns:
      None  Light  Medium  Heavy
Mass  0.316062 0.233161 0.321244 0.129534
ChiDist 0.394490 0.173996 0.198127 0.355109
Inertia 0.049186 0.007059 0.012610 0.016335
Dim. 1 -1.438471 0.363746 0.718017 1.074445
Dim. 2 -0.304659 1.409433 0.073528 -1.975960

```



b).

The patterns on the plot are present the staff group. The pattern 4 is the biggest one and pattern 3 is the darkest one. Pattern 4 means this group has the most people, pattern 3 mean this group has the most possibility on none smoking. And the perpendicular distance from patterns to the vector means the smoking tendency of the group.

c).

First two eigenvectors account for 99.51% of the inertia. From the result, only one eigenvector get to 80 of the inertia. It is easy to plot the data with on dimensions.