Isogenies and finite subgroups

1 Isogenies and finite subgroups

Theorem 1. Let A be an abelian variety of dimension d over k. Then the subgroup A[n] of n torsion points is finite and we have

- (a) if n is coprime to $\operatorname{char}(\mathbf{k})$, then $A[n] \cong (\mathbb{Z}/n\mathbb{Z})^{2d}$;
- (b) if $n = p^k$ for $p = \text{char}(\mathbf{k}) > 0$

Proof. Yang: To be completed.

Theorem 2. Let A be an abelian variety over k. There is a bijection between the isogenies from A over k and the finite subgroup schemes of A.

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