

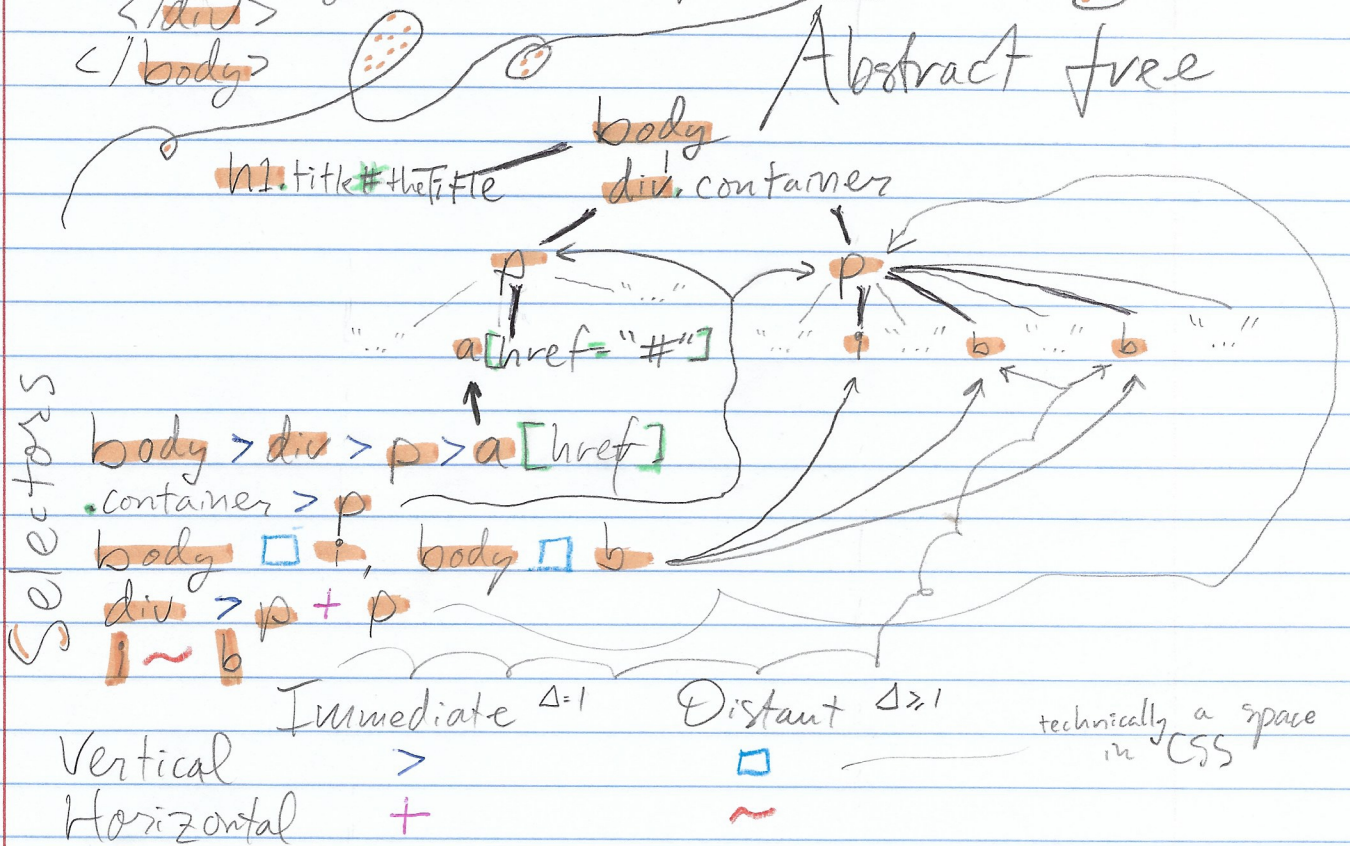
# Introduction

## CSS Selectors & HTML trees

### (X)(HT)ML:

Combine  
Match only

```
<body>
  <h1 class="title" id="theTitle">Title </h1>
  <div class="container">
    <p>Welcome to this <a href="#">presentation</a> </p>
    <p>Hopefully you will learn at least <i>something</i>
      about <b>CSS selectors</b> and <b>Boolean
      Algebras</b> </p>
  </div>
</body>
```



Observations

- Can add more **attributes**: `div.container.special[title]` but not more **elements**, since a node has only one element type: `div` and `p` never overlap.
- Can match more things with `,` commas
- Can **negate** a selector: `:not(div > p)`
- Other pseudo-classes & elements: `:hover` `::selection`
- Always: `*`, never: `:not(*)`



Excluded Middle:  $t \vee \neg t = a \vee \neg a$

# Introduction (continued)

Boolean Algebra everywhere in language and mathematics

data Bool = T | F

Boolean Algebra Bool where

$t = T, f = F, \neg T = F, \neg F = T$

$t \vee \neg t = \text{id}$   
 $\neg \neg t = t$

$T \&\& T = T, -\&\&- = F$  "conjunction"

$F \vee F = F, -\vee- = T$  "disjunction"

Lift over Tuple as expected.

Even predicates:  $\forall a, b. \text{Boolean Algebra } b. a \Rightarrow b$

e.g. isKeyword = (eq "let")  $\vee$  eq "in"  $\vee$  eq "where"  $\vee$  ...

isOperator = eq ">"  $\vee$  eq ">="  $\vee$  ...

classify = isKeyword  $\&\&\&$  isOperator

$(\&\&\&) :: \forall a b c. (a \Rightarrow b) \Rightarrow (a \Rightarrow c) \Rightarrow (a \Rightarrow \text{Tuple } b c)$

Properties:

Conjunction forms a idempotent, commutative monoid with  $t$  as identity,  $f$  as annihilator.

Disjunction: similar story,  $t$  and  $f$  swap roles.

Distributivity:  $(a \&\& b) \vee c = (a \vee c) \&\& (b \vee c)$   
 $(a \vee b) \&\& c = (a \&\& c) \vee (b \&\& c)$

De Morgan:  $\neg (a \&\& b) = \neg a \vee \neg b$   
 $\neg (a \vee b) = \neg a \&\& \neg b$

## Big Reveal... (Disjunctive) Normal Form

DNF ::= clause | clause  $\vee$  DNF

clause ::= term | term  $\&\&$  clause

term ::= 'not' var | var

var ::= 'a' - 'z'

actually, this is whatever datatype.

newtype DNF var = Set (Map var Boolean)

set of  $\uparrow$   
disjoined  
clauses

each variable may appear  
negated or unnegated  
in a conjunctive clause

B-tree Assoc.  
Simplif  
List  
gtr structure

Conjunctive Multiset  
Ideas  
Set

monoid  
homomorphism

coherence  
sensicality

BNF  
did it again