

A Full Ott Spec

vars, n, a, x, y, z, w, m, o

ivar, i, k, j, l

const, b

$A, B, C \quad ::=$
 $\quad \mid \quad \mathbf{B}$
 $\quad \mid \quad \mathbf{UnitS}$
 $\quad \mid \quad A \triangleright B$
 $\quad \mid \quad A \multimap B$
 $\quad \mid \quad A \leftarrow B$
 $\quad \mid \quad \mathbf{FX}$

$X, Y, Z \quad ::=$
 $\quad \mid \quad \mathbf{B}$
 $\quad \mid \quad \mathbf{UnitT}$
 $\quad \mid \quad X \otimes Y$
 $\quad \mid \quad X \multimap Y$
 $\quad \mid \quad \mathbf{GA}$

$T \quad ::=$
 $\quad \mid \quad A$
 $\quad \mid \quad X$

$\Phi, \Psi \quad ::=$
 $\quad \mid \quad \cdot$
 $\quad \mid \quad \Phi_1, \Phi_2$
 $\quad \mid \quad X$
 $\quad \mid \quad (\Phi) \quad \mathbf{S}$

$\Gamma, \Delta \quad ::=$
 $\quad \mid \quad \cdot$
 $\quad \mid \quad A$
 $\quad \mid \quad \Phi$
 $\quad \mid \quad \Gamma_1, \Gamma_2$
 $\quad \mid \quad (\Gamma) \quad \mathbf{S}$

$\boxed{\Phi \vdash_C X}$

$$\frac{}{X \vdash_C X} \mathbf{T_AX}$$

$$\frac{\Phi, \Psi \vdash_C X}{\Phi, \mathbf{UnitT}, \Psi \vdash_C X} \mathbf{T_UNITL}$$

$$\frac{}{\cdot \vdash_C \mathbf{UnitT}} \mathbf{T_UNITR}$$

$$\frac{\Phi, X, Y, \Psi \vdash_C Z}{\Phi, Y, X, \Psi \vdash_C Z} \mathbf{T_BETA}$$

$$\begin{array}{c}
\frac{\Phi_1, X, \Phi_2, X, \Phi_3 \vdash_C Y}{\Phi_1, \Phi_2, X, \Phi_3 \vdash_C Y} \quad \text{T_CONTRR} \\
\frac{\Phi_1, X, \Phi_2, X, \Phi_3 \vdash_C Y}{\Phi_1, X, \Phi_2, \Phi_3 \vdash_C Y} \quad \text{T_CONTRL} \\
\frac{\Phi, \Psi \vdash_C Y}{\Phi, X, \Psi \vdash_C Y} \quad \text{T_WEAK} \\
\frac{\Phi \vdash_C X}{\Psi_1, \Phi, \Psi_2 \vdash_C Y} \quad \text{T_CUT} \\
\frac{\Phi \vdash_C X}{\Psi_1, \Phi, \Psi_2 \vdash_C Y} \quad \text{T_CUTN} \\
\frac{\Phi, X, Y, \Psi \vdash_C Z}{\Phi, X \otimes Y, \Psi \vdash_C Z} \quad \text{T_TENL} \\
\frac{\Phi \vdash_C X \quad \Psi \vdash_C Y}{\Phi, \Psi \vdash_C X \otimes Y} \quad \text{T_TENR} \\
\frac{\Phi \vdash_C X}{\Psi_1, \Phi, X \multimap Y, \Psi_2 \vdash_C Z} \quad \text{T_IMPL} \\
\frac{\Phi, X, \Psi \vdash_C Y}{\Phi, \Psi \vdash_C X \multimap Y} \quad \text{T_IMPR} \\
\frac{\Phi \vdash_{\mathcal{L}} A}{\Phi \vdash_C \text{GA}} \quad \text{T_Gr}
\end{array}$$

$$\boxed{\Gamma \vdash_{\mathcal{L}} A}$$

$$\begin{array}{c}
\frac{}{A \vdash_{\mathcal{L}} A} \quad \text{S_AX} \\
\frac{\Gamma, \Delta \vdash_{\mathcal{L}} A}{\Gamma, \text{UnitT}, \Delta \vdash_{\mathcal{L}} A} \quad \text{S_UNITL1} \\
\frac{\Gamma, \Delta \vdash_{\mathcal{L}} A}{\Gamma, \text{UnitS}, \Delta \vdash_{\mathcal{L}} A} \quad \text{S_UNITL2} \\
\frac{}{\cdot \vdash_{\mathcal{L}} \text{UnitS}} \quad \text{S_UNITR} \\
\frac{\Gamma, X, Y, \Delta \vdash_{\mathcal{L}} A}{\Gamma, Y, X, \Delta \vdash_{\mathcal{L}} A} \quad \text{S_BETA} \\
\frac{\Gamma_1, X, \Gamma_2, X, \Gamma_3 \vdash_{\mathcal{L}} A}{\Gamma_1, \Gamma_2, X, \Gamma_3 \vdash_{\mathcal{L}} A} \quad \text{S_CONTRR} \\
\frac{\Gamma_1, X, \Gamma_2, X, \Gamma_3 \vdash_{\mathcal{L}} A}{\Gamma_1, X, \Gamma_2, \Gamma_3 \vdash_{\mathcal{L}} A} \quad \text{S_CONTRL} \\
\frac{\Gamma, \Delta \vdash_{\mathcal{L}} A}{\Gamma, X, \Delta \vdash_{\mathcal{L}} B} \quad \text{S_WEAK} \\
\frac{\Phi \vdash_C X \quad \Gamma_1, X, \Gamma_2 \vdash_{\mathcal{L}} A}{\Gamma_1, \Phi, \Gamma_2 \vdash_{\mathcal{L}} A} \quad \text{S_CUT1}
\end{array}$$

$$\begin{array}{c}
\frac{\Gamma \vdash_{\mathcal{L}} A \quad \Delta_1, A, \Delta_2 \vdash_{\mathcal{L}} B}{\Delta_1, \Gamma, \Delta_2 \vdash_{\mathcal{L}} B} \quad \text{S_CUT2} \\
\\
\frac{\Gamma, X, Y, \Delta \vdash_{\mathcal{L}} A}{\Gamma, X \otimes Y, \Delta \vdash_{\mathcal{L}} A} \quad \text{S_TENL1} \\
\\
\frac{\Gamma, A, B, \Delta \vdash_{\mathcal{L}} C}{\Gamma, A \triangleright B, \Delta \vdash_{\mathcal{L}} C} \quad \text{S_TENL2} \\
\\
\frac{\Gamma \vdash_{\mathcal{L}} A \quad \Delta \vdash_{\mathcal{L}} B}{\Gamma, \Delta \vdash_{\mathcal{L}} A \triangleright B} \quad \text{S_TENR} \\
\\
\frac{\Phi \vdash_C X \quad \Gamma, Y, \Delta \vdash_{\mathcal{L}} A}{\Gamma, \Phi, X \multimap Y, \Delta \vdash_{\mathcal{L}} A} \quad \text{S_IMPL} \\
\\
\frac{\Gamma \vdash_{\mathcal{L}} A \quad \Delta, B \vdash_{\mathcal{L}} C}{\Delta, A \multimap B, \Gamma \vdash_{\mathcal{L}} C} \quad \text{S_IMPLR} \\
\\
\frac{\Gamma \vdash_{\mathcal{L}} A \quad B, \Delta \vdash_{\mathcal{L}} C}{\Gamma, B \multimap A, \Delta \vdash_{\mathcal{L}} C} \quad \text{S_IMPLL} \\
\\
\frac{\Gamma, A \vdash_{\mathcal{L}} B}{\Gamma \vdash_{\mathcal{L}} A \multimap B} \quad \text{S_IMPRR} \\
\\
\frac{A, \Gamma \vdash_{\mathcal{L}} B}{\Gamma \vdash_{\mathcal{L}} B \multimap A} \quad \text{S_IMPLR} \\
\\
\frac{\Phi \vdash_C X}{\Phi \vdash_{\mathcal{L}} \text{FX}} \quad \text{S_FR} \\
\\
\frac{\Gamma, X, \Delta \vdash_{\mathcal{L}} A}{\Gamma, \text{FX}, \Delta \vdash_{\mathcal{L}} A} \quad \text{S_FL} \\
\\
\frac{\Gamma, A, \Delta \vdash_{\mathcal{L}} B}{\Gamma, \text{GA}, \Delta \vdash_{\mathcal{L}} B} \quad \text{S_GL}
\end{array}$$