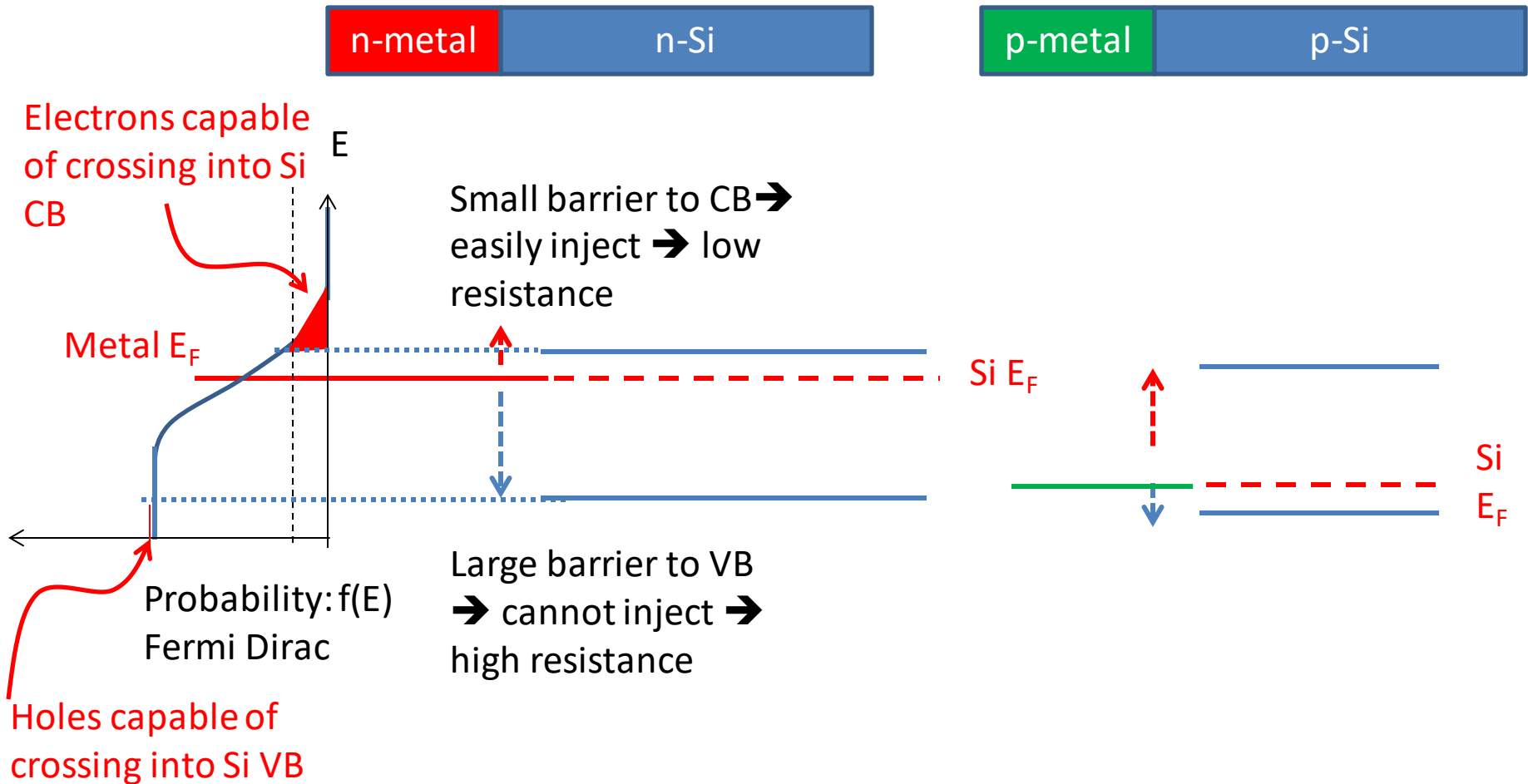


EE 724 PN Junctions L3

Udayan Ganguly

March 4, 2019

n/p-metal contact to semiconductor

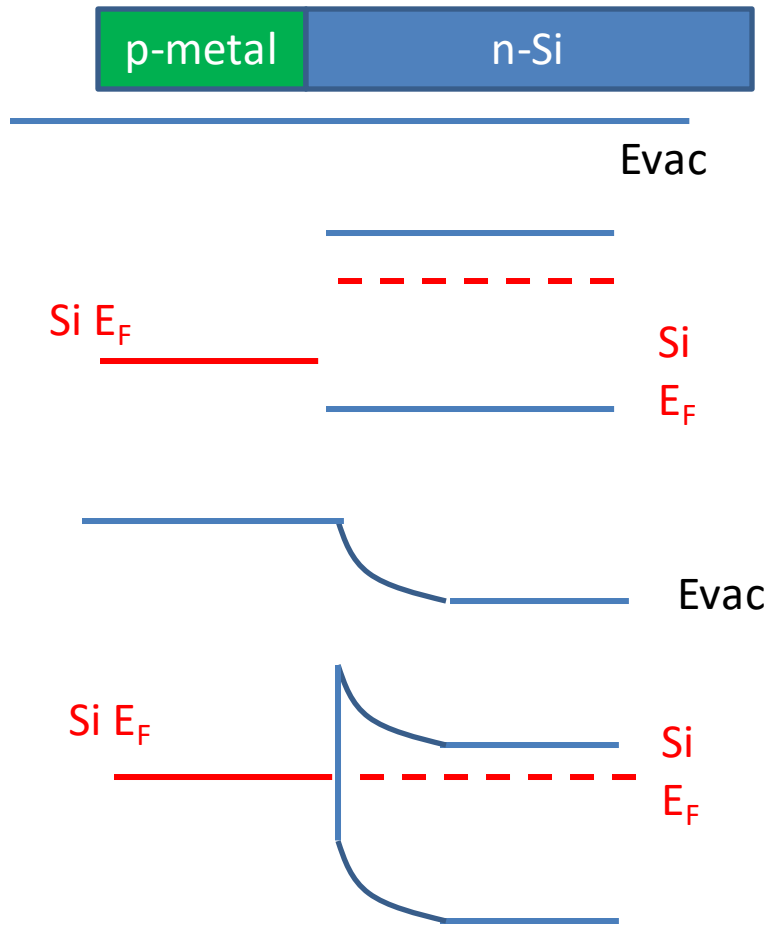


A metal work function closer to Si CB is able to inject electrons easily into CB but not holes into VB : n-type metal
Conversely p-metal may be defined.

Note: band bending is small because metal / Si Fermi levels are initially aligned.

Schottky barrier

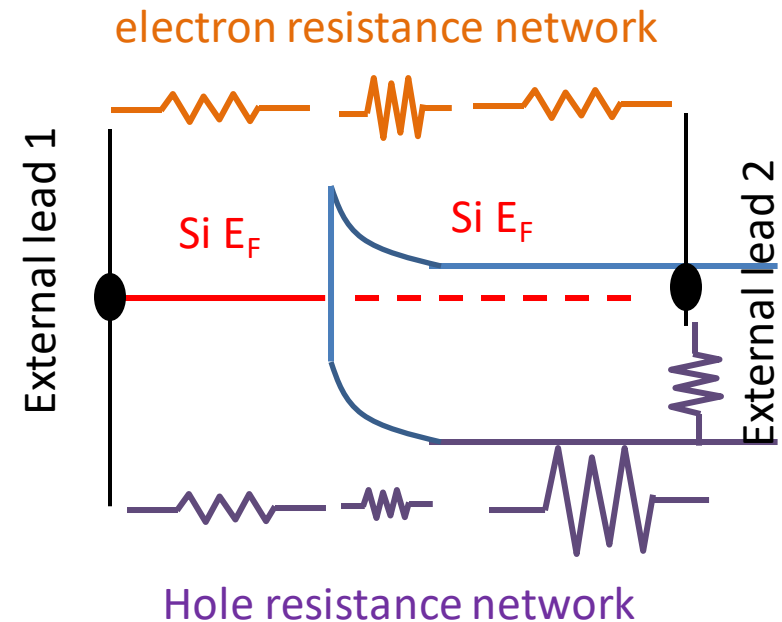
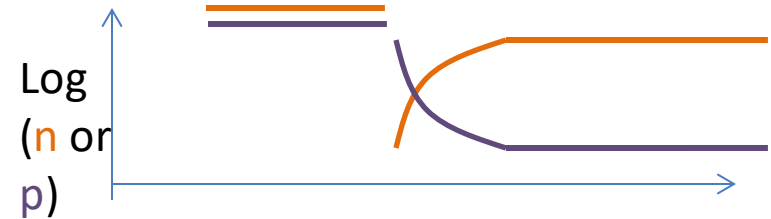
1. Electrostatics



Band bending can be calculated by depletion approximation

2. Transport

To make resistor network, (1) plot free carrier profile (2) convert $R=1/q\mu n$

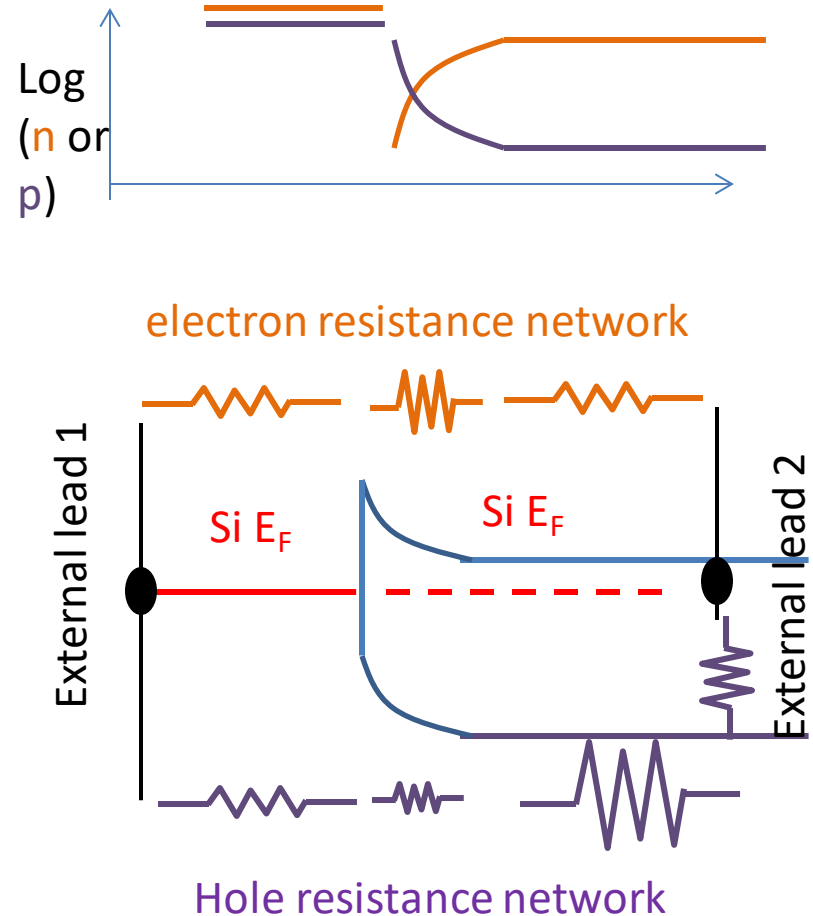


Based on the resistor network, electron current will dominate.

PS: External lead 2 must be an n-contact; so there may be addition resistance to VB

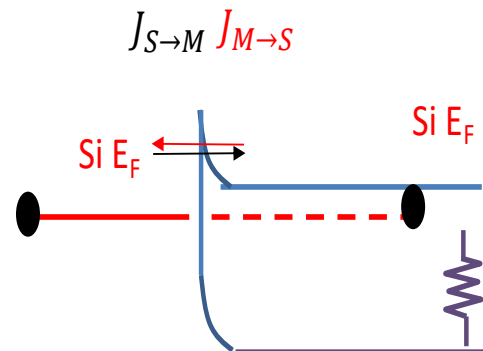
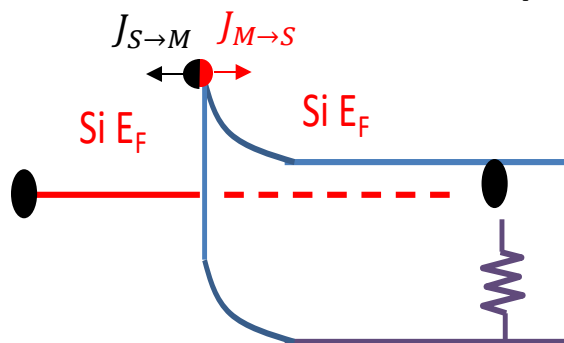
Method

1. Choose Equilibrium band diagram
 2. Plot $n(x)$ and $p(x)$
 3. If there was a small bias applied, where will the Fermi level bend?
 4. If larger bias was applied where will it bend?
- Think – if Q4 was asked before Q3, what would be the trouble in answering Q4 directly? Would it be easier if you asked yourself Q3 first?

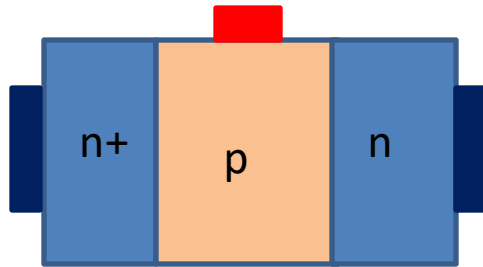


Three limiting cases

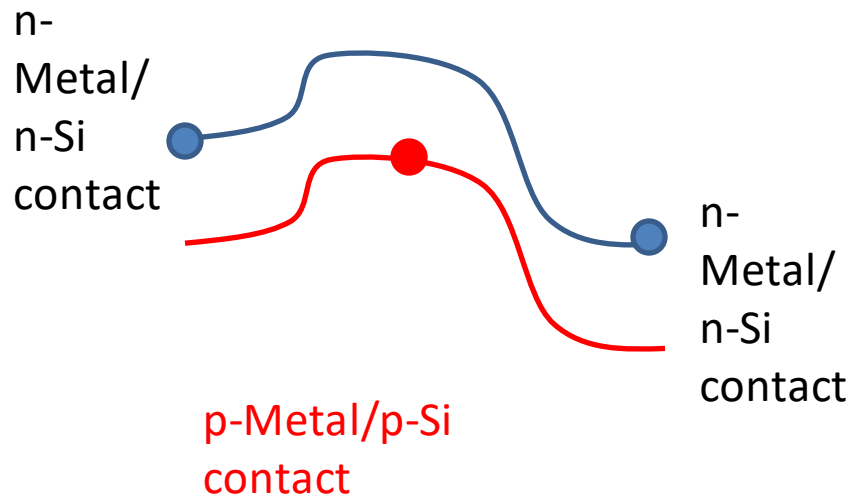
- Over-the-Barrier-Current
 - only T dependent in reverse bias
- Tunneling
 - No T dependence but strong V dependence in reverse bias
- Mixed
 - Both T and V dependence



Application1: Band Transport in a BJT



Question 1: Stepwise show how far the current may be calculated using QFL arguments.



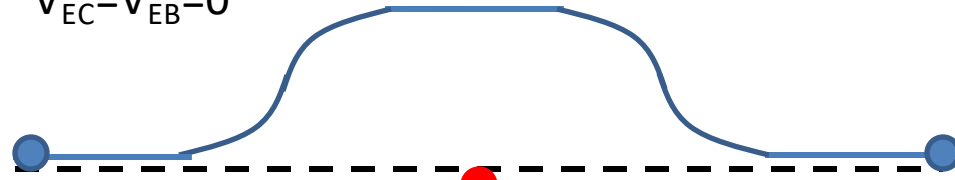
Assume depletion regions are not merged (i.e. not punch-through).

Show I_C , I_b vs V_B @ constant V_C and V_C @ constant V_B

Electrostatics & Transport in BJT

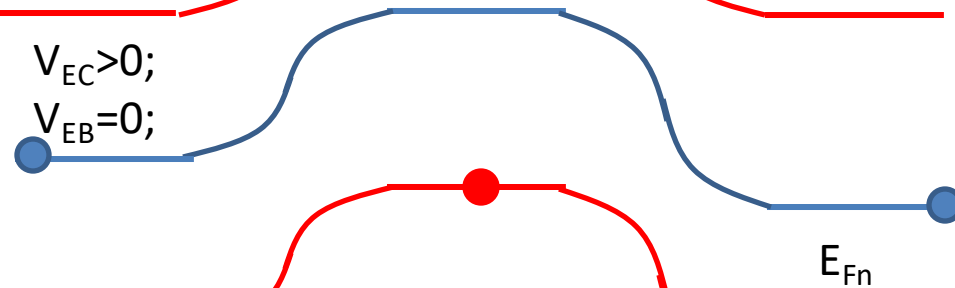
1. Electrostatics: Use Depletion approximation

$$V_{EC}=V_{EB}=0$$

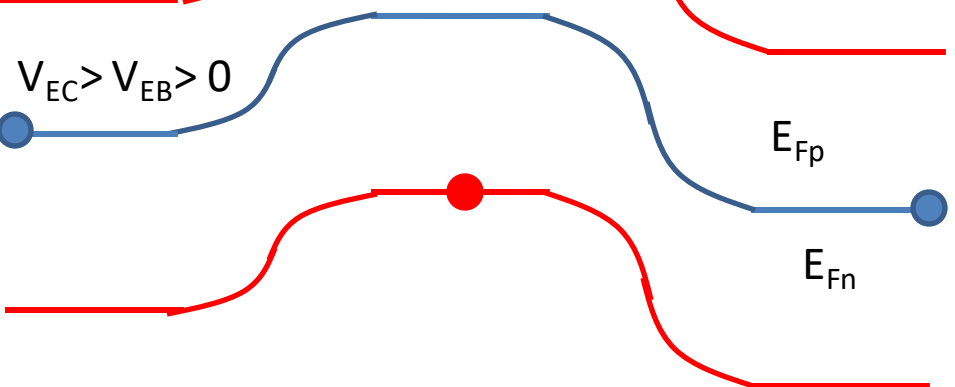


$$V_{EC}>0;$$

$$V_{EB}=0;$$



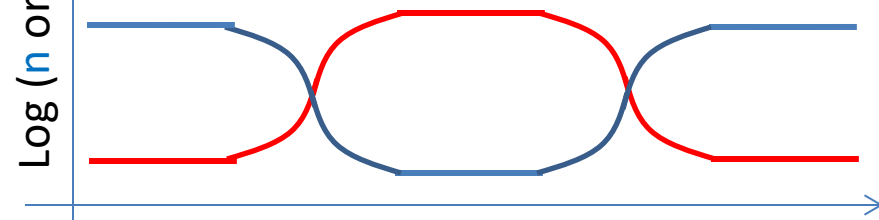
$$V_{EC}>V_{EB}>0$$



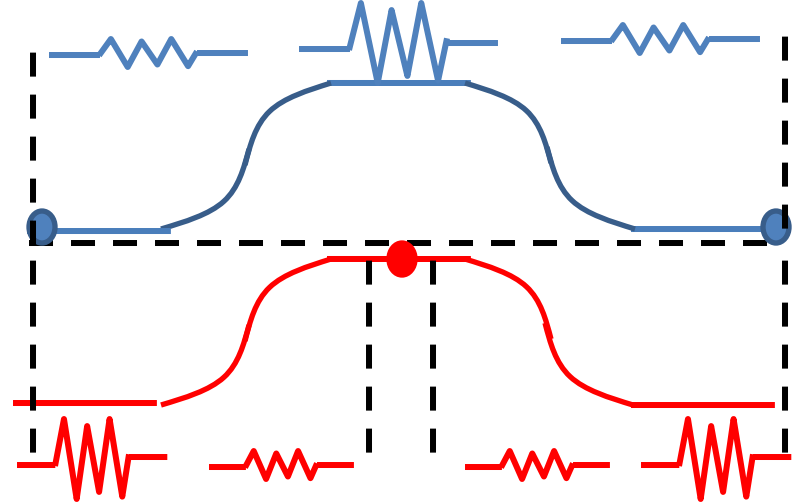
2 Transport (use previous algorithm)

Log (n or p)

2.1 carrier profile is drawn

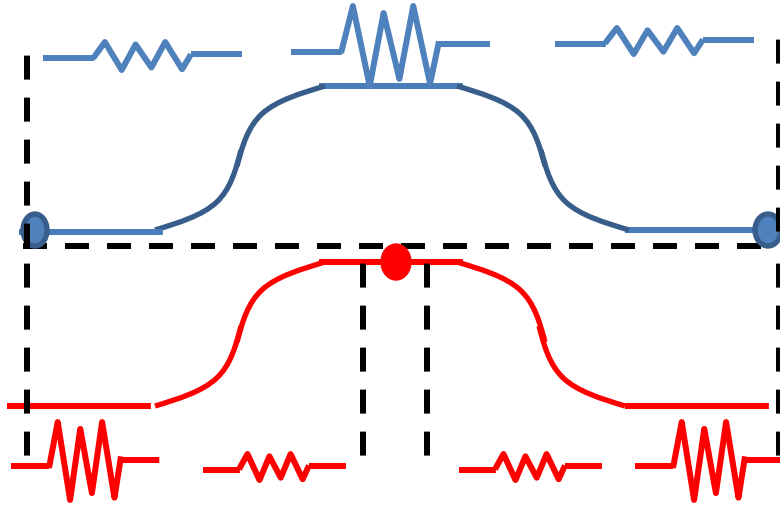


2.2 resistance network is drawn

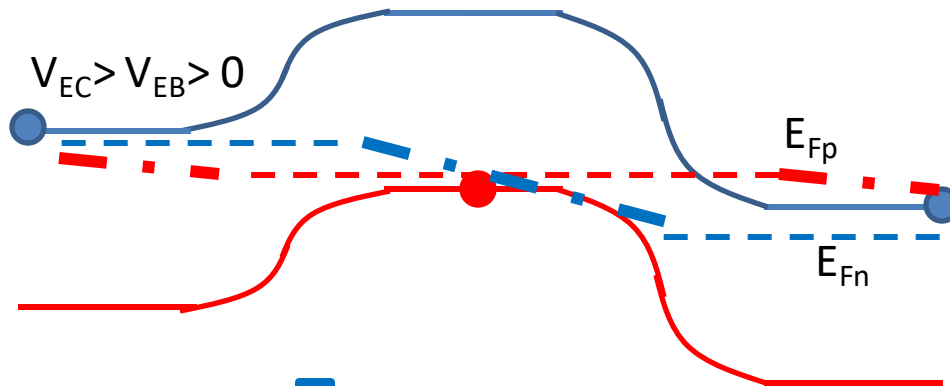


So we know where the E_{Fn} and E_{Fp} will bend. Or conversely where is it flat. Can we draw this? See in the next page!

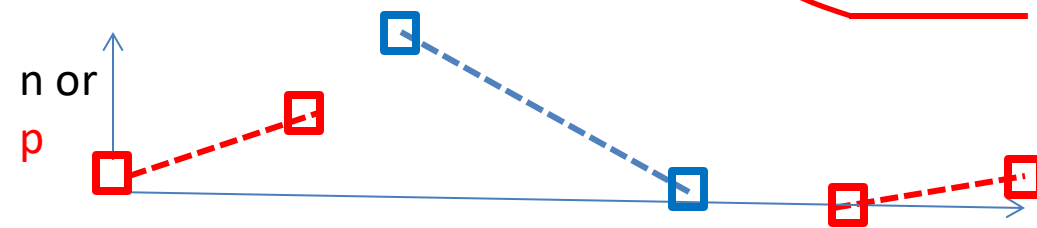
BJT transport calculation



2.3 Based on resistor network, we know where E_{Fn} and E_{Fp} is flat
Electron and hole conc at edges of diffusion calculation zones known
electron □ hole. □



2.4 Electron --- and hole --- profiles are drawn based on transport e.g. diffusion in this case. Other mechanisms will be shown later



2.5 E_{Fn} and E_{Fp} profiles in diffusion calculation regions (where there is gradient) are created based on n and p profiles

Calculating current

Electron current calculated in p-region

$$\frac{dn}{dt} = \nabla J + R = D \frac{d^2 n}{dx^2} + \frac{n - n_o}{\tau} = 0$$

Assume no recombination $\tau \rightarrow \infty$

e-Current from E to C

$$J_o = J(x) = qD \frac{dn}{dx} = \text{constant}$$

$$\rightarrow \frac{dn}{dx} = \text{constant} = \frac{n_L - n_R}{l_p}$$

Where $n_L = \frac{n_i^2}{N_A} \exp(\frac{V_{EB}}{V_T})$; forward biased

$n_R = \frac{n_i^2}{N_A} \exp(-\frac{V_{BC}}{V_T})$; reverse biased

l_p : quazi neutral p-region (which also has a V_{BE} and V_{BC} dependence based on depletion approximation)

e-Current from E to C

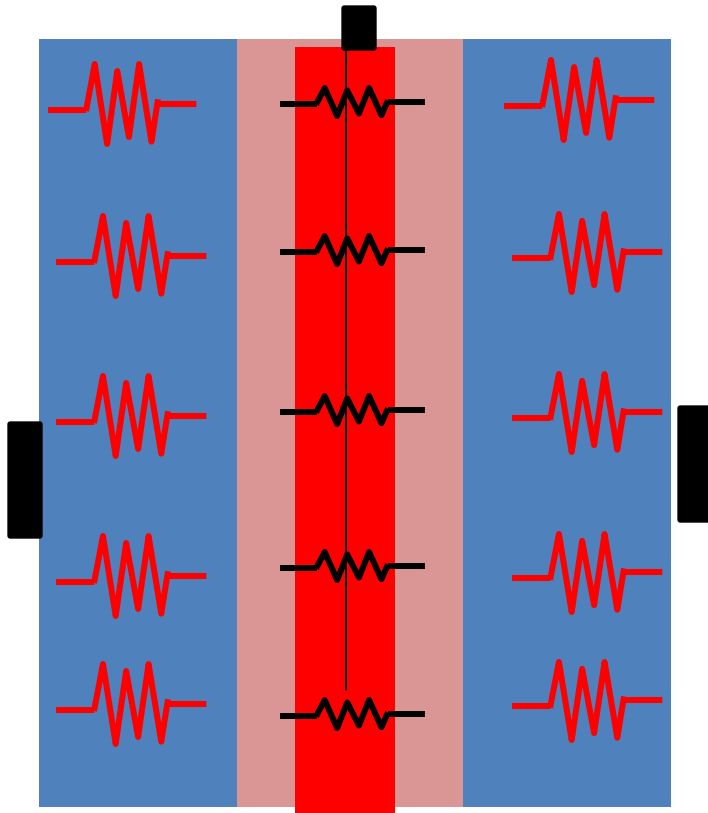
$$J_o = \frac{qD}{l_p} \frac{n_i^2}{N_A} (\exp(\frac{V_{EB}}{V_T}) - \exp(-\frac{V_{BC}}{V_T}))$$

Similarly; you may calculate hole current at the various junctions
Which hole current dominated EB or CB?

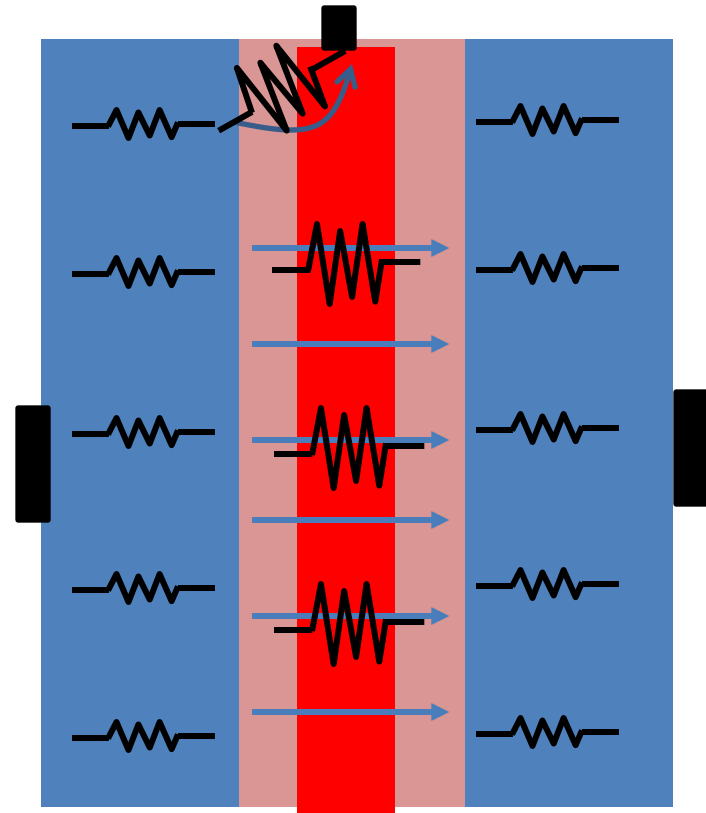
h-Current from E to C

$$J_o = \frac{qD}{l_{nE}} \frac{n_i^2}{N_{DE}} (\exp(\frac{V_{EB}}{V_T}) - 1)$$

Difference between base contact effect to control base potential vs. current sink

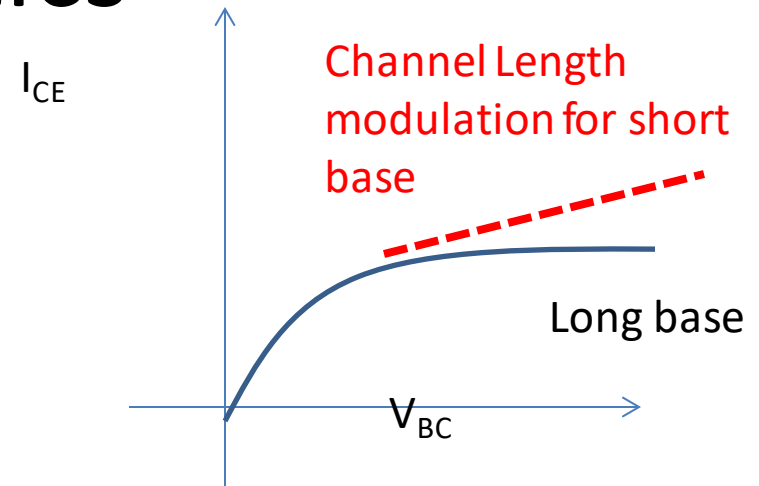
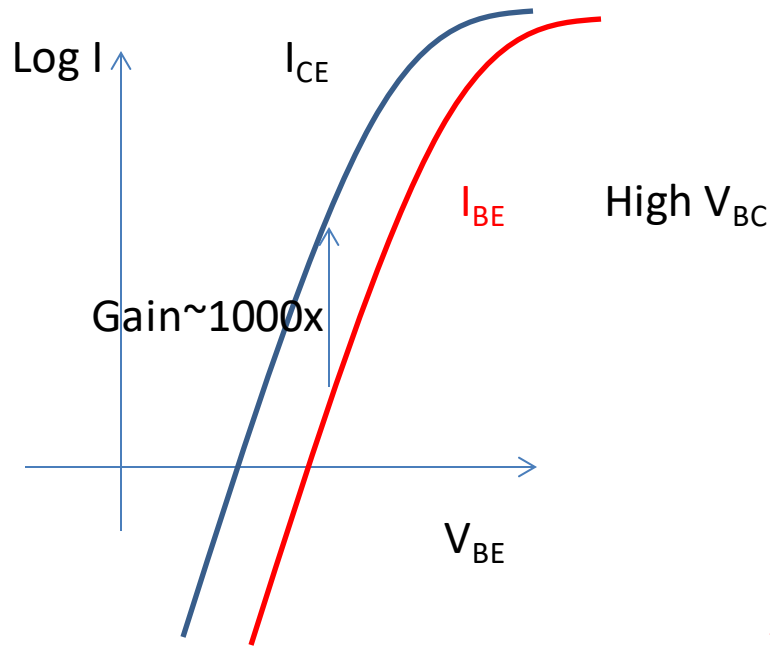


Base contact is strongly electrically coupled (potential divider model) to entire base



Fraction of e-current makes it to base contact due to geometry effect; Only a small fraction (local) electrons reach base; rest majority reach S/D

BJT IV characteristics

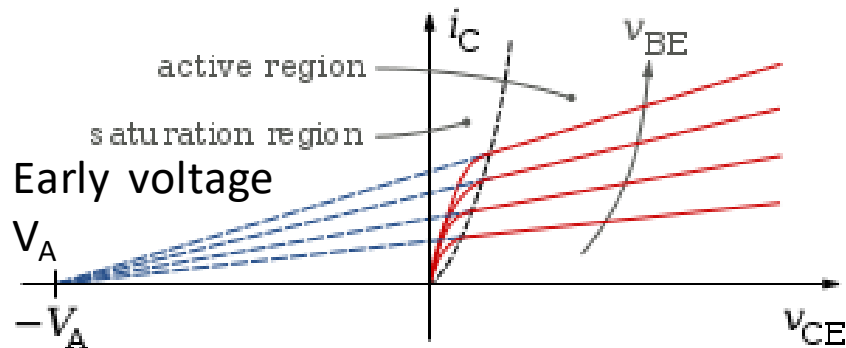


e-Current from E to C

$$J_o = \frac{qD}{l_p} \frac{n_i^2}{N_A} \left(\exp\left(\frac{V_{EB}}{V_T}\right) - \exp\left(-\frac{V_{BC}}{V_T}\right) \right)$$

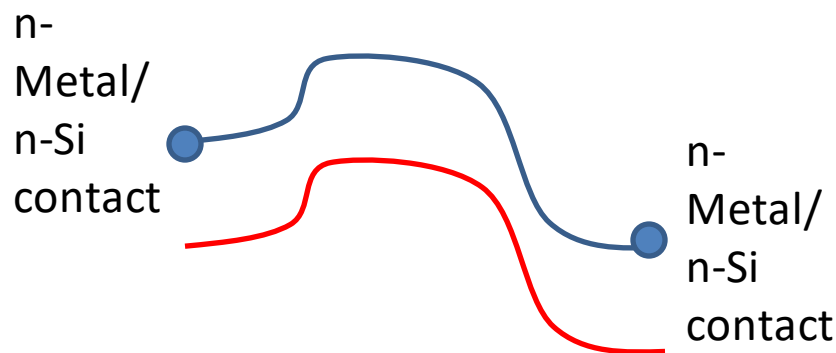
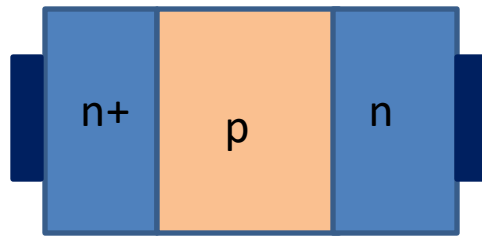
l_p : quazi neutral p-region (which also has a V_{BE} and V_{BC} dependence based on depletion approximation)

For long base, l_p % change due to V_{BC} is low but high for short base



Application 2: Transport in punch-through diode

Punch-through diodes are used for (i) ESD protection (b) RRAM selector devices



No p-Metal/p-Si contact

Question 1: Show how far the current may be calculated using QFL arguments;

a) With punch-through of depletions at $V=0$ b) With punch-through of depletions at $V=V_+$? Guess the IV characteristics and band profile.

Given are other device options;

i) 2 antiparallel diodes

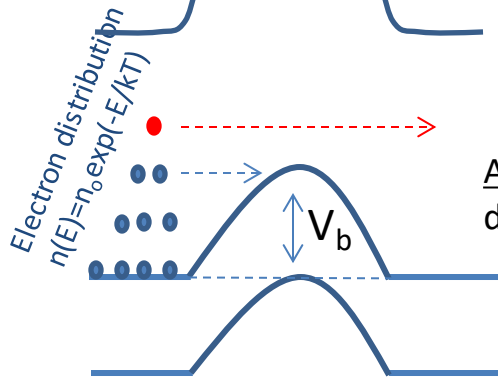
ii) Two anti-serial Schottky diodes

What are the advantages vs. disadvantages

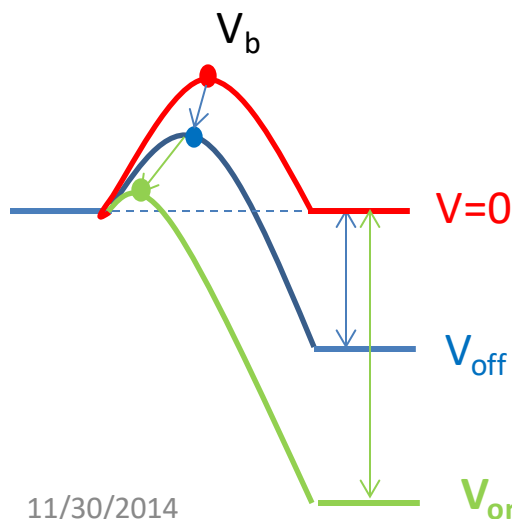
Punch-through diode as Selector

n+ p n+

Conventional n+pn+ junction:
depletion regions are
separate (e.g. BJT, MOSFET)



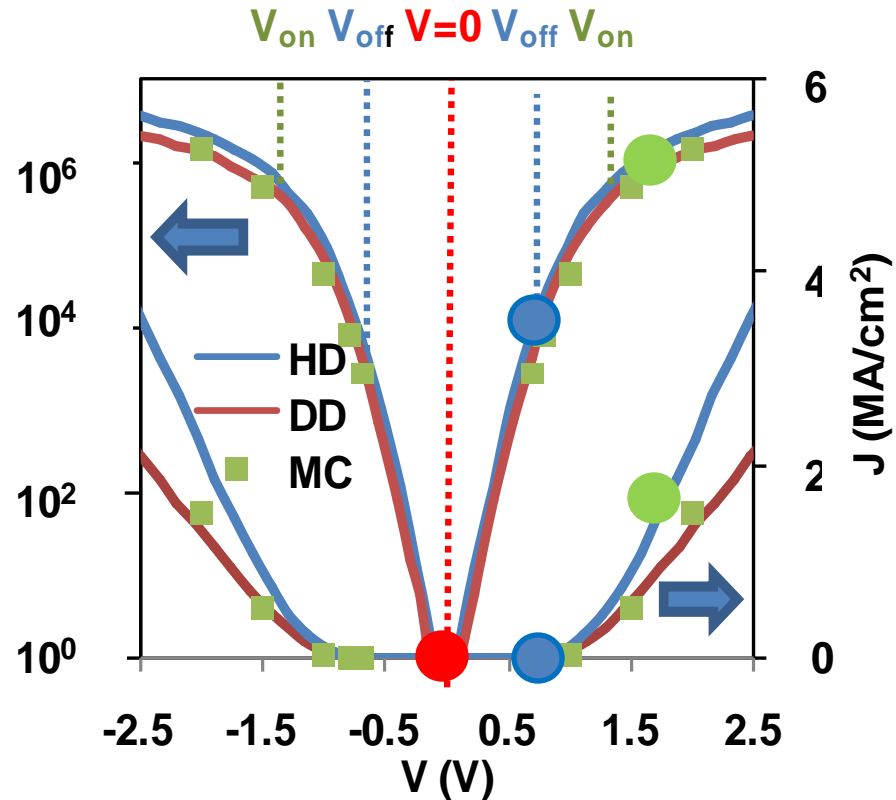
A punch-through diode:
depletion regions are merged



Punch-through

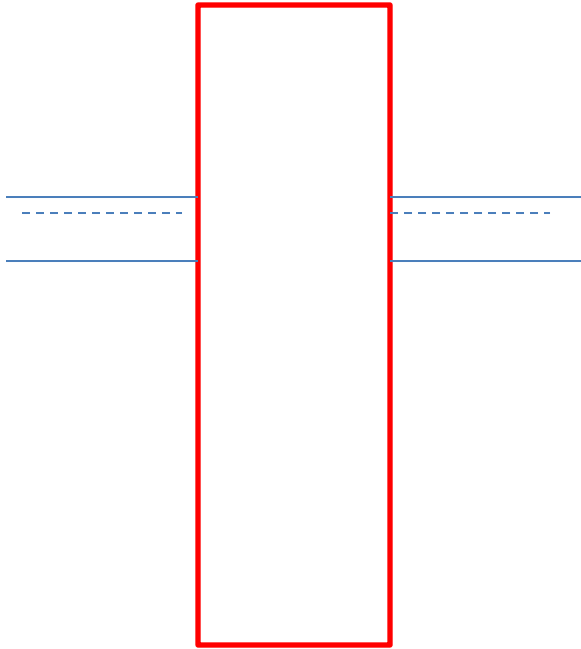
Barrier modulated
($I \sim \exp(V)$)

SCLC ($I \sim V, V^2$)



Ambipolar operation (turns on in both polarity) based on punch-through

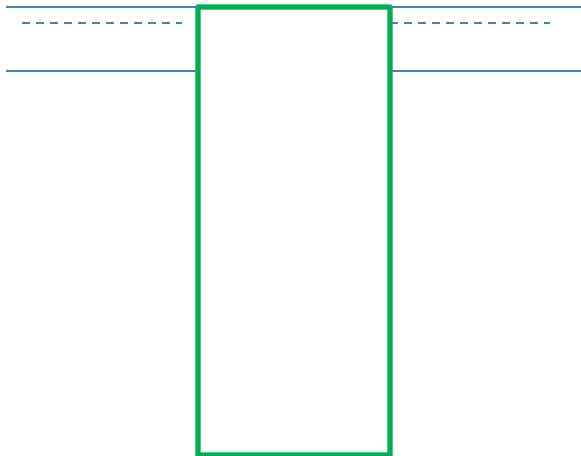
Application 3a: A case of Si n⁺/insulator/n⁺ junction



- Plot carrier profiles; Where is the maximum resistance?
- Does it matter
 - if the contacts are metals or highly doped semiconductors? Draw band diagram & derive current. What type of device is this?

Application 3b: A case of Si n+/insulator/n+ junction

Contact resistance is defined by Fermi level pinning:



- What happens when the conduction band offset is zero with a fine valance band offset? What type of device is this?

Space Charge Limited Current

- In Ohmic conduction: V only adds electric field that moves intrinsic Carriers
- In insulators; intrinsic charge is low, injected charged is voltage depend (like charging up a capacitor);

- $$J(x) = q\mu n(V)E(V) = \mu \left(\frac{CV}{L}\right) \left(\frac{V}{L}\right) = \mu \left(\frac{\epsilon V}{L^2}\right) \left(\frac{V}{L}\right) = \frac{\epsilon\mu V^2}{L^3}$$

- More accurate derivation: Drift is dominant
- $J(x) = q\mu n(x)E(x) = J_0$ as there is no recombination

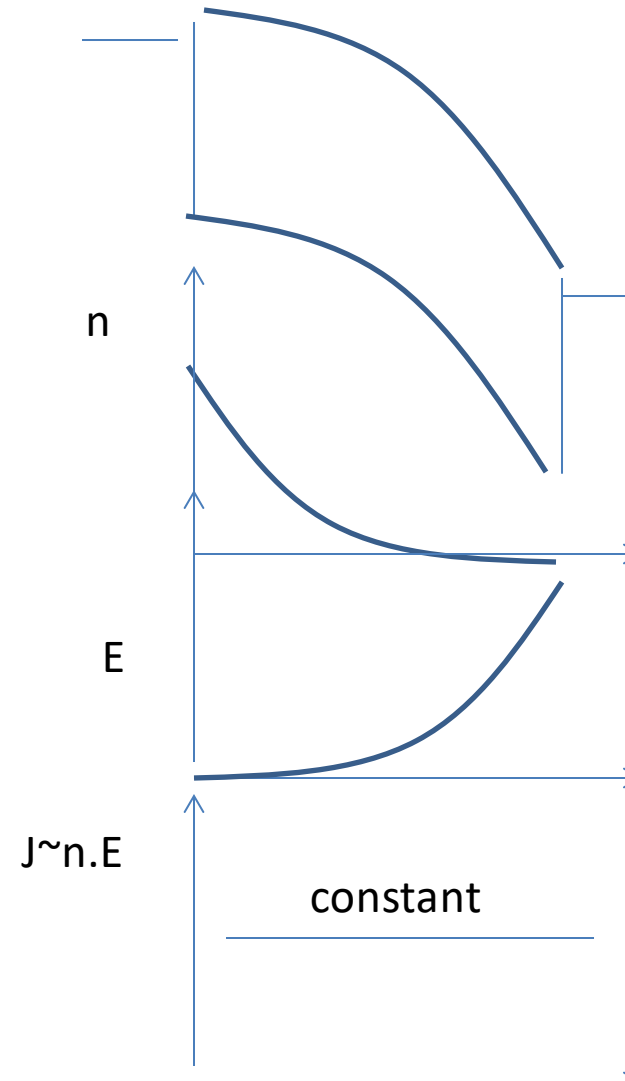
- $n(x) = \frac{J_0}{q\mu E} \dots$ from Drift based transport

- $\frac{dE}{dx} = -\frac{qn(x)}{\epsilon}$ from Poisson

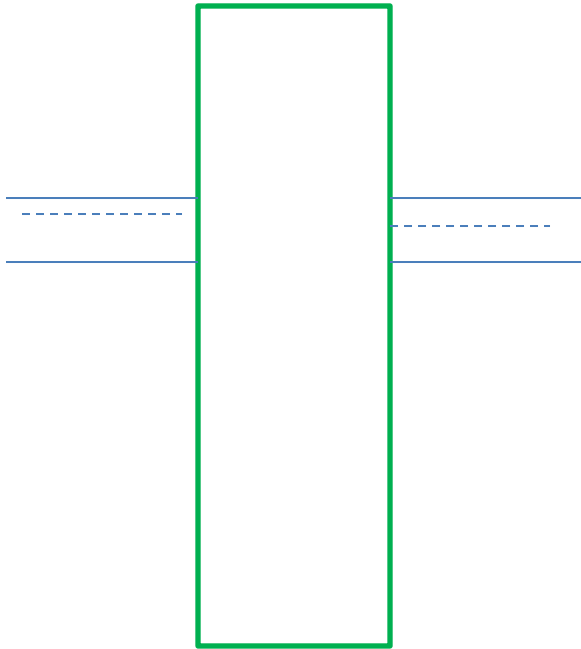
- $\frac{dE}{dx} = -\frac{q}{\epsilon} \frac{J_0}{q\mu E}$

- $E^2 = \frac{2q}{\epsilon} \frac{J_0}{q\mu} x \rightarrow \frac{dV}{dx} = \left(2 \frac{q}{\epsilon} \frac{J_0}{q\mu} x\right)^{1/2}$

- $V = \frac{2}{3} \left(\frac{2q}{\epsilon} \frac{J_0}{q\mu}\right)^{1/2} (x)^{3/2} \rightarrow J_0 = \frac{9}{8} \frac{\epsilon\mu V^2}{L^3}$



Application 3c: A case of Si n⁺/insulator/n⁺ junction



- What if one side is low doped semiconductors?
Draw band diagram & derive current.
What type of device is this?