

# Scratchwork: Divergences

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It's time to get serious. I can nearly put it together myself.

How do I review this proof without it degenerating into some kind of recitation of facts? One of my critiques of analytic number theory is that... it doesn't look like number theory. If I spend all this effort to prove the Prime Number Theorem... I already believed it was true!

I started to look for arguments where the connection to prime factorization or to Geometry or Probability or any other branch of Math.<sup>1</sup> Talking to professors, I'm pretty much out of luck. They are satisfied with the current arguments. They are professionals, I'm not.

Try to imagine if Hollywood or a Hip-Hop label adopted the garbled narrative style of a Math Textbook. To me, Mathematics has been a giant bait-and-switch. They sold me one result, I got completely another.

I'm trying not to do that to you.

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<sup>1</sup>If I express someone of my aggravation, and provide a partial demonstration / answer, that could be new.

## References

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- (4) Simon Rubinstein-Salzedo **Could Euler have conjectured the prime number theorem?** [arXiv:1701.04718](https://arxiv.org/abs/1701.04718)
- (5) Andrew Granville, Adam J Harper, K. Soundararajan **A more intuitive proof of a sharp version of Halász's theorem** [arXiv:1706.03755](https://arxiv.org/abs/1706.03755)
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- (8) David Sauzin **Introduction to 1-summability and resurgence** [arXiv:1405.0356](https://arxiv.org/abs/1405.0356)
- (9) Don Zagier **On Newman's Short Proof of the Prime Number Theorem** <http://people.mpim-bonn.mpg.de/zagier/files/doi/10.2307/2975232/fulltext.pdf>