

# Scratchwork: Box-Counting

In this note of [Okounkov-Reshetikhin-Vafa](https://arxiv.org/abs/hep-th/0309208) they show how to  $q$ -count plane partitions by using vertex operators:

$$Z = \exp \left[ \frac{\chi}{2} \sum_g g_s^{2g-2} \int_{\overline{\mathcal{M}}_g} c_{g-1}^3(\mathcal{H}) \right] = \left[ \frac{1}{(1-q^n)^n} \right]^{\frac{\chi}{2}}$$

here  $c_{g-1}$  is the Chern class of the Hodge bundle of the moduli space of curves of genus  $g$ .

## References

[1] **The Stacks Project** <https://stacks.math.columbia.edu/tag/0DMJ>

## References

[1] Anton Deitmar **Automorphic Forms** (Universitext) Springer, 2011.

[2] Klaus Roth, Hein Halberstam **Sequences** OUP, 1966. Springer 1983 / 2012.

[3] H. Montgomery, R. Vaughan **Multiplicative Number Theory** Cambridge University Press, 2006.

[4] Goro Shimura  
**Elementary Dirichlet Series and Modular Forms** Springer, 2007.  
**Modular Forms, Basics and Beyond** Springer, 2012.