

# Programming of robotic arm with computer vision based control

21. April 2022

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## Introduction

## **Kuka iiwa lbr 14 mechanical setup**

## **Kuka iiwa lbr 14 software setup**

## Custom robotic arm mechanical design

### CAD

The CAD model can be found on github <sup>1</sup>. This folder includes:

- The original CATIA V5 assembly
- The assembly in STEP format
- An overview drawing of the robot arm
- A complete parts list with assembly structure item STLs for 3D printing

The parts list <sup>2</sup> ( see table 1) includes part numbers referencing the CAD parts, their Quantities and a comment on manufacturing or ISO numbers.

### Iterations

The robotic arm went through several iterations, which have not been fully documented. For fun, here are some pictures of legacy versions. The current one is not included, because it is fully documented on gihub.



Figure 1: Evolution of the robot arm

### Force Calculations

#### Workspace and strength capabilities

Figure 2 shows a 90° cutout of the current hardware configuration of the workspace of the robot. (This means the first link is still the old one with  $a_3 = 96$  mm). Because of the joint limitations <sup>3</sup>, the robot cant reach close to its base, thus highly limiting the workspace.

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<sup>1</sup><https://github.com/MonsisGit/MyRobot/tree/master/CAD>

<sup>2</sup><https://github.com/MonsisGit/MyRobot/blob/master/CAD/partslist.pdf>

<sup>3</sup>In matlab, joint limits are currently set to [-130, 130; -180, 0; -100, 100; -100, 100];

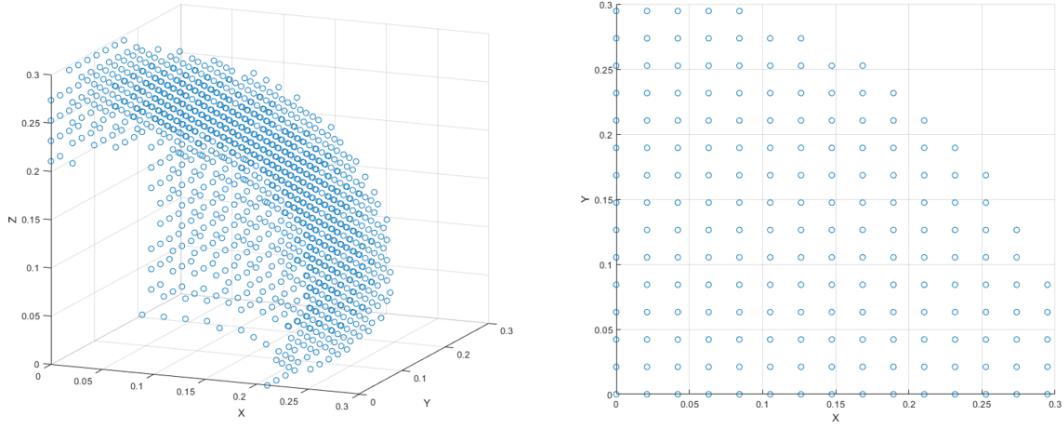


Figure 2: Cut out of the robots workspace (current hardware config)

In figure 3, the same workspace can be seen using the D.H. parameters from the theoretical configuration shown in CAD. Due to time constraints, this was not implemented in hardware. An increase in reach can be seen.

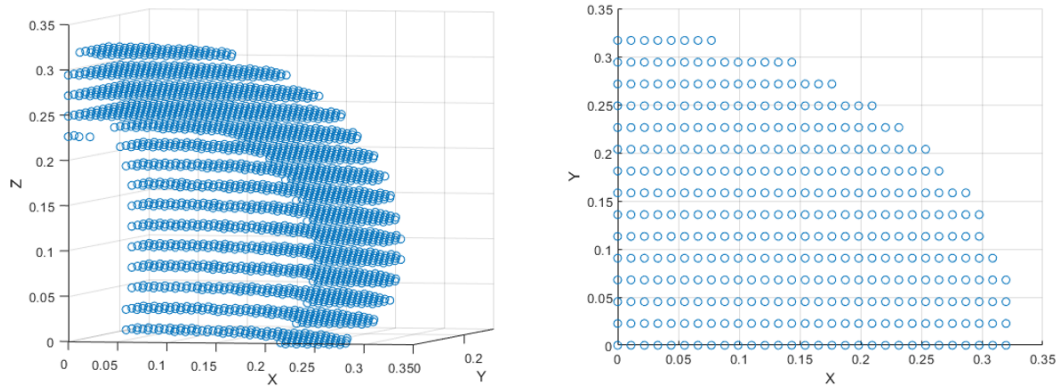


Figure 3: Cut out of the robots workspace

Due to these hardware constraints, the robots reachable space is quite limited and inverse kinematics tend to fail often for arbitrary values. The robots strength is determined using the stall torque of the second motor and the robot arms length at full extension. Here, dynamic forces and the robots own weight are neglected.

$$\begin{aligned}
 L_{arm} &= 0.3821m \\
 Torque_{stall} &= 1.5Nm \\
 Force_{max} &= \frac{1.5Nm}{0.3821m} = 3.9257
 \end{aligned} \tag{1}$$

This results in a lift capability of 0.4 kg at maximum extension.

## Dynamixel AX-12A Motors

In the Robot arm, four identical Dynamixel AX-12A motors are use. Relevent specifications of the motors are:

Input Voltage (min,max) [V]	9-12
Stall Torque [Nm]	1.5
No Load Speed [rpm]	59
Resolution [deg/pulse]	0.2930
Weight [g]	55
Feedback	Position, Temperature, Load, Input Voltage
Dimensions (W,H,D) [mm]	32 X 50 X 40
Gear Ratio	22:31:00

The technical drawings in Figures 10, 11, 12 show relevant details needed for the modeling of the links and base in combination of the motors. More extensive details can be found on the manufacturers website.

Robotis provides the Dynamixel SDK 4 to control the motors using various programming languages.

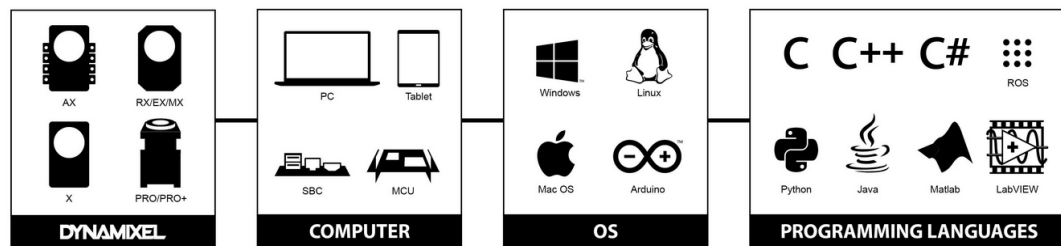


Figure 4: Dynamixel SDK [dynamixel'sdk]



## Custom robotic arm theory

For effective usage of the robot arm, the Denavit Hartenberg (D.H.) parameters need to be defined to figure out forward and inverse kinematics. The D.H. parameters are defined using following coordinate systems. The base is drawn in black. Joints are numbered 1-4. The base corresponds to the black coordinate system.

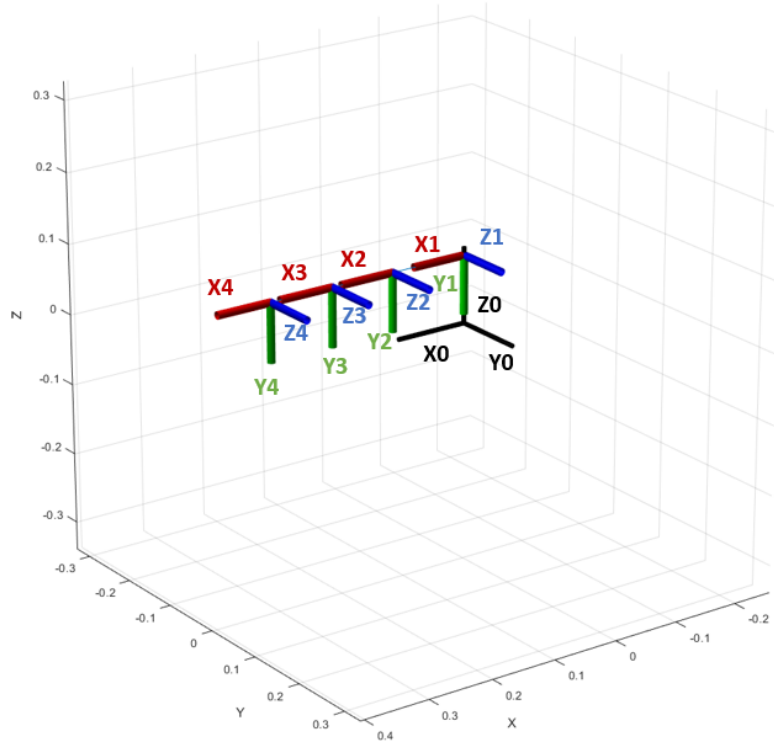


Figure 5: Configuration of the robot in home position

This results in following D.H. parameters:

$$D.H. = \begin{bmatrix} 0 & -\pi/2 & 0.0955 & 0 \\ 0.116 & 0 & 0 & 0 \\ 0.096 & 0 & 0 & 0 \\ 0.09611 & 0 & 0 & 0 \end{bmatrix} \quad (2)$$

In matlab, the D.H. parameters are defined as:

```
% Denavit Hartenberg Parameters for Robot (a (link length),  
% alpha (link twist), d (link offset), theta(joint angle))  
dh = [0,-pi/2,0.0955,0;  
      0.116,0,0,0;  
      0.096,0,0,0;  
      0.09611,0,0,0];
```

Remark:  $a_3$  not being the same then  $a_2$  is due to the current hardware configuration realized while writing this report. In the CAD model,  $a_3$  is the same then  $a_2$ .

## Forward Kinematics

Forward kinematics using the D.H. convention are calculated using following equations:

$$A_i = \text{Rot}_{z,\theta_i} \text{Trans}_{z,d_i} \text{Trans}_{x,a_i} \text{Rot}_{x,\alpha_i}$$

$$A_i = \begin{bmatrix} c_{\theta_i} & -s_{\theta_i}c_{\alpha_i} & s_{\theta_i}s_{\alpha_i} & a_i c_{\theta_i} \\ s_{\theta_i} & c_{\theta_i}c_{\alpha_i} & -c_{\theta_i}s_{\alpha_i} & a_i s_{\theta_i} \\ 0 & s_{\alpha_i} & c_{\alpha_i} & d_i \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (3)$$

$$A_{14} = A_1 * A_2 * A_3 * A_4 \quad (4)$$

where:

$\theta_i$  : joint angle  
 $d_i$  : link offset  
 $a_i$  : link length  
 $\alpha_i$  : link twist

Forward kinematics are calculated in matlab using following code:

```
function ee_cartesian_coords = forward(self, j_a)

%forward function for the MyRobot Class.
%   Calculates forward transformation for all joint positions
%   and end effector coordinates
%
%Inputs:
%   j_a : a vector of four joint angles in [rad]
%Outputs:
%   ee_cartesian_coords : returns cartesian coordinates of end
%   effector in the base coordinate system in [m]

self.forward_transform = [cosd(j_a(1)) -sind(j_a(1))*cos(self.dh(1,2)) sind(j_a(1))*sin(self.dh(1,2))
    sind(j_a(1)) cosd(j_a(1))*cos(self.dh(1,2)) -cosd(j_a(1))*sin(self.dh(1,2)) self.dh(1,1)*sin
    0 sin(self.dh(1,2)) cos(self.dh(1,2)) self.dh(1,3);
    0 0 0 1];

self.joint_pos(:,1) = self.forward_transform * [0 0 0 1]' ;
self.joint_pos(:,1) = self.joint_pos(:,1) / self.joint_pos(4,1);

for i=2:length(j_a)
    self.forward_transform = self.forward_transform * [cosd(j_a(i)) -sind(j_a(i))*cos(self.dh(i,2)) sind(j_a(i))*sin(self.dh(i,2)) self.dh(i,1)*sin
        sind(j_a(i)) cosd(j_a(i))*cos(self.dh(i,2)) -cosd(j_a(i))*sin(self.dh(i,2)) self.dh(i,1)*sin
        0 sin(self.dh(i,2)) cos(self.dh(i,2)) self.dh(i,3);
        0 0 0 1];
    self.joint_pos(:,i) = self.forward_transform * [0 0 0 1]' ;
    self.joint_pos(:,i) = self.joint_pos(:,i) / self.joint_pos(4,i);
```

```
end

ee_cartesian_coords = self.joint_pos(:,4);
end
```

For example, the forward transformation for the home position (joint angles all zero degree) results in:

$$f_{transform} = \begin{bmatrix} 1.0000 & 0 & 0 & 0.3081 \\ 0 & 0.0000 & 1.0000 & 0 \\ 0 & -1.0000 & 0.0000 & 0.0955 \\ 0 & 0 & 0 & 1.0000 \end{bmatrix} \quad (5)$$

with joint positions (colored coordinate systems 1-4 in figure 5) :

$$j_{position} = \begin{bmatrix} 0 & 0.1160 & 0.2120 & 0.3081 \\ 0 & 0 & 0 & 0 \\ 0.0955 & 0.0955 & 0.0955 & 0.0955 \\ 1.0000 & 1.0000 & 1.0000 & 1.0000 \end{bmatrix} \quad (6)$$

For example, we can see that the end-effector is in position x: 308,1mm, y: 0mm, z: 0.0995 mm.

## Inverse Kinematics

The inverse kinematics can be numerically solved using matlabs robot toolbox and the following script:

```
if self.rbt == 0
    self.create_rbt();
end

j_a = zeros(4,1);
initialguess = self.rbt.homeConfiguration;
tform = [ 1 0 0 x;
          0 0 1 y;
          0 -1 0 z;
          0 0 0 1];

[configSoln,solnInfo] = self.ik('link4',tform,self.ik_weights,initialguess);
if strcmp(solnInfo.Status,'success')
    for i=1:4
        j_a(i) = configSoln(i).JointPosition*180/pi;
    end
elseif strcmp(solnInfo.Status,'best available')
    fprintf("Status: '%s', using Angles:\n", solnInfo.Status);
    for i=1:4
        j_a(i) = configSoln(i).JointPosition*180/pi;
        fprintf("%f°  ",configSoln(i).JointPosition*180/pi);
    end
else
    fprintf("Unsuccesfull IK, with status: '%s'", solnInfo.Status);
end

function create_rbt(self)
    self.rbt = rigidBodyTree;
    bodies = cell(4,1);
    joints = cell(4,1);
    for i = 1:4
        bodies{i} = rigidBody(['link' num2str(i)]);
        joints{i} = rigidBodyJoint(['jnt' num2str(i)],"revolute");
        joints{i}.PositionLimits = [self.joint_limits(i,1)*pi/180,self.joint_limits(i,2)*pi/180];
        setFixedTransform(joints{i},self.dh(i,:), "dh");
        self.ik = inverseKinematics('RigidBodyTree',self.rbt);
    end
end
```

Since this produces inconsistent results and is a slower, less transparent approach, an analytical approach was used, using geometrical interpretations of the robot arms movements. For joint 1, figure 6 shows the geometric interpretation of the robot arms position. The equation for  $\theta_1$  can be derived:

$$\theta_1 = \arctan\left(\frac{x_{current}}{y_{current}}\right) \quad (7)$$

for  $(x_{current}, y_{current}) \neq (0, 0)$  which is implemented in matlab with:

```
j1 = atan2(y,x);
```

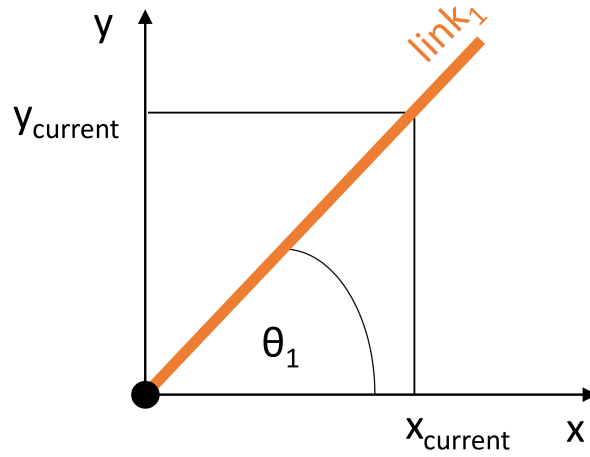


Figure 6: Geometric interpretation for joint 1

To figure out  $\theta_2$  and  $\theta_3$ , figure 7 shows the geometric interpretation. Following equations can be used to derive the joint angles:

$$L_{arm} = \sqrt{x_{current}^2 + y_{current}^2} \quad (8)$$

$$s_z = z_{current} - d_1 \quad (9)$$

from the law of cosines:

$$\cos \theta_3 = \frac{L_{arm} + s_z - a_2^2 - a_3^2}{2 * a_2 * a_3} \quad (10)$$

$$\theta_3 = \arccos \frac{L_{arm} + s_z - a_2^2 - a_3^2}{2 * a_2 * a_3} \quad (11)$$

We can find two solutions for elbow-up/ elbow-down:

$$\theta_3 = \text{Atan2} \left( \cos \theta_3, \pm \sqrt{1 - \cos^2 \theta_3} \right) \quad (12)$$

Now  $\theta_2$  can be found with:

$$\theta_2 = \text{Atan2}(L_{arm}, s_z) - \text{Atan2}(a_2 + a_3 * \cos \theta_3, a_3 \sin \theta_3) \quad (13)$$

which is implemented in matlab with:

```
j3 = acos( ((sqrt(x^2+y^2)-self.dh(4,1)*cos(pitch))^2 + (self.dh(1,3)-z)^2 - self.dh(2,1)^2 ...
- self.dh(3,1)^2) / (2*self.dh(2,1)*self.dh(3,1)) );
```

```
j2 = -atan2(z-self.dh(1,3)-self.dh(4,1)*sin(pitch),sqrt(x^2+y^2)-self.dh(4,1)*cos(pitch)) ...
- atan2(self.dh(3,1)+self.dh(2,1)*cos(j3),self.dh(2,1)*sin(j3)) + (pi/2-j3);
```

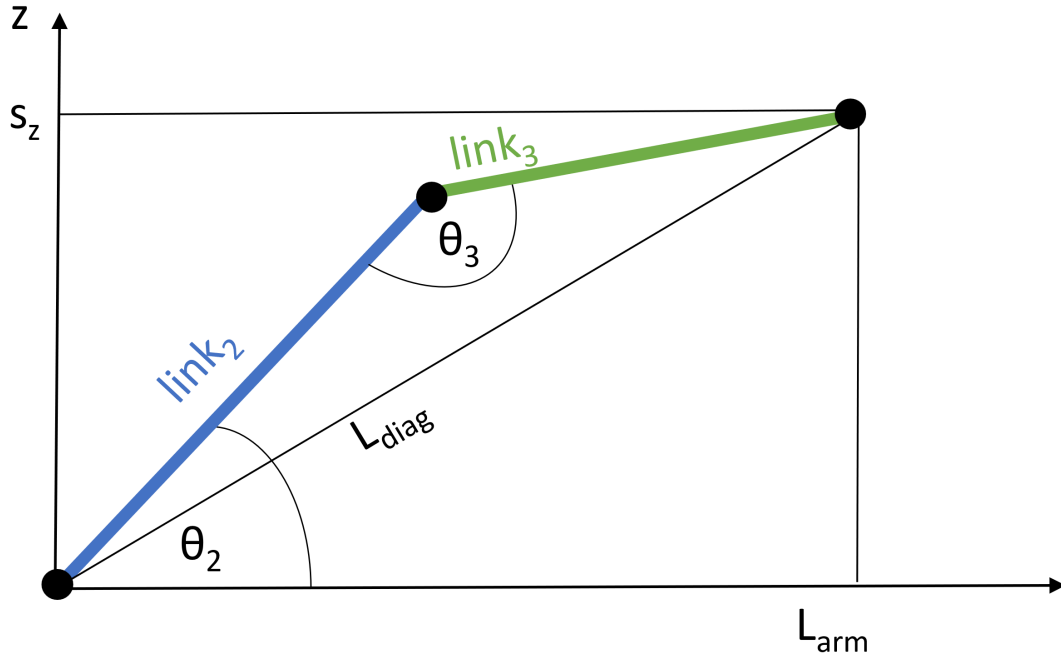


Figure 7: Geometric interpretation for joint 2 and joint 3

To figure out  $\theta_4$ , we need to take the pitch of the end-effector into consideration, which is its angle to the horizontal plane, as can be seen in figure 8.  $\theta_4$  is calculated in dependence of the pitch angle, which is a user input:

$$\theta_4 = \text{pitch} - \theta_2 - \theta_3 \quad (14)$$

which is implemented in matlab with:

```
j4 = pitch - j2 - j3;
```

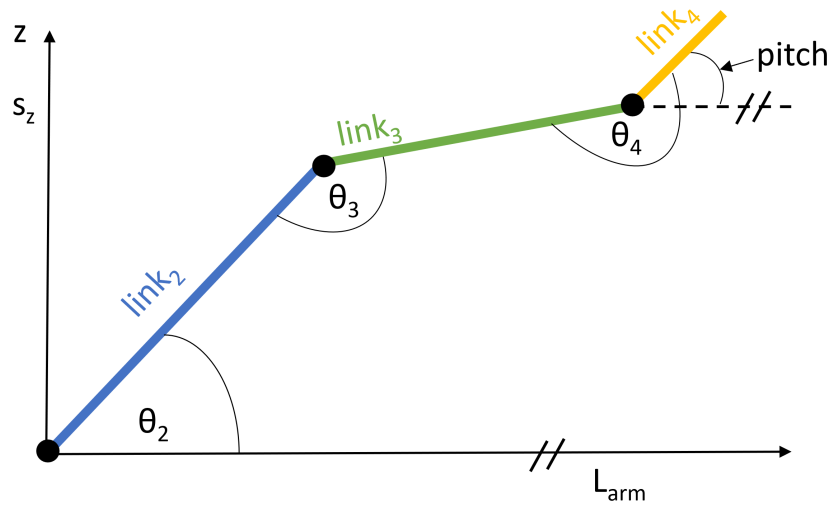


Figure 8: Geometric interpretation for joint 4

A check if the joint angles contain complex numbers can catch impossible configurations of the robot arm:

```
assert(isreal(j_a),"Configuration Impossible");
```

## Custom robotic arm software design

The MyRobot<sup>4</sup> class in matlab was created to control the robots functionalities and also to track the robots current parameters like joint angles, joint positions, speed, torque etc. For setup and documentation, see the github<sup>5</sup>. More detailed documentation for the individual methods can be found by typing into the matlab command window

```
doc MyRobot
```

which will open the matlab html documentation. Example usage of the class could look like:

```
% Initialize the robot, it should move to home configuration
% (0°,0°,0°,0°)
robot = MyRobot();
%
% Set movements speed of each individual joint, update interal joint
% speeds for later commands
robot.set_speed([0.1,0.1,0.1,0.2],true);
%
% Set all motors to maximum torque
robot.set_torque_limit([1,1,1,1]);
%
% Draw the current configuration of the robot
robot.draw_robot();
%
% Move the robots joints
robot.move_j(20,-90,0,50);
%
% Actuate the gripper. If the gripper is currently closed, it will open
robot.actuate_gripper();
%
% Get the robots current joint positions
current_joint_positions = robot.joint_pos
%
% Disable all motors. This is necessary to free up the com port. If you
% forgot to do this and clear the robot object, it will fail at
% reinitialization. To fix this unplug the robots USB cable and clear
% the workspace
robot.disable_motors();
```

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<sup>4</sup><https://github.com/MonsisGit/MyRobot/blob/master/matlab/MyRobot.m>

<sup>5</sup><https://github.com/MonsisGit/MyRobot/blob/master/README.md>Basic-Usage-of-MyRobot



A graphical user interface has been created to ease the interaction with the robot. It can be installed using the `mlappinstall`<sup>6</sup> file on github or simply run using the `mlapp`<sup>7</sup> file. The interface is shown in figure 9 and further detailed on github<sup>8</sup>. The GUI accesses the internal state of the robot, thus updating its status like joint angles or end-effector position with every robot interaction. Buttons like *Open Gripper* change to *Close Gripper* once the gripper is open or *Show Configuration* to *Hide Configuration*.

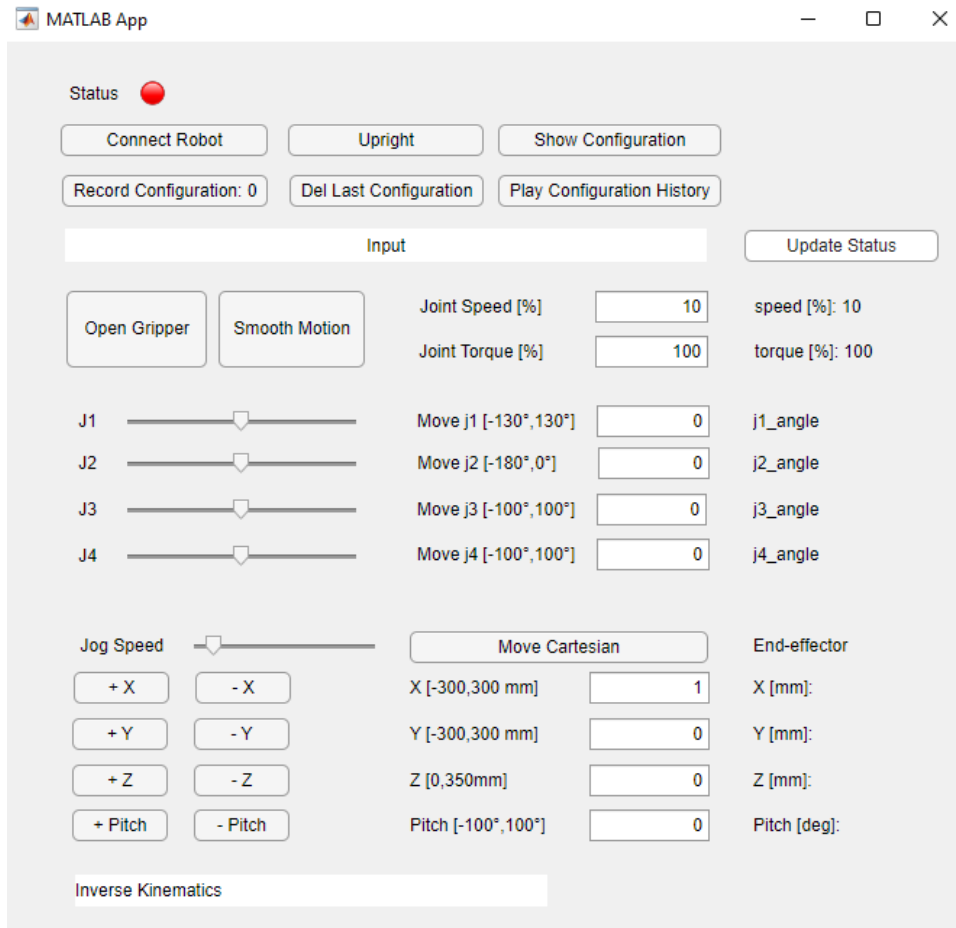


Figure 9: GUI for the MyRobot class

<sup>6</sup>[https://github.com/MonsisGit/MyRobot/blob/master/matlab/MyRobot\\_studio.mlappinstall](https://github.com/MonsisGit/MyRobot/blob/master/matlab/MyRobot_studio.mlappinstall)

<sup>7</sup>[https://github.com/MonsisGit/MyRobot/blob/master/matlab/MyRobot\\_studio.mlapp](https://github.com/MonsisGit/MyRobot/blob/master/matlab/MyRobot_studio.mlapp)

<sup>8</sup><https://github.com/MonsisGit/MyRobot/blob/master/README.mdUsing-the-GUI>

## Custom robotic arm solution visual servo

## **Evaluation of commercial and custom robotic arm solution**

## Possible improvements custom robotic arm

### Software

- Improve the calculation of the inverse kinematics by catching certain cases which cause non-valid results or singularities.
- In case of elbow-up/ elbow-down solutions in the inverse kinematics, finding the angle with the least residual rotation compared to the current position.
- Solve the blocked port problem when robot is not disconnected properly.
- Implement manipulator jacobian and trajectory planning.

### Hardware

- Install a bearing in the robots base above the first motor.
- Improve gripper by mechanically linking the two fingers, for example with gears. The current gripper has trouble with smooth, simultaneous closing and opening. Once the tensions on the bowden cable is alleviated by closing one side of the gripper, the other side sometimes only closes partially.
- Select motors based on torque requirements, thus saving weight, money and space. Consider using two motors to actuate the second joint.
- Select and install robot on a stable base.
- Further iterations on the robot arm could include moving the motors for joint 3 and joint 4 one link length down to joint 2 and joint 3. These motors would work using pulleys or links which reach through the link to actuate the actual joint, thus decreasing the leverage on the motors weight. A good showcase of this is the ABB irb 460 robot<sup>9</sup>.

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<sup>9</sup><https://new.abb.com/products/robotics/industrial-robots/irb-460>

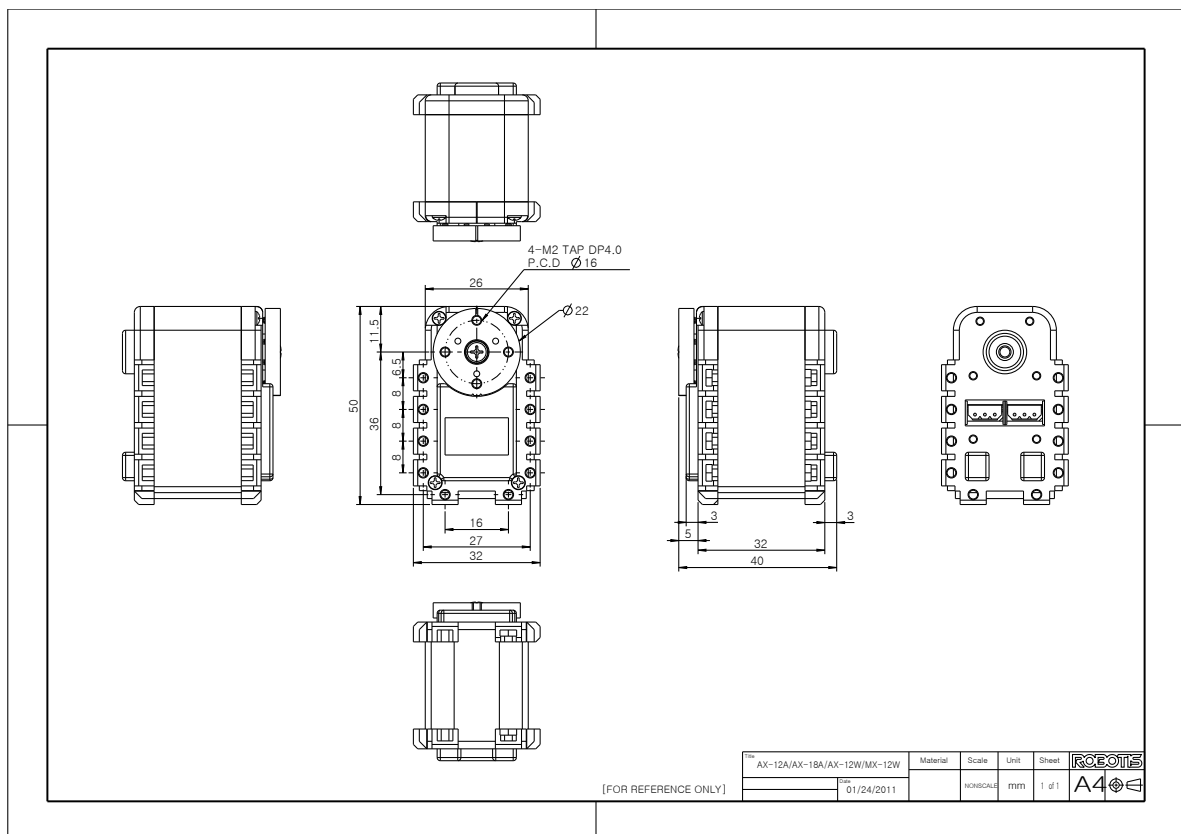


Figure 10: Dynamixel AX-12A motor [ax-12a]

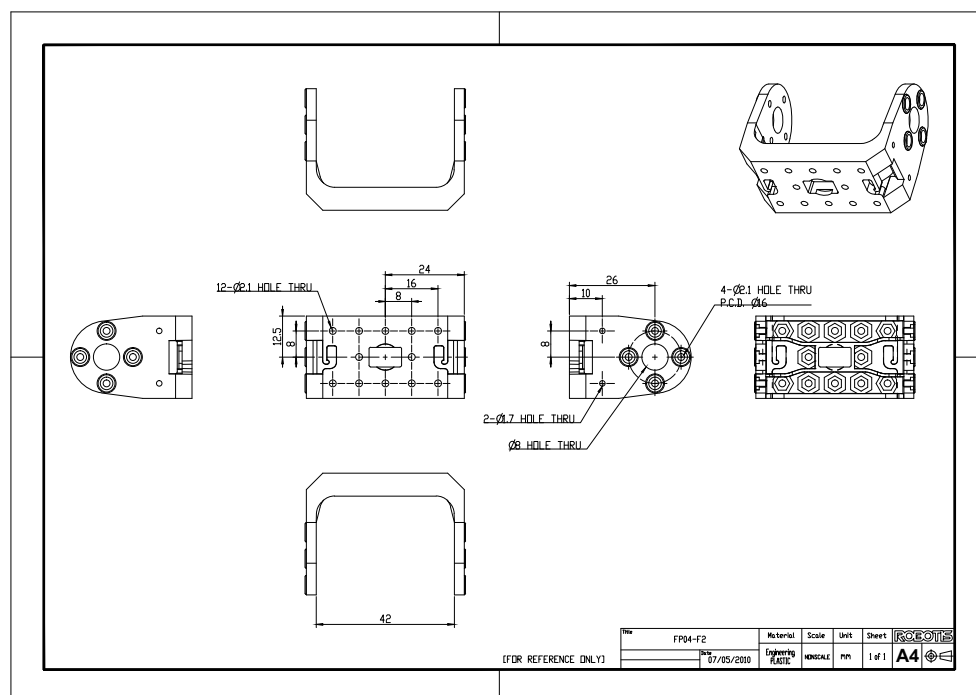


Figure 11: Flange 1 (FP04-F2) [**robotis'f2**]

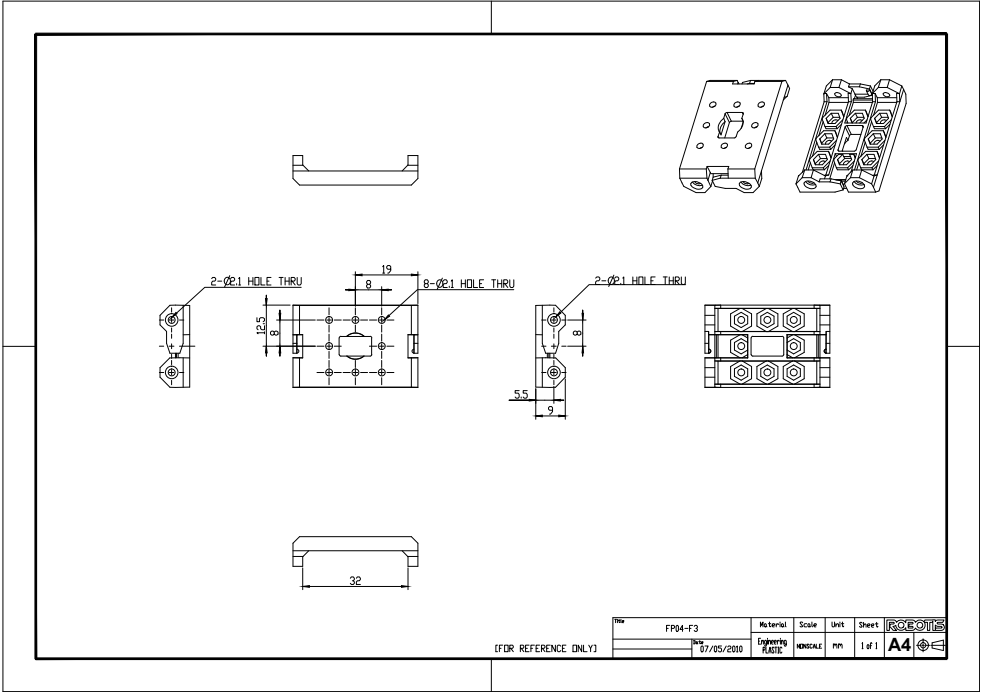


Figure 12: Flange 2 (FP04-F3) [robotis'f3]

Table 1: Parts List

Part Number			Quantity	Name	Comment
0			1	Robot Arm	
	010		1	Base Assembly	
		011	1	Base Wall	FDM 3D-Print
		012	1	Base Cover	FDM 3D-Print
		013	1	Base Bracket	FDM 3D-Print
		014	1	Bowden Pulley	SLA 3D-Print
		015	6	ISO 10642 M4x16	Countersunk
		016	12	ISO 7046 M2x6	Robotis Part
		017	2	ISO 4762 M3x16	
		018	2	ISO 4032 NUT M3	
		019	8	ISO 4032 NUT M2	Robotis Part
		040	2	Dynamixel AX-12A	Robotis Part
		070	1	Zip Tie	
		071	2	Robot Cable-3P 200mm	Robotis Part
		072	1	Usb2dynamixel	Robotis Part
		073	1	Power Supply 12V, 2A	
		074	1	USB Extension Cable	
		075	5ml	Loctite	Apply to 016,024
	020		1	Bottom Link Assembly	
		021	1	Link	SLA 3D-Print
		022	1	Washer	SLA 3D-Print
		023	1	FP04-F3	Robotis Part
		024	1	ISO 4762 M3x12	Robotis Part
		016	16	ISO 7046 M2x6	Robotis Part
		071	2	Robot Cable-3P 200mm	Robotis Part
		075	5ml	Loctite	Apply to 016,024
		040	1	Dynamixel AX-12A	Robotis Part
	030		1	Top Link Assembly	
		021	1	Link	SLA 3D-Print
		022	1	Washer	SLA 3D-Print
		040	2	Dynamixel AX-12A	Robotis Part
		016	8	ISO 7046 M2x6	
		024	1	ISO 4762 M3x12	
		071	1	Robot Cable-3P 200mm	Robotis Part
		075	5ml	Loctite	Apply to 016,024
	050		1	Gripper Assembly	
		051	1	Bowden Tube	length ca. 500m, d:2,4mm
		052	1	Gripper Base Plate	SLA 3D-Print
		053	1	Bowden Tube Clamp	SLA 3D-Print
		054	2	Gripper Fingers	SLA 3D-Print
		055	2	Gripper Tips	SLA 3D-Print
		056	1	Bowden Roller	SLA 3D-Print
		057	1	FP04-F2	Robotis Part
		058	1	AX123_Bushing-F (BPF-BU)	Robotis Part
		059	2	ISO 4762 M3x20	
		060	1	ISO 10642 M3x25	
		061	2	ISO 10642 M3x30	
		062	7	NUT M3 Thread Locking	
		063	1	Bowden Cable	length ca. 500m, outside d:2mm
		064	2	Rubber Bands	length ca. 200mm
		065	3	Cable Crimp	endstop for bowden cable