## Compiler Construction 2025

## — Exercise 0 —

## General Remarks

- Exercises are *optional*, i.e., not required for admission to exams. However, corrections to students' solutions are provided as annotations to the submissions.
- Please use the corresponding task in the Moodle room to submit your solution. Paper submissions are not accepted.
- Please hand in your solutions in *groups of four* and hand in only one solution per group. You can use the forum in this Moodle room to find group members.

Exercise 1 (0 Points)

Which of the following statements hold?

- (a) Deterministic finite automata (DFA) are strictly less expressive than regular expressions.
- (b) Non-deterministic finite automata (NFA) are strictly more expressive than DFA.
- (c) The regular languages are closed under:
  - (i) union,
  - (ii) intersection,
  - (iii) complement,
  - (iv) concatenation,
  - (v) Kleene closure.
- (d) Context Free Languages (CFL) are closed under:
  - (i) union,
  - (ii) intersection,
  - (iii) complement,
  - (iv) concatenation,
  - (v) Kleene closure.
- (e) DCFL is the set of context free languages that are accepted by deterministic push down automata. Is DCFL = CFL?

Exercise 2 (0 Points)

(a) Describe the language of the following regular expression in words:

$$r = (0+1)^*0(0+1)^*0(0+1)^*.$$

- (b) Construct the regular expression for...
  - (i) the set of all strings with at most one pair of consecutive 0's and at most one pair of consecutive 1's,
  - (ii) the set of all strings with equal number of 0's and 1's such that no prefix has two more 0's than 1's nor two more 1's than 0's.

(c) Construct a context free grammar (CFG) for a set of strings of  $\{(,)\}^*$  such that every string of the set has equal number of left and right parenthesis, and every prefix has at least as many left parenthesis as right parenthesis.

Exercise 3 (0 Points)

- (a) Let r and s be regular expressions. Consider the set X such that  $X = r \cdot X + s$ . Under the assumption that the language of r does not contain  $\varepsilon$  (i.e.,  $\varepsilon \notin L(r)$ ), find X.
- (b) (i) Show that the language  $L = \{0^{i^2} \mid i \in \mathbb{N}\}$  is not regular.
  - (ii) Show that the language  $L = \{a^i b^i c^i \mid i \in \mathbb{N}\}$  is not a CFL.