Application 6: Regression Model for Concentration

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This example illustrates how to use the regression model to estimate concentration rather than load. Concentrations can be estimated for daily or shorter time frames directly from the load regression output. Time-weighted mean concentrations for longer time periods can be computed using the method described for application 6 in Runkel and others (2004), or simply computing the mean daily if confidence intervals are not needed. Flow-weighted mean concentrations can be computed by estimating the flux for each period of time, dividing by the mean flow and dividing by the correct conversion factor; the confidence interval can be computed in the same manner.

This example uses the second revised model from example application 5. The user is directed to that example vignette for details on constructing that model. Part 2 illustrates how to estimate time-weighted mean (TWM) monthly concentrations. Part 3 illustrates how to estimate flow-weighted mean (FWM) concentrations.

- > # Load the rloadest package and the data
- > library(rloadest)
- > data(app5.calib)
- > head(app5.calib)

	DATES	TIMES	FLOW	SC	Alkalinity
1	1995-02-28	1231	10.0	1425.0	248
2	1995-03-24	1301	11.3	1010.0	205
3	1995-03-28	0801	190.0	519.0	78
4	1995-04-12	0931	13.1	784.0	204
5	1995-04-24	1301	22.4	1750.0	231
6	1995-05-08	1301	2700.0	98.9	27

1 Predict Daily Concentrations for 1999

The concentration model is computed using loadReg. The default print does not print the concentration model, but it can be printed by setting load.only to FALSE.

```
> # Create the and print load model with concentration.
> app6.lr <- loadReg(Alkalinity ~ quadratic(log(FLOW)) + log(SC) +
                        fourier(DATES),
                      data = app5.calib, subset=DATES < "1998-01-01",
                      flow = "FLOW", dates = "DATES", conc.units="mg/L",
                      station="Arkansas River at Halstead, Ks.")
> print(app6.lr, load.only=FALSE)
*** Load Estimation ***
Constituent: Alkalinity
          Number of Observations: 74
Number of Uncensored Observations: 74
          Center of Decimal Time: 1996.566
                 Center of ln(Q): 5.1571
                Period of record: 1995-02-28 to 1997-12-29
Selected Load Model:
_____
Alkalinity ~ quadratic(log(FLOW)) + log(SC) + fourier(DATES)
Model coefficients:
                              Estimate Std. Error z-score p-value
(Intercept)
                               5.95099 0.31973 18.612 0e+00
quadratic(log(FLOW))(5.12598)1 0.91116
                                         0.01875 48.605
                                                           0e+00
quadratic(log(FLOW))(5.12598)2 0.02903
                                         0.00516 5.626
                                                           0e+00
                                         0.04857 15.111
log(SC)
                              0.73392
                                                           0e+00
fourier(DATES)sin(k=1)
                             -0.10864
                                         0.02358 -4.608 0e+00
fourier(DATES)cos(k=1)
                              -0.09143
                                         0.02670 -3.425
                                                           6e-04
AMLE Regression Statistics
Residual variance: 0.01496
R-squared: 99.06 percent
G-squared: 345.6 on 5 degrees of freedom
P-value: <0.0001
Prob. Plot Corr. Coeff. (PPCC):
 r = 0.9789
 p-value = 0.0172
```

Serial Correlation of Residuals: 0.1002

```
Variance Inflation Factors:
quadratic(log(FLOW))(5.12598)1 quadratic(log(FLOW))(5.12598)2
                   5.855930
                                               1.180957
                    log(SC)
                                  fourier(DATES)sin(k=1)
                   7.341722
                                               1.284316
       fourier(DATES)cos(k=1)
                   1.440525
Comparison of Observed and Estimated Loads
_____
     Summary Stats: Loads in kg/d
_____
    Min 25% 50% 75% 90% 95% Max
Est 5540 10300 16400 66400 169000 283000 865000
Obs 5290 10100 16900 58600 176000 281000 947000
Bias Diagnostics
Bp: -2.08 percent
PLR: 0.9792
 E: 0.9867
Selected Concentration Model:
_____
Alkalinity ~ quadratic(log(FLOW)) + log(SC) + fourier(DATES)
Model coefficients:
                           Estimate Std. Error z-score p-value
(Intercept)
                           -0.06969 0.31973 -0.218 0.8202
quadratic(log(FLOW))(5.12598)1 -0.08884 0.01875 -4.739 0.0000
quadratic(log(FLOW))(5.12598)2 0.02903 0.00516 5.626 0.0000
                           0.73392 0.04857 15.111 0.0000
log(SC)
fourier(DATES)sin(k=1)
                          -0.10864 0.02358 -4.608 0.0000
fourier(DATES)cos(k=1)
                           -0.09143 0.02670 -3.425 0.0006
AMLE Regression Statistics
Residual variance: 0.01496
R-squared: 97.17 percent
G-squared: 263.9 on 5 degrees of freedom
P-value: <0.0001
Prob. Plot Corr. Coeff. (PPCC):
```

r = 0.9789

p-value = 0.0172

Comparison of Observed and Estimated Concentrations

Summary Stats: Concentrations in mg/L

Min 25% 50% 75% 90% 95% Max Est 25.8 93.2 221 273 290 295 300 Obs 27.0 98.0 228 268 284 298 310

Bias Diagnostics

Bp: 0.328 percent

PCR: 1.003 E: 0.9564

The rloadest package contains the function predConc that will estimate concentrations for daily or shorter time periods, depending on the time step. Note that the daily estimation data set, app5.est, has 7 missing days and so has only 358 observations instead of 365 for 1999.

- > # Get the estimation data
- > data(app5.est)
- > # Predict daily concentrations
- > app6.cd <- predConc(app6.lr, app5.est, by="day")</pre>
- > head(app6.cd)

	Date	Flow	Conc	Std.Err	SEP	L95	U95
1	1999-01-01	44	230.4691	8.075796	29.42066	178.8196	178.8196
2	1999-01-02	40	238.0191	8.203423	30.34716	184.7349	184.7349
3	1999-01-03	41	232.3866	7.982030	29.62166	180.3745	180.3745
4	1999-01-04	38	238.2327	8.071336	30.33699	184.9580	184.9580
5	1999-01-05	41	235.7455	8.146778	30.06315	182.9613	182.9613
6	1999-01-06	38	235.2900	7.922827	29.94932	182.6931	182.6931

2 Part 2 Predict Monthly Time-weighted Mean Concentrations for 1999

The estimation of TWM concentrations requires the user to "trick" the regression model by substituting a constant synthetic value for the flow column that actually estimates concentrations in stead of load when using the predLoad function. The details of the development of the method are described in Runkel and others (2004). This example application only describes the implementation using rloadest functions.

The first step is to create a synthetic flow column in both the calibration and the estimation data sets. The value of the data is the conversion factor from load to concentration, or the reciprocal of the conversion factor from concentration to loads that can be gotten by using the c2load function.

```
> # Create synthetic flow values
> app6.calib <- transform(app5.calib, Sflow=1/c2load(1, 1,
     conc.units="mg/L"))
> app6.est <- transform(app5.est, Sflow=1/c2load(1, 1,
     conc.units="mg/L"))
> head(app6.calib)
       DATES TIMES
                     FLOW
                              SC Alkalinity
                                                Sflow
1 1995-02-28 1231
                     10.0 1425.0
                                        248 0.4087324
2 1995-03-24 1301
                     11.3 1010.0
                                        205 0.4087324
3 1995-03-28 0801 190.0 519.0
                                         78 0.4087324
4 1995-04-12 0931
                                        204 0.4087324
                     13.1 784.0
5 1995-04-24 1301
                     22.4 1750.0
                                        231 0.4087324
6 1995-05-08 1301 2700.0
                            98.9
                                         27 0.4087324
```

The next step is to construct the calibrated model. This example will use the previously calibrated model, so that diagnostics plots will not be created. The only difference between this model and the previous model is that the flow column is defined as the synthetic flow column. The printed report for this load model should agree with the printed report for the concentration model in the previous section.

Constituent: Alkalinity Number of Observations: 74 Number of Uncensored Observations: 74 Center of Decimal Time: 1996.566 Center of ln(Q): -0.8947 Period of record: 1995-02-28 to 1997-12-29 Selected Load Model: _____ Alkalinity ~ quadratic(log(FLOW)) + log(SC) + fourier(DATES) Model coefficients: Estimate Std. Error z-score p-value -0.06969 0.31973 -0.218 0.8202 (Intercept) quadratic(log(FLOW))(5.12598)1 -0.08884 0.01875 -4.739 0.0000 quadratic(log(FLOW))(5.12598)2 0.02903 0.00516 5.626 0.0000 log(SC) -0.10864 0.02358 -4.608 0.0000 fourier(DATES)sin(k=1) fourier(DATES)cos(k=1) AMLE Regression Statistics Residual variance: 0.01496 R-squared: 97.17 percent G-squared: 263.9 on 5 degrees of freedom P-value: <0.0001 Prob. Plot Corr. Coeff. (PPCC): r = 0.9789p-value = 0.0172 Serial Correlation of Residuals: 0.1002 Variance Inflation Factors: quadratic(log(FLOW))(5.12598)1 quadratic(log(FLOW))(5.12598)2 5.855930 1.180957 log(SC) fourier(DATES)sin(k=1) 7.341722 1.284316 fourier(DATES)cos(k=1) 1.440525

Comparison of Observed and Estimated Loads

Summary Stats: Loads in kg/d

Min 25% 50% 75% 90% 95% Max Est 25.8 93.2 221 273 290 295 300

Obs 27.0 98.0 228 268 284 298 310

Bias Diagnostics

Bp: 0.328 percent

PLR: 1.003 E: 0.9564

The user can now estimate TWM concentrations for periods longer than 1 day. Remember that the estimation dataset has 7 missing days and no estimates for those months will be made.

- > # Predict monthly TWM concentrations using the \textt{predLoad} function.
- > app6.TWM <- predLoad(app6.lrTWM, app6.est, by="month")</pre>
- > # Change the name of the Flux column to Conc
- > names(app6.TWM)[3] <- "Conc"
- > app6.TWM

	Pe	eriod	Ndays	Conc	Std.Err	SEP	L95	U95
1	January	1999	31	213.1878	7.081182	8.529423	196.95746	230.3869
2	February	1999	28	149.5486	5.216405	6.361388	137.46681	162.3985
3	March	1999	31	194.6095	5.790947	7.210804	180.85773	209.1198
4	April	1999	30	107.1358	3.026241	4.009600	99.49121	115.2064
5	May	1999	31	121.6526	3.345660	4.355846	113.33779	130.4103
6	June	1999	29	NA	NA	NA	NA	NA
7	July	1999	28	NA	NA	NA	NA	NA
8	August	1999	31	168.6656	6.141413	7.344922	154.72644	183.5125
9	September	1999	27	NA	NA	NA	NA	NA
10	October	1999	31	211.5238	6.786674	8.240603	195.83063	228.1284
11	November	1999	30	252.3945	8.046272	9.846216	233.64435	272.2351
12	December	1999	31	189.3642	6.175727	7.502260	175.08417	204.4880

A quick check of the mean daily concentrations verifies that computations. Note that there is no protection against incomplete months when the TWM concentrations are computed manually, so values are obtained for June, July and September.

> with(app6.cd, tapply(Conc, month(Date, label=TRUE), mean))

Jan Feb Mar Apr May Jun Jul Aug 213.18784 149.54864 194.60951 107.13581 121.65264 106.54503 85.02916 168.66561 Sep Oct Nov Dec 130.05797 211.52384 252.39450 189.36420

3 Part 3 Predict Monthly Flow-weighted Mean Concentrations for 1999

The estimation of FWM concentrations is a two-step process. The first step is to build the rating-curve model for loads and estimate the flux desired for each period. The second step is to compute the mean flow for each period and divide the flux by the flow and correct to concentration units. The load model for this example (app6.lr) was created in the first part of this vignette.

```
> # Compute the monthly fluxes.
> app6.FWM <- predLoad(app6.lr, app6.est, by="month")</pre>
> # Compute the mean flows
> app6.FWM$Flow <- as.vector(with(app6.est, tapply(FLOW, month(DATES), mean)))
> # Compute the FWM concentration
 app6.FWM <- transform(app6.FWM, FWMC=Flux/Flow/</pre>
                          c2load(1, 1, conc.units="mg/L"))
> app6.FWM
           Period Ndays
                              Flux
                                     Std.Err
                                                   SEP
                                                              L95
                                                                        U95
     January 1999
                         35442.25 1309.7176 2155.2335
                                                        31405.46
                                                                   39850.55
1
                     31
2
    February 1999
                     28
                         63032.12 2511.7167 3783.9322
                                                        55940.53
                                                                   70767.67
3
       March 1999
                     31 25388.38 768.4968 957.4235
                                                        23563.38
                                                                   27315.89
4
       April 1999
                     30 127971.05 4415.6512 6011.0352 116592.86 140150.41
5
         May 1999
                     31 67572.50 1854.0435 2724.5044
                                                        62389.33
6
        June 1999
                     29
                                NA
                                          NA
                                                    NA
                                                               NA
                                                                         NA
                     28
7
        July 1999
                                NA
                                          NA
                                                    NA
                                                               NA
                                                                         NA
8
      August 1999
                     31 100304.10 3710.5034 5197.4230
                                                        90502.12 110870.01
   September 1999
9
                     27
                                NA
                                          NA
                                                    NA
                                                               NA
                                                                         NA
10
     October 1999
                     31
                         12434.02 397.2618
                                              484.1962
                                                        11511.91
                                                                   13409.65
                         15924.63 507.6033 621.6939
11
   November 1999
                     30
                                                        14740.76
                                                                   17177.40
    December 1999
                     31
                         23377.49 805.5262 1009.0498 21461.96
                  FWMC
        Flow
  121.74194 118.99263
1
2
   353.57143 72.86580
3
    53.58065 193.67169
4
   815.46667
             64.14230
5
   327.41935
              84.35380
  787.03448
7
   932.00000
                    NΑ
8
   620.48387
             66.07348
   136.25926
9
   24.29032 209.22673
   25.86667 251.63317
12 57.61290 165.85062
```

For these data, the FWM concentration is less than the TWM concentration. In general, the FWM concentration will less than the TWM concentration when the concentration and flow are negatively correlated.