Application 6: Regression Model for Concentration

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This example illustrates how to use the regression model to estimate
concentration rather than load. Concentrations can be estimated for daily or
shorter time frames directly from the load regression output. Time-weighted
mean concentrations for longer time periods can be computed using the
method described for application 6 in Runkel and others (2004), or simply
computing the mean daily if confidence intervals are not needed.
Flow-weighted mean concentrations can be computed by estimating the flux
for each period of time, dividing by the mean flow and dividing by the correct
conversion factor; the confidence interval can be computed in the same manner.

This example uses the second revised model from example application 5. The
user is directed to that example vignette for details on constructing that
model. Part 2 illustrates how to estimate time-weighted mean (TWM)
monthly concentrations. Part 3 illustrates how to estimate flow-weighted mean
(FWM) concentrations.

```
> # Load the rloadest package and the data
> library(rloadest)
> data(app5.calib)
> head(app5.calib)


        DATES TIMES   FLOW      SC Alkalinity
1 1995-02-28  1231   10.0 1425.0          248
2 1995-03-24  1301   11.3 1010.0          205
3 1995-03-28  0801  190.0  519.0           78
4 1995-04-12  0931   13.1  784.0          204
5 1995-04-24  1301   22.4 1750.0          231
6 1995-05-08  1301 2700.0   98.9           27
```

1 Predict Daily Concentrations for 1999

The concentration model is computed using `loadReg`. The default print does not print the concentration model, but it can be printed by setting `load.only` to `FALSE`.

```
> # Create the and print load model with concentration.
> app6.lr <- loadReg(Alkalinity ~ quadratic(log(FLOW)) + log(SC) +
+                       fourier(DATES),
+                     data = app5.calib, subset=DATES < "1998-01-01",
+                     flow = "FLOW", dates = "DATES", conc.units="mg/L",
+                     station="Arkansas River at Halstead, Ks.")
> print(app6.lr, load.only=FALSE)


*** Load Estimation ***

Station: Arkansas River at Halstead, Ks.
Constituent: Alkalinity

          Number of Observations: 74
Number of Uncensored Observations: 74
          Center of Decimal Time: 1996.566
                 Center of ln(Q): 5.1571
                 Period of record: 1995-02-28 to 1997-12-29


Selected Load Model:
--------------------


Alkalinity ~ quadratic(log(FLOW)) + log(SC) + fourier(DATES)

Model coefficients:
                               Estimate Std. Error z-score p-value
(Intercept)                     5.95099    0.31973  18.612   0e+00
quadratic(log(FLOW))(5.12598)1  0.91116    0.01875  48.605   0e+00
quadratic(log(FLOW))(5.12598)2  0.02903    0.00516   5.626   0e+00
log(SC)                         0.73392    0.04857  15.111   0e+00
fourier(DATES)sin(k=1)         -0.10864    0.02358  -4.608   0e+00
fourier(DATES)cos(k=1)         -0.09143    0.02670  -3.425   6e-04

AMLE Regression Statistics
Residual variance: 0.01496
R-squared: 99.06 percent
G-squared: 345.6 on 5 degrees of freedom
P-value: <0.0001
Prob. Plot Corr. Coeff. (PPCC):
```

```
  r = 0.9789
  p-value = 0.0172
Serial Correlation of Residuals: 0.1002

Variance Inflation Factors:
                                 VIF
quadratic(log(FLOW))(5.12598)1 5.856
quadratic(log(FLOW))(5.12598)2 1.181
log(SC)                        7.342
fourier(DATES)sin(k=1)         1.284
fourier(DATES)cos(k=1)         1.441

Comparison of Observed and Estimated Loads
------------------------------------------
      Summary Stats: Loads in kg/d
----------------------------------------------
     Min    25%    50%    75%     90%     95%     Max
Est 5540 10300 16400 66400 169000 283000 865000
Obs 5290 10100 16900 58600 176000 281000 947000

Bias Diagnostics
----------------
 Bp: -2.08 percent
PLR: 0.9792
  E: 0.9867

Selected Concentration Model:
-----------------------------

Alkalinity ~ quadratic(log(FLOW)) + log(SC) + fourier(DATES)

Model coefficients:
                              Estimate Std. Error z-score p-value
(Intercept)                   -0.06969    0.31973  -0.218  0.8202
quadratic(log(FLOW))(5.12598)1 -0.08884   0.01875  -4.739  0.0000
quadratic(log(FLOW))(5.12598)2  0.02903   0.00516   5.626  0.0000
log(SC)                        0.73392    0.04857  15.111  0.0000
fourier(DATES)sin(k=1)        -0.10864    0.02358  -4.608  0.0000
fourier(DATES)cos(k=1)        -0.09143    0.02670  -3.425  0.0006

AMLE Regression Statistics
Residual variance: 0.01496
R-squared: 97.17 percent
G-squared: 263.9 on 5 degrees of freedom
P-value: <0.0001
Prob. Plot Corr. Coeff. (PPCC):
```

```
  r = 0.9789
  p-value = 0.0172
Serial Correlation of Residuals: 0.1002


Comparison of Observed and Estimated Concentrations
---------------------------------------------------
      Summary Stats: Concentrations in mg/L
---------------------------------------------
     Min  25% 50% 75% 90% 95% Max
Est 25.8 93.2 221 273 290 295 300
Obs 27.0 98.0 228 268 284 298 310


Bias Diagnostics
----------------
 Bp: 0.328 percent
PCR: 1.003
  E: 0.9564
```

The `rloadest` package contains the function `predConc` that will estimate concentrations for daily or shorter time periods, depending on the time step. Note that the daily estimation data set, `app5.est`, has 7 missing days and so has only 358 observations instead of 365 for 1999.

```
> # Get the estimation data
> data(app5.est)
> # Predict daily concentrations
> app6.cd <- predConc(app6.lr, app5.est, by="day")
> head(app6.cd)


        Date Flow     Conc   Std.Err      SEP      L95      U95
1 1999-01-01   44 230.4691 8.075796 29.42066 177.3864 294.6353
2 1999-01-02   40 238.0191 8.203423 30.34716 183.2577 304.1994
3 1999-01-03   41 232.3866 7.982030 29.62166 178.9330 296.9834
4 1999-01-04   38 238.2327 8.071336 30.33699 183.4825 304.3841
5 1999-01-05   41 235.7455 8.146778 30.06315 181.4977 301.3075
6 1999-01-06   38 235.2900 7.922827 29.94932 181.2371 300.5938
```

2 Part 2 Predict Monthly Time-weighted Mean Concentrations for 1999

The estimation of TWM concentrations requires the user to "trick" the regression model by substituting a constant synthetic value for the flow column that actually estimates concentrations in stead of load when using the `predLoad` function. The details of the development of the method are described in Runkel and others (2004). This example application only describes the implementation using `rloadest` functions.

The first step is to create a synthetic flow column in both the calibration and the estimation data sets. The value of the data is the conversion factor from load to concentration, or the reciprocal of the conversion factor from concentration to loads that can be gotten by using the `c2load` function.

```
> # Create synthetic flow values
> app6.calib <- transform(app5.calib, Sflow=1/c2load(1, 1,
+     conc.units="mg/L"))
> app6.est <- transform(app5.est, Sflow=1/c2load(1, 1,
+     conc.units="mg/L"))
> head(app6.calib)

        DATES TIMES   FLOW     SC Alkalinity     Sflow
1 1995-02-28  1231   10.0 1425.0        248 0.4087324
2 1995-03-24  1301   11.3 1010.0        205 0.4087324
3 1995-03-28  0801  190.0  519.0         78 0.4087324
4 1995-04-12  0931   13.1  784.0        204 0.4087324
5 1995-04-24  1301   22.4 1750.0        231 0.4087324
6 1995-05-08  1301 2700.0   98.9         27 0.4087324
```

The next step is to construct the calibrated model. This example will use the previously calibrated model, so that diagnostics plots will not be created. The only difference between this model and the previous model is that the flow column is defined as the synthetic flow column. The printed report for this load model should agree with the printed report for the concentration model in the previous section.

```
> # Create the and print load model.
> app6.lrTWM <- loadReg(Alkalinity ~ quadratic(log(FLOW)) + log(SC) +
+                       fourier(DATES),
+                    data = app6.calib, subset=DATES < "1998-01-01",
+                    flow = "Sflow", dates = "DATES", conc.units="mg/L",
+                    station="Arkansas River at Halstead, Ks.")
> print(app6.lrTWM)
```

```
*** Load Estimation ***

Station: Arkansas River at Halstead, Ks.
Constituent: Alkalinity

          Number of Observations: 74
Number of Uncensored Observations: 74
          Center of Decimal Time: 1996.566
                  Center of ln(Q): -0.8947
                Period of record: 1995-02-28 to 1997-12-29

Selected Load Model:
--------------------


Alkalinity ~ quadratic(log(FLOW)) + log(SC) + fourier(DATES)

Model coefficients:
                              Estimate Std. Error z-score p-value
(Intercept)                   -0.06969    0.31973  -0.218  0.8202
quadratic(log(FLOW))(5.12598)1 -0.08884    0.01875  -4.739  0.0000
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log(SC)                        0.73392    0.04857  15.111  0.0000
fourier(DATES)sin(k=1)        -0.10864    0.02358  -4.608  0.0000
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AMLE Regression Statistics
Residual variance: 0.01496
R-squared: 97.17 percent
G-squared: 263.9 on 5 degrees of freedom
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Prob. Plot Corr. Coeff. (PPCC):
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Serial Correlation of Residuals: 0.1002

Variance Inflation Factors:
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fourier(DATES)sin(k=1)         1.284
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Comparison of Observed and Estimated Loads
------------------------------------------
     Summary Stats: Loads in kg/d
```

```
--------------------------------------------
      Min  25% 50% 75% 90% 95% Max
Est 25.8 93.2 221 273 290 295 300
Obs 27.0 98.0 228 268 284 298 310

Bias Diagnostics
----------------
 Bp: 0.328 percent
PLR: 1.003
  E: 0.9564
```

The user can now estimate TWM concentrations for periods longer than 1 day.
Remember that the estimation dataset has 7 missing days and no estimates for
those months will be made.

```
> # Predict monthly TWM concentrations using the \textt{predLoad} function.
> app6.TWM <- predLoad(app6.lrTWM, app6.est, by="month")
> # Change the name of the Flux column to Conc
> names(app6.TWM)[3] <- "Conc"
> app6.TWM

             Period Ndays     Conc  Std.Err      SEP       L95       U95
1     January 1999     31 213.1878 7.081182 8.529423 196.95746 230.3869
2    February 1999     28 149.5486 5.216405 6.361388 137.46681 162.3985
3       March 1999     31 194.6095 5.790947 7.210804 180.85773 209.1198
4       April 1999     30 107.1358 3.026241 4.009600  99.49121 115.2064
5         May 1999     31 121.6526 3.345660 4.355846 113.33779 130.4103
6        June 1999     29       NA       NA       NA        NA        NA
7        July 1999     28       NA       NA       NA        NA        NA
8      August 1999     31 168.6656 6.141413 7.344922 154.72644 183.5125
9   September 1999     27       NA       NA       NA        NA        NA
10    October 1999     31 211.5238 6.786674 8.240603 195.83063 228.1284
11   November 1999     30 252.3945 8.046272 9.846216 233.64435 272.2351
12   December 1999     31 189.3642 6.175727 7.502260 175.08417 204.4880
```

A quick check of the mean daily concentrations verifies that computations.
Note that there is no protection against incomplete months when the TWM
concentrations are computed manually, so values are obtained for June, July
and September.

```
> with(app6.cd, tapply(Conc, month(Date, label=TRUE), mean))

      Jan       Feb       Mar       Apr       May       Jun       Jul       Aug       Sep
213.18784 149.54864 194.60951 107.13581 121.65264 106.54503  85.02916 168.66561 130.05797
      Oct       Nov       Dec
211.52384 252.39450 189.36420
```

3 Part 3 Predict Monthly Flow-weighted Mean Concentrations for 1999

The estimation of FWM concentrations is a two-step process. The first step is to build the rating-curve model for loads and estimate the flux desired for each period. The second step is to compute the mean flow for each period and divide the flux by the flow and correct to concentration units. The load model for this example (app6.lr) was created in the first part of this vignette.

```
> # Compute the monthly fluxes.
> app6.FWM <- predLoad(app6.lr, app6.est, by="month")
> # Compute the mean flows
> app6.FWM$Flow <- as.vector(with(app6.est, tapply(FLOW, month(DATES), mean)))
> # Compute the FWM concentration
> app6.FWM <- transform(app6.FWM, FWMC=Flux/Flow/
+                       c2load(1, 1, conc.units="mg/L"))
> app6.FWM
```

	Period	Ndays	Flux	Std.Err	SEP	L95	U95	Flow	FWM
1	January 1999	31	35442.25	1309.7176	2155.2335	31405.46	39850.55	121.74194	118.9926
2	February 1999	28	63032.12	2511.7167	3783.9322	55940.53	70767.67	353.57143	72.8658
3	March 1999	31	25388.38	768.4968	957.4235	23563.38	27315.89	53.58065	193.6716
4	April 1999	30	127971.05	4415.6512	6011.0352	116592.86	140150.41	815.46667	64.1423
5	May 1999	31	67572.50	1854.0435	2724.5044	62389.33	73067.49	327.41935	84.3538
6	June 1999	29	NA	NA	NA	NA	NA	787.03448	N
7	July 1999	28	NA	NA	NA	NA	NA	932.00000	N
8	August 1999	31	100304.10	3710.5034	5197.4230	90502.12	110870.01	620.48387	66.0734
9	September 1999	27	NA	NA	NA	NA	NA	136.25926	N
10	October 1999	31	12434.02	397.2618	484.1962	11511.91	13409.65	24.29032	209.2267
11	November 1999	30	15924.63	507.6033	621.6939	14740.76	17177.40	25.86667	251.6331
12	December 1999	31	23377.49	805.5262	1009.0498	21461.96	25416.63	57.61290	165.8506

For these data, the FWM concentration is less than the TWM concentration. In general, the FWM concentration will less than the TWM concentration when the concentration and flow are negatively correlated.