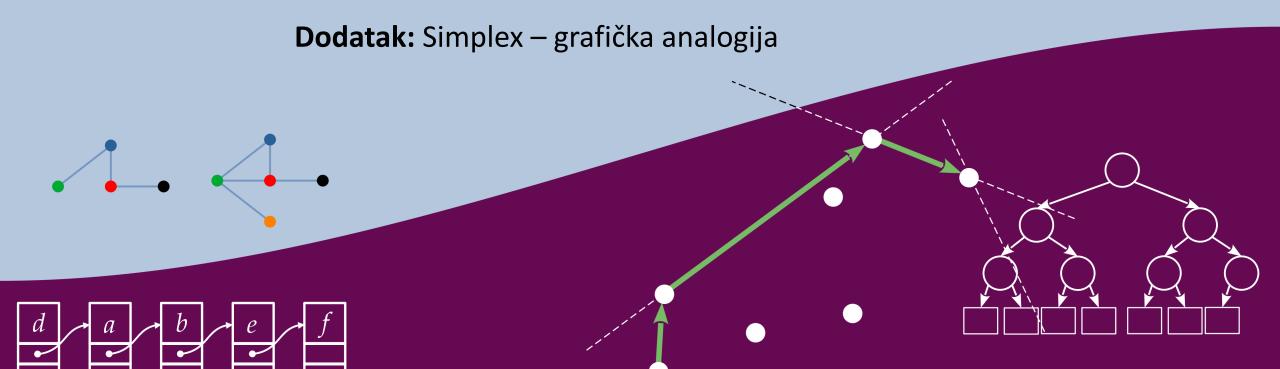


# Napredni algoritmi i strukture podataka



#### Problem

#### Riješite:

max 
$$3x_1 + 5x_2$$
  
uz  $x_1 + 5x_2 \le 40$   
 $2x_1 + x_2 \le 20$   
 $x_1 + x_2 \le 12$   
 $x_1, x_2 \ge 0$ 



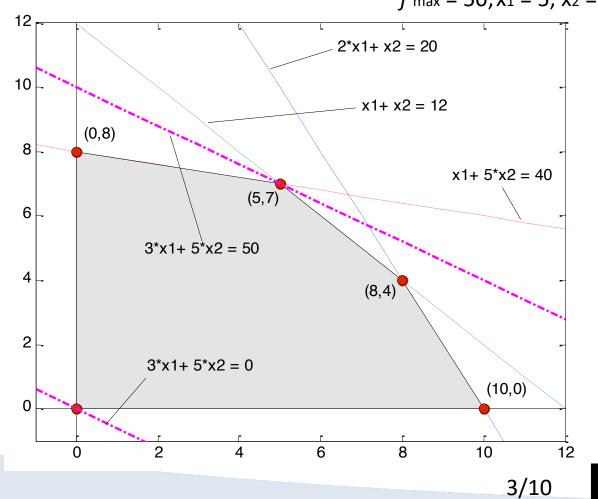


#### Rješenje grafičkom metodom

#### Grafičko rješenje

$$f_{\text{min}} = 0$$
;  $x_1 = 0$ ,  $x_2 = 0$   
 $f_{\text{max}} = 50$ ;  $x_1 = 5$ ,  $x_2 = 7$ 

max 
$$3x_1 + 5x_2$$
  
uz  $x_1 + 5x_2 \le 40$   
 $2x_1 + x_2 \le 20$   
 $x_1 + x_2 \le 12$   
 $x_1, x_2 \ge 0$ 





# Simplex – init (iteracija 0)

Pretvorba u standardnu formu:

min

uz

$$-3x_1 - 5x_2$$
 $x_1 + 5x_2 + x_3$ 
 $2x_1 + x_2 + x_4$ 
 $x_1 + x_2 + x_3$ 
 $x_1 + x_2 + x_3$ 
 $x_2 + x_3$ 
 $x_3 = 40$ 
 $x_1 + x_2 + x_3$ 
 $x_4 = 20$ 
 $x_1 + x_2 + x_3$ 
 $x_5 = 12$ 

$$x_1, x_2, x_3, x_4, x_5 \ge 0$$

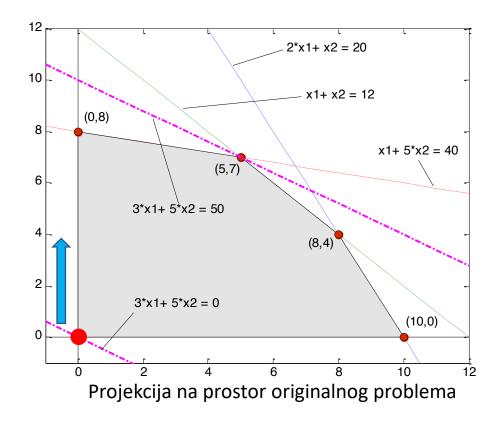
Izražavanje rješenja u bazi stupčanih vektora matrice A

- Kao polazno rješenje uzimamo ekstrem  $\mathbf{x}_0 = [0, 0, 40, 20, 12]^T$ .  $f(x_0) = 0$
- Bazične varijable (x<sub>3</sub>,x<sub>4</sub>,x<sub>5</sub>)



$a_1$	$a_2$	<b>a</b> 3	<b>a</b> 4	<b>a</b> 5	RHS
<b>-</b> 3	<b>-</b> 5	0	0	0	0
1	5	1	0	0	40
2	1	0	1	0	20
1	1	0	0	1	12

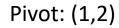
$$x_{(0)} = [0,0,40,20,12]^T$$
,  $f(x_{(0)}) = 0$ 



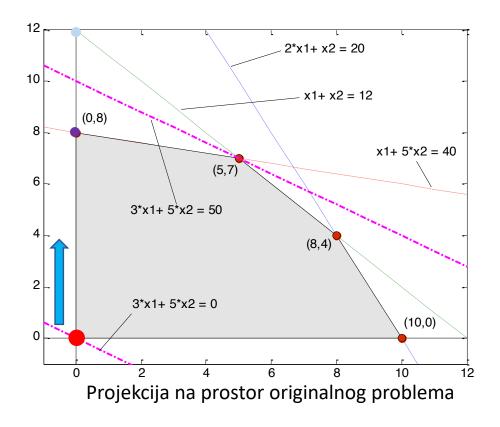




$a_1$	<b>a</b> <sub>2</sub>	<b>a</b> <sub>3</sub>	<b>a</b> 4	<b>a</b> <sub>5</sub>	RHS	Q
<b>-</b> 3	<b>-</b> 5	0	0	0	0	
1	5	1	0	0	40	8
2	1	0	1	0	20	20
1	1	0	0	1	12	12



<sup>\*</sup>Iteracija se završava pivotiranjem

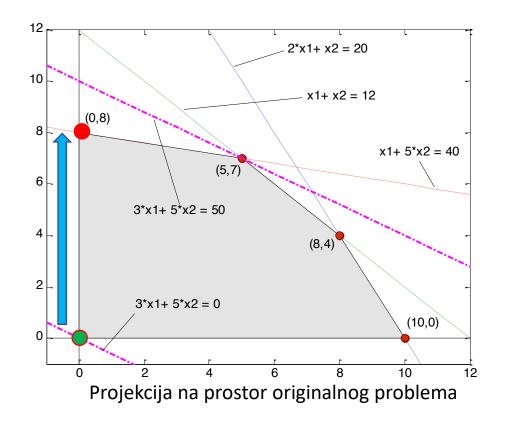




$a_1$	a <sub>2</sub>	<b>a</b> <sub>3</sub>	<b>a</b> 4	<b>a</b> 5	RHS
<b>-2</b>	0	1	0	0	40
1/5	1	1/5	0	0	8
9/5	0	-1/5	1	0	12
4/5	0	-1/5		1	4

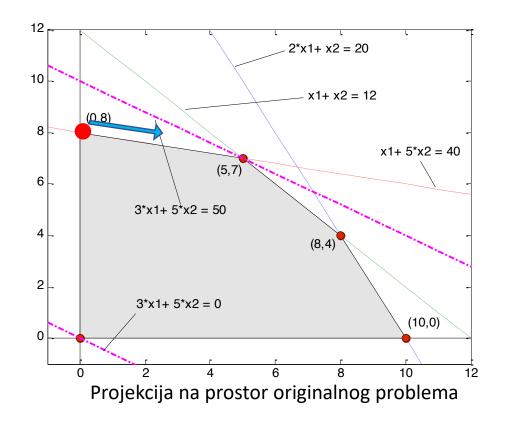
Skok iz x<sub>(0)</sub> u:

$$x_{(1)} = [0,8,0,12,4]^T$$
,  $f(x_{(1)}) = -40$ 





$a_1$	a <sub>2</sub>	<b>a</b> 3	<b>a</b> 4	<b>a</b> <sub>5</sub>	RHS
-2	0	1	0	0	40
1/5	1	1/5	0	0	8
9/5	0	-1/5	1	0	12
4/5	0	-1/5	0	1	4

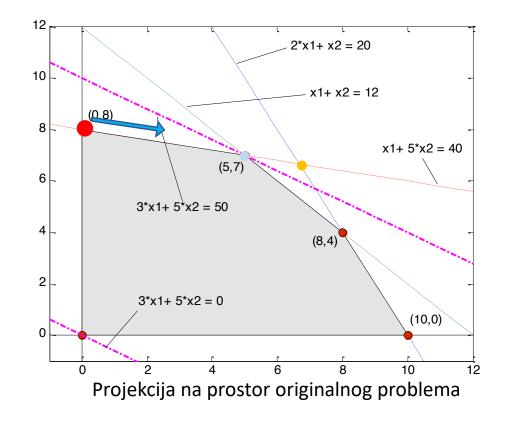






$a_1$	a <sub>2</sub>	<b>a</b> <sub>3</sub>	<b>a</b> 4	<b>a</b> <sub>5</sub>	RHS	Q
-2	0	1	0	0	40	
1/5	1	1/5	0	0	8	40
9/5	0	-1/5	1	0	12	60/9
4/5	0	-1/5	0	1	4	5

Pivot: (3,1)



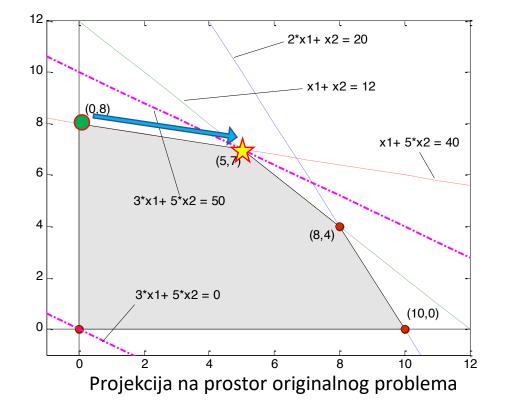




a <sub>1</sub>	$a_2$	<b>a</b> 3	a <sub>4</sub>	<b>a</b> 5	RHS
0	0	1/2	0	10/4	50
0	1	1/20	0	-1/4	7
0	0	1/4	1	-9/4	3
1	0	-1/4	0	5/4	5

#### Skok iz x<sub>(1)</sub> u:

 $x_{(2)} = [5,7,0,3,0]^T$ ,  $f(x_{(2)}) = -50$ 



#### **OPTIMUM!**

