



CS 329P: Practical Machine Learning (2021 Fall)

# 5.4 Stacking

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https://c.d2l.ai/stanford-cs329p

### Stacking



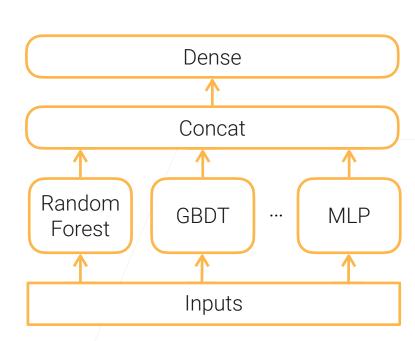
- Combine multiple base learners to reduce variance
  - Base learners can be different model types
  - Linearly combine base learners outputs by learned parameters



- Widely used in competitions
- bagging VS stacking



- Bagging: bootstrap samples to get diversity
- Stacking: different types of models extract different features



#### Stacking Results



Evaluate on house sales data, compare to bagging and GBDT we

implemented before

	Test Error
GBDT	0.259
RandomForest	0.243
Stacking (AutoGluon)	0.229

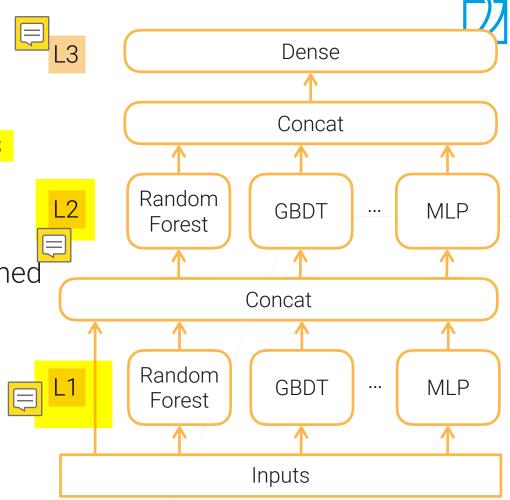
from autogluon.tabular import TabularPredictor

predictor = TabularPredictor(label=label).fit(train)

score\_test score\_val pred\_time\_test WeightedEnsemble\_L2 -0.229626 -0.222406 3.953961 ExtraTrees -0.232468 -0.232027 1.831407 CatBoost -0.238690 2 -0.230338 0.016279 3 LightGBM -0.239441 -0.226900 0.203499 NeuralNetMXNet -0.241847 -0.246979 4.397190 **RandomForest** -0.242904 -0.234931 1.750319 **XGBoost** -0.249837 0.086715 6 -0.240684 7 **KNeighbors** -0.457131 -0.443591 0.107212

# **Multi-layer Stacking**

- Stacking base learners in multiple levels to reduce bias
  - Can use a different set of base learners at each level
- Upper levels (e.g. L2) are trained on the outputs of the level below (e.g. L1)
  - Concatenating original inputs helps



# Overfitting in Multi-layer Stacking



- Train leaners from different levels on different data to alleviate overfitting
  - Split training data into A and B, train L1 learners on A, run inference on B to generate training data for L2 learners
- Repeated *k*-fold bagging:
  - Train k models as in k-fold cross validation
  - Combine predictions of each model on out-of-fold data
  - Repeat step 1,2 by n times, average the n predictions of each example for the next level training

## Multi-layer Stacking Results

- Use 1 additional staked level, with 5-fold repeated bagging
  - Error:  $0.229 \rightarrow 0.227$
  - Training time: 39 sec  $\rightarrow$  207 sec (5x)

```
from autogluon.tabular import TabularPredictor
```

```
predictor = TabularPredictor(label=label).fit(
train, num_stack_levels=1, num_bag_folds=5)
```



	mo	score_test	score_val	
0	NeuralNetMXNet_BAG	_L2	-0.225332	-0.219718
1	WeightedEnsemble	_L3	-0.226921	-0.216254
2	CatBoost_BAG	_L2	-0.227525	-0.217471
3	WeightedEnsemble	_L2	-0.228386	-0.218298
4	LightGBM_BAG	_L2	-0.228400	-0.218374
5	XGBoost_BAG	_L2	-0.228660	-0.218824
6	ExtraTrees_BAG	_L2	-0.228751	-0.217563
7	ExtraTrees_BAG	_L1	-0.233527	-0.224974
8	RandomForest_BAG	_L2	-0.234270	-0.220346
9	CatBoost_BAG	_L1	-0.237356	-0.227126
10	LightGBM_BAG	-0.238102	-0.225848	
11	NeuralNetMXNet_BAG	-0.238413	-0.238786	
12	XGBoost_BAG	_L1	-0.241698	-0.235570
13	RandomForest_BAG	_L1	-0.242029	-0.227800
14	KNeighbors_BAG	_L1	-0.457909	-0.447980

## **Model Combination Summary**









Reduce	Bias	Variance	Computation Cost	Parallelizati on	
Bagging	-	Υ	n	n	
Boosting	Υ	-	n	1	
Stacking	-	Y	n	n	
K-fold multi- level stacking	Υ	Υ	nxlxk	nxk	

n: number of learners, l: number of levels, k: k-fold