

# MAST20005/MAST90058: Week 2 Lab Solutions

1. 

```
sum(log(1:100))
```

```
## [1] 363.7394
```
2. 

```
x <- rnorm(100000, 1, sqrt(2))
```

```
mean(x^2)
```

```
## [1] 3.000038
```
3. Run `help(qnorm)` to access the documentation. `qnorm(0.1)` calculates  $\pi_{0.1}$  for a standard normal distribution. `qnorm(0.1, lower.tail = FALSE)` calculates  $\pi_{1-0.1} = \pi_{0.9}$ , and therefore gives the same answer as `qnorm(0.9)`.
4. 

```
exp1pdf <- function(x) {
```

```
  if (x < 0)
```

```
    d <- 0
```

```
  else
```

```
    d <- exp(-x)
```

```
  return(d)
```

```
}
```

```
exp1pdf(-1) # should equal zero
```

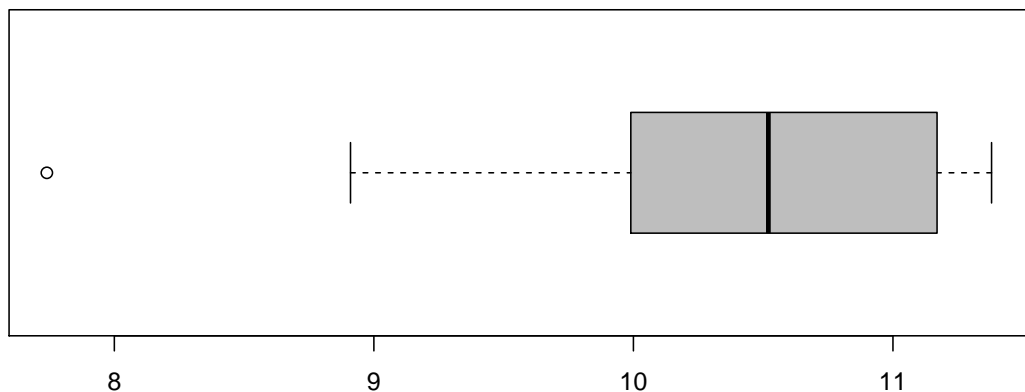
  

```
## [1] 0
```
5. 

```
x <- c(10.39, 10.43, 9.99, 11.17, 8.91,
```

```
      11.20, 11.38, 7.74, 10.61, 11.11)
```

```
boxplot(x, col = 8, horizontal = TRUE) # using the R defaults
```



6. See the solutions to the tutorial problems.
7. We need to simulate from the given distribution. First, calculate the cdf,

$$F(x) = \int_{-1}^x \frac{3}{2}y^2 dy = \left[ \frac{1}{2}y^3 \right]_{-1}^x = \frac{x^3 + 1}{2}, \quad \text{where } -1 < x < 1.$$

Then invert to get the inverse cdf,

$$F^{-1}(p) = (2p - 1)^{\frac{1}{3}},$$

which we will use to simulate  $X$ .

```
# Function to handle powers for negative numbers properly.
exponent <- function(x, p)
  sign(x) * abs(x)^p

# Function to generate random X's.
rx <- function(n)
  exponent(2 * runif(n) - 1, 1/3)

# Function to generate random Y's.
ry <- function(n) {
  y <- 1:n
  for (i in 1:n)
    y[i] <- sum(rx(15))
  return(y)
}

# A more efficient way to do the same thing is:
ry <- function(n)
  replicate(n, sum(rx(15)))

# Simulate Y's.
ys <- ry(10000)

# Estimate the probability.
mean((-0.3 < ys) & (ys < 1.5))

## [1] 0.2277
```

Notes:

- The `exponent` function is needed to properly handle powers for negative numbers. See [this discussion](#) for more info.
- The comparison operator (`<`) and the logical operator (`&`) are both vectorised, allowing a very compact expression for counting up how many of the simulated  $Y$ 's are inside the interval of interest.