## Chapter 3

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- Scalars have only magnitude. Vectors have both magnitude and direction.
- Two vectors  $\vec{a}$  and  $\vec{b}$  may be added geometrically by drawing them to a common scale and placing them head to tail. The vector connecting the tail of the first to the head of the second is the vector sum  $\vec{s}$ . Vector addition is commutative and obeys the associative law.
- The components of a a two-dimensional vector  $\vec{a}$  are given as  $a_x = \cos \theta$  and  $a_y = a \sin \theta$
- Magnitude and orientation of a vector are given as  $a = \sqrt{a_x^2 + a_y^2}$  and  $\tan \theta = \frac{a_y}{a_x}$
- Unit vectors  $\hat{i}, \hat{j}, \hat{k}$  have magnitudes of unity and are directed in the positive directions of the x, y, and x axes. Unit vectors are defined as  $\hat{v} \equiv \frac{v}{|v|}$
- The scalar (or dot product) of two vectors  $\vec{a}$  and  $\vec{b}$  is written  $\vec{a}\vec{b}$  and is the scalar quantity given by  $ab\cos\theta$  where  $\theta$  is the angle between the directions of  $\vec{a}$  and  $\vec{b}$ .
- The vector (or cross) product of two vectors is a vector whose magnitude is given as  $c = ab \sin \theta$ . The rest of it is ugly and we do not care.

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