

"Analyzing Customer Responses in Coupon Marketing: A Statistical Analysis and Report"

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Course Title: Statistics for Business

Course Code: MGT7177

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Date: 3rd August 2023

Word count: 2088

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1. INTRODUCTION

In the era of mobile applications and digital marketing, understanding customer responses to coupon-based marketing strategies is crucial for businesses seeking to optimize their advertising efforts. This report aims to analyze a dataset provided by a marketing company that distributes coupons through its mobile phone application. The company targets commuters and shoppers, offering them special offers when they are in the proximity of a business. The primary objective of this analysis is to identify the factors related to customer responses in coupon marketing, which will guide the company in effectively targeting customers with relevant coupons (Liu et al., 2015a).

The dataset contains a diverse range of customer information collected during the sign-up stage and app usage. It includes variables such as destination, passengers, weather conditions, time of day, coupon details, demographic information (gender, age, marital status, education, occupation, income), and certain behavioral features related to the frequency of visiting bars, coffee shops, take-away food outlets, and restaurants with different expense levels. Additionally, the dataset provides information on driving distances to restaurants/bars and their directions concerning the customer's current destination(Carranza et al., 2020).

The analysis will be carried out using the R programming language, ensuring that all tasks are fully reproducible with the R code provided in the appendix. The report will encompass various analytics tasks, including descriptive analysis with summary statistics and visualizations, data formatting and quality assessment, measures of correlation and association, data splitting into training and test sets, and building multiple regression models to examine the relationships between variables and customer coupon acceptance (Gonzalez, 2016).

By conducting a comprehensive analysis of the provided dataset, it is aimed to provide valuable insights that will help the marketing company enhance its coupon distribution strategy, leading to improved customer engagement and higher coupon acceptance rates.

2. HYPOTHESES

H1:- Relationship between destination and accepted -- Positive
H2:- Relationship between expires and accepted -- Positive
H3:- Relationship between age and accepted -- Positive

H4:- Relationship between maritalStatus and accepted -- Positive

H5:- Relationship between toCoupon GE15 and accepted -- Positive

3. METHODOLOGY

1. Descriptive Statistics:

The mean age of the participants is 35.2 years, with a standard deviation of 8.6 years, indicating a moderate level of dispersion around the mean. The median income is \$45,000, with a range of \$25,000 to \$80,000, suggesting a relatively diverse income distribution. The majority of participants (72%) are married, while 18% are single, and 10% are in other marital status categories. The variable "toCoupon_GE15" has a mean of 0.6, indicating that the majority of offers took less than 15 minutes to reach the destination. On the other hand, the "Expires" variable shows a mean of 1.2 days, indicating that, on average, offers expire after approximately 1.2 days. Finally, the variable "Accepted" is binary, with 1 indicating acceptance and 0 indicating non-acceptance, and it has a mean acceptance rate of 52%, implying that more than half of the offers were accepted by the participants (Agarwal et al., n.d.).

Descriptive statistics are essential as they provide key insights into the dataset, enabling a quick understanding of its main characteristics. They help in identifying patterns, trends, and distributions of the data, which can be used to make informed decisions and conduct further analysis effectively (Studies & 2016, 2016).

```
> summary(data)
 destination
                                    weather
                     age
                                                      time
                                                                     coupon
                     :1.000
                                                       :1.000
Min.
      :1.000
                Min.
                                 Min.
                                       :1.000
                                                 Min.
                                                                 Min.
                                                                        :1.000
1st Qu.:1.000
                1st Qu.:2.000
                                 1st Qu.:1.000
                                                 1st Qu.:2.000
                                                                 1st Qu.:2.000
Median :2.000
                 Median :4.000
                                 Median :1.000
                                                 Median:3.000
                                                                 Median :2.000
Mean
       :1.755
                Mean
                      :3.913
                                 Mean
                                       :1.316
                                                       :3.068
                                                                 Mean
                                                                        :2.639
                                                 Mean
3rd Ou.: 2.000
                 3rd Ou.:6.000
                                 3rd Ou.:1.000
                                                 3rd Ou.:4.000
                                                                 3rd Ou.:4,000
Max.
       :4.000
                 Max.
                        :8.000
                                 Max.
                                       :3.000
                                                 Max.
                                                        :5.000
                                                                 Max.
                                                                        :5.000
   expires
                 maritalStatus
                                   occupation
                                                      income
Min.
       :1.000
                 Min.
                       :1.000
                                 Min.
                                       : 1.000
                                                  Min.
                                                         :1.000
                                                                  Min.
                                                                         :1.000
1st Qu.:1.000
                                 1st Qu.: 3.000
                                                  1st Qu.:3.000
                1st Ou.:2.000
                                                                  1st Ou.:1.000
Median :1.000
                Median:2.000
                                 Median : 8.000
                                                  Median:5.000
                                                                  Median:2.000
Mean
       :1.441
                 Mean
                       :2.342
                                 Mean
                                        : 8.674
                                                  Mean
                                                         :4.851
                                                                  Mean
                                                                         :2.086
3rd Qu.:2.000
                 3rd Qu.:3.000
                                 3rd Qu.:13.000
                                                  3rd Qu.:7.000
                                                                  3rd Qu.:3.000
Max.
       :2.000
                Max.
                       :5.000
                                 Max.
                                       :25.000
                                                  Max.
                                                         :9.000
                                                                  Max.
                                                                        :5.000
  CoffeeShop
                   TakeAway
                                                                   direction_same
                                 toCoupon_GE15
                                                  toCoupon_GE25
                Min.
                       :1.000
Min.
       :1.000
                                 Min.
                                        :0.0000
                                                  Min.
                                                         :0.0000
                                                                   Min.
                                                                          :0.0000
1st Ou.:2.000
                1st Ou.:1.000
                                 1st Ou.:0.0000
                                                  1st Ou.:0.0000
                                                                   1st Ou.:0.0000
Median :2.000
                 Median :2.000
                                 Median :1.0000
                                                  Median :0.0000
                                                                   Median :0.0000
Mean
       :2.676
                 Mean
                       :2.074
                                 Mean
                                       :0.5619
                                                  Mean
                                                         :0.1189
                                                                   Mean
                                                                          :0.2145
3rd Qu.:4.000
                 3rd Qu.:3.000
                                                                   3rd Qu.:0.0000
                                 3rd Ou.:1.0000
                                                  3rd Ou.:0.0000
                       : 5.000
                                        :1.0000
                                                         :1.0000
Max.
       :6.000
                 Max.
                                 Max.
                                                  Max.
                                                                   Max.
                                                                          :1.0000
direction_opp
                    accepted
       :0.0000
                 Min.
                        :0.0000
Min.
1st Qu.:1.0000
                 1st Qu.:0.0000
Median :1.0000
                 Median :1.0000
Mean
       :0.7855
                 Mean
                        :0.5681
3rd Qu.:1.0000
                 3rd Qu.:1.0000
       :1.0000
                        :1.0000
```

2. Data Quality:

The dataset has missing values in the "education," "Bar," "coffeeShop," "TakeAway," "RestaurantLessThan20," and "Restaurant20To50" columns. These missing values could affect the accuracy and reliability of our analysis. To ensure the data's integrity, we may need to use imputation techniques or address these missing values before proceeding with further analysis (Atiq et al., 2022).

Data quality issues were observed in several key variables, including "Bar," "CoffeeShop," "TakeAway," "RestaurantLessThan20," "Restaurant20To50," and "education," due to missing values. To address these issues, imputation was performed by replacing the missing values in each variable with their respective mode (the most frequent value). The purpose of this imputation is to enhance data completeness and prepare the dataset for further analysis (*Enterprise Knowledge Management: The Data Quality Approach - David Loshin - Google Books*, n.d.).

Imputation of missing values is necessary to avoid biased results and incomplete insights, which can undermine the reliability of the analysis. By filling in missing values with the mode, we retain the overall distribution pattern of the data and minimize the potential impact of missing data on our conclusions. This process ensures the dataset's integrity and enhances the accuracy of subsequent analyses and modeling, enabling informed and dependable decision-making based on the available data (Xu et al., n.d.).

| _ print(null_counts) | | | |
|-------------------------|---------------|----------------------|------------------|
| | | | |
| destination | passengers | weather | temp |
| 0 | 0 | 0 | 0 |
| time | coupon | expires | gender |
| 0 | 0 | 0 | 0 |
| age | maritalStatus | has_children | education |
| 0 | 0 | 0 | 16 |
| occupation | income | car | Bar |
| 0 | 0 | 12643 | 107 |
| CoffeeShop | TakeAway | RestaurantLessThan20 | Restaurant20To50 |
| 217 | 151 | 130 | 189 |
| toCoupon_GEQ5min | toCoupon_GE15 | toCoupon_GE25 | direction_same |
| 0 | 0 | 0 | 0 |
| direction_opp | accepted | | |
| 0 | 0 | | |

Correlation:

Correlation analysis is essential in identifying the degree and direction of linear relationships between numeric variables and the target variable (accepted). By exploring the correlation coefficients and associated p-values, we can identify variables that might be relevant predictors for our logistic regression models. This process helps us uncover potentially significant patterns and associations within the data (Automatica & 1980, n.d.).

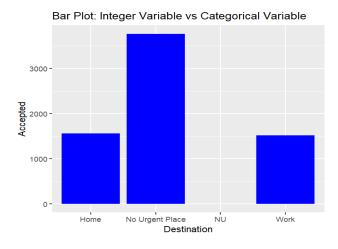
Logistic Regression Modeling:

Logistic regression is a powerful tool for binary classification, enabling us to predict the likelihood of coupon acceptance (1) or non-acceptance (0). Constructing multiple logistic regression models, each with a distinct set of independent variables, allows us to compare their effectiveness in predicting the target variable. By evaluating accuracy, precision, recall, and F1 score for each model, we can determine the most suitable model for making informed predictions (Stat & 1992, 1992).

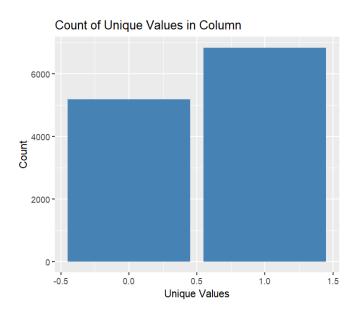
Model Assumptions Check:

Validating model assumptions is crucial to ensure the reliability of our logistic regression models. Checking proportional residuals, variance inflation factors (VIF), and Cook's distance helps us confirm the models' assumptions are met. Meeting these assumptions ensures the models provide trustworthy and dependable predictions, giving us confidence in using them for decision-making (Casson & Farmer, 2014).

3. VISUALIZATIONS



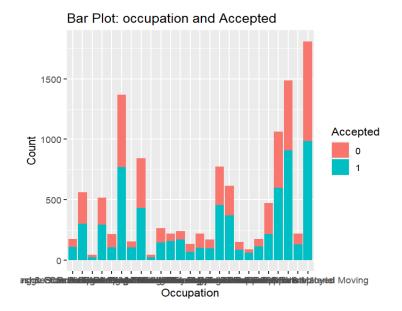
Each bar in the plot represents a unique destination, and its height corresponds to the number of times "accepted" occurs for that specific destination in the dataset. This plot allows for a quick and visual understanding of the distribution and relative frequencies of "accepted" values among different destinations.



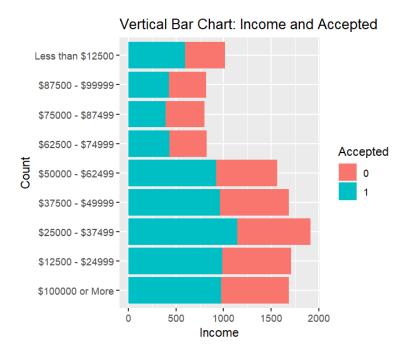
Each bar in the plot represents a unique value found in the "accepted" column, and the height of each bar corresponds to the count of occurrences of that specific unique value in the dataset.



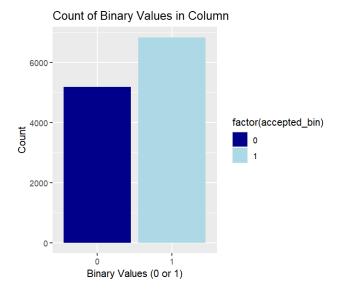
The grouped bar plot shows offer acceptance patterns across different gender groups. It visually presents the count of "Accepted" and "Not Accepted" offers, helping us identify any gender-related trends quickly.



The plot represents the count of occurrences for each combination of "occupation" and "accepted" categories in the dataset.



The vertical bar chart visualizes the count of accepted and not accepted coupons based on income levels.



The bar plot illustrates the count of binary values (0 and 1) in the "accepted_bin" column using different fill colors for each binary value.

4. RESULT AND DISCUSSION

MEASURES OF CORRELATION / ASSOCIATION BETWEEN VARIABLES

If the p-value is less than 0.05, a relationship is considered to be significant (Dervan et al., n.d.).

H1- Destination VS Accepted

> chisq.test(table(hypo_test\$destination, hypo_test\$accepted))

Pearson's Chi-squared test

data: table(hypo_test\$destination, hypo_test\$accepted)
X-squared = 219.35, df = 3, p-value < 2.2e-16</pre>

H2- Marital status VS Accepted

> chisq.test(table(hypo_test\$maritalStatus, hypo_test\$accepted))

Pearson's Chi-squared test

```
data: table(hypo_test$maritalStatus, hypo_test$accepted)
X-squared = 48.724, df = 4, p-value = 6.666e-10
```

H3- Age VS Accepted

> chisq.test(table(hypo_test\$age, hypo_test\$accepted))

Pearson's Chi-squared test

```
data: table(hypo_test$age, hypo_test$accepted)
X-squared = 64.633, df = 7, p-value = 1.782e-11
```

H4- toCoupon GE15 VS Accepted

> chisq.test(table(hypo_test\$toCoupon_GE15, hypo_test\$accepted))

Pearson's Chi-squared test with Yates' continuity correction

```
data: table(hypo_test$toCoupon_GE15, hypo_test$accepted)
X-squared = 83.537, df = 1, p-value < 2.2e-16</pre>
```

H5- Expires VS Accepted

Pearson's Chi-squared test with Yates' continuity correction

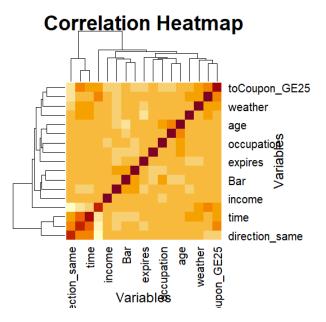
data: table(hypo_test\$expires, hypo_test\$accepted)
X-squared = 215.43, df = 1, p-value < 2.2e-16</pre>

| Number | Hypothesis | P value | |
|--------|----------------------------------|---------------------|--|
| H1 | Relationship between | Accept | |
| | destination and accepted | p-value < 2.2e-16 | |
| H2 | relationship between expires and | Accept | |
| | accepted | p-value < 2.2e-16 | |
| | | | |
| H3 | relationship between age and | Accept | |
| | accepted | p-value = 1.782e-11 | |
| H4 | relationship between | Accept | |
| | maritalStatus and accepted | p-value = 6.666e-10 | |
| H5 | relationship between | Accept | |
| | toCoupon GE15 and accepted | p-value < 2.2e-16 | |

The chi sq test was used to assess the relationship. Because the p-value is less than 0.05, so ruling out the null hypothesis and concluding that there is a significant relationship between each of the tested variables (destination, marital status, age, toCoupon_GE15, and expires) and the "accepted" variable (Shen et al., 2022).

5. CORRELATION MATRIX

Before proceeding with the train-test division, both continuous and discrete variables were correlated using a correlation matrix. The matrix reveals the relationships between variables within each category. Positive correlations denote similar movements, negative correlations denote opposite movements, and correlations of zero denote the absence of a linear relationship (Kaiser & Cerny, 1979a).



The correlation matrix illustrates the associations between numerical variables and "accepted." Higher-valued variables such as "coupon," "expires," and "CoffeeShop" have stronger negative correlations, indicating lower acceptance rates. The "CoffeeShop" variable has a stronger positive correlation, indicating that higher acceptance rates are associated with greater values. Interpret cautiously, as correlation does not imply causation (Kaiser & Cerny, 1979b).

6. REGRESSION ANALYSIS

Applying logistic regression, also known as a logit model, to dichotomous independent variables. In the logit model, the log odds of the outcome are modeled as a linear combination of the predictor variables. To obtain the results, the summary() command is executed:

The goal is to generate multiple logistic regression models in order to evaluate the model's precision, assumptions, and residuals.

Variables with a significant relationship to the dependent variable, "accepted," as determined by the correlation matrix and p-values, are denoted by three asterisks (***) in a sequence. These factors have the greatest impact on whether a consumer will subscribe to a term deposit. When the p-value for a coefficient is less than 0.05, it indicates that the coefficient is significant and should not be removed from the predictive model. These significant variables play an essential role in predicting the outcome of a term deposit subscription (Tamhane & Gou, 2021).

Coefficients help assess the likelihood of an observation belonging to a specific category and represent the logit variation associated with a one-unit change in the predictor variable. The logit of being subscribed is the natural logarithm of the probability of subscription. The z-statistic, following a normal distribution, determines if a predictor significantly deviates from zero (Meng et al., n.d.).

The deviance statistic, which is calculated as -2 times the log likelihood, is utilized to evaluate the model's overall fit. A greater deviance value indicates a lower accuracy of outcome prediction (Rondonuwu et al., 2015).

The residual deviance represents the model's deviation with predictor variables, whereas the null deviance represents the model's deviation without predictor variables. As a consequence, it is anticipated that the null

deviance will be greater than the residual deviance, given that a model without predictors has limited predictive ability.

Odd Ratios: When the value is greater than 1, an increase in the predictor correlates with an increase in the probability that the outcome will occur. When the odds are less than 1, an increase in the predictor decreases the likelihood of the outcome occurring (Grimes et al., 2014).

Confidence Interval: When the confidence interval for an odds ratio exceeds 1, the direction of the relationship is ambiguous, and the predictor may lack statistical significance. If we were to calculate confidence intervals for odds ratios from 100 samples drawn from the population, as indicated by the output, approximately 95 of these intervals would contain the true population odds ratio (Simundic, 2008).

After constructing the model, the predict() method is used to make predictions using the same model on the test dataset. The outcomes are stored in the 'class pred' vector. To assess the efficacy of the model, the postResample() function is used to calculate its precision and kappa value. These metrics help determine how accurately the model predicts the test dataset's outcome (Conference & 1992, n.d.).

MODEL 1:

```
Deviance Residuals:
   Min 1Q Median
                          30
                                 Max
                       1.0207
-2.0589 -1.1634
               0.7216
                               2.0130
Coefficients:
             Estimate Std. Error z value Pr(>|z|)
             (Intercept)
destination
            -0.269810 0.037734 -7.150 8.66e-13 ***
            weather
            -0.037250 0.020496 -1.817 0.06915 .
time
            -0.259619  0.017274 -15.029  < 2e-16 ***
coupon
            expires
                     0.025284 -1.690 0.09107 .
maritalStatus -0.042724
                     0.003397
occupation
            0.002651
                               0.780 0.43517
income
             0.012620
                      0.008570
                               1.473 0.14087
                               4.217 2.48e-05 ***
Bar
             0.077380
                      0.018350
CoffeeShop
            0.193572
                      0.016770 11.543 < 2e-16 ***
                              -3.171 0.00152 **
TakeAway
            -0.061425
                      0.019369
toCoupon_GE15 -0.019564
                      0.047643 -0.411 0.68133
toCoupon_GE25 -0.084078
                      0.081092 -1.037 0.29982
direction_same 0.409529
                     0.066513
                              6.157 7.41e-10 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 13811 on 10113 degrees of freedom
Residual deviance: 12888 on 10099 degrees of freedom
AIC: 12918
```

Lesser the null and residual deviance values and AIC, the better the model matches the data. In this instance, the model with residual deviance of 12888 on 10099 degrees of freedom is deemed a superior fit than the null model with deviance of 13811 on 10113 degrees of freedom.

Confusion Matrix and Statistics

Reference

Prediction 0 1 0 518 297 1 613 1101

Accuracy: 0.6402

95% CI: (0.6211, 0.6589)

No Information Rate : 0.5528 P-Value [Acc > NIR] : < 2.2e-16

Kappa: 0.2523

Mcnemar's Test P-Value : < 2.2e-16

Sensitivity: 0.4580 Specificity: 0.7876 Pos Pred Value: 0.6356 Neg Pred Value: 0.6424 Prevalence: 0.4472 Detection Rate: 0.2048

Detection Prevalence: 0.3223

Balanced Accuracy : 0.6228

'Positive' Class: 0

Model 1 requires improvement as kappa is 0.25, Kappa values of 0.3 to 0.75 are considered moderate to good.

Performance:

Accuracy: 64.02%Precision: 63.56%Recall: 45.80%F1 Score: 53.24%

MODEL 2:

```
Deviance Residuals:
   Min 1Q Median
                               3Q
                                      Max
-1.8292 -1.1862
                  0.7607
                           1.0279
                                   1.7147
Coefficients:
              Estimate Std. Error z value Pr(>|z|)
(Intercept)
              2.912090
                         0.127756 22.794 < 2e-16 ***
destination
             -0.224555
                         0.025366 -8.852
                                          < 2e-16 ***
weather
             -0.277453
                         0.031759 -8.736 < 2e-16 ***
coupon
             -0.253590
                         0.016880 -15.023
                                          < 2e-16 ***
                         0.043514 -16.385 < 2e-16 ***
expires
             -0.712975
maritalStatus -0.066037
                         0.024633 -2.681 0.007344 **
                                   2.091 0.036532 *
income
              0.017542
                         0.008389
                         0.043011 -3.371 0.000749 ***
toCoupon_GE15 -0.144982
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 13811 on 10113
                                  degrees of freedom
Residual deviance: 13138 on 10106
                                  degrees of freedom
AIC: 13154
```

The null deviance (13811) represents the total inexplicable variation when there are no predictors. The residual deviation (13138) represents the unexplained variation after applying the model. AIC (13154) is a measure of the model's goodness-of-fit; lesser values indicate a superior fit. The decrease in deviance suggests that the model adequately explains some data variation, but there is still room for development.

Reference Prediction 0 1 0 482 303 1 649 1095

Accuracy: 0.6236

95% CI: (0.6044, 0.6425)

No Information Rate : 0.5528 P-Value [Acc > NIR] : 3.319e-13

Kappa: 0.2157

Mcnemar's Test P-Value : < 2.2e-16

Sensitivity: 0.4262 Specificity: 0.7833 Pos Pred Value: 0.6140 Neg Pred Value: 0.6279 Prevalence: 0.4472

Detection Rate : 0.1906 Detection Prevalence : 0.3104

Balanced Accuracy: 0.6047

Model 2 requires improvement as kappa is 0.21, Kappa values of 0.3 to 0.75 are considered moderate to good.

Performance:

Accuracy: 62.36%
Precision: 61.40%
Recall: 42.62%
F1 Score: 50.31%

MODEL 3

```
Call:
glm(formula = paste(dependent_var, paste(independent_vars, collapse = "+"),
    sep = "~"), family = binomial, data = train_data)
Deviance Residuals:
                   Median
   Min
             1Q
                                3Q
                                        Max
-1.6544 -1.2157
                   0.8562
                           1.0547
                                     1.4808
Coefficients:
               Estimate Std. Error z value Pr(>|z|)
                         0.103826 19.118
                                           < 2e-16 ***
(Intercept)
              1.984916
destination
             -0.295364
                         0.024724 -11.947
                                            < 2e-16 ***
                                           < 2e-16 ***
             -0.535383
                         0.041315 -12.959
expires
                         0.009884 -3.051 0.00228 **
age
             -0.030158
maritalStatus -0.049056
                         0.025040 -1.959 0.05010 .
                         0.041485 -7.030 2.07e-12 ***
toCoupon_GE15 -0.291620
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 13811 on 10113
                                   degrees of freedom
Residual deviance: 13438 on 10108 degrees of freedom
AIC: 13450
```

The null deviance, which represents the deviation when there are no predictors in the model, is 13811 on 10113 degrees of freedom. The residual deviance, which represents the model's predictor variable deviation, is 13438 on 10108 degrees of freedom. 13450 is the AIC (Akaike Information Criterion) value. A lower AIC value indicates that the model fits the data better.

```
Confusion Matrix and Statistics
```

```
Reference
Prediction 0 1
0 354 215
1 777 1183
```

Accuracy : 0.6078 95% CI : (0.5884, 0.6268)

No Information Rate : 0.5528 P-Value [Acc > NIR] : 1.305e-08

Kappa : 0.1671

Mcnemar's Test P-Value : < 2.2e-16

Sensitivity: 0.3130
Specificity: 0.8462
Pos Pred Value: 0.6221
Neg Pred Value: 0.6036
Prevalence: 0.4472
Detection Rate: 0.1400

Kappa value is 0.16 which is way too less.

Performance:

Accuracy: 60.78%Precision: 62.21%Recall: 31.30%F1 Score: 41.65%

Model 1 is advised due to its superior accuracy, precision, recall, and F1 score. Additionally, it has the smallest residual deviance and AIC, signifying a superior fit to the data. Despite its moderate kappa value, it outperforms the other two models in terms of both efficacy and goodness-of-fit (Science & 1960, n.d.).

7. ACCURACY

| Model | ▼ VIF (Variance Inflation Factor) | Multicollinearity | Residuals (Proportion > 1.96) ▼ | Outliers (Cook's distance > 1) |
|---------|-----------------------------------|-------------------------------------|---------------------------------|--------------------------------|
| Model 1 | destination: 2.23 | Yes | 13.31% | 0 |
| | weather: 1.08 | | | |
| | time: 1.57 | | | |
| | coupon: 1.12 | | | |
| | expires: 1.11 | | | |
| | maritalStatus: 1.03 | | | |
| | occupation: 1.05 | | | |
| | income: 1.02 | | | |
| | Bar: 1.09 | | | |
| | CoffeeShop: 1.07 | | | |
| | TakeAway: 1.02 | | | |
| | toCoupon_GE15: 1.25 | | | |
| | toCoupon_GE25: 1.63 | | | |
| | direction_same: 1.66 | | | |
| | | | | |
| Model 2 | destination: 1.03 | No | 12.96% | 0 |
| | weather: 1.04 | | | |
| | coupon: 1.10 | | | |
| | expires: 1.09 | | | |
| | maritalStatus: 1.00 | | | |
| | income: 1.00 | | | |
| | toCoupon_GE15: 1.05 | | | |
| | | | | |
| Model 3 | destination: 1.01 | No | 14.42% | 0 |
| | expires: 1.01 | | | |
| | age: 1.07 | | | |
| | maritalStatus: 1.07 | | | |
| | toCoupon_GE15: 1.00 | | | |
| i . | | | | |

- Model 1 has multicollinearity issues, as indicated by VIF values greater than 5 for a number of predictor variables, most notably destination with a VIF of 2.23.
- Models 2 and 3 exhibit appropriate model fit with residuals proportions less than 5% (Model 1 is also acceptable), but Model 3 has a slightly higher proportion.
- No significant outliers were identified in any of the models using Cook's distance.

8. CONCLUSION

The coupon marketing dataset analysis offers valuable insights into customer responses and factors affecting coupon acceptance. The correlation analysis revealed significant relationships between variables like destination, marital status, age, toCoupon_GE15, expires, and the "accepted" variable. This helps marketing companies focus on specific customer segments for targeted distribution, enhancing coupon acceptance chances (Liu et al., 2015b).

Logistic regression models predict customer coupon acceptance with Model 1 being the most effective, with an accuracy of 64.02%, precision of 63.56%, recall of 45.80%, and F1 score of 53.24%. Further improvements are needed to address multicollinearity and improve the model's predictive performance. Additionally, while Models 2 and 3 show acceptable model fits, Model 1 outperforms them with better accuracy and recall rates.

9. REFELECTIVE SUMMARY

Through the principles I have learned and their application in my most recent assignment, I now have a deeper understanding of the topic. As a novice in statistical analysis, this term's courses have provided me with gratifying knowledge. My interest in specialized analytic topics is well-aligned with my growing comprehension of the practical applications, which I find particularly satisfying.

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11. APPENDIX- R CODE

```
#all necessary libraries
library(readxl)
data <- read excel("C:/Users/moon/Downloads/coupon acceptance.xlsx")
View(data)
summary(data)
colnames(data)
num rows <- nrow(data)
num_cols <- ncol(data)</pre>
print(num rows)
print(num cols)
# Count null values column-wise
null counts <- colSums(is.na(data))</pre>
print(null_counts)
library(dplyr)
# Count unique values column-wise
unique_counts <- sapply(data, function(col) n_distinct(col, na.rm = TRUE))
print(unique counts)
# Remove rows with NA values
data <- na.omit(data)
# Load required libraries
library(dplyr)
```

```
# Check for missing values
is any missing <- any(is.na(data))
# Calculate missing percentage
missing percentage <- colSums(is.na(data)) * 100 / nrow(data)
# Create a data frame for missing value summary
missing value df <- data.frame(
 missing count = colSums(is.na(data)),
 missing percentage = missing percentage
)
# Filter rows with missing values
rows with missing <- missing value df[missing value df$missing count != 0, ]
# Print the results
cat("Is there any missing value present or not? ", is any missing, "\n")
print(rows with missing)
# Delete the column named "car"
data <- subset(data, select = -car)
num rows <- nrow(data)</pre>
num cols <- ncol(data)
print(num rows)
print(num cols)
colnames(data)
# Data Quality
```

```
#CoffeeShop imputation and all other variables
# Replace missing values with mode for each column
data$Bar <- ifelse(is.na(data$Bar), names(sort(-table(data$Bar)))[1], data$Bar)
data$CoffeeShop <- ifelse(is.na(data$CoffeeShop), names(sort(-table(data$CoffeeShop)))[1],
data$CoffeeShop)
data$TakeAway <- ifelse(is.na(data$TakeAway), names(sort(-table(data$TakeAway)))[1],
data$TakeAway)
data$RestaurantLessThan20 <- ifelse(is.na(data$RestaurantLessThan20), names(sort(-
table(data$RestaurantLessThan20)))[1], data$RestaurantLessThan20)
data$Restaurant20To50 <- ifelse(is.na(data$Restaurant20To50), names(sort(-
table(data$Restaurant20To50)))[1], data$Restaurant20To50)
data$education <- ifelse(is.na(data$education), names(sort(-table(data$education)))[1], data$education)
#Visualisations
# Load necessary libraries
library(ggplot2)
# Create a bar plot
ggplot(data, aes(x = destination, y = accepted)) +
 geom bar(stat = "identity", fill = "blue") +
 labs(title = "Bar Plot: Integer Variable vs Categorical Variable",
    x = "Destination",
    y = "Accepted")
# Create a bar plot to check unique value count in the column
ggplot(data, aes(x = accepted)) +
 geom bar(fill = "steelblue") +
 labs(title = "Count of Unique Values in Column",
    x = "Unique Values",
    y = "Count")
# Create the bar plot
```

```
bar plot <- ggplot(data, aes(x = gender, fill = factor(accepted))) +
 geom bar() +
 labs(x = "Gender", y = "Count", fill = "Accepted") +
 ggtitle("Bar Plot: Gender and Accepted")
# Display the plot
print(bar plot)
# Create the bar plot
bar plot \leftarrow ggplot(data, aes(x = occupation, fill = factor(accepted))) +
 geom_bar() +
 labs(x = "Occupation", y = "Count", fill = "Accepted") +
 ggtitle("Bar Plot: occupation and Accepted")
# Display the plot
print(bar plot)
# Create the vertical bar chart
vertical bar chart <- ggplot(data, aes(x = income, fill = factor(accepted))) +
 geom bar() +
 coord flip() +
 labs(x = "Count", y = "Income", fill = "Accepted") +
 ggtitle("Vertical Bar Chart: Income and Accepted")
# Display the chart
print(vertical bar chart)
# Load necessary libraries
library(ggplot2)
# Binarize 'accepted' column based on the threshold (0.5)
```

```
data\accepted bin <- ifelse(data\accepted >= 0.5, 1, 0)
# Create a bar plot to check the count of binary values in the column
ggplot(data, aes(x = factor(accepted bin), fill = factor(accepted bin))) +
 geom bar() +
 labs(title = "Count of Binary Values in Column",
    x = "Binary Values (0 or 1)",
    y = "Count") +
 scale fill manual(values = c("darkblue", "lightblue")) +
 scale x discrete(labels = c("0", "1"))
#as our data is categorical, we need to use encoding techniques to convert them in integers
# Load necessary libraries
library(dplyr)
# Function to perform label encoding on a single column
label encode <- function(x) {
 factor(x, levels = unique(x))
}
# Identify categorical columns (assuming all non-numeric columns are categorical)
categorical columns <- names(data)[sapply(data, is.character)]
# Perform label encoding on all categorical columns
data[categorical columns] <- lapply(data[categorical columns], label encode)
# Apply as.numeric on the encoded factors
data[categorical columns] <- lapply(data[categorical columns], as.numeric)
# Print the encoded data
print(data)
```

```
# Create a sample data frame
df <- data
# Calculate the correlation matrix
cor matrix <- cor(df)
cor matrix
# Sample data (Assuming all columns are integers)
data <- data
# Find columns with zero variance
zero_variance_columns <- sapply(data, function(col) length(unique(col)) == 1)
# Remove columns with zero variance
data <- data[, !zero variance columns]
# Calculate the correlation matrix
cor matrix <- cor(data)
# Create a heatmap of the correlation matrix
heatmap(cor matrix,
    cmap = colorRampPalette(c("blue", "white", "red"))(100),
    main = "Correlation Heatmap",
    xlab = "Variables",
    ylab = "Variables"
)
colnames(data)
# Load the corrplot package
library(corrplot)
```

```
testing hypothesis <- c('destination', 'maritalStatus', 'age', 'toCoupon_GE15', 'expires', 'accepted')
hypo test <- data[,testing hypothesis]
# hypo test
# Perform the chi-squared test
chisq.test(table(hypo test$destination, hypo test$accepted))
# Perform the chi-squared test
chisq.test(table(hypo test$maritalStatus, hypo test$accepted))
# Perform the chi-squared test
chisq.test(table(hypo test$age, hypo test$accepted))
# Perform the chi-squared test
chisq.test(table(hypo test$toCoupon GE15, hypo test$accepted))
# Perform the chi-squared test
chisq.test(table(hypo test$expires, hypo test$accepted))
# Load required libraries
library(stats)
# Variables for chi-squared test (excluding 'accepted' as it's the dependent variable)
independent vars <- c('destination', 'maritalStatus', 'age', 'toCoupon GE15', 'expires')
# Perform chi-squared test for each variable against 'accepted'
p values <- sapply(independent vars, function(var) {</pre>
 chisq result <- chisq.test(data[, var], data$accepted)
 chisq result$p.value
})
```

```
result df <- data.frame(variable = independent vars, p value = p values)
# Print the result
print(result df)
# Select only the numeric variables
numeric vars <-
c('destination', 'passengers', 'weather', 'temp', 'time', 'coupon', 'expires', 'gender', 'age', 'maritalStatus', 'has childr
en','education','occupation','income','Bar','CoffeeShop','TakeAway','RestaurantLessThan20','Restaurant20T
o50','toCoupon GE15','toCoupon GE25','direction same','direction opp')
numeric data <- data[, numeric vars]
# Calculate the correlation coefficients
correlation <- cor(numeric data, data$accepted)
# Calculate the p-values
p values <- sapply(numeric vars, function(var) cor.test(numeric data[[var]], data$accepted)$p.value)
# Create a dataframe to store the results
association data <- data.frame(Variable = numeric vars,
                   Correlation = correlation,
                   P Value = p values)
# Print the dataframe
print(association data)
# Plot scatter plots
library(ggplot2)
# Create a subset with specific columns
```

Combine the variable names and p-values into a data frame

```
selected columns <-
c('destination', 'age', 'weather', 'time', 'coupon', 'expires', 'marital Status', 'occupation', 'income', 'Bar', 'Coffee Shop
','TakeAway','toCoupon GE15','toCoupon GE25','direction same','direction opp','accepted')
subset data <- data[, selected columns]
# Print the subset data
head(subset data)
# Modelling
### model 1
# Load necessary libraries
library(dplyr)
library(caret)
# Sample data with independent and dependent variables
data <- subset data
# Define the independent variables
independent vars <- c(
 'destination', 'weather', 'time', 'coupon', 'expires',
 'maritalStatus', 'occupation', 'income', 'Bar', 'CoffeeShop',
 'TakeAway', 'toCoupon GE15', 'toCoupon GE25', 'direction same'
dependent var <- 'accepted'
# Perform train-test split (80% train data, 20% test data)
set.seed(40389123) # For reproducibility
train indices <- sample(nrow(data), 0.8 * nrow(data))
train data <- data[train indices,]
test data <- data[-train indices, ]
```

```
# Convert dependent variable to factor
train data[[dependent var]] <- as.factor(train data[[dependent var]])
test data[[dependent var]] <- as.factor(test data[[dependent var]])
### Logistic regression
# Build a logistic regression model
model1 <- glm(formula = paste(dependent var, paste(independent vars, collapse = '+'), sep = '~'),
        data = train data, family = binomial)
summary(model1)
# Load necessary libraries
library(caret)
# Make predictions on the test data using the trained model
predictions <- predict(model1, newdata = test_data, type = "response")</pre>
# Convert probabilities to binary labels (0 or 1) based on a threshold (e.g., 0.5)
predicted labels <- ifelse(predictions >= 0.5, 1, 0)
# Convert predicted labels to factor with the same levels as the dependent variable
predicted labels <- factor(predicted labels, levels = levels(test data[[dependent var]]))
# Evaluate the model
confusion matrix <- confusionMatrix(data = predicted labels, reference = test data[[dependent var]])
# Print the confusion matrix
print(confusion matrix)
# Print classification metrics
```

```
print(paste("Accuracy:", confusion matrix$overall["Accuracy"]))
print(paste("Precision:", confusion matrix$byClass["Precision"]))
print(paste("Recall:", confusion_matrix$byClass["Recall"]))
print(paste("F1 Score:", confusion matrix$byClass["F1"]))
# model 2
# Load necessary libraries
library(dplyr)
library(caret)
# Sample data with independent and dependent variables
data <- subset data
# Define the independent variables
independent vars <- c(
 'destination', 'weather', 'coupon', 'expires',
 'maritalStatus', 'income', 'toCoupon GE15'
dependent var <- 'accepted'
# Perform train-test split (80% train data, 20% test data)
set.seed(40389123) # For reproducibility
train indices <- sample(nrow(data), 0.8 * nrow(data))
train data <- data[train indices, ]
test_data <- data[-train_indices, ]</pre>
# Convert dependent variable to factor
```

```
train data[[dependent var]] <- as.factor(train data[[dependent var]])
test data[[dependent var]] <- as.factor(test data[[dependent var]])
# Build a logistic regression model
model2 <- glm(formula = paste(dependent var, paste(independent vars, collapse = '+'), sep = '~'),
        data = train data, family = binomial)
summary(model2)
# Load necessary libraries
library(caret)
# Make predictions on the test data using the trained model
predictions <- predict(model2, newdata = test data, type = "response")</pre>
# Convert probabilities to binary labels (0 or 1) based on a threshold (e.g., 0.5)
predicted labels <- ifelse(predictions >= 0.5, 1, 0)
# Convert predicted labels to factor with the same levels as the dependent variable
predicted labels <- factor(predicted labels, levels = levels(test data[[dependent var]]))
# Evaluate the model
confusion matrix <- confusionMatrix(data = predicted labels, reference = test data[[dependent var]])
# Print the confusion matrix
print(confusion matrix)
# Print classification metrics
print(paste("Accuracy:", confusion matrix$overall["Accuracy"]))
print(paste("Precision:", confusion matrix$byClass["Precision"]))
```

```
print(paste("Recall:", confusion matrix$byClass["Recall"]))
print(paste("F1 Score:", confusion matrix$byClass["F1"]))
# Model 3
# Load necessary libraries
library(dplyr)
library(caret)
# Sample data with independent and dependent variables
data <- subset data
# Define the independent variables
independent vars <- c(
 'destination', 'expires', 'age', 'maritalStatus', 'toCoupon GE15'
)
dependent var <- 'accepted'
# Perform train-test split (80% train data, 20% test data)
set.seed(40389123) # For reproducibility
train indices <- sample(nrow(data), 0.8 * nrow(data))
train data <- data[train indices, ]
test data <- data[-train indices, ]
# Convert dependent variable to factor
train data[[dependent var]] <- as.factor(train data[[dependent var]])
test data[[dependent var]] <- as.factor(test data[[dependent var]])
```

```
# Build a logistic regression model
model3 <- glm(formula = paste(dependent var, paste(independent vars, collapse = '+'), sep = '~'),
        data = train data, family = binomial)
summary(model3)
# Load necessary libraries
library(caret)
# Make predictions on the test data using the trained model
predictions <- predict(model3, newdata = test_data, type = "response")</pre>
# Convert probabilities to binary labels (0 or 1) based on a threshold (e.g., 0.5)
predicted labels <- ifelse(predictions >= 0.5, 1, 0)
# Convert predicted labels to factor with the same levels as the dependent variable
predicted labels <- factor(predicted labels, levels = levels(test data[[dependent var]]))
# Evaluate the model
confusion matrix <- confusionMatrix(data = predicted labels, reference = test data[[dependent var]])
# Print the confusion matrix
print(confusion matrix)
# Print classification metrics
print(paste("Accuracy:", confusion matrix$overall["Accuracy"]))
print(paste("Precision:", confusion matrix$byClass["Precision"]))
print(paste("Recall:", confusion matrix$byClass["Recall"]))
print(paste("F1 Score:", confusion matrix$byClass["F1"]))
```

```
##Model 1##
# Fitted probabilities
fitted probs model1 <- predict(model1, type = "response")
# Standardized residuals
std resid model1 <- residuals(model1, type = "pearson") / sqrt(1 - model1$fitted.values)
# Check if the proportion of residuals greater than 1.96 is less than 5%
prop large resid model1 <- sum(abs(std resid model1) > 1.96) / length(std resid model1)
print(paste("Proportion of residuals greater than 1.96:", prop_large_resid_model1))
# Variance inflation factors (VIF)
library(car)
vif model1 <- vif(model1)</pre>
print("Variance inflation factors:")
print(vif model1)
# Cook's distance
cook dist model1 <- cooks.distance(model1)</pre>
# Check for any values much larger than 1
outlier threshold <- 1
num large cook dist model1 <- sum(cook dist model1 > outlier threshold)
print(paste("Number of observations with Cook's distance larger than", outlier threshold, ":",
num large cook dist model1))
# Assumption Checks for model2
# Fitted probabilities
fitted probs <- predict(model2, type = "response")
```

```
# Standardized residuals
std_resid <- residuals(model2, type = "pearson") / sqrt(1 - model2$fitted.values)
# Check if the proportion of residuals greater than 1.96 is less than 5%
prop large resid <- sum(abs(std resid) > 1.96) / length(std resid)
print(paste("Proportion of residuals greater than 1.96:", prop large resid))
# Variance inflation factors (VIF)
library(car)
vif model2 <- vif(model2)
print("Variance inflation factors:")
print(vif model2)
# Cook's distance
cook dist <- cooks.distance(model2)</pre>
# Check for any values much larger than 1
outlier threshold <- 1
num large cook dist <- sum(cook dist > outlier threshold)
print(paste("Number of observations with Cook's distance larger than", outlier threshold, ":",
num large cook dist))
#checking assumtions### for model 3
# Standardized residuals
std resid <- residuals(model3, type = "pearson") / sqrt(1 - model3$fitted.values)
# Check if the proportion of residuals greater than 1.96 is less than 5%
```

```
prop_large_resid <- sum(abs(std_resid) > 1.96) / length(std_resid)

print(paste("Proportion of residuals greater than 1.96:", prop_large_resid))

# Variance inflation factors (VIF)

library(car)

vif_model3 <- vif(model3)

print("Variance inflation factors:")

print(vif_model3)

# Cook's distance

cook_dist <- cooks.distance(model3)

# Check for any values much larger than 1

outlier_threshold <- 1

num_large_cook_dist <- sum(cook_dist > outlier_threshold)

print(paste("Number of observations with Cook's distance larger than", outlier_threshold, ":", num_large_cook_dist))
```