

Lab 1

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This lab is due 11:59 PM Saturday 2/9/19.

You should have RStudio installed to edit this file. You will write code in places marked “TO-DO” to complete the problems. Some of this will be a pure programming assignment. The tools for the solutions to these problems can be found in the class practice lectures. I want you to use the methods I taught you, not for you to google and come up with whatever works. You won’t learn that way.

To “hand in” the homework, you should compile or publish this file into a PDF that includes output of your code. Once it’s done, push by the deadline to your repository in a directory called “labs”.

- Print out the numerical constant pi with ten digits after the decimal point using the internal constant pi.

```
options(digits=11)
pi
```

```
## [1] 3.1415926536
```

```
options(digits=7)
```

- Sum up the first 100 terms of the series $1 + 1/2 + 1/4 + 1/8 + \dots$

```
sum((1/2)^(0:99))
```

```
## [1] 2
```

- Find the product of the first 100 terms of $1 * 1/2 * 1/4 * 1/8 * \dots$

```
prod((1/2)^(0:99))
```

```
## [1] 0
```

- Find the product of the first 500 terms of $1 * 1/2 * 1/4 * 1/8 * \dots$. Answer in English: is this answer correct?

```
prod((1/2)^(0:499))
```

```
## [1] 0
```

```
"Nope, numerical underflow"
```

```
## [1] "Nope, numerical underflow"
```

- Figure out a means to express the answer more exactly. Not compute exactly, but express more exactly.

```
paste("10 e", -log10(2)*sum(0:499))
```

```
## [1] "10 e -37553.4919590817"
```

- Use the left rectangle method to numerically integrate x^2 from 0 to 1 with rectangle size $1e-6$.

```
sum(seq(0,1,by=(1e-6))^2)*(1e-6)
```

```
## [1] 0.3333338
```

- Calculate the average of 100 realizations of standard Bernoullis in one line using the `sample` function.

```
sum(sample((0:1),100,replace = TRUE))/100
```

```
## [1] 0.43
```

- Calculate the average of 500 realizations of Bernoullis with $p = 0.9$ in one line using the `sample` function.

```
sum(sample(c(0,1,1,1,1,1,1,1,1,1),500,replace=TRUE))/500
```

```
## [1] 0.91
```

- Calculate the average of 1000 realizations of Bernoullis with $p = 0.9$ in one line using `rbinom`.

```
sum(rbinom(1000,1,0.9))/1000
```

```
## [1] 0.879
```

- Use the `strsplit` function and `sample` to put the sentences below in random order.

```
lorem = "Lorem ipsum dolor sit amet, consectetur adipiscing elit. Morbi posuere varius volutpat. Morbi :  
paste(paste(sample(unlist(strsplit(lorem,"[.] "))), collapse = ". "), ".", sep = "")
```

```
## [1] "Lorem ipsum dolor sit amet, consectetur adipiscing elit. Donec at tempor erat. Aenean nulla ant
```

- In class we generated the variable criminality with levels “none”, “infraction”, “misdemeanor” and “felony”. Create a variable `x_2` here with 100 random elements (equally probable) and ensure the proper ordinal ordering.

```
y=c("none", "infraction", "misdemeanor", "felony")  
x_2 = factor(sample(y,100,replace = TRUE),levels = c("none", "infraction", "misdemeanor", "felony"), or  
x_2
```

```
## [1] felony      infraction    misdemeanor  misdemeanor  infraction  
## [6] infraction    felony        infraction   none         none  
## [11] none          infraction    misdemeanor  none         misdemeanor  
## [16] none          none          none         misdemeanor  infraction  
## [21] none          misdemeanor  felony       none         infraction  
## [26] infraction    infraction    misdemeanor  none         misdemeanor  
## [31] misdemeanor  none          none         felony       felony  
## [36] misdemeanor  misdemeanor  infraction    misdemeanor  felony  
## [41] none          none          misdemeanor  none         felony  
## [46] none          infraction    infraction    none         infraction  
## [51] infraction    none          felony       misdemeanor  none  
## [56] none          infraction    none         felony       none  
## [61] felony       none          misdemeanor  infraction    infraction  
## [66] none          felony        infraction    felony       felony  
## [71] felony       none          none         infraction    misdemeanor  
## [76] none          misdemeanor  felony       misdemeanor  misdemeanor  
## [81] misdemeanor  infraction    misdemeanor  misdemeanor  felony  
## [86] none          none          infraction    infraction    misdemeanor  
## [91] none          none          infraction    misdemeanor  none  
## [96] infraction    felony        misdemeanor  misdemeanor  infraction  
## Levels: none < infraction < misdemeanor < felony
```

- Convert this variable to binary where 0 is no crime and 1 is any crime. Answer in English: is this the proper binary threshold?

```
x_3=as.numeric(x_2!="none")  
"No, it doesn't appropriately inform the proclivity to pay back."
```

```
## [1] "No, it doesn't appropriately inform the proclivity to pay back."
```

```
#I'm a bit concerned I have the wrong idea about the binary threshold.
```

- Convert this variable to an unordered, nominal factor variable.

```
#if converting binary to nominal
#for(index in 1:length(x_3)){
#   if(x_3[index]==1){
#     x_3[index] = "crime"
#   }else{
#     x_3[index] = "no crime"
#   }
#}
#x_3
#if converting from ordinal to nominal
factor(x_2,ordered = FALSE)
```

```
##   [1] felony      infraction  misdemeanor misdemeanor infraction
##   [6] infraction  felony      infraction  none         none
##  [11] none        infraction  misdemeanor none         misdemeanor
##  [16] none        none        none         misdemeanor infraction
##  [21] none        misdemeanor felony      none         infraction
##  [26] infraction  infraction  misdemeanor none         misdemeanor
##  [31] misdemeanor none        none         felony       felony
##  [36] misdemeanor misdemeanor infraction  misdemeanor felony
##  [41] none        none        misdemeanor none         felony
##  [46] none        infraction infraction  none         infraction
##  [51] infraction  none        felony      misdemeanor none
##  [56] none        infraction none         felony       none
##  [61] felony      none        misdemeanor infraction  infraction
##  [66] none        felony      infraction  felony       felony
##  [71] felony      none        none         infraction  misdemeanor
##  [76] none        misdemeanor felony      misdemeanor misdemeanor
##  [81] misdemeanor infraction misdemeanor misdemeanor felony
##  [86] none        none        infraction  infraction  misdemeanor
##  [91] none        none        infraction  misdemeanor none
##  [96] infraction  felony      misdemeanor misdemeanor infraction
## Levels: none infraction misdemeanor felony
```

- Convert this variable into three binary variables without any information loss and put them into a data matrix.

```
#create level vectors
msdmnr = c()
infrctn = c()
flny = c()
# assign appropriate binary value
for(instance in x_2){
  flny = c(flny, as.numeric(instance == "felony"))

  msdmnr = c(msdmnr, as.numeric(instance == "misdemeanor"))

  infrctn = c(infrctn, as.numeric(instance == "infraction"))
}
#columns correspond to order listed in the following function. If row is composed of zeroes, no crim hi.
x_4 = matrix(c(infrctn,msdmnr,flny),100,3)
x_4
```

```
##           [,1] [,2] [,3]
```

##	[1,]	0	0	1
##	[2,]	1	0	0
##	[3,]	0	1	0
##	[4,]	0	1	0
##	[5,]	1	0	0
##	[6,]	1	0	0
##	[7,]	0	0	1
##	[8,]	1	0	0
##	[9,]	0	0	0
##	[10,]	0	0	0
##	[11,]	0	0	0
##	[12,]	1	0	0
##	[13,]	0	1	0
##	[14,]	0	0	0
##	[15,]	0	1	0
##	[16,]	0	0	0
##	[17,]	0	0	0
##	[18,]	0	0	0
##	[19,]	0	1	0
##	[20,]	1	0	0
##	[21,]	0	0	0
##	[22,]	0	1	0
##	[23,]	0	0	1
##	[24,]	0	0	0
##	[25,]	1	0	0
##	[26,]	1	0	0
##	[27,]	1	0	0
##	[28,]	0	1	0
##	[29,]	0	0	0
##	[30,]	0	1	0
##	[31,]	0	1	0
##	[32,]	0	0	0
##	[33,]	0	0	0
##	[34,]	0	0	1
##	[35,]	0	0	1
##	[36,]	0	1	0
##	[37,]	0	1	0
##	[38,]	1	0	0
##	[39,]	0	1	0
##	[40,]	0	0	1
##	[41,]	0	0	0
##	[42,]	0	0	0
##	[43,]	0	1	0
##	[44,]	0	0	0
##	[45,]	0	0	1
##	[46,]	0	0	0
##	[47,]	1	0	0
##	[48,]	1	0	0
##	[49,]	0	0	0
##	[50,]	1	0	0
##	[51,]	1	0	0
##	[52,]	0	0	0
##	[53,]	0	0	1
##	[54,]	0	1	0

```
## [55,] 0 0 0
## [56,] 0 0 0
## [57,] 1 0 0
## [58,] 0 0 0
## [59,] 0 0 1
## [60,] 0 0 0
## [61,] 0 0 1
## [62,] 0 0 0
## [63,] 0 1 0
## [64,] 1 0 0
## [65,] 1 0 0
## [66,] 0 0 0
## [67,] 0 0 1
## [68,] 1 0 0
## [69,] 0 0 1
## [70,] 0 0 1
## [71,] 0 0 1
## [72,] 0 0 0
## [73,] 0 0 0
## [74,] 1 0 0
## [75,] 0 1 0
## [76,] 0 0 0
## [77,] 0 1 0
## [78,] 0 0 1
## [79,] 0 1 0
## [80,] 0 1 0
## [81,] 0 1 0
## [82,] 1 0 0
## [83,] 0 1 0
## [84,] 0 1 0
## [85,] 0 0 1
## [86,] 0 0 0
## [87,] 0 0 0
## [88,] 1 0 0
## [89,] 1 0 0
## [90,] 0 1 0
## [91,] 0 0 0
## [92,] 0 0 0
## [93,] 1 0 0
## [94,] 0 1 0
## [95,] 0 0 0
## [96,] 1 0 0
## [97,] 0 0 1
## [98,] 0 1 0
## [99,] 0 1 0
## [100,] 1 0 0
```

- What should the sum of each row be (in English)? Verify that.

```
"The sum of each row should be equal to 0 or 1, depending on the existence of criminal history"
```

```
## [1] "The sum of each row should be equal to 0 or 1, depending on the existence of criminal history"
```

```
for(i in (1:100)){
  if(!(sum(x_4[i,]) == 1 | sum(x_4[i,]) == 0)){
    stop("Sum of row is not 0 or 1")
  }
}
```

```

    }
  }
  print(TRUE)

```

```
## [1] TRUE
```

- How should the column sum look (in English)? Verify that.

```
"The column sum should be between 0 and 100, though it will likely be around 25 since all 4 outcomes are
```

```
## [1] "The column sum should be between 0 and 100, though it will likely be around 25 since all 4 outcomes are
```

```

sumCol1 = sum(x_4[,1])
sumCol2 = sum(x_4[,2])
sumCol3 = sum(x_4[,3])
nones=100-sum(sumCol1,sumCol2,sumCol3)
print(paste("Sum of column 1 is less than 100 and greater than 0: ",(sumCol1 > 0 && sumCol1 < 100)))

```

```
## [1] "Sum of column 1 is less than 100 and greater than 0: TRUE"
```

```
print(paste("Sum of column 2 is less than 100 and greater than 0: ",(sumCol2 > 0 && sumCol2 < 100)))
```

```
## [1] "Sum of column 2 is less than 100 and greater than 0: TRUE"
```

```
print(paste("Sum of column 3 is less than 100 and greater than 0: ",(sumCol3 > 0 && sumCol3 < 100)))
```

```
## [1] "Sum of column 3 is less than 100 and greater than 0: TRUE"
```

- Generate a matrix with 100 rows where the first column is realization from a normal with mean 17 and variance 38, the second column is uniform between -10 and 10, the third column is poisson with mean 6, the fourth column is exponential with lambda of 9, the fifth column is binomial with n = 20 and p = 0.12 and the sixth column is a binary variable with 24% 1's.

```

y = matrix(c(rnorm(100,17,38),runif(100,-10,10),rpois(100,6),rexp(100,6),rbinom(100,20,.12),sample(c(c(
y

```

```

##           [,1]      [,2] [,3]      [,4] [,5] [,6]
## [1,]  48.1430292  3.1698593    3 0.212683025    0    0
## [2,]  83.5049455 -7.6844535    5 0.206588366    2    0
## [3,]  11.3714642  2.0583412    7 0.225542315    4    0
## [4,]  82.2744792 -3.2612535    9 0.197403248    1    0
## [5,] -21.1017262 -7.0628280    5 0.087423046    2    1
## [6,]  -3.3684629  4.9960593    0 0.586893787    1    1
## [7,]  45.8265133  7.5636526    4 0.099993632    0    0
## [8,] -29.3986845  1.7893580    3 0.098861584    2    0
## [9,]  15.9569871 -4.1495855    7 0.468270345    1    1
## [10,] 48.7339727  3.1591708    5 0.342233479    0    0
## [11,] 63.0436185 -8.7232064    3 0.236525753    2    1
## [12,] -19.4225013 -1.0244633    7 0.109144047    2    1
## [13,] -24.2345300  1.9490713    7 0.053467992    3    1
## [14,]  -9.0942130  5.1475284    8 0.214685222    2    0
## [15,] -12.1726942 -4.9928132    4 0.158168468    2    0
## [16,]   3.2278016  6.1440970    9 0.017971820    6    0
## [17,] -37.4015800 -2.3615438    9 0.099573719    2    0
## [18,]  17.7022401 -4.0550228    7 0.249941372    5    0
## [19,]  33.9733891  7.9406918    9 0.361386696    0    0
## [20,]  52.4052033  8.9505159    6 0.059507507    3    0
## [21,] 119.3070884  1.3162027    8 0.055698742    4    1

```

##	[22,]	-11.4015365	9.5503022	7	0.088927229	5	0
##	[23,]	45.9205155	-9.3749536	8	0.001905976	1	1
##	[24,]	44.9232525	-2.4052832	6	0.281959965	1	0
##	[25,]	-9.4514858	3.1883660	6	0.090045903	1	0
##	[26,]	60.3947649	-2.3932643	7	0.031530863	1	1
##	[27,]	25.8524287	1.7663256	5	0.248584054	3	0
##	[28,]	59.9410370	-9.6416085	2	0.075504153	3	1
##	[29,]	19.4064053	7.4404462	7	0.010987456	2	0
##	[30,]	19.1471225	4.8782985	7	0.412132324	1	0
##	[31,]	19.9046562	-1.7968123	5	0.314405829	3	0
##	[32,]	24.1018526	0.1834998	5	0.164021527	3	0
##	[33,]	21.8446439	0.4294380	10	0.229544390	1	1
##	[34,]	22.1317453	-3.6786202	10	0.083557108	2	0
##	[35,]	101.0223912	6.3076633	5	0.599970828	2	0
##	[36,]	50.5747712	-3.7540650	4	0.109292756	3	0
##	[37,]	-25.7304999	-1.3778161	7	0.014947046	2	0
##	[38,]	9.2599091	-0.5576643	7	0.254059994	1	1
##	[39,]	39.3466147	0.4600024	4	0.216980529	4	0
##	[40,]	5.9422123	-2.2149208	5	0.090788996	3	0
##	[41,]	132.8102400	1.6492225	7	0.211844496	3	0
##	[42,]	-2.3826510	2.7216480	5	0.079368532	3	0
##	[43,]	3.1812527	7.4483995	6	0.063330268	1	0
##	[44,]	75.1315612	7.7204373	6	0.305679578	5	0
##	[45,]	-3.6976954	-0.1214477	8	0.804033233	1	1
##	[46,]	41.4554162	1.2415721	6	0.180999642	2	0
##	[47,]	-32.2677138	8.0918031	10	0.015197762	6	0
##	[48,]	8.6186154	-9.7487193	8	0.022745948	3	0
##	[49,]	16.4584408	1.1113568	5	0.040318638	2	0
##	[50,]	13.8856585	-4.0748206	5	0.065166328	0	1
##	[51,]	-1.0857766	0.9676041	9	0.541694040	4	0
##	[52,]	32.9840461	-1.8004526	5	0.634044964	0	0
##	[53,]	53.7940701	-8.3443292	5	0.013882163	3	0
##	[54,]	26.4520786	-1.8942290	5	0.333848502	4	0
##	[55,]	-0.1481111	8.4598749	2	0.199615145	0	1
##	[56,]	-24.7662111	-3.0088421	6	0.114023050	0	0
##	[57,]	12.4387246	-5.3000560	6	0.428846551	4	0
##	[58,]	0.7672397	-4.5653742	5	0.103988953	0	1
##	[59,]	62.6780110	4.7866920	6	0.204684893	3	0
##	[60,]	90.0647514	9.2279339	6	0.055142135	3	1
##	[61,]	-23.2729208	-7.1021284	6	0.108902142	1	1
##	[62,]	-9.5652954	-6.6763619	6	0.247014378	2	0
##	[63,]	53.5046229	-5.4596357	5	0.199275442	2	1
##	[64,]	3.7936526	3.3277803	2	0.632693220	6	0
##	[65,]	12.3141368	3.2244027	5	0.112429765	2	0
##	[66,]	-44.8680596	-0.7981700	5	0.061340523	4	0
##	[67,]	18.8909771	-5.7127703	2	0.028405868	2	0
##	[68,]	36.7810066	8.1851450	5	0.029967511	2	0
##	[69,]	46.7413118	5.7027082	5	0.020484788	4	0
##	[70,]	-12.0523036	-8.0822428	2	0.168758113	4	0
##	[71,]	29.6002659	9.3383025	7	0.083647604	2	0
##	[72,]	26.3170366	0.5993754	8	0.261363487	0	1
##	[73,]	59.3033010	2.9837055	6	0.176530490	4	0
##	[74,]	40.5123747	-0.5950302	6	0.013768228	2	0
##	[75,]	-71.0514039	-0.9135701	2	0.451630064	3	0

##	[76,]	34.4831316	0.4136837	6	0.480954580	2	0
##	[77,]	-2.1353821	-2.4973729	5	0.019363562	1	0
##	[78,]	-2.8761503	-0.8920657	5	0.141183877	2	0
##	[79,]	23.8331186	9.1034300	7	0.195406940	2	0
##	[80,]	76.6398865	-3.5140923	4	0.191840376	2	0
##	[81,]	26.8226961	8.4413865	13	0.242139814	3	0
##	[82,]	-10.3137036	4.4958528	7	0.061839041	3	0
##	[83,]	51.8497048	-4.5286362	9	0.163180926	2	0
##	[84,]	-28.0026358	-7.6434645	10	0.002979791	2	1
##	[85,]	-39.9750790	7.7261454	7	0.018758265	4	0
##	[86,]	-24.9995396	-8.0420404	8	0.475761023	4	0
##	[87,]	4.7863197	0.5904083	6	0.070132082	2	0
##	[88,]	-10.0008550	-6.3034864	2	0.021677439	2	1
##	[89,]	34.0845156	-1.6093452	5	0.154304647	1	0
##	[90,]	13.8809186	-5.1395897	7	0.016318114	1	0
##	[91,]	38.0287397	9.3739368	4	0.091785723	3	0
##	[92,]	-18.3645631	7.5507351	7	0.485419569	1	0
##	[93,]	-2.1267003	7.0683146	6	0.107104988	4	0
##	[94,]	163.2281037	-4.5900027	5	0.051787121	2	1
##	[95,]	24.2271371	-1.3436805	10	0.246174308	1	0
##	[96,]	48.6082167	6.6464817	10	0.193005788	2	0
##	[97,]	-43.7688812	-6.5349047	8	0.033122367	5	0
##	[98,]	-34.3021104	5.6834702	6	0.053131755	4	0
##	[99,]	-25.9333772	5.4396327	5	0.060809941	1	1
##	[100,]	-31.8315675	-1.6918193	6	0.194953517	2	0