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Lec 10 Math 390 4/19/19

New problem... given the same X , then we may transform (a)
of x , (b) many H 's and (c) many A 's all producing
different models $g_1(\tilde{x}), g_2(\tilde{x}), \dots, g_M(\tilde{x})$.

Since all models are approximate, there is no concept
of a "correct" model. But you still need to
choose one to use. This is the fundamental problem
of "Model selection" ^{it's tricky & subtle!!} Since the dawn of time!!

Whole textbooks written on this... e.g. with $p=1$...

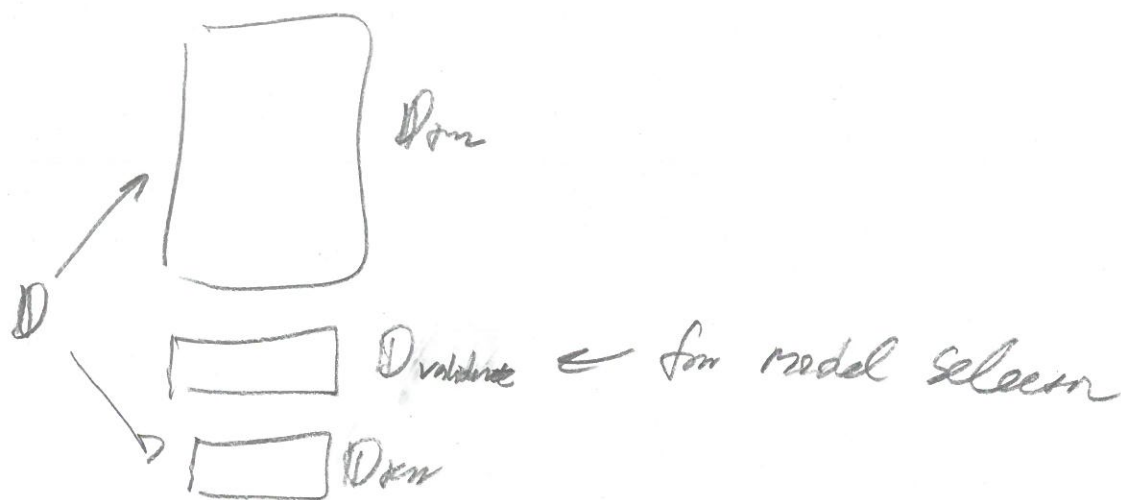
$$g_1(x) = b_0 + b_1 x$$

$$g_2(x) = b_0 + b_1 x + b_2 x^2$$

$$g_3(x) = b_0 + b_1 \ln(x)$$

$$g_4(x) = b_0 + b_1 \mathbb{I}_{x \in [0,1)} + b_2 \mathbb{I}_{x \in [0,2)} + \dots \quad x \text{ is non ordered!}$$

In our class, we will do model selection using one technique. This
is not the only technique....



Procedure:

- ① Fit g_1 using D_{train} and get an ~~error~~ error est on $D_{validation}$
- ② Fit g_2 / / / / /
- ⋮
- ① Fit g_m / / / / /
- ①+1 Locate model m^* with lowest error on $D_{validation}$ (model selection step)
- ①+2 Fit g_{m^*} on $D_{train} \cup D_{validation}$ and get ~~error~~ error on D_{test} .
- ①+3 Fit g_{m^*} on $D = \text{all data}$ and ship.

This also allows for lowest model approximation.