

Math 390.4

01/29/18 ~ Tuesday

"Models" are approximations and/or abstractions to reality/absolute truth/systems/phenomena.

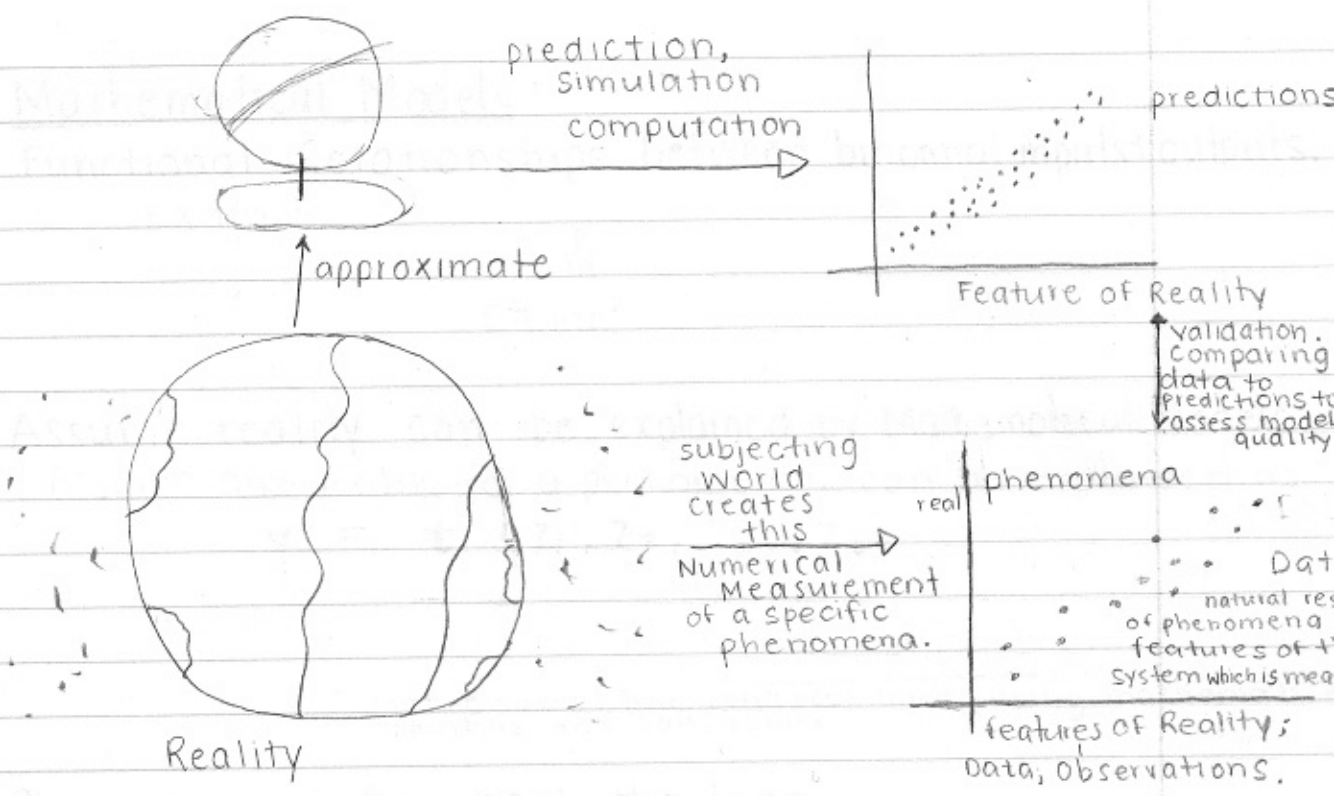
Model	Reality
Model Airplane	Real Airplane
Street Map	Road System
Wind Tunnel	Fast Moving Air
"Early to bed, Early to rise, makes a man healthy, wealthy and wise."	Human Success

"All models are wrong, but some are useful." - George Box
by definition, They serve useful functions for us.
which are technically wrong.

Two main Goals of Models:

1. Prediction: the model will tell us what will happen to a certain phenomena in a certain setting.
2. Explanation: understanding how the universe works.

Example: Dropping piece of chalk
→ Theory of Gravity



Mathematical Models

"Early to bed, Early to rise

Makes a man Healthy, Wealthy, & Wise."

→ BUT TOO AMBIGUOUS!

Variable/Features	Metrics	symbol
• Early to Bed	average bed time in 24hr time (ex: 22h20) - or - as measured by # of minutes after 6pm. (Ex: 268 vs. 363)	b
• Early to Rise	average wake time is... 4am	w
• Health	Longevity in years	l
• Wealth	Networth	n
• wisdom	some sort of test	s

With properly defined inputs/outputs

f is called a
Mathematical Model:

$$\begin{bmatrix} l \\ n \\ s \end{bmatrix}$$

$$\vec{a} = f([L, W])$$

is this true? NO

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dimension of output = 1

phenomena
outputs
Endpoints
dependent
variables
Responses?

Functional Relationships between inputs & outputs model

Features, inputs, attributes, characteristics
independent variables, covariates,
regressors.

Mathematical Models:

Functional Relationships between binomial inputs+outputs.

Example:

$$a = \frac{F}{m}$$

$$E = mc^2$$

Assume reality can be explained by Mathematical Models.

Assume any metric for a phenomenon can be explained as:

$$Y = t(Z_1, Z_2, \dots, Z_t)$$

Y : aim.
phenomenon

Z_1, Z_2, \dots, Z_t : causal inputs

t : the true "function" that "nature" uses to create the phenomenon.
the true function that conduces inputs using mathematical operators and constraints.

Phenomenon: Pay back the loan.

$$Y = \{ \text{pay back, not pay back} \}$$

$$Y \in \{ 0, 1 \} \quad \text{Encoding} = Y \text{ - output}$$

Z_1 : has sufficient funds day before $\in \{0, 1\}$

Z_2 : Criminal intent $\in \{0, 1\}$

Z_3 : Access to Branch $\in \{0, 1\}$

$$Y = t(Z_1, Z_2, Z_3) = Z_1(1 - Z_2)(1 - Z_3)$$

Big Problem: We are totally ignorant of the Z 's
and further we may not know t

Next best thing is to obtain features that approximate the causal information in Z_1, Z_2, \dots, Z_t .

Denote these features X_1, X_2, \dots, X_p .

you want X 's to reflect Z 's.

Ex) X_1 : income, bank account balance

X_2 : prior criminal record

X_3 : Had internet

X_4 : credit score.

* F is the model
 t is the real