

**CS F214**  
**Logic in CS**  
**BITS Pilani, Hyderabad Campus**  
**Assignment -2**  
**Due Date : 17th October 2018 (by Midnight)**  
**Total Marks: 30 (weightage : 10%)**

**Objective:** This assignment is to help you understand that you can design a proof checking engine for rules of natural deduction. There are two parts of the assignment.

**Part-I:**

You have to implement the construction of a parse tree for a propositional logic formula. You can assume that the formula is well formed and fully parenthesized. The input to your program should be a propositional logical formula in infix notation. The connective symbols you will use for this assignment is as follows.

1.  $\sim$  for negation
2.  $\vee$  for OR
3.  $\wedge$  for AND
4.  $\supset$  for implication.

Your code should have **separate functions** to perform the given tasks.

**Task 1:**

Write a function to **convert the infix** propositional logic expression **into a postfix** propositional logic expression. [5]

**Task 2:**

Write a function to **convert the postfix expression into a rooted binary parse tree.** [5]

**Task 3:**

Write a function to traverse the parse tree to **output the infix expression** back by in-order traversal of the parse tree. [5]

Once you have made a parse tree, you should be able to verify that a given formula is well formed.

**Part II:**

A tool for verifying whether a certain proof of a given sequent is valid or not. Allowed proof rules are :

- |                                 |     |
|---------------------------------|-----|
| 1. Premise                      | [1] |
| 2. AND introduction/elimination | [4] |
| 3. OR introduction              | [5] |
| 4. IMPLIES elimination          | [5] |
| Extra credit for : MT           | [3] |

**Definitions:**

$\langle \text{statement} \rangle ::= p \mid \neg p \mid \neg(\langle \text{statement} \rangle) \mid (\langle \text{statement} \rangle \wedge \langle \text{statement} \rangle) \mid (\langle \text{statement} \rangle \vee \langle \text{statement} \rangle) \mid (\langle \text{statement} \rangle \rightarrow \langle \text{statement} \rangle)$

$\langle \text{rule} \rangle ::= \wedge i \mid \wedge e1 \mid \wedge e2 \mid \vee i1 \mid \vee i2 \mid \rightarrow e \mid P$

**Input:**

First line:

n (number of statements)

Next n lines:

$\langle \text{statement} \rangle / \langle \text{rule} \rangle [ / \text{line1} [ / \text{line2} ] ]$  (parameter in [] is optional whose existence will be determined by  $\langle \text{rule} \rangle$ )

**Output:**

Valid Proof (or) Invalid Proof

**Assumptions:**

1. Line number starts from 1.
2.  $\langle \text{statement} \rangle$  should be perfectly parenthesized, e.g.  $((a \wedge b) \wedge c)$  is valid,  $(a \wedge b) \wedge c$  is invalid,  $((a \wedge b))$  is invalid,  $(a \wedge b)$  is valid,  $(a \wedge b \wedge c)$  is invalid,  $p$  is valid,  $(p)$  is invalid.
3.  $\neg$  can be succeeded by a literal or '(' only.

**Sample test case:****Input:**

3  
a/P  
b/P  
 $(a \wedge b) / \wedge i / 1 / 2$

**Output:** Valid Proof

**General Instructions:**

1. This assignment will be done in groups of max three students.
2. **Enter your team details in Google spreadsheet shared.**
3. **Code must be written in C/C++ language and gcc compiler only.**
4. **The details of how to submit the code will be given later.**
5. **You can discuss with your friends but refrain from copying the code and submitting. Also please do not use code downloaded from internet. Such codes will receive 0 credits.**
6. **You have to demo the code to the instructor on a scheduled date and timing after submission. It is important to attend the demo, as absence from demo will amount to no credit for the assignment.**

7. Copied codes will receive no credits. No arguments will be entertained such as who copied from whom. All involved parties will get 0 credit.

**References to look into:**

[http://scanfree.com/Data\\_Structure/infix-to-prefix](http://scanfree.com/Data_Structure/infix-to-prefix)

Algorithms in C++ by Robert Sedgewick