| Transformation Name | Affine Matrix, A | Coordinate Equations | Example |
|---|--|---|-----------|
| Identity | $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ | x' = x $y' = y$ | y' |
| Scaling/Reflection (For reflection, set one scaling factor to -1 and the other to 0) | $egin{bmatrix} c_x & 0 & 0 \ 0 & c_y & 0 \ 0 & 0 & 1 \end{bmatrix}$ | $x' = c_x x$ $y' = c_y y$ | x' |
| Rotation (about the origin) | $\begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$ | $x' = x \cos \theta - y \sin \theta$ $y' = x \sin \theta + y \cos \theta$ | x' |
| Translation | $\begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix}$ | $x' = x + t_x$ $y' = y + t_y$ | x' |
| Shear (vertical) | $egin{bmatrix} 1 & s_v & 0 \ 0 & 1 & 0 \ 0 & 0 & 1 \end{bmatrix}$ | $x' = x + s_v y$ $y' = y$ | y' x' |
| Shear (horizontal) | $\begin{bmatrix} 1 & 0 & 0 \\ s_h & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ | $x' = x$ $y' = s_h x + y$ | <i>x'</i> |