

Combinatorial Testing

Part A

Dr Fani Deligianni,

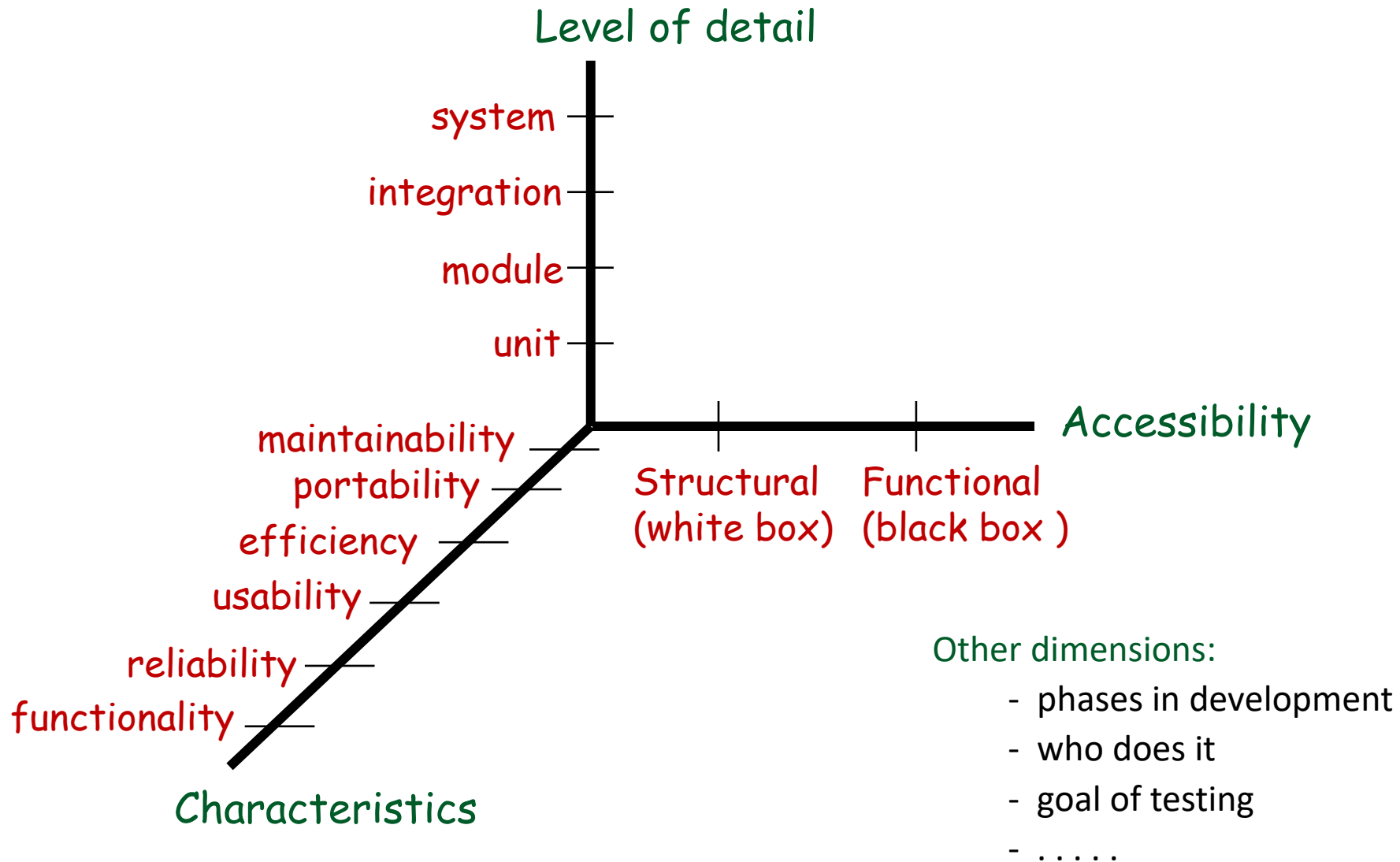
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Learning Objectives

1. Understand and apply different software testing techniques:
 - Exhaustive Testing
 - Random Testing
 - Partition Testing
 - Boundary Value Testing
2. Understand the two main techniques in Input Domain Modelling
 - Learn and apply a systematic approach to functional testing
 - Apply the category-partition method for generation of test cases.

Dimensions of Testing – Previous Lecture



Functional Specification

- Statement of the application functional and operational requirements.
- It serves as a contract between the developer and the customer for whom the system is being developed.

Functional (Black-Box) Testing

- ▶ Advantages:
 - ▶ Focus on the domain
 - ▶ No need for the code - Makes early test design possible
 - ▶ Catches logic effects
 - ▶ Applicable at all granularity levels

Functional Specification

NAME

grep - search a file for a pattern

SYNOPSIS

grep <pattern> <filename>

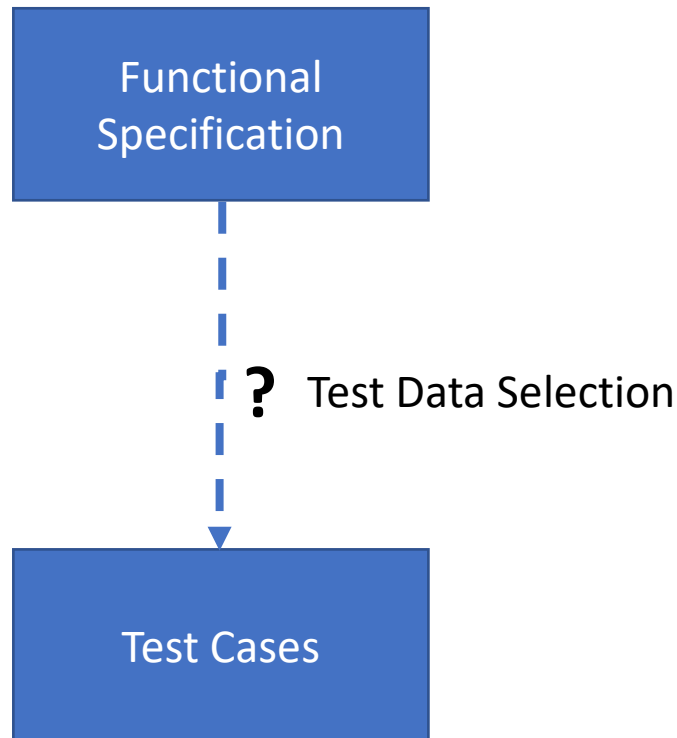
DESCRIPTION

The `grep` utility searches files for a `pattern` and prints all lines that contain that `pattern` on the standard output. A line that contains multiple occurrences of the `pattern` is printed only once.

The `pattern` is any sequence of characters. To include a blank in the `pattern`, the entire `pattern` must be enclosed in single quotes (`'`). To include a quote sign in the `pattern`, the quote sign must be escaped (`\'`). In general, It is safest to enclose the entire `pattern` in single quotes `'...'`.

Functional (Black-Box) Testing

- From Functional Specification to Test cases



Test Data Selection

- Addresses the problem of identifying relevant inputs for a software feature.



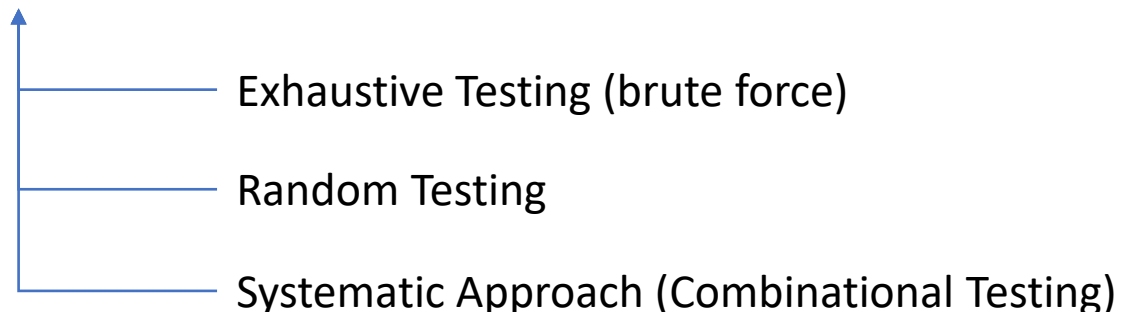
Test Data Selection

- Addresses the problem of identifying relevant inputs for a software feature.



Challenge:

How can we select meaningful inputs for the software



Exhaustive Testing is Hard

```
int max(int x, int y) {  
    if (x > y)  
        return x;  
    else  
        return y;  
}
```

- ▶ How long will it take to exhaustively test max (assuming 32 bit integers)
 - ▶ Total number of test cases: $2^{32} * 2^{32} = 2^{64} \simeq 10^{19}$
 - ▶ Assume that you can run 1 test per nanosecond, then we have 10^9 Tests/Sec
 - ▶ Total Time: 10^{10} seconds overall \simeq **600 years**

Exhaustive Testing is Hard

```
int max(int x, int y) {  
    if (x > y)  
        return x;  
    else  
        return x;  
}
```

- **Do bigger test sets help?**

Test set $\{(x=3, y=2), (x=2, y=3)\}$ will detect the error

Exhaustive Testing is Hard

```
int max(int x, int y) {  
    if (x > y)  
        return x;  
    else  
        return x;  
}
```

- **Do bigger test sets help?**

Test set $\{(x=3,y=2),(x=4,y=3),(x=5,y=1)\}$ will not detect the error although it has more test cases

Exhaustive Testing is Hard

- ▶ Assume that the input for the max method was an integer array of size n
 - ▶ Then number of test cases: $2^{32 * n}$
- ▶ Assume that the size of the input array is not bounded
 - ▶ then number of test cases: ∞

Random Testing

- ▶ Use a random number generator to generate test cases
- ▶ Derive estimates for the reliability of the software using some probabilistic analysis
- ▶ Coverage is a problem



Random Testing

```
boolean isEqual(int x, int y) {  
    if (x == y)  
        return false;  
    else  
        return false;  
}
```

- If we pick test cases randomly it is unlikely that we will pick a case where x and y have the same value

Random Testing

```
boolean isEqual(int x, int y) {  
    if (x == y)  
        return false;  
    else  
        return false;  
}
```

- ▶ If x and y can take 2^{32} different values, there are 2^{64} possible test cases, and in 2^{32} of them x and y are equal
- ▶ Thus: The probability of picking a case where x is equal to y is 2^{-32}

Random Testing

```
boolean isEqual(int x, int y) {  
    if (x == y)  
        return false;  
    else  
        return false;  
}
```

- ▶ It is not a good idea to pick the test cases randomly (with uniform distribution) in this case.
- ▶ Naive random testing will not be effective

Summary

- Exhaustive testing is impractical even for small functions
- Random testing may seem to have some advantages
- However random testing is also impractical

Combinatorial Testing

Part B

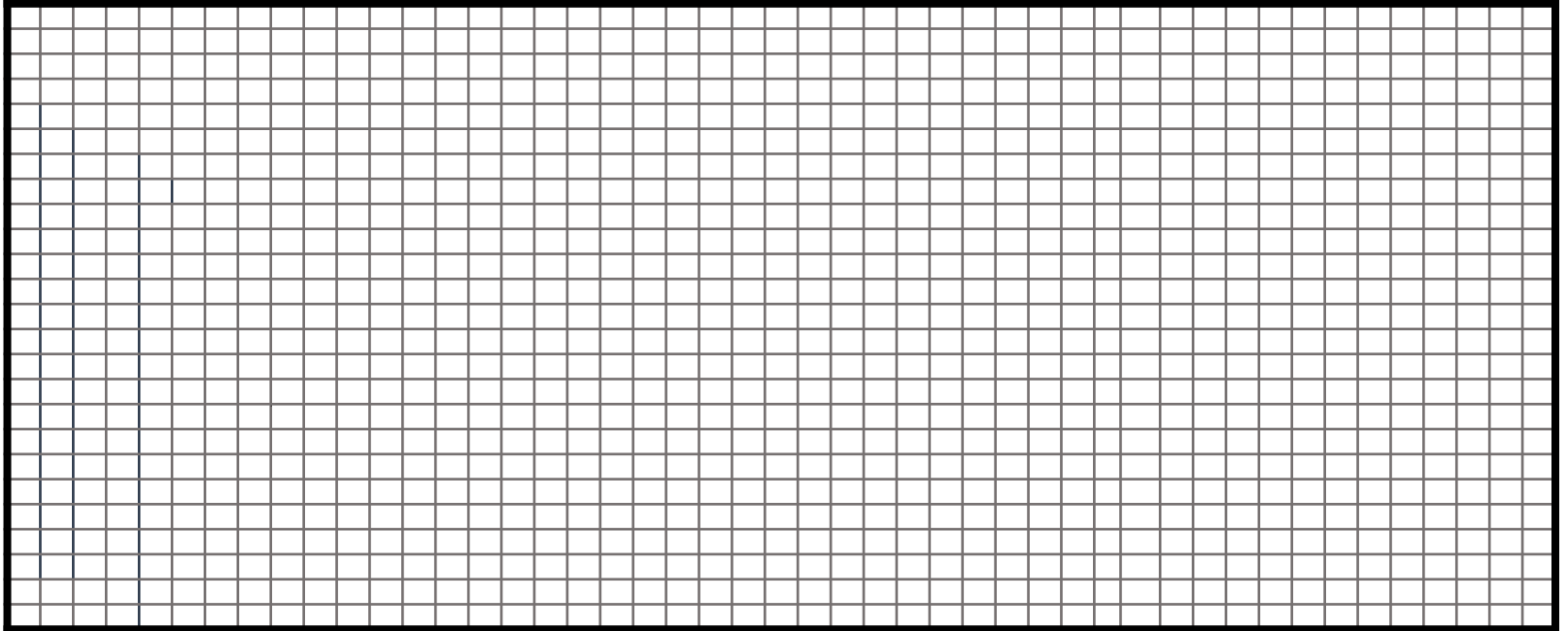
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Partition Testing

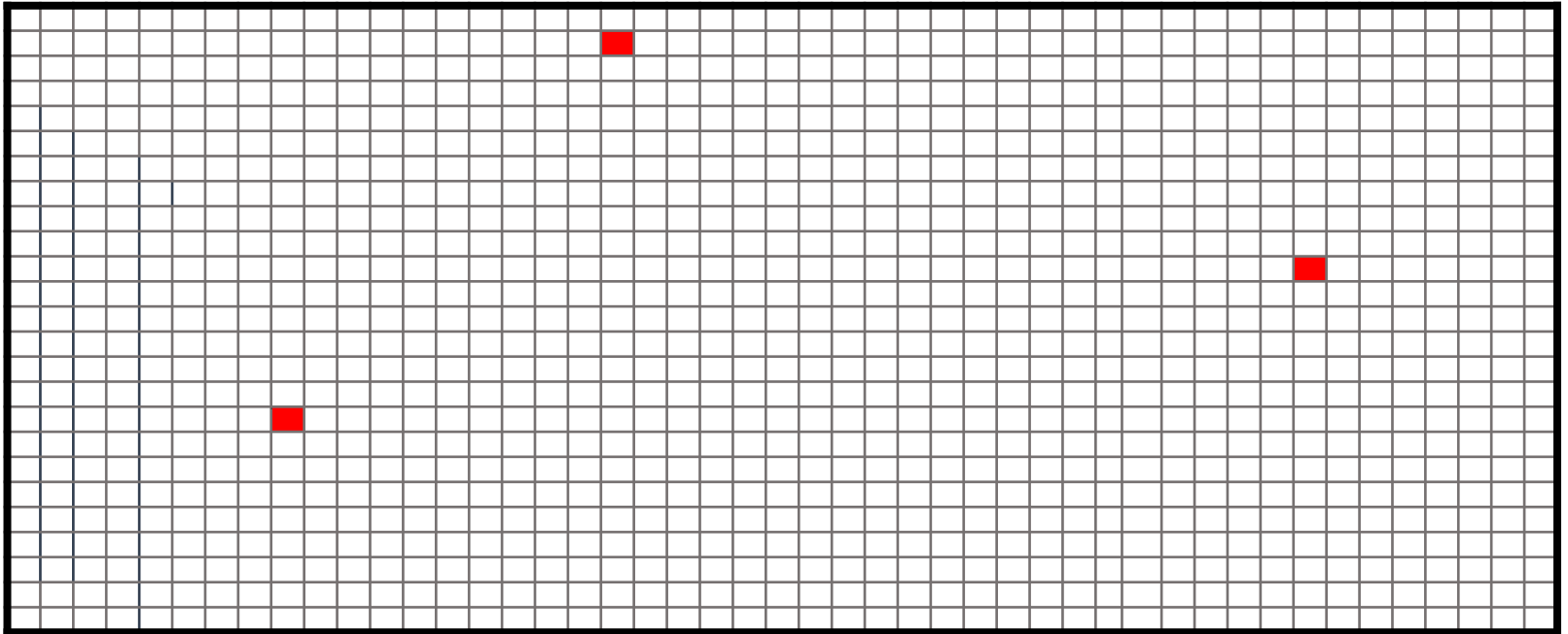
Input domain for a software program



- ▶ Each square represents an input value

Partition Testing

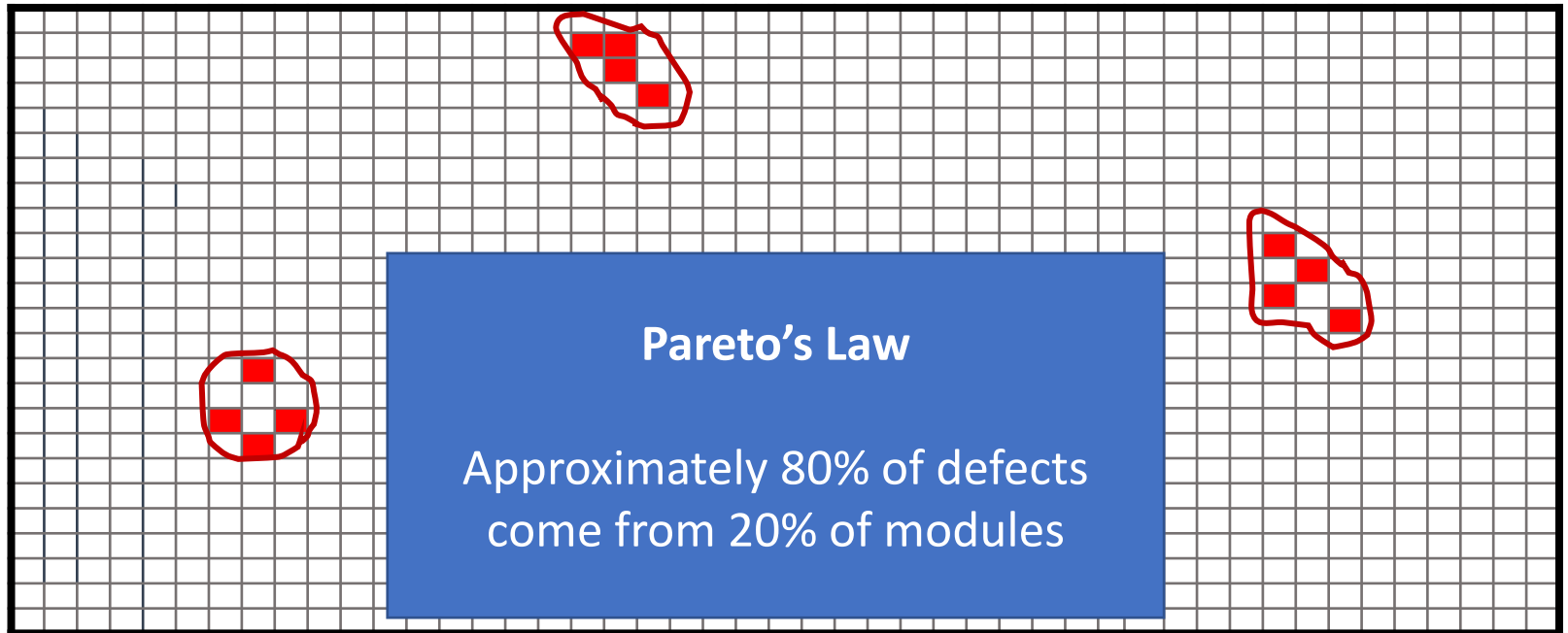
Input domain for a software program



- ▶ Failing inputs are generally sparse
- ▶ Randomly finding bug is like looking for a needle in a haystack

Partition Testing

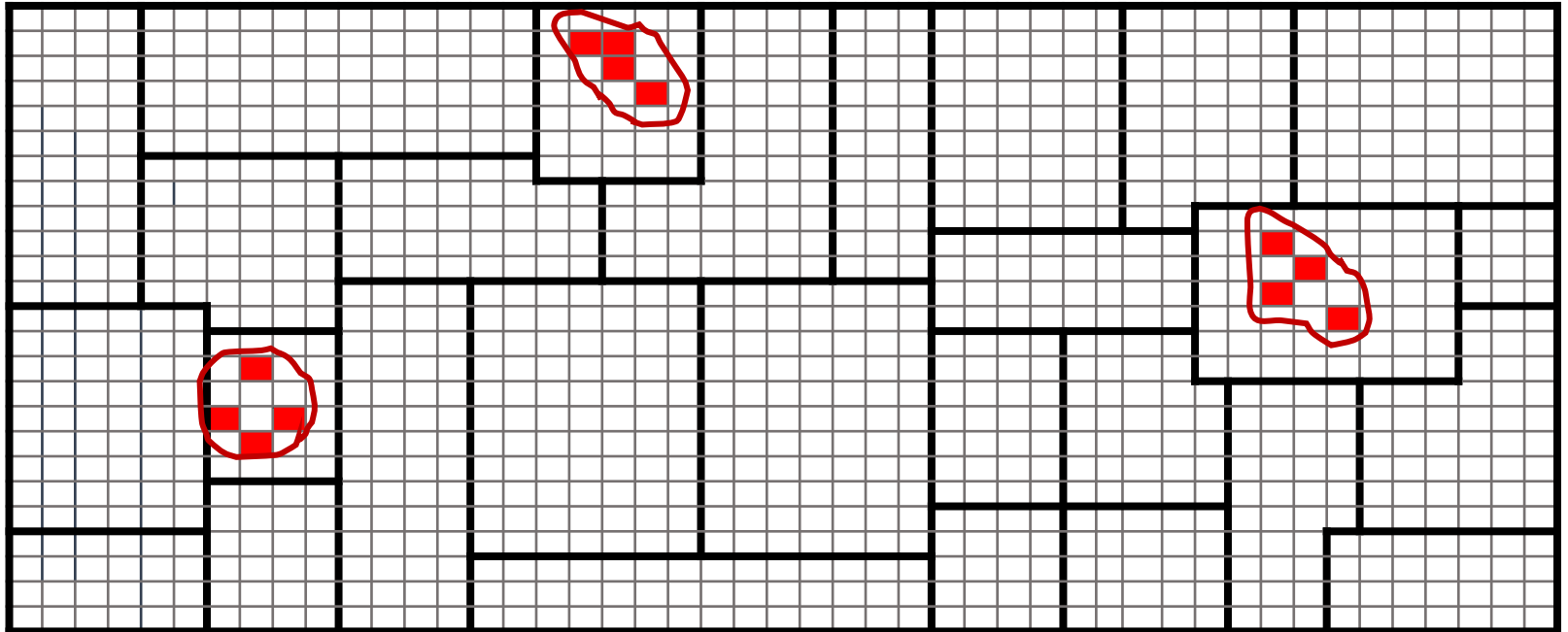
Input domain for a software program:



- However, failing inputs tend to be dense in some parts of the domain

Partition Testing

Input domain for a software program:



- ▶ Input domain tends to be naturally split into partitions
- ▶ Each partition is a block that defines a set of **equivalent subdomains**

Partition Testing

Equivalent Sub-domains

Calendar example:

- ▶ A function that takes any month of the year and returns the number of days.

Sub-domains:

- Month less than 1
- Month between 1-12
- Month greater than 12

Month Value
characteristics used
to define equivalent
sub-domains

Partition Testing

Equivalent Sub-domains

Bus ticketing price example:

- ▶ Children under 6 years go free. Young people pay £2.50, Adults £5.00 and Senior Citizen pay £1.00.

Classes:

Age:0-5 → Price:0

Age:6-18 → Price:2.50

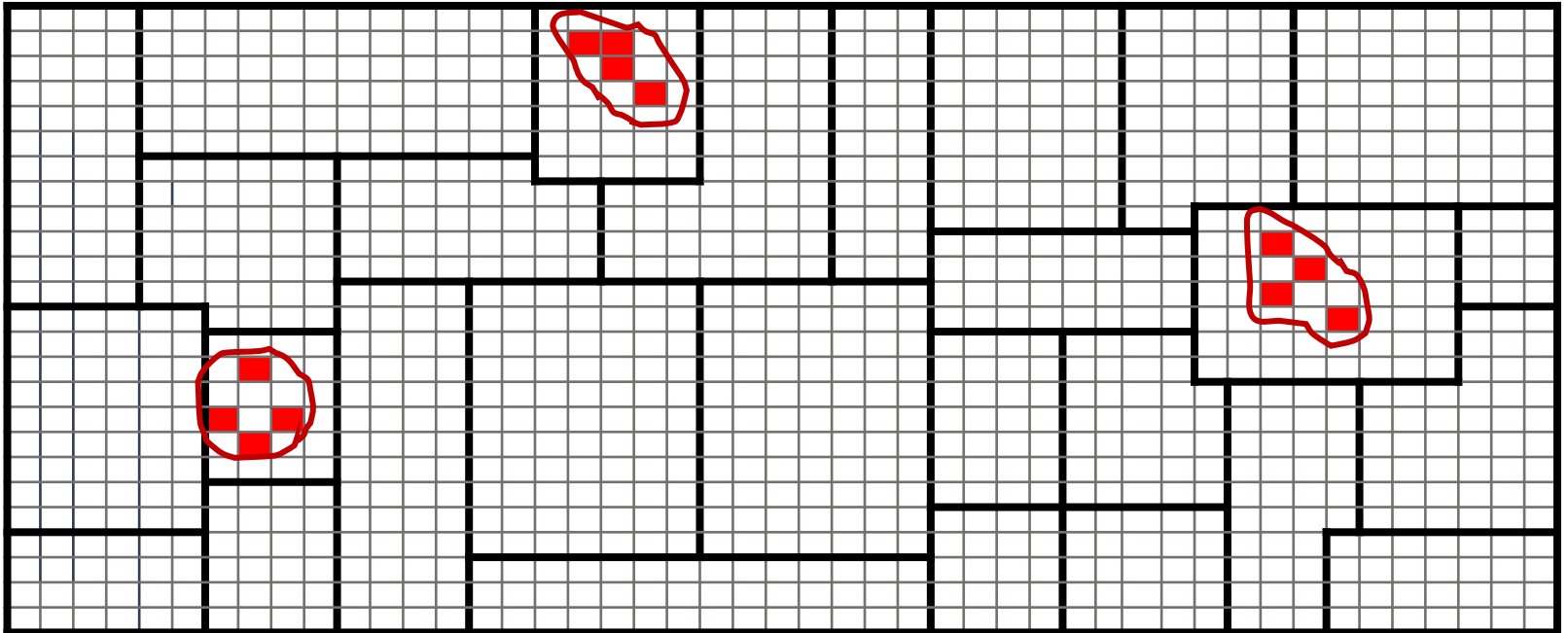
Age:19-64 → Price:5.00

Age:65-infinity → Price:1

age value
characteristic used
to define equivalent
classes

Partition Testing

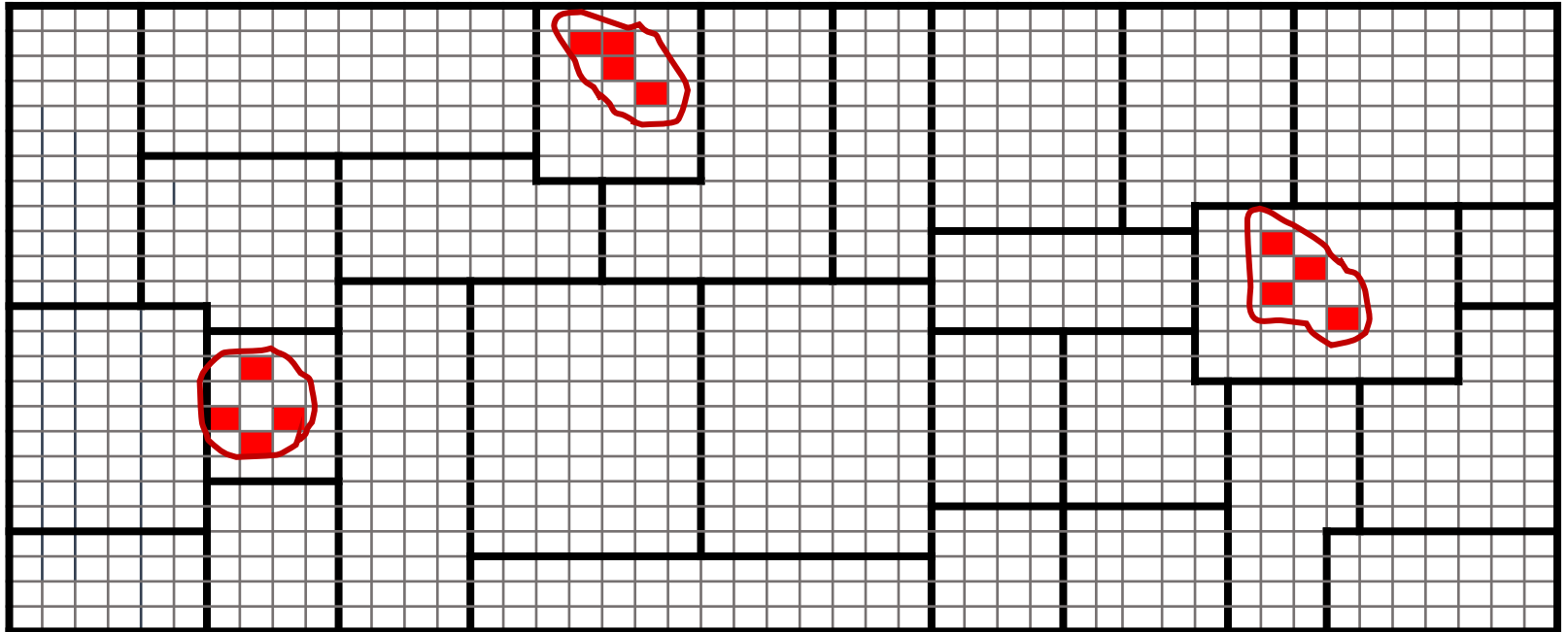
Input domain for a software program:



- So a partition is usually based on some **characteristic** of the program and the program's inputs

Partition Testing

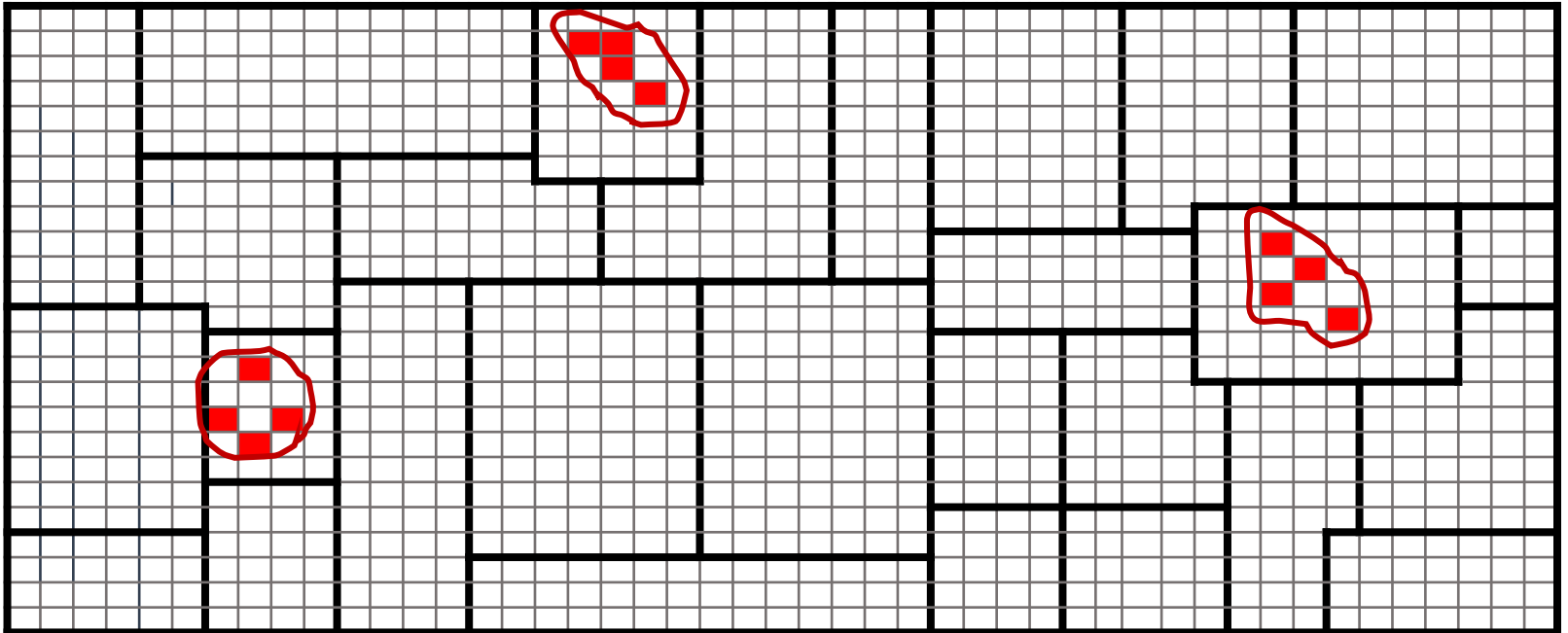
Input domain for a software program:



- ▶ Other possible **characteristic** examples:
 - ▶ Input X is (null, not null)
 - ▶ Order of file F (sorted, inverse sorted, arbitrary)
 - ▶ Min separation distance of two aircraft (>10 km, >20 km)

Partition Testing

Input domain for a software program:



- ▶ Formally, a partition must satisfy two properties:
 1. The partition must cover the entire domain (completeness)
 2. The blocks must not overlap (disjoint)

Combinatorial Testing

Part C

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Input Domain Model

► Example:

1. consider the characteristic “order of file F ”. This could be used to create the following (defective) partitioning:
 - Order of file F
 - $b1$ = Sorted in ascending order
 - $b2$ = Sorted in descending order
 - $b3$ = Arbitrary order

This is a defective and invalid partitioning because:

- If the file is of length 0 or 1, then the file will belong in all three blocks. That is, the blocks are **not disjoint**.

Input Domain Model

► Example:

- Order of file F (defective)
 - b_1 = Sorted in ascending order
 - b_2 = Sorted in descending order
 - b_3 = Arbitrary order

1. File F sorted ascending (valid)
– b_1 = True
– b_2 = False

2. File F sorted descending (valid)
– b_1 = True
– b_2 = False

files of length 0 or 1 are only in the True block for both characteristics.

Input Domain Model

► Approaches:

1. Interface-based input domain modelling:

- Develops ***characteristics*** directly from input parameters to the program under test
- Typically each input parameter is considered in isolation.
- **Advantage:** Relatively easy to identify characteristics
- **Disadvantage:** Not all information is reflected in the interface, and testing some functionality may require parameters in combination

Input Domain Model

Interface-based input domain modelling

► *Example:*

Q: Define two interface-based characteristics for **list**, including blocks and values in the function below:

```
public boolean findElement (List list, Object element)  
// Effects: if list or element is null throw NullPointerException  
// else returns true if element is in the list, false otherwise
```

Input Domain Model

Interface-based input domain modelling

► *Example:*

Q: Define two interface-based characteristics for `list`, including blocks and values in the function below:

```
public boolean findElement (List list, Object element)
// Effects: if list or element is null throw NullPointerException
// else returns true if element is in the list, false otherwise
```

A:

1. list is null	2. list is empty
– $b_1 = \text{True}$	– $b_1 = \text{True}$
– $b_2 = \text{False}$	– $b_2 = \text{False}$

Input Domain Model

- ▶ Approaches:

- 2. *functionality-based* input domain modelling:

- Develops **characteristics** from a functional or behavioral view of the program under test.

Input Domain Model

Functionality-based input domain modelling

► *Example:*

Q: Define two functionality-based characteristics for `list`, including blocks and values in the function below:

```
public boolean findElement (List list, Object element)
// Effects: if list or element is null throw NullPointerException
// else returns true if element is in the list, false otherwise
```

- A:**
- | | |
|---|---------------------------------|
| 1. Number of occurrences of element in list | 2. Element occurs first in list |
| – $b_1 = 0$ | – $b_1 = \text{True}$ |
| – $b_2 = 1$ | – $b_2 = \text{False}$ |
| – $b_3 = >1$ | |

Partition Testing

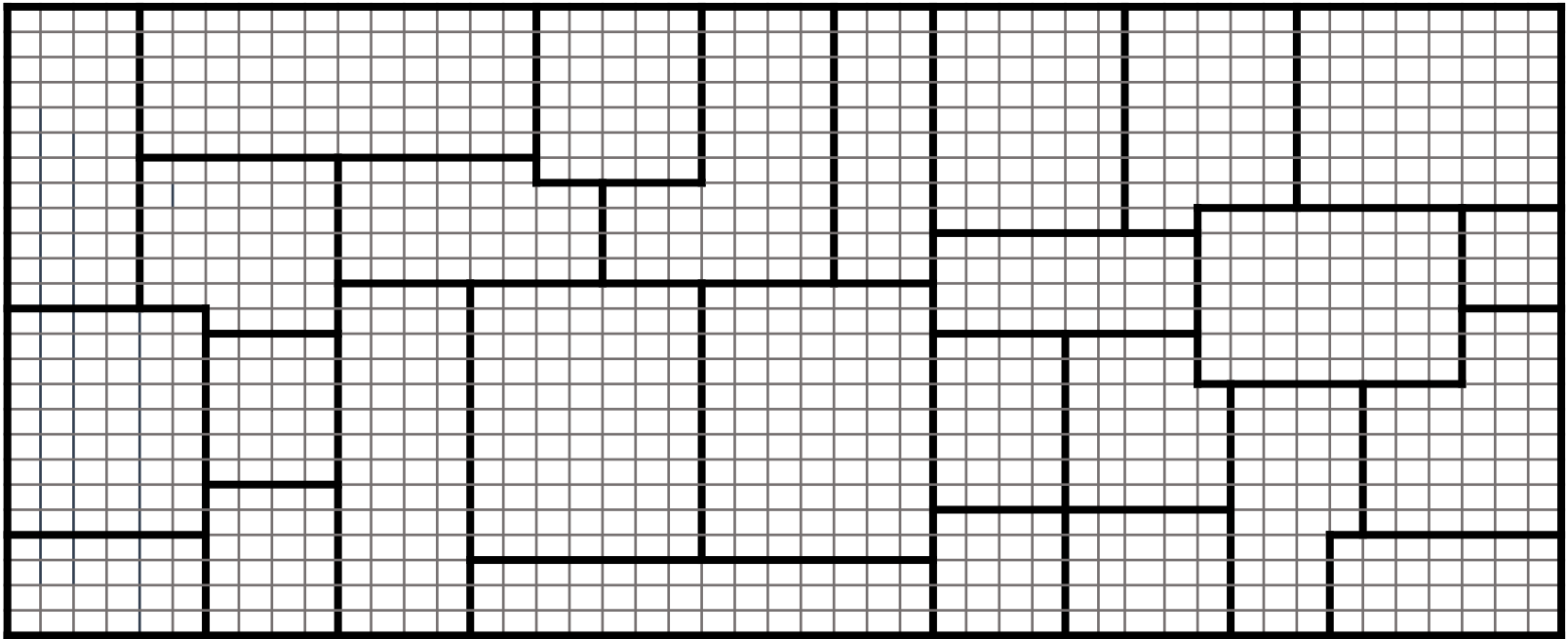
- ▶ Choosing blocks and values:
 - ▶ More blocks will result in more tests, requiring more resources but possibly finding more faults.
 - ▶ Fewer blocks will result in fewer tests, saving resources but possibly reducing test effectiveness.

Partition Testing

- ▶ Strategies for choosing blocks and values:
 - ▶ **Valid values:** Include at least one group of valid values.
 - ▶ **Invalid values:** Include at least one group of invalid values.
 - ▶ **Boundaries:** Values at or close to boundaries often cause problems.
 - ▶ **Missing partitions:** Check that the union of all blocks of a characteristic completely covers the input space of that characteristic.
 - ▶ **Overlapping partitions:** Check that no value belongs to more than one block.

Boundary Values

- ▶ Errors tend to occur at the boundary of a partition



- ▶ The objective is to select input at these boundaries
- ▶ Boundary testing (i.e. selection of boundary inputs) is complementary to partition testing

Boundary Value

► Example:

- Define the partitions, blocks, values and possible boundary inputs for the split function

String[] split(String *str*, *int* *size*)

1. *Partition*: *size* value

– $b_1 = < 0$

– $b_2 = 0$

– $b_3 = > 0$

Possible inputs:

– b_1 : *size* = -1

– b_2 : *size* = 0

– b_3 : *size* = 1

– b_3 : *size* = MAXINT

2. *Partition*: *str* with length

– $b_1 = < \text{size}$

– $b_2 = \text{in}[\text{size}, \text{size} * 2]$

– $b_3 = > \text{size} * 2$

Possible inputs:

– b_1 : *str* with length = *size* – 1

– b_2 : *str* with length = *size*

– b_3 : *str* with length = *size* * 2 + 1

etc...

Summary

- Partition Testing is a non-naïve random testing approach
- It leverages the observation that software defects are sparse and clustered in small regions
- Split the input domain into disjoint and non-overlapping regions based on appropriately picked characteristics
- Boundary values are complementary to partition testing

A Systematic Functional Testing Approach Part A

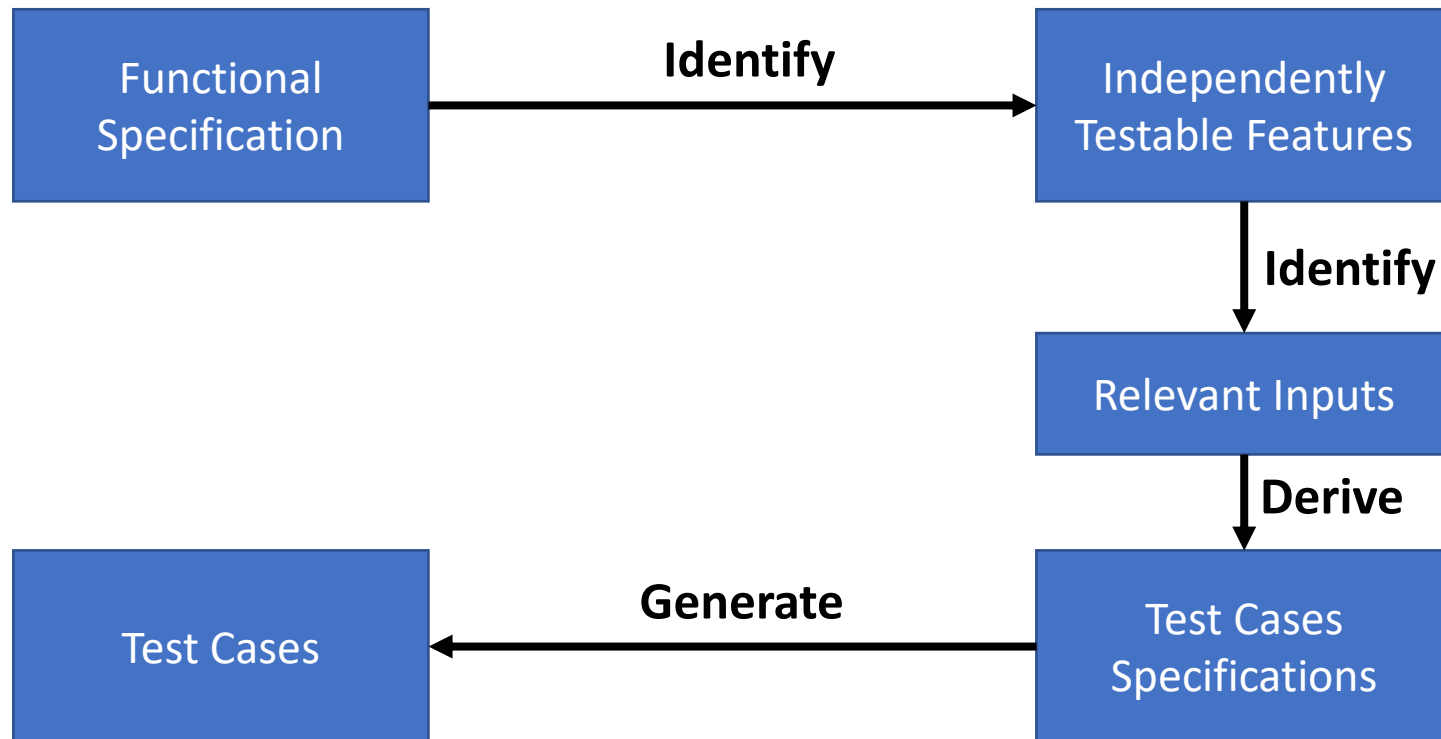
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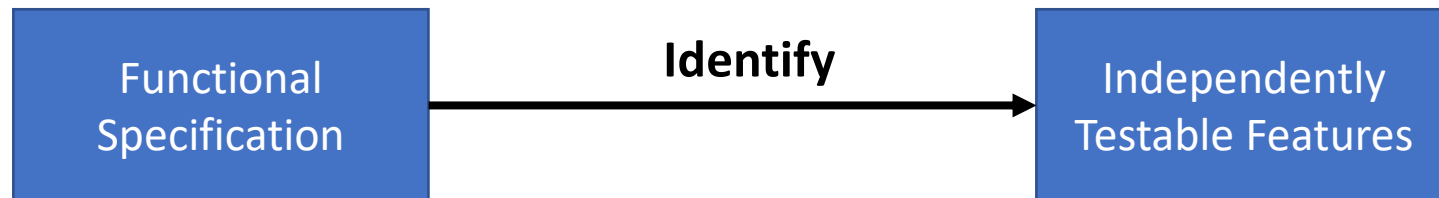
Systematic Approach

- From Functional Specification to Test cases



Systematic Approach

- Identifying Independently testable features



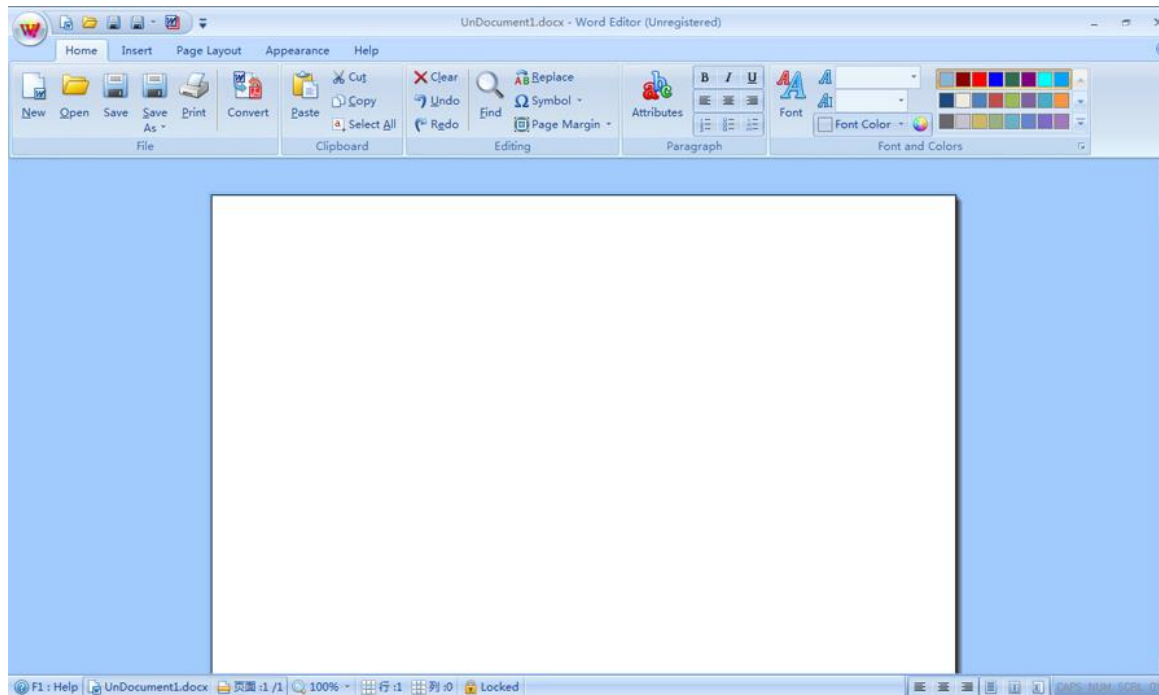
`getSum(int a int b)`

Q: How many independently testable features do we have in getSum?

A: [] 1
[] 2
[] 3
[] >3

Systematic Approach

- Identifying Independently testable features

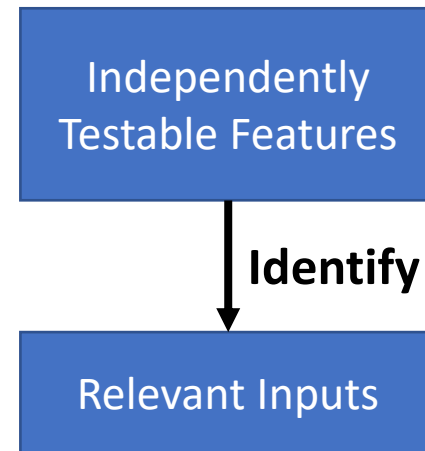


Q: List three independently testable feature of a word processor?

A: (1) _____ (2) _____ (3) _____

Systematic Approach

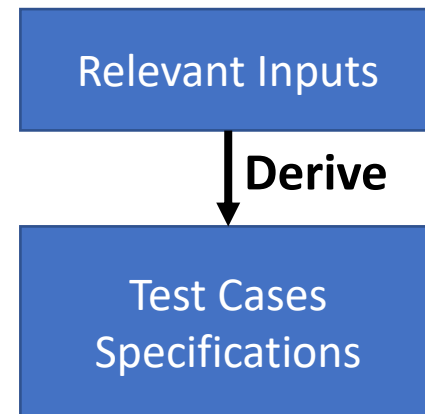
- ▶ Identifying relevant inputs for each features
 - ▶ Using Partition and Boundary Value Testing



Systematic Approach

- ▶ Deriving test case specifications:

A test case specification defines how value of relevant inputs should be put together when testing the system.



Test Case Specification

- ▶ Example:

- ▶ Write the test case specification for the split function

String[] split(String str, int size)

Possible inputs:

- b_1 : size = -1
- b_2 : size = 0
- b_3 : size = 1
- b_3 : size = MAXINT

Possible inputs:

- b_1 : str with length = size-1
- b_2 : str with length = size
- b_3 : str with length = size*2+1
- etc...

Test Case Specifications

Test Case Specification

- ▶ Example:

- ▶ Write the test case specification for the split function

String[] split(String str, int size)

Possible inputs:

- b_1 : size = -1
- b_2 : size = 0
- b_3 : size = 1
- b_3 : size = MAXINT



Possible inputs:

- b_1 : str with length = size-1
- b_2 : str with length = size
- b_3 : str with length = size*2+1
- etc...

- ▶ Test Case Specifications – **Combinatorial Approach**

size = -1 , str with length = -2

size = -1 , str with length = -1

size = -1 , str with length = 0

Test Case Specification

- ▶ Example:

- ▶ Write the test case specification for the split function

String[] split(String str, int size)

- ▶ Test Case Specifications – Combinatorial Approach

size = -1 , str with length = -2

size = -1 , str with length = -1

size = -1 , str with length = 0

size = 0 , str with length = -1

size = 0 , str with length = 0

size = 0 , str with length = 1

etc...



Combinatorial
Explosion

Test Case Specification

- ▶ Example:

- ▶ Write the test case specification for the split function

String[] split(String str, int size)

- ▶ Test Case Specifications – Combinatorial Approach

size = -1 , str with length = -2

size = -1 , str with length = -1

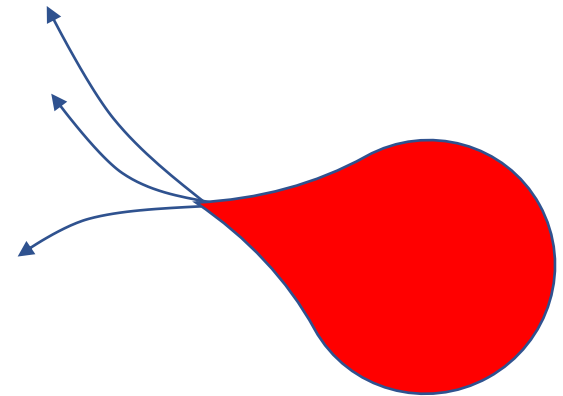
size = -1 , str with length = 0

size = 0 , str with length = -1

size = 0 , str with length = 0

size = 0 , str with length = 1

etc...



Combinations that don't
make much sense

A Systematic Functional Testing Approach Part B

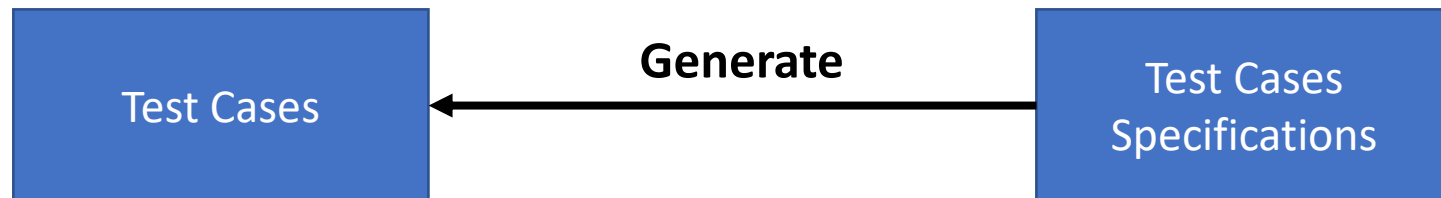
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Systematic Approach

- ▶ The last step of generating test cases from test case specification is a fairly mechanical process



The Category-Partition Method

- ▶ Ostrand & Balcer , CACM, June 1988



T. J. Ostrand and M. J. Balcer. 1988. The category-partition method for specifying and generating functional tests. *Commun. ACM* 31, 6 (June 1988), 676-686.

The Category-Partition Method



Specification



1. Identify independently testable features
2. Identify **categories**
3. **Partition** categories into choices
4. Identify constraints among choices
5. Produce/evaluate test case specification
6. Generate test case from test case specifications



Test Cases

The Category-Partition Method

1. Identify independently testable features

- ▶ We are already familiar with this step in our systematic approach

The Category-Partition Method

2. Identify Categories

- Where each category is the *characteristics* of each input element

```
String[] split(String str, int size)
```

Input **str**

–length

–content

Input **size**

–value

The Category-Partition Method

3. Partition categories into choices

`String[] split(String str, int size)`

Input `str`

–length

- 0
- `size` -1
- ...

–content

- spaces
- special characters
- ...

Input `size`

–value

- 0
- >0
- <0
- MAXINT
- ...

The Category-Partition Method

4. Identify constraints among choices

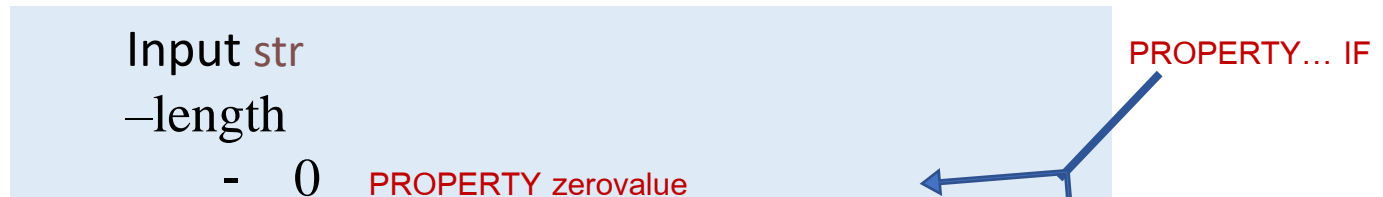
- ▶ To eliminate meaningless combinations
- ▶ To reduce the number of test cases
- ▶ Three types of constraint properties:
 - ▶ PROPERTY... IF,
 - ▶ ERROR,
 - ▶ SINGLE

The Category-Partition Method

4. Identify constraints among choices

PROPERTY... IF

String[] split(String str, int size)



- We can define **zero value** as a special property to highlight when length is 0
- We can then use this property to exclude some meaningless combinations (for instance a string of length =0 cannot be a special character).

The Category-Partition Method

4. Identify constraints among choices

ERROR

```
String[] split(String str, int size)
```

Input **size**

–value

- <0 ERROR
- MAXINT

- The choice <0 for input size is marked as an error property.
- This means that when generating possible combination of test case specifications, the choice <0 will be considered only once.

The Category-Partition Method

4. Identify constraints among choices

SINGLE

```
String[] split(String str, int size)
```

Input **size**

–value

- < 0
- MAXINT SINGLE

- Used when the objective is to limit the number of test cases.
- The choice is used only once, and not combined multiple times.
- A SINGLE property for MAXINT means that we will only have one test case for which the size equals MAXINT

The Category-Partition Method

5. Produce/evaluate test case specification

- ▶ Can be completely automated
- ▶ The result is a set of **test frames**



**Specification of
a test**

Example:

Test frame #34

Input **str**

Length: size -1

content: special characters

Input **size**

value: >1

The Category-Partition Method

6. Generate test case from test case specifications

- ▶ Involves simple instantiation of test frames.
- ▶ **Final Result:** Set of concrete test cases

Example: Test frame #34
 Input **str**
 Length: size -1
 content: special characters
 Input **size**
 value: >1

Test case #34
Str = "ABCC!\n\tβ"
Size=11

