





Computational dynamics

Computer Laboratory 1: Introduction to Elastodynamics in FEniCSx. Boundary Conditions

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OUTLINE

- Introduction
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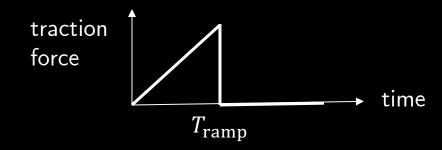
INTRODUCTION

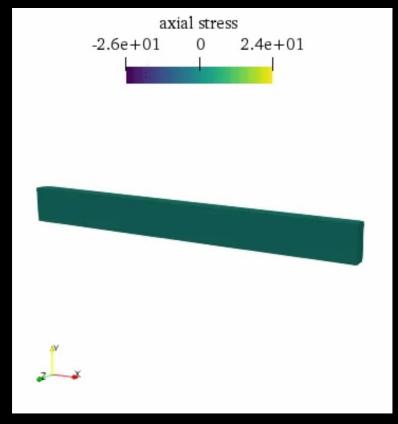
- Reminder: Installation and Demo Code on https://github.com/MorenoMiguelES/CD-computdynamics

- Tutorial on Elastodynamics on FEniCS legacy (2019): https://comet-tutorial.org/

fenics.readthedocs.io/en/latest/demo/elastodynamics/demo_elastodynamics.py.html

- Fixed on Dirichlet boundary on left side.
- Traction forces on Neumann boundary on right side.





(Bleyer, J., comet demo)

Import modules

1111111 Demo code for the Computational Dynamics SS2025 course ELASTODYNAMICS: Newmark-beta method, traction forces / displacement loading. Author: Dr. Miguel Angel Moreno-Mateos #Import: not necessary to specify it later from future import print function import numpy as np from numpy import array import dolfinx import ufl from mpi4py import MPI import dolfinx.io import dolfinx.geometry import math from petsc4py.PETSc import ScalarType from petsc4py import PETSc import petsc4py import matplotlib.pyplot as plt from petsc4py import PETSc default scalar type = PETSc.ScalarType from dolfinx import fem import basix

import dolfinx.fem.petsc
import dolfinx.nls.petsc

Import mesh:



Function Space & functions:

```
#Import mesh & subdomains from .msh file:
filename="Box"
from dolfinx.io import gmshio
mesh, cell_markers, facet_markers = gmshio.read_from_msh(filename+'.msh',
MPI.COMM WORLD, gdim=3)
metadata = {"quadrature degree": 2}
dx = ufl.Measure('dx')(domain=mesh, subdomain data=cell markers,
metadata=metadata) #Integration measures for each subdomain
P1 = basix.ufl.element("CG", mesh.basix_cell(), 2, shape=(mesh.geometry.dim,)) #
For displacements
V = dolfinx.fem.functionspace(mesh, P1)
# FUNCTIONS IN THE FUNCTION SPACE V (Function - Trial - Test).
u = dolfinx.fem.Function(V) #Unkown.
u old = dolfinx.fem.Function(V)
v old = dolfinx.fem.Function(V)
a old = dolfinx.fem.Function(V)
du = ufl.TrialFunction(V)
v = ufl.TestFunction(V)
dd = len(u) # space dimension
```

Boundary conditions:

- a) Encastre $\partial\Omega_{\mathrm{D}}$:
- b) Traction forces $\partial \Omega_N$:

```
###### Encastre Displacement:
def bnd encastre(x):
tol=1e-4
return np.isclose(x[2],0)
bnd encastre dofs0 = dolfinx.fem.locate dofs geometrical(V,bnd encastre)
u encastre vect0 = np.array((0,) * mesh.geometry.dim, dtype=default scalar type)
bc boundar = dolfinx.fem.dirichletbc(u encastre vect0,bnd encastre dofs0,V)
# Definition of 2 problems: bcu1 with Dirichlet BC on right side,
#bcu2 without them for free oscillation. If traction forces, it is not necessary.
bcu1 = [bc boundar]#, bc dispload] #Step 1: Dirichlet BC
bcu2 = [bc boundar] #Step 2: Oscillation
def bnd side(x):
return np.isclose(x[2],1)
forcemax = 1
t = dolfinx.fem.Constant(mesh, 0.0)
traction = ufl.as vector([forcemax * (t )/(T ramp),0,0])
right facets = dolfinx.mesh.locate entities boundary(mesh, mesh.topology.dim - 1,
bnd side)
facet tag = dolfinx.mesh.meshtags(mesh, mesh.topology.dim - 1, right facets, 1)
dss = ufl.Measure('ds', domain=mesh, subdomain data=facet tag, subdomain id=1)#,
metadata=metadata)
```

Time discretization: Newmark Method

```
\gamma \in [0,1],
\beta \in [0,0.5],
```

```
# alpha m = alpha f = 0: recovers Newmark method. Otherwise, generalized-alpha
method.
alpha m = 0 \# in [0,1]
alpha f = 0 \# in [0,1]
# HIGH-FREQUENCY DISSIPATION (NUMERICAL DAMPING) IN NEWMARK METHOD:
qamma = 1
beta = 0.5
# Note: Not necessary for high-frequency dissipation if gamma and beta are
properly chosen.
eta m = 0 \# 1e-4
eta k = 0 \#1e-4
def avg(x old,x new,alpha):
return alpha*x old + (1-alpha)*x new
def update a(u,u old,v old,a old):
dt = dt
beta = beta
return (u-u old-dt *v old)/beta /dt **2 - (1-2*beta )/2/beta *a old
def update v(a,u old,v old,a old):
dt = dt
gamma_{-} = gamma
return v old + dt *((1-gamma)*a old + gamma *a)
a new = update a(u,u old,v old,a old)
v new = update v(a new,u old,v old,a old)
```

Primary fields (Kinematics):

```
## PRIMARY FIELDS
dd = len(u) # Spatial dimension
I = ufl.Identity(dd) # Identity tensor
F = I + ufl.grad(avg(u_old,u,alpha_f)) # Deformation gradient from current time
step
Fv = I + ufl.grad(avg(v_old,v_new,alpha_f)) # Deformation gradient from current
time step
CG = ufl.dot(F.T,F) # Right Cauchy-Green (CG) tensor
BG = ufl.dot(F,F.T) # Left Cauchy-Green (CG) tensor
```

Constitutive model:

```
## CONSTITUTIVE MODEL:
####### YEOH-MODEL (COMPRESSIBLE)
C10 = [0.5*1000, 0]
C20 = [0, 0]
C30 = [0, 0]
poisson = [0.3, 0]
kappa = [2*(2*C10[0])*(1+poisson[0])/3/(1-2*poisson[0]),
2*(2*C10[0])*(1+poisson[0])/3/(1-2*poisson[0])
#density:
rho = 1.0
def Piso(F,i):
j,k,l,m = ufl.indices(4)
Id = ufl.Identity(3)
FinvT = ufl.inv(F).T
J = ufl.det(F)
A1 = ufl.as_tensor(Id[j,l]*Id[k,m],(j,k,l,m))
A2 = ufl.as tensor(-1/3*FinvT[j,k]*F[l,m],(j,k,l,m))
Pfourth = A1+A2
Fiso = 1/ufl_det(F)**(1/3)*F
I1 = ufl.tr(ufl.dot(Fiso.T,Fiso) )
P yeoh= 2* ( C10[i] + C20[i] *2* (I1-3)**1 + C30[i] *3 * (I1-3)**2 )* Fiso
P = 1/(J**(1/3))*ufl.as_tensor(Pfourth[j,k,l,m]*P_yeoh[l,m],(j,k))
return P
def Pvol(F,i): #volumetric part
J = ufl.det(F)
Pvol= kappa[i]*J*(J-1)*ufl.inv(F).T
return Pvol
```

Weak form:

```
####### VARIATIONAL PROBLEM - WEAK FORM
Res_u =
(ufl.inner(Piso(F, 0), ufl.grad(v)) + ufl.inner(Pvol(F, 0), ufl.grad(v))\\
+ eta_m*rho*ufl.inner(avg(v_old,v_new,alpha_m),v)\\
+ eta_k*(ufl.inner(Piso(Fv, 0), ufl.grad(v)) + ufl.inner(Pvol(Fv, 0), ufl.grad(v)))\\
+ rho*ufl.inner(avg(a_old,a_new,alpha_m),v)) * dx - ufl.inner(traction,v) * dss(1)
```

FEniCSx problem:

```
# Setup Non-linear variational problem
problem u1 = fem.petsc.NonlinearProblem(Res u,u,bcu1)
from dolfinx import nls
solver problem u1 = nls.petsc.NewtonSolver(mesh.comm, problem u1)
solver problem u1.atol = 1e-8
solver problem u1.rtol = 1e-8
solver problem u1.convergence criterion = "incremental"
ksp = solver problem u1.krylov solver
opts = PETSc.Options()
option prefix = ksp.getOptionsPrefix()
opts[f"{option_prefix}ksp_type"] = "preonly" # "preonly" works equally well
opts[f"{option prefix}pc type"] = "lu" # do not use 'gamg' pre-conditioner
opts[f"{option_prefix}pc_factor_mat_solver_type"] = "mumps"
opts[f"{option prefix}ksp max it"] = 30
ksp.setFromOptions()
# Note: defining two non linear problems would allow to set different Dirichlet
BC before and after T ramp
problem u2 = fem.petsc.NonlinearProblem(Res u,u,bcu2)
solver problem u2 = nls.petsc.NewtonSolver(mesh.comm, problem u2)
solver problem u2.atol = 1e-8
solver problem u2.rtol = 1e-8
solver problem u2.convergence criterion = "incremental"
```

Initialisation of variables to store data:

Note: output file is VTK format.

```
# Save results into vtk files
uVector= dolfinx.fem.Function(VV, name = "displacement")
FTensor=dolfinx.fem.Function(TT, name = "F")
PTensor=dolfinx.fem.Function(TT, name = "P")
mesh.topology.create connectivity(mesh.topology.dim-1, mesh.topology.dim)
vtx writer=dolfinx.io.VTXWriter(mesh.comm, "Output.bp", [uVector, FTensor,
PTensor], engine="BP4")
##### EVALUATE DISPLACEMENT AT A POINT ##################
time vec = []
disp \times point1 = []
point1 = np.array([[0.0, 0.0, 1.0]])
# Create a PointLocator for finding cells containing points
mesh.topology.create connectivity(mesh.topology.dim, mesh.topology.dim)
bb tree = dolfinx.geometry.bb tree(mesh, mesh.topology.dim)
# Find cells containing the points
cell candidates = dolfinx.geometry.compute collisions points(bb tree, point1)
colliding cells = dolfinx.geometry.compute colliding cells(mesh, cell candidates,
point1)
points on proc = []
cells = []
for i, point in enumerate(point1):
if len(colliding cells.links(i)) >= 0: # Check if point was found on this process
points on proc.append(point)
cells.append(colliding cells.links(i)[0])
print(points on proc)
```

Time-incremental solving loop:

```
while (tiempo < T):
    #Display report simulation
    from dolfinx import log
    log.set log level(log.LogLevel.INFO)
                                                          traction force
    ##Update time-dependent parameters:
    loaddisp .t = tiempo
    loaddisp.interpolate(loaddisp.eval)
    if tiempo < T ramp:</pre>
        t .value = tiempo
    else:
                                                             \overline{T}_{ramp}
        t .value = 0
    if tiempo < T ramp: solver problem u1.solve(u)</pre>
    else: solver problem u2.solve(u)
    a vec = dolfinx.fem.Expression(update a(u,u old,v old,a old),
    V.element.interpolation points());
    v vec = dolfinx.fem.Expression(update v(update a(u,u old,v old,a old),u old,v old,a old),
    V.element.interpolation points());
    u vec = dolfinx.fem.Expression(u, V.element.interpolation points());
    a old.interpolate(a vec)
    v old.interpolate(v vec)
    u old.interpolate(u vec)
    u expr = dolfinx.fem.Expression(u, VV.element.interpolation points())
    uVector.interpolate(u expr)
    F expr = dolfinx.fem.Expression(F, TT.element.interpolation points())
    FTensor.interpolate(F expr)
    P = dolfinx.fem.Expression(Piso(F,0)+Pvol(F,0), TT.element.interpolation points())
    PTensor.interpolate(P expr)
```

Save displacement; update output file:

```
# EVALUATE DISPLACEMENT AT A POINT (CONTINUATION)#####
points_on_proc = np.array(points_on_proc, dtype=np.float64)
disp1 = u.eval(points on proc, cells)
disp x point1 = np.append(disp x point1, disp1[0])
time_vec = np.append(time_vec,tiempo)
# VTK output
vtx writer.write(tiempo)
np.savetxt("displacement x point1.txt", disp x point1)
np.savetxt("time.txt", time vec)
plt.figure()
plt.plot(time_vec[:],disp_x_point1[:])
plt.grid();plt.xlabel("Time [s]");plt.ylabel("Displacement x [mm]")
plt.savefig('Oscillation x point1.png')
plt.close()
# Define next time step
steps += 1
tiempo += dt
```

TASKS

1. Run simulation.



Terminal, navigate to folder, activate conda environment, run python script.

2. Visualize the output file in Paraview.



Drag VTK output folder to ParaView workspace. Display nodal values, clips, etc.

3. Modify code: Replace Neumann BC by Dirichlet BCs.

Call the instructor for doubts and after successful completion of each task and report it. Enjoy!

HINT TASK 3. APPLY DIRICHLET BCs

Dirichlet BC:

```
def bnd point(x):
    return np.isclose(x[2],1) & np.isclose(x[0],0.04)
dispmax = 0.2
class MyDisp:
   def init (self):
       self.t = 0.0
   def eval(self,x):
    #. Add some spatial/temporal variation here:
       #x.shape[1]: number of columns.
       if True:
           return np.full(x.shape[1], dispmax * (self.t)/(T_ramp))
       else:
           return np.full(x.shape[1], dispmax * (self.t)/(T ramp))
V real = dolfinx.fem.functionspace(mesh, ("CG",2))
loaddisp = MyDisp()
loaddisp .t = 0.0
loaddisp = dolfinx.fem.Function(V real)
loaddisp.interpolate(loaddisp .eval)
bnd load dofs0 =
dolfinx.fem.locate dofs geometrical((V.sub(0), V.sub(0).collapse()[0]),bnd point)
bc dispload = dolfinx.fem.dirichletbc(loaddisp,bnd load dofs0,V.sub(0))
# Definition of 2 problems: bcu1 with Dirichlet BC on right side,
#bcu2 without them for free oscillation. If traction forces, it is not necessary.
bcu1 = [bc_boundar, bc_dispload]#, bc_dispload] #Step 1: Dirichlet BC
bcu2 = [bc boundar] #Step 2: Oscillation
```