A crash course on regular expressions and regular grammars

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EECS 348: Software Engineering

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FSM: Basic components



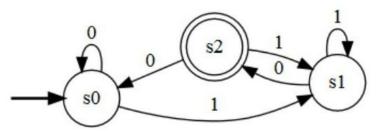
- A set of states, S
 - An initial state S₀
 - A possible set of one or more final states (F)
 - The initial and final states can be the same
- A set of inputs, I, also called the input vocabulary
- A set of outputs, O, also called the output vocabulary
- A finite-state automaton *accepts* a string x if $\delta(S_0, x) \in F$; i.e., the finite state automaton ends up in a final state

Brief Introduction to FSMs

FSM: Basic components



- A finite state automaton (FSA) is a graph with directed labeled arcs, two types of nodes, final and a unique start state
 - An FSA can have more than one final state
 - Also called a state machine
 - Deterministic FSA: For each state and for each input alphabet, there is exactly one transition
- The language accepted by a FSM is set of strings that move from start node to a final node



A couple of related terms



- **BNF** (Backus-Naur Form): a formal meta language used in defining context-free grammars, e.g., in compiler design
 - <terminal>
 - Defined as: ::=
 - Alternative:
 - Optional: []

Some symbols are just for convenience

- Combining: ()
- Maybe: ?
- Repeated: (...)* some also suggest {...}
- One or more: $(...)^+$
- Recursion: <integer> ::= <digit> | <integer> <digit>

Some BNF examples



```
NUMBER ::= WHOLE_PART FRACTION_PART?

WHOLE_PART ::= NUMERAL_SEQUENCE

FRACTION_PART ::= "." NUMERAL_SEQUENCE

NUMERAL_SEQUENCE ::= NUMERAL NUMERAL*

NUMERAL ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

EXPRESSION ::= NUMERAL | (EXPRESSION OPTR EXPRESSION)

OPTR ::= + | -
```

Regular expressions

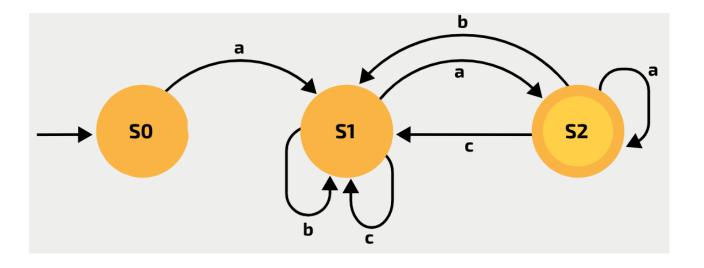


- Not as powerful as BNF (e.g., no recursion)
- Regular expressions can express finite languages by defining a pattern for finite strings of symbols
- The grammar defined by regular expressions is known as regular grammar
- A regular expression is a pattern that can be recognized by a FSM
 - Regular expressions and FSMs are equivalent concepts
 - Semantically the same; one is textual (metal language), one is graphical

Examples of regular expressions



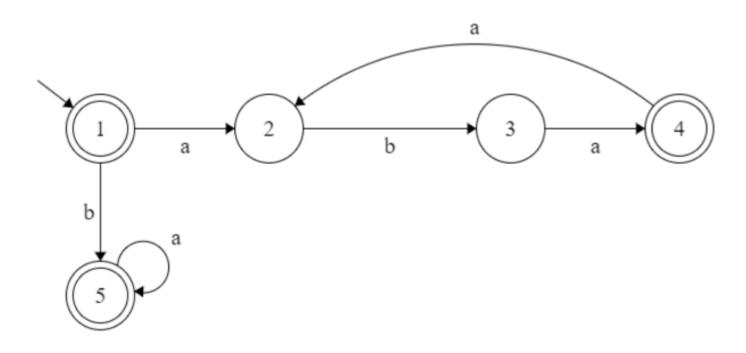
$$a(a|b|c)*a$$



Examples of regular expressions



• (aba)+|ba*



Examples of regular expressions



What do these represent?

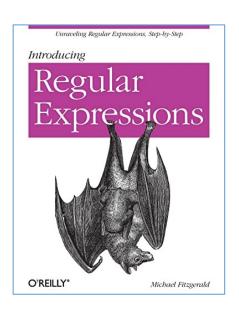


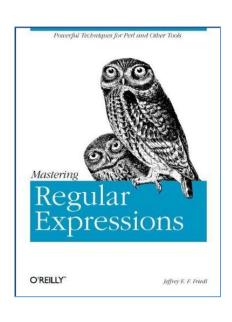
- A very similar concept, slightly different notation
- Extremely powerful for pattern matching (vim, grep, sed, ...)
- Common Unix symbols

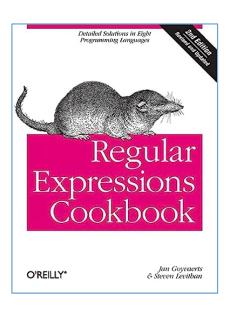
Symbol	Descriptions
	replaces any character
٨	matches start of string
\$	matches end of string
*	matches up zero or more times the preceding character
\	Represent special characters
0	Groups regular expressions
?	Matches up exactly one character



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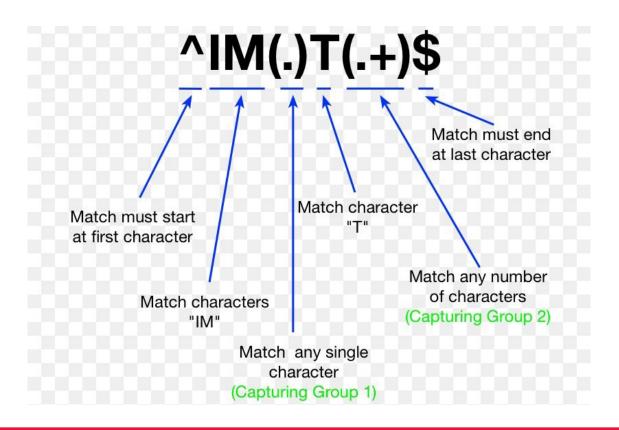






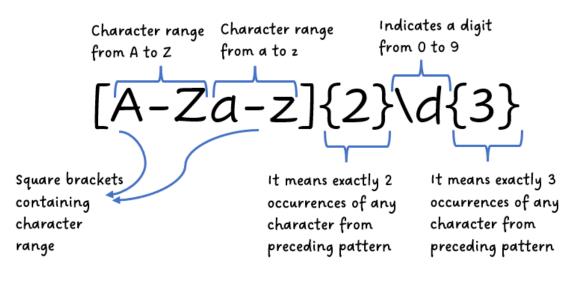


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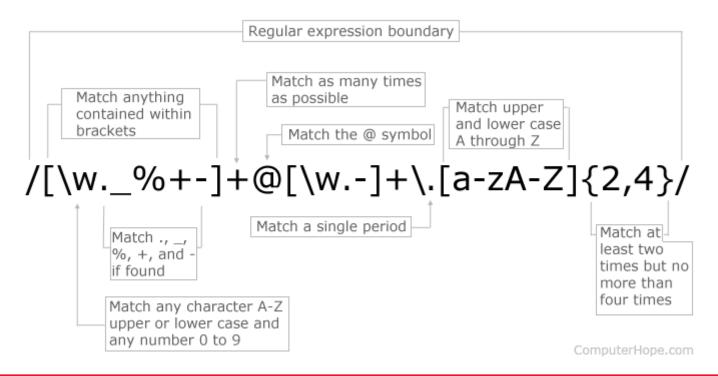


e.g., CS229, CS231

Examples that match above pattern



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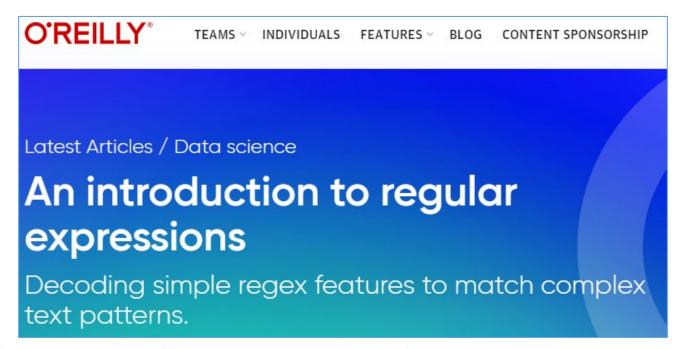
A short RE cheat sheet



```
[abc]
         A single character: a, b or c
[^abc]
         Any single character but a, b, or c
         Any single character in the range a-z
[a-z]
[a-zA-Z]
            Any single character in the range a-z or A-Z
     Start of line
     End of line
      Start of string
\A
     End of string
١z
     Any single character
      Any whitespace character
۱s
\S
      Any non-whitespace character
\d
      Any digit
      Any non-digit
\D
      Any word character (letter, number, underscore)
\W
      Any non-word character
\b
      Any word boundary character
(\dots)
         Capture everything enclosed
(a|b)
         a or b
       Zero or one of a
      Zero or more of a
      One or more of a
a{3}
       Exactly 3 of a
       3 or more of a
a{3,}
a{3,6}
          Between 3 and 6 of a
```



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https://www.oreilly.com/content/an-introduction-to-regular-expressions