



Logistic regression model



Logistic Regression Model

- ✓ Target is categorical.
- ✓ $P(y=1 \mid X) \rightarrow$ the probability of the variable being 1 given the values of X (the predictors).

Logistic Regression Model

$$P(y=1 | X) = \frac{1}{1 + e^{-(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n)}}$$

- X are the independent variables.
- Y is the target, which is class target.

Logistic Regression Model

$$P(y=1 | X) = \frac{1}{1 + e^{-(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n)}}$$

The logistic function (or sigmoid function) is used to restrict the outcome to a value between 0 and 1.

Logistic Regression Model

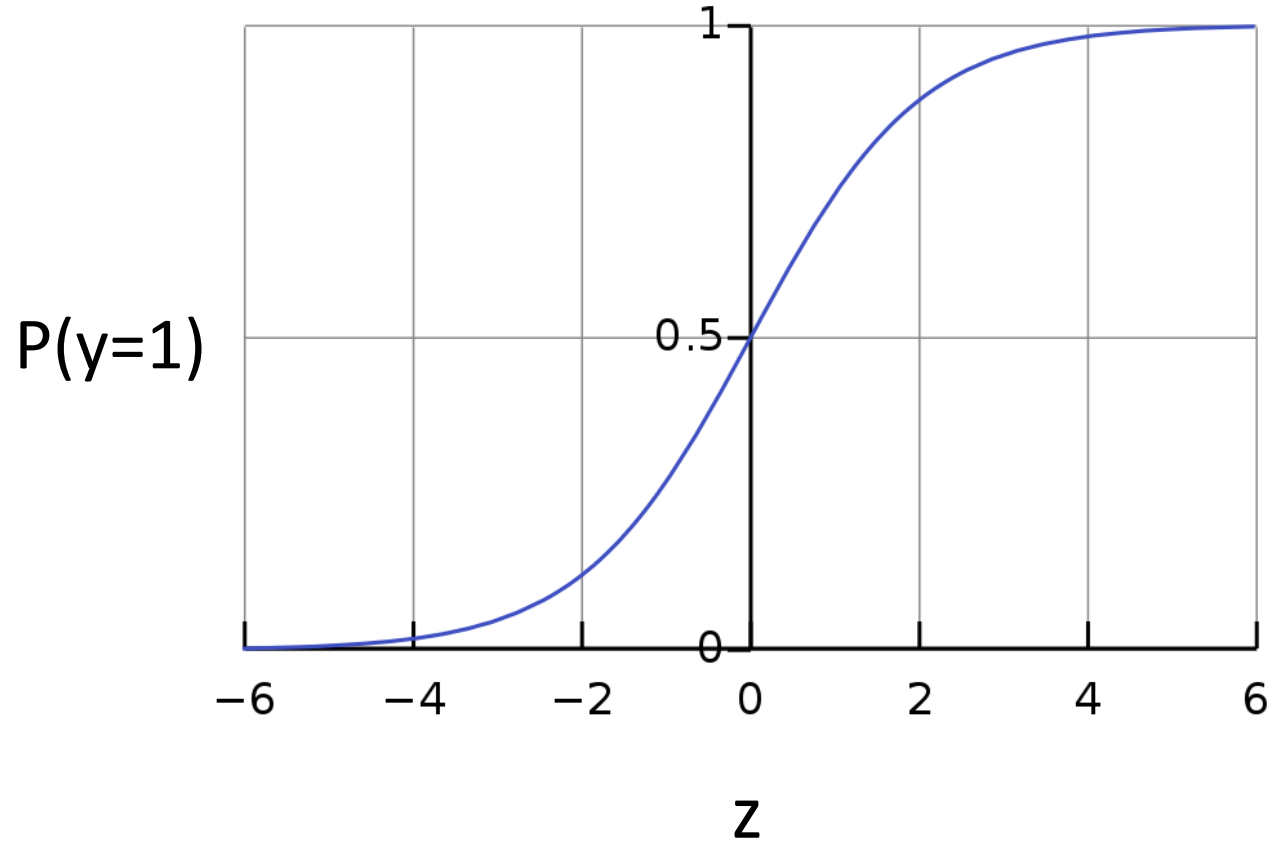
$$P(y=1 \mid X) = \frac{1}{1 + e^{-(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n)}}$$

$$z = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n$$

$$P(y=1 \mid X) = \frac{1}{1 + e^{-z}}$$

Logistic function

- Positive values of z ($z > 0$) are predictive of class 1.
- Negative values of z ($z < 0$) are predictive of class 0.



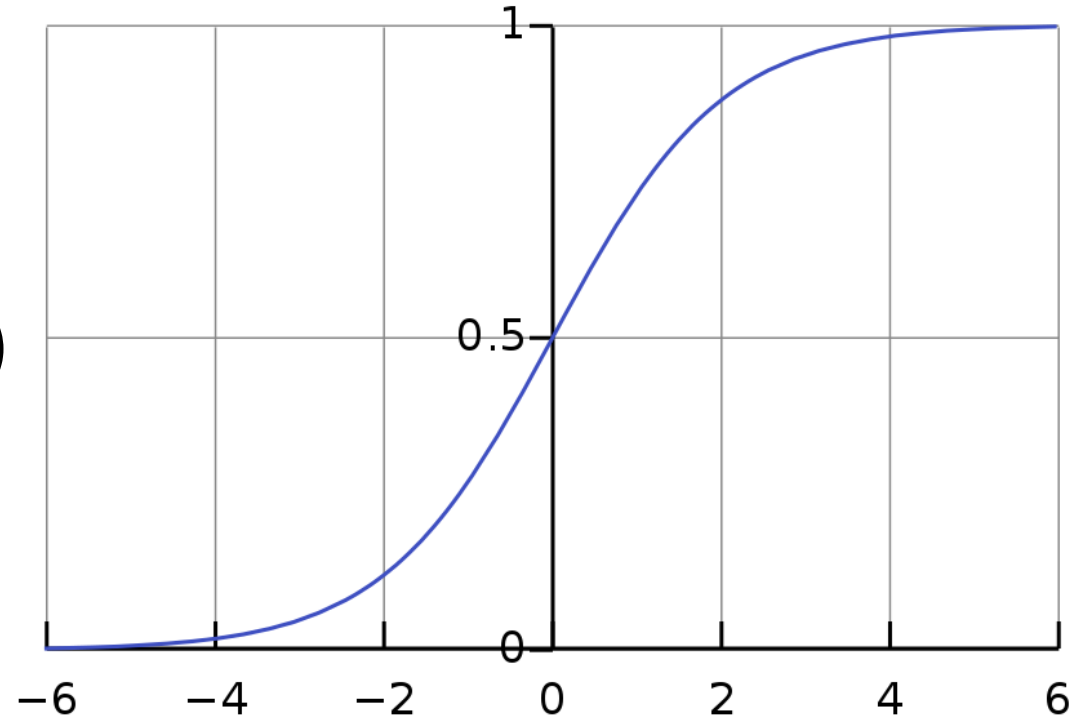
Logistic function

$Y = 1$, when $z > 0$

...

$$(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n) > 0$$

$P(y=1)$

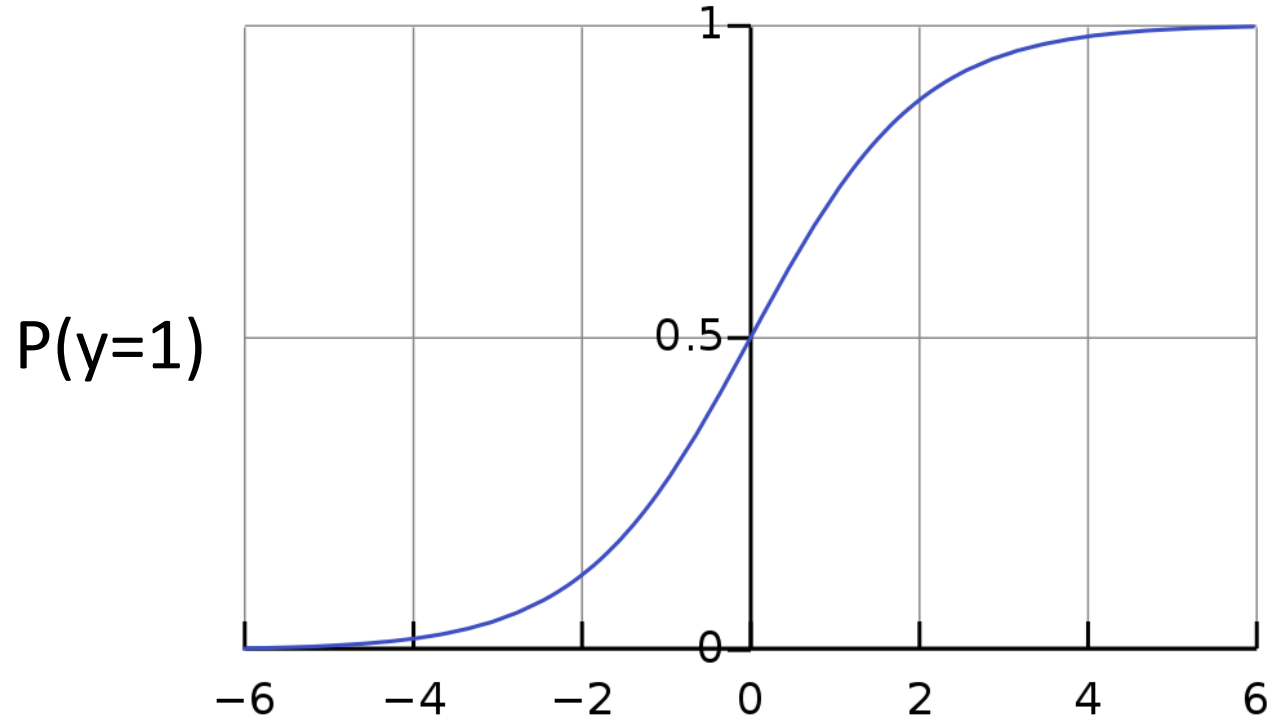


$$(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n)$$

Logistic function

$$(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n) > 0$$

- If $\beta = 0$, the feature does NOT affect the probability of the outcome.
- Positive values of β increase the probability of the outcome.
- Negative values of β decrease the probability of the outcome.

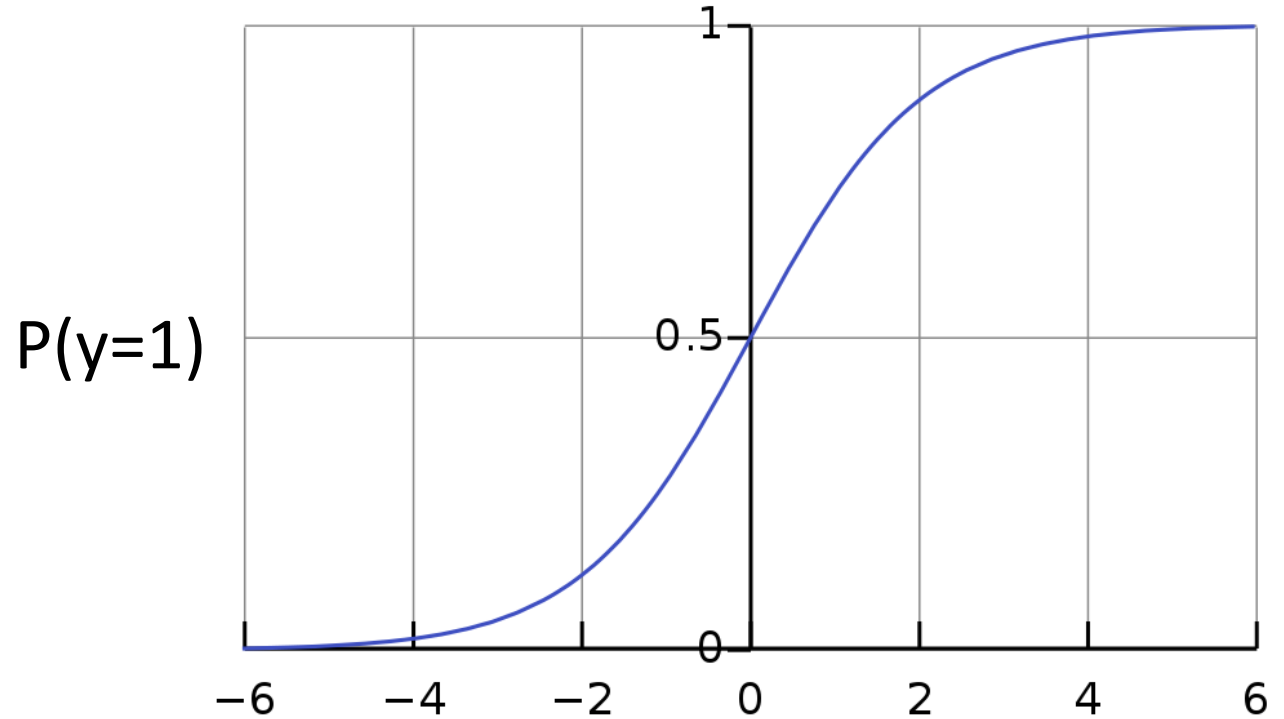


$$(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n)$$

Logistic function

The coefficients (β) are selected to predict:

- High probability when $y = 1$.
- Low probability when $y = 0$.



$$(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n)$$

THANK YOU

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