



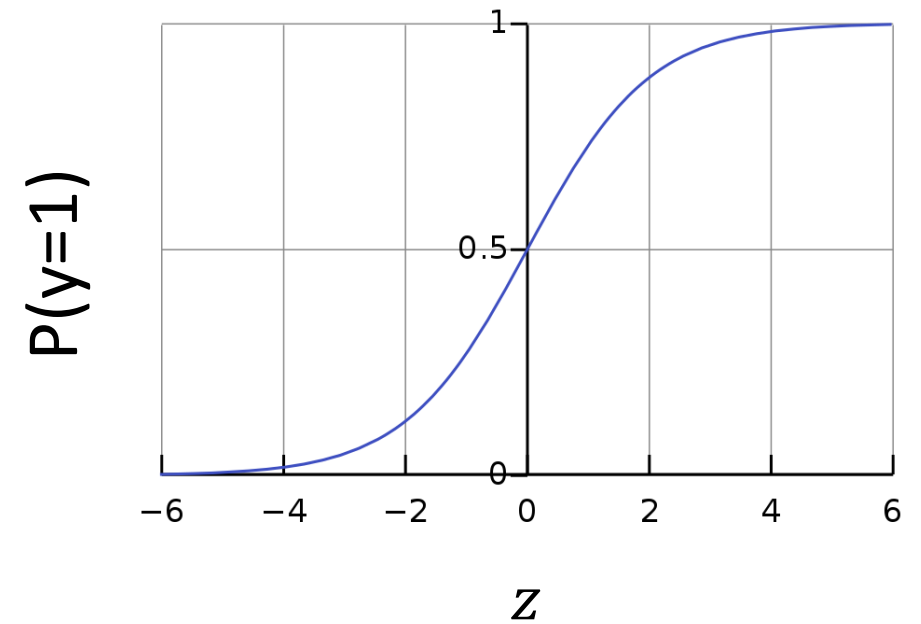
# Assessing the coefficients



# Logistic Regression Model

$$P(y=1 | X) = \frac{1}{1 + e^{-(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n)}}$$

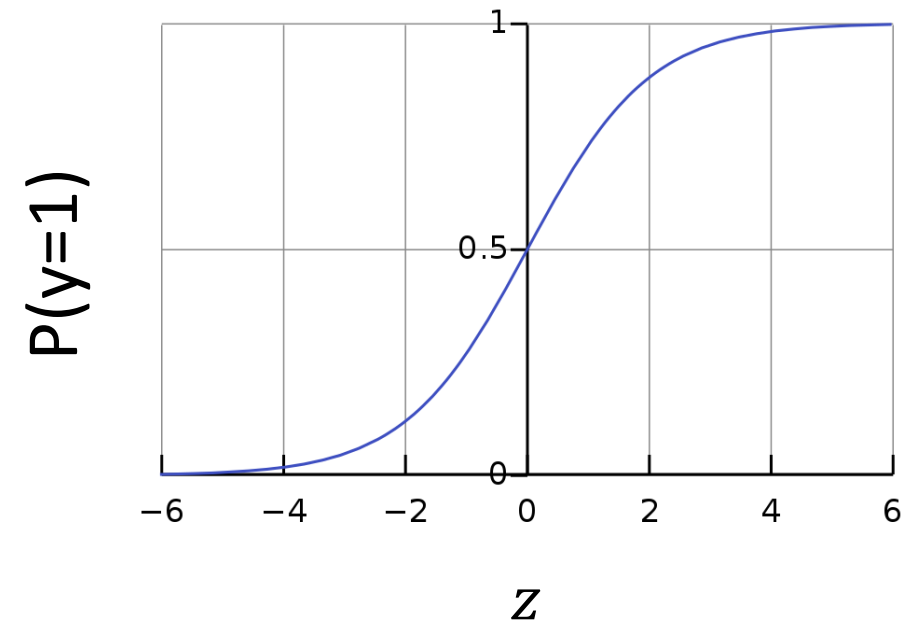
$$P(y=1 | X) = \frac{1}{1 + e^{-z}}$$



# Logistic Regression Model

$$(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n) > 0$$

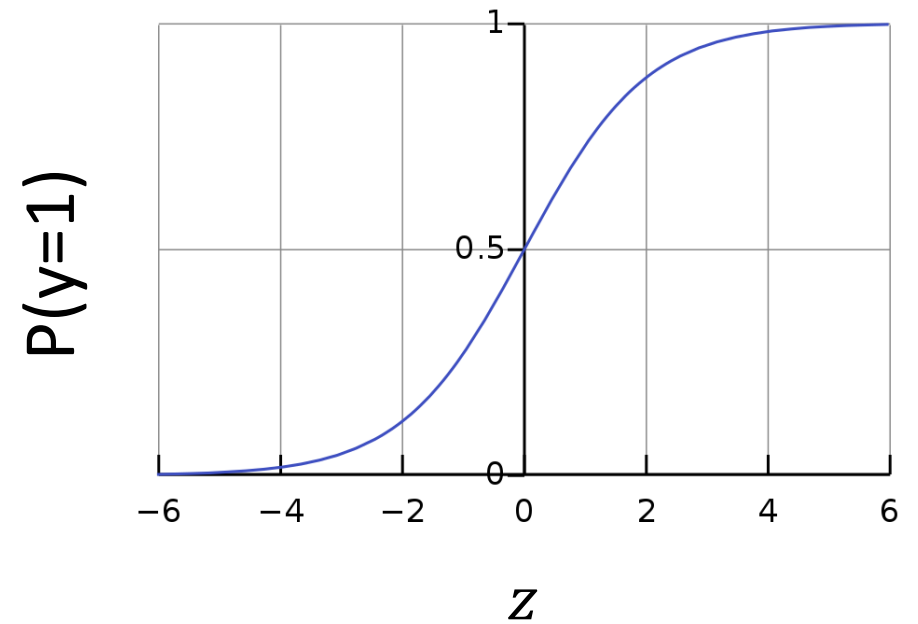
- $\beta = 0$ , the feature does NOT affect the probability of the outcome.
- $\beta > 0 \rightarrow$  increase  $p(y=1)$
- $\beta < 0 \rightarrow$  decrease  $p(y=1)$



# Logistic Regression Model

$$(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n) > 0$$

Is  $\beta$  significantly different from 0?



# Wald-test

Null hypothesis:  $\beta = 0$

$$z = \frac{\beta}{SE\beta}$$

$z \sim$  normal distribution

Large  $\beta$  or smaller  $SE\beta$  indicate that we can trust the coefficient.

# Wald-test

Null hypothesis:  $\beta = 0$

$$z = \frac{\beta}{SE\beta}$$

$z \sim$  normal distribution



When  $\beta$  is large,  $SE\beta$  is inflated  
→  $z$  is underestimated



# Coefficients error

How can we calculate it?



# Coefficients error estimation

- Cross-validation
- Bootstrapping
- Empirically



# Statsmodels

$$\hat{se}_j = \sqrt{((X^T \hat{W} X)^{-1})_{jj}},$$

- X is the predictor matrix
- W is the covariance matrix

<https://web.stanford.edu/class/archive/stats/stats200/stats200.1172/Lecture26.pdf>

# THANK YOU

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