

Electro- magnetic field of a moving point charge

See landar / Linkitz:

The electric field

The electric field of a moving change e @ position sie with velocity sie is given as

$$\vec{\epsilon}(\vec{x}) = e^{-\frac{\vec{x}^2 - \vec{x}_e}{|\vec{x} - \vec{x}_e|^3}} \frac{1 - v^2}{\left(1 - v^2 \sin^2 \theta\right)^{3/2}}$$

where (\$\frac{1}{2} - \frac{1}{2} = |\vec{v}| |\frac{1}{2} - \frac{1}{2} | \cos \text{0}

The downant conhistion in the limit region is

$$\vec{E}(\vec{x}) = e \vec{x} - \vec{x}_e + O(v^2)$$

$$|\vec{x} - \vec{x}_e|^3$$

The magnetic field

The magnetic field of change e @ position The velocity to is given as

The do-innt conhibetion is

$$\vec{H} = e \frac{\vec{v} \times (\vec{x} - \vec{x}_e)}{|\vec{x} - \vec{x}_e|^3} + O(v^3)$$

Next, we consider two charges it each other potential, moving on a circular orbit, and determine the frequency:

Eq. of notion of a particle in que external field:

where $\vec{p} = \frac{m}{\sqrt{1-re^2}} \vec{v}$, For low velocities:

$$m \frac{d\vec{v}}{dt} = e \left[\vec{E}_{ext} + \vec{v} \times \vec{H}_{ext} \right]$$

now, insert the fields produced by a change ez @ \fiz 13

$$M_1 \frac{\sqrt{\vec{v}_1}}{dt} = e_1 \left[e_2 \frac{\vec{x}_1 - \vec{x}_2}{|\vec{x}_1 - \vec{x}_2|^3} + e_2 \vec{v}_1 \times \left(\vec{v}_2 \times \frac{\vec{x}_1 - \vec{x}_2}{|\vec{x}_1 - \vec{x}_2|^3} \right) \right] + O(\vec{v}_2^2)$$

=
$$e_1 e_2 \frac{\vec{x}_1 - \vec{x}_2}{|\vec{x}_1 - \vec{x}_2|^3} + O\left(\text{Max}\left(\vec{n}_1^2, \vec{v}_2^2, \vec{v}_1 \vec{v}_2\right)\right)$$

For the purpole 2; we obtain the sme equation modulo 1472 is

$$\frac{d}{dt} \left(\overrightarrow{v}_1 - \overrightarrow{v}_2 \right) = e_1 e_2 \frac{\overrightarrow{x}_1 - \overrightarrow{x}_2}{|\overrightarrow{x}_1 - \overrightarrow{x}_2|^3} \left(\frac{1}{m_1} + \frac{1}{m_2} \right)$$

define $\vec{x}_1 - \vec{x}_2 = \vec{y}$, $\frac{m_1 m_2}{m_1 + m_2} = : \rho$, get $e_1 e_2 = : \times$

$$\mu \frac{d^2}{dt^2} \vec{y} = \propto \frac{\vec{y}}{|\vec{y}|^3}$$

we also find that
$$\frac{d}{dt} \left(m_1 \vec{v}_1 + m_2 \vec{v}_2 \right) = 0$$

Let's try the solution
$$\overline{y} = \begin{pmatrix} \cos(\omega t) \\ \sin(\omega t) \end{pmatrix} d$$
, and obtain

$$-\mu\omega^{2}\vec{y} = \alpha \frac{\vec{y}}{d^{3}} \iff \omega^{2} = -\frac{\mu\alpha}{d^{3}}$$

Then position of the charges:

$$\vec{x}_s = m_1 \vec{x}_1 + m_2 \vec{x}_2 \implies \vec{x}_2 = \frac{1}{m_2} \left(\vec{x}_s - m_1 \vec{x}_1 \right)$$

$$\vec{y} = \vec{x}_1 - \vec{x}_2 \iff \vec{x}_1 = \vec{y} + \vec{x}_2$$

$$= \frac{1}{1 + \frac{m_1}{m_2}} \left(\vec{x} + \frac{\vec{x}_3}{m_2} \right) = \frac{m_2}{m_2 + m_1} \left(\vec{x} + \frac{\vec{x}_3}{m_2} \right)$$

Here:
$$\vec{x}_s = 0$$
, thus $\vec{x}_s = \frac{m_z}{m_z + m_z} \vec{x}$

$$\vec{x}_{z} = \frac{m_{z}}{m_{z} + m_{z}} \vec{y}$$

$$\vec{x}_{z} = -\frac{m_{z}}{m_{z} + m_{z}} \vec{y}$$

All is decked out, results are gathered on find proge

$$\vec{x}_1 = \frac{M}{M_1}$$

$$\vec{z}_1 = \frac{\mu}{m_1} \vec{z} = -\frac{\mu}{m_2} \vec{z}$$

$$\vec{y} = \begin{pmatrix} \cos(\omega t) \\ \sin(\omega t) \end{pmatrix} d$$

$$\omega^2 = -\frac{\text{Menez}}{\text{d}^3} \qquad \mu = \frac{m_1 m_2}{m_1 + m_2}$$

fields:
$$\vec{E}(\vec{z}) = e_1 \frac{\vec{x} - \vec{x_1}}{|\vec{z} - \vec{x_1}|^3} + e_2 \frac{\vec{z} - \vec{x_2}}{|\vec{z} - \vec{x_2}|^3} + O(v^2)$$

$$\vec{H}(\vec{z}) = O(v)$$