

$$H = H_{c.p.p.} + H_{EM}$$

$$= \sum_{\text{particles } i} \left\{ -(1+A_i) E_k^i - \frac{1}{2} \left[ \frac{1}{2} (\bar{\psi}_i^{\alpha\beta} - \bar{\bar{\psi}}_i^{\alpha\beta}) \frac{k_\alpha^i k_\beta^i}{(E_k^i)} + \frac{1}{2} (\bar{\psi}_i^{\alpha\beta} + \bar{\bar{\psi}}_i^{\alpha\beta}) \gamma_{\alpha\beta} \frac{(k_i)^2}{(E_k^i)} \right] \right\}$$

$$+ \int d^3x \left\{ -N^\alpha(x) \left[ A_\alpha \partial_\mu \pi^\mu + \sum_i p_\alpha^i \delta_{x_i}(x) \right] \right\}$$

$$+ \int d^3x \left\{ -(1+A) \left[ 2\pi \gamma_{\alpha\beta} \pi^\alpha \pi^\beta + \frac{1}{8\pi} \gamma_{\alpha\beta} H^\alpha H^\beta \right] - N^\alpha \epsilon_{\alpha\mu\nu} H^\mu \pi^\nu \right.$$

$$- \frac{1}{2} (\bar{\psi}^{\alpha\beta} - \bar{\bar{\psi}}^{\alpha\beta}) \left[ 2\pi (\delta_\sigma^\alpha \delta_\tau^\beta - \frac{1}{2} \gamma^{\alpha\beta} \gamma_{\sigma\tau}) \pi_\alpha \pi_\beta + \frac{1}{8\pi} (\delta_\sigma^\alpha \delta_\tau^\beta - \frac{1}{2} \gamma^{\alpha\beta} \gamma_{\sigma\tau}) H_\alpha H_\beta \right]$$

$$+ \frac{1}{2} (\bar{\bar{\psi}}^{\alpha\beta} + \bar{\psi}^{\alpha\beta}) \left[ 2\pi (\delta_\sigma^\alpha \delta_\tau^\beta - \frac{1}{2} \gamma^{\alpha\beta} \gamma_{\sigma\tau}) \pi_\alpha \pi_\beta + \frac{1}{8\pi} (-\delta_\sigma^\alpha \delta_\tau^\beta - \frac{1}{2} \gamma^{\alpha\beta} \gamma_{\sigma\tau}) H_\alpha H_\beta \right]$$

$$+ \bar{\bar{\psi}}_\mu^\beta (\delta_\nu^\mu \delta_\beta^\alpha - \delta_\beta^\mu \delta_\nu^\alpha) [H^\nu \pi_\alpha] \left. \right\} + \int d^3x \left\{ -(1+A(x)) \phi(x) \left( \partial_\alpha \pi^\alpha + \sum_i e_i \delta_{x_i}(x) \right) \right\}$$


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$$E_k^i = \sqrt{m_i^2 + k_i^2}$$

$$k_i^\alpha = p_i^\alpha - e A_i^\alpha$$

$$H^\alpha = \frac{1}{2} \epsilon^{\alpha\mu\nu} F_{\mu\nu}$$

Fields with index  $i$  are evaluated @  $\lambda_i$ , eg  $\phi_i(t) := \phi(\lambda_i(t), t)$

Canonical momenta are  $\{p_\alpha^i\}$  and  $\pi^\alpha$ , indices pulled with  $\gamma$ .

Substitute  $p_i^\alpha - e A_i^\alpha$  into the com to see that all above stuff is gauge invariant!