

# Standard Adversarial Training

## Theory and Review

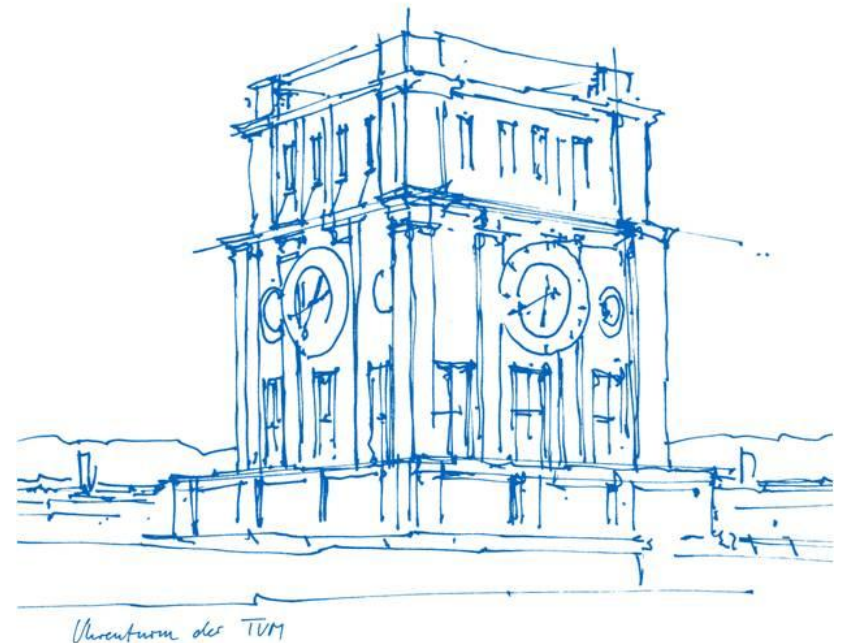
Technical University Munich

Chair of Computer Science

Machine Learning Seminar, SS21

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# Adversarial Examples

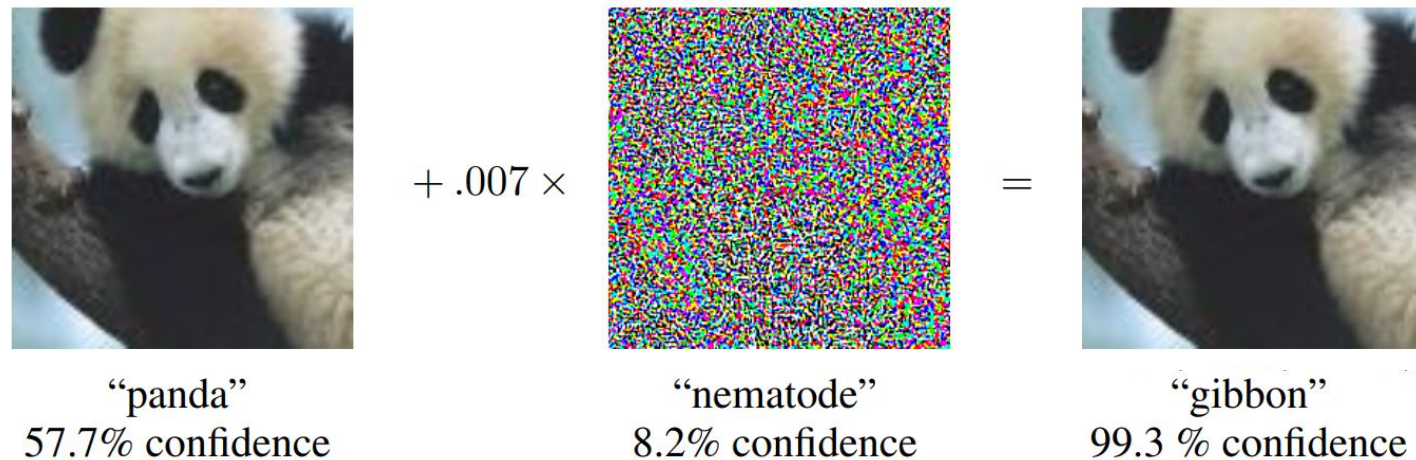


Fig 1: Adversarial example on GoogLeNet [1]

- Perturbing input s.t. it causes misclassification
- Here, perturbations constrained within  $L_p$  - ball

# Adversarial Examples



Fig 2: Adversarial example in real life applications, left: graffiti, right adversarial attack [2]

- Stop sign get classified as speed limit sign

# Adversarial Examples

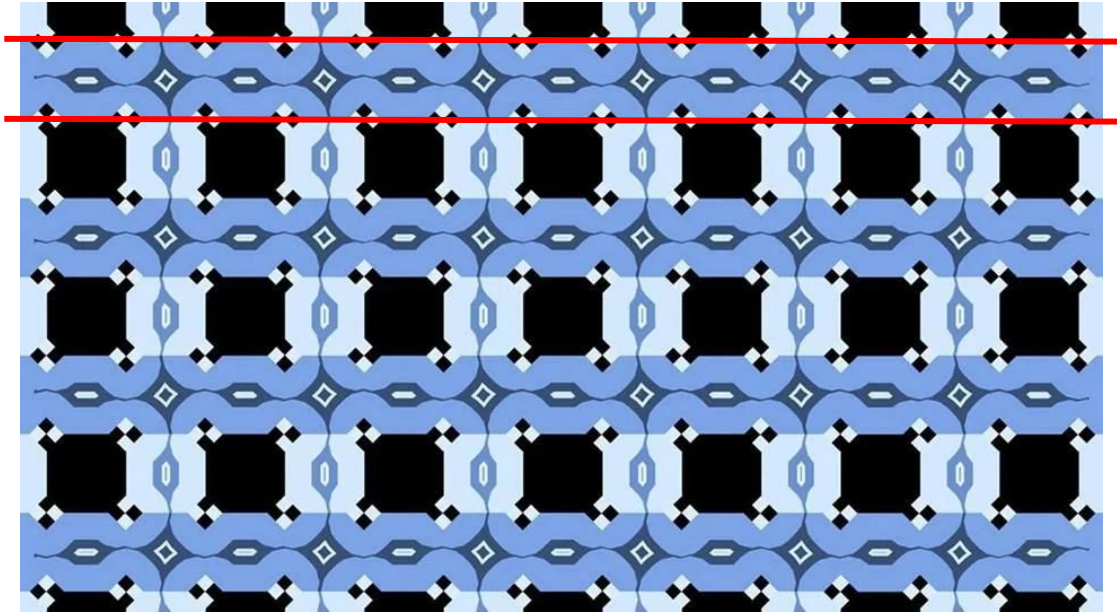


Fig 3: optical illusion for human brain [3]

- blue lines are straight and horizontal

# Why are neural networks prone to adversarial examples?

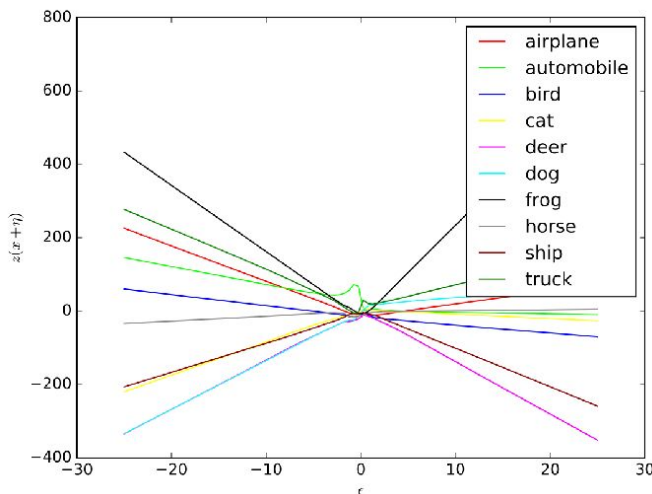


Fig 4: decision boundaries for a model trained on CIFAR10 [4]

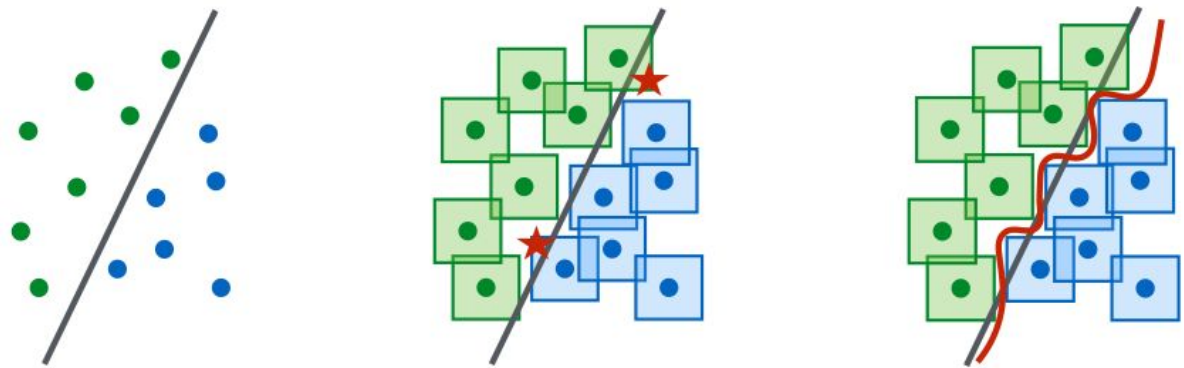


Fig 5: conceptual illustration of standard and adversarial decision boundaries [5]

- Excessive linearity of the decision boundaries

[4] Image taken from “Adversarial Examples and Adversarial Training” by Goodfellow et al.

[5] Image taken from “Towards Deep Learning Models Resistant to Adversarial Attacks” by Madry et al.

# How to create adversarial examples?

- find perturbation  $\delta$  that maximizes classification loss  $\ell$

$$\max_{\delta \in \Delta} \ell(f_{\theta}(x_i + \delta), y_i)$$

$$\Delta = \{\delta : \|\delta\|_p \leq \epsilon\} \quad \text{with} \quad \epsilon > 0$$

- $\Delta$  being the threat model  
(bounded by an  $L_p$  - ball of size  $\epsilon$ )
- How? projected gradient ascent for  $x$

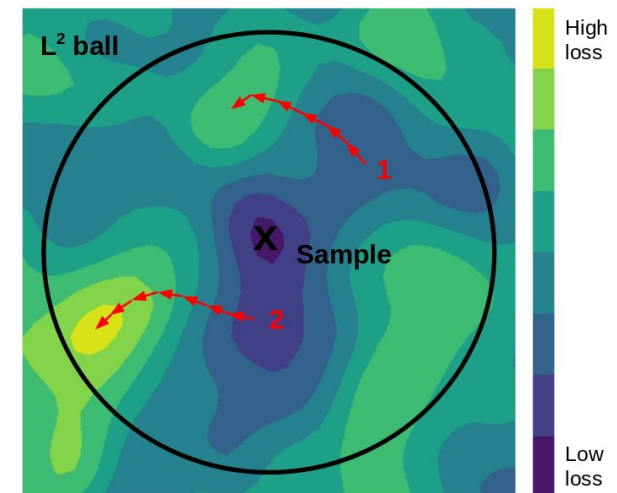
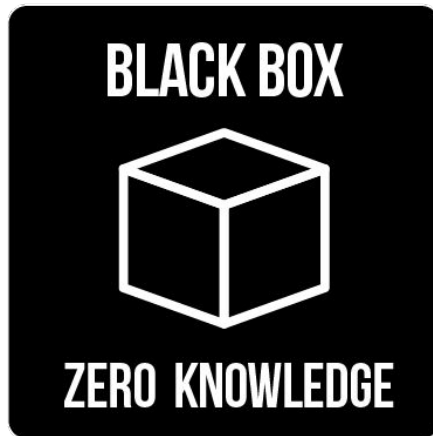
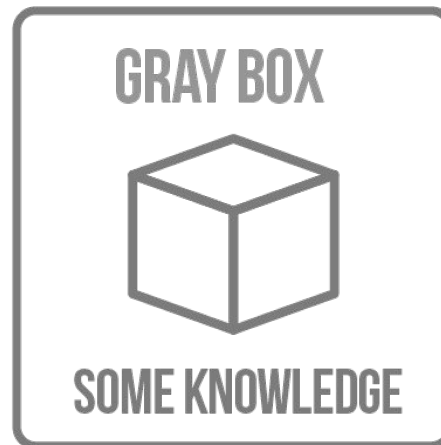


Figure 6: “The dynamics of a PGD attack in the loss landscape” [6]

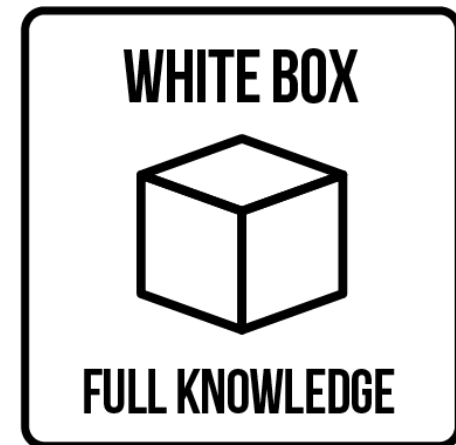
# Types of adversarial attacks



manual process,  
starting with random  
input



train substitute model,  
proceed like white box  
attack



gradient ascent to  
generate adversarial  
samples

Adversarial attacks are **model agnostic!**



# Types of adversarial attacks



Figure 7: Examples of adversarial attacks[7]



# How to defend against adversarial attacks?

- basic idea: use adversarial examples for training

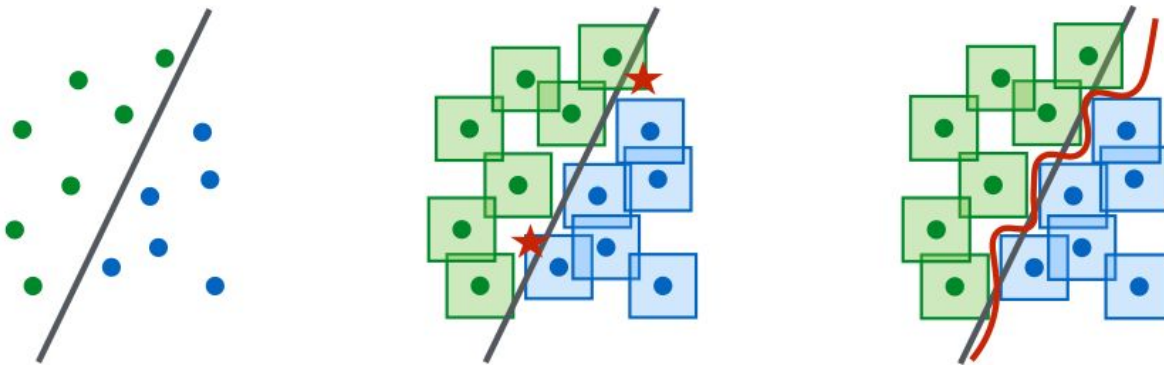


Fig 8: conceptual illustration of standard and adversarial decision boundaries [5]

# How to defend against adversarial attacks?

- basic idea: use adversarial examples for training

$$\min_{\theta} \sum_i \max_{\delta \in \Delta} l(f_{\theta}(x_i + \delta), y_i)$$

$$\Delta = \{\delta : \|\delta\|_p \leq \epsilon\} \quad \text{with} \quad \epsilon > 0$$

- Challenge: how to calculate derivative?

# Danskin's Theorem

*The (sub)gradient of a function containing a max term can be found by taking the gradient at the point of the maximum  $\delta^*$ .*

$$\nabla_{\theta} \max_{\|\delta\| \leq \epsilon} l(f_{\theta}(x_i + \delta), y_i) = \nabla_{\theta} l(f_{\theta}(x_i + \delta^*(x_i)), y_i)$$

- Requirements:
  - Convex loss function
  - only holds for exact maximum
- Limitations:
  - robustness depends on precision of maximum

# Robust Optimization

- formulation as saddle point problem

$$\min_{\theta} \sum_i \max_{\delta \in \Delta} l(f_{\theta}(x_i + \delta), y_i)$$
$$\Delta = \{\delta : \|\delta\|_p \leq \epsilon\} \quad \text{with} \quad \epsilon > 0$$

- robustness stems from strongness of attack model

# Fast Gradient Sign Method (FGSM)

- take single step into gradient direction
- step size =  $\epsilon$  to stay in  $L_p$  - ball

$$\tilde{x} = x + \epsilon \cdot \text{sgn}(\nabla_x l(\theta, x, y))$$

- Fast, but not accurate

# Multistep Projected Gradient Descent (K-PGD)

- take  $k$  smaller steps into gradient direction
- step size =  $\alpha$
- project back on  $L_p$  - ball if step outside

$$\tilde{x} = \Pi(x + \alpha \cdot \text{sgn}(\nabla_x l(\theta, x, y)))$$

setting  $k = 1$  and  $\alpha = \epsilon$  resembles FGSM

- more accurate, but slow

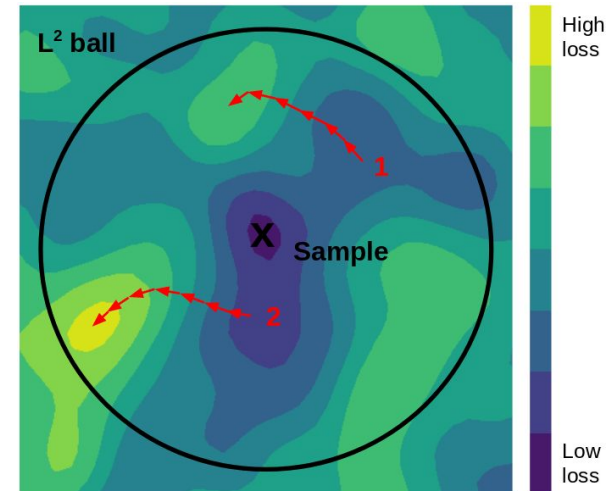


Figure 9: “The dynamics of a PGD attack in the loss landscape” [6]

# Multistep Projected Gradient Descent (K-PGD)

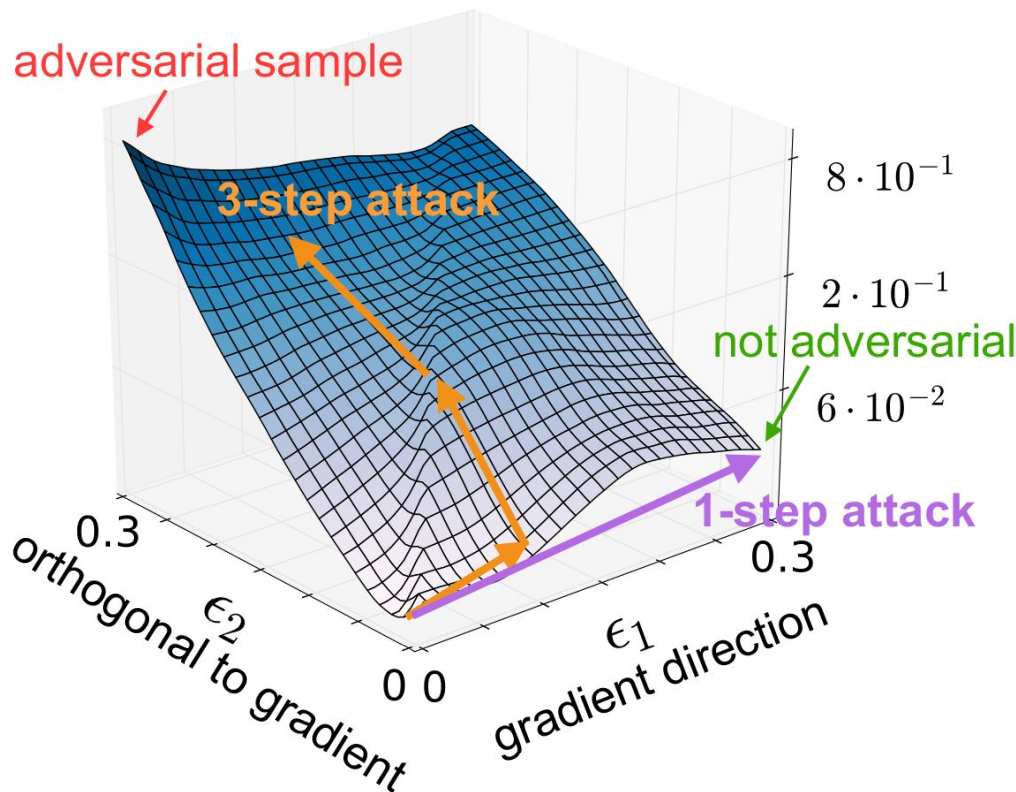


Figure 10: Comparison of FGSM and 3-PGD [8]



# Advancements on FGSM

- Free Training:
  - re-use gradients from previous time step
  - mini batch replay
  - warm start with previous perturbation
- Fast Training:
  - re-use gradients from previous time step
  - random initialize perturbation

# Universal Adversarial Training

- find a **single** perturbation that works on many inputs

$$\min_{\theta} \max_{\delta \in \Delta} \frac{1}{N} \sum_{i=1}^N \hat{l}(f_{\theta}(x_i + \delta), y_i)$$

with  $\hat{l}(f_{\theta}(x_i + \delta), y_i) = \min\{l(f_{\theta}(x_i + \delta), y_i), \beta\}$

- $\beta$  bounds the loss from above to hinder a single sample to dominate the average loss
- advancement: relax formulation to allow perturbations **per class**

# Universal Adversarial Training

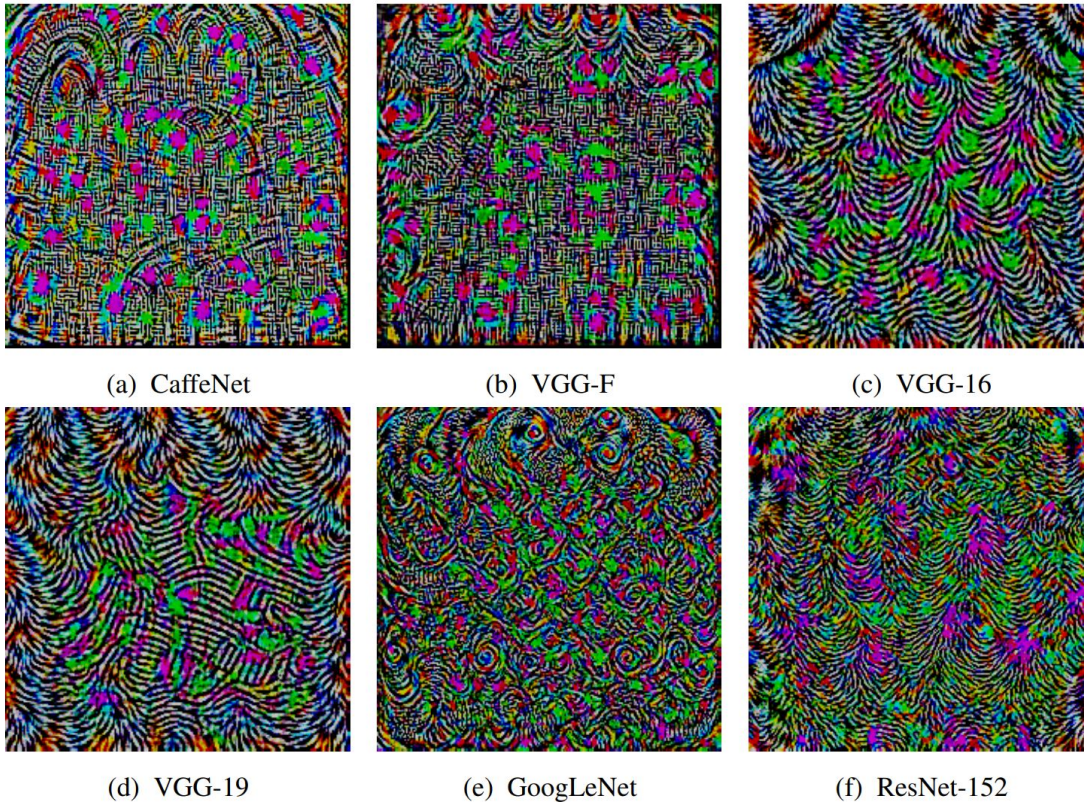


Figure 11: “Universal perturbations computed for different deep neural network architectures.” [9]

# Margin Maximization

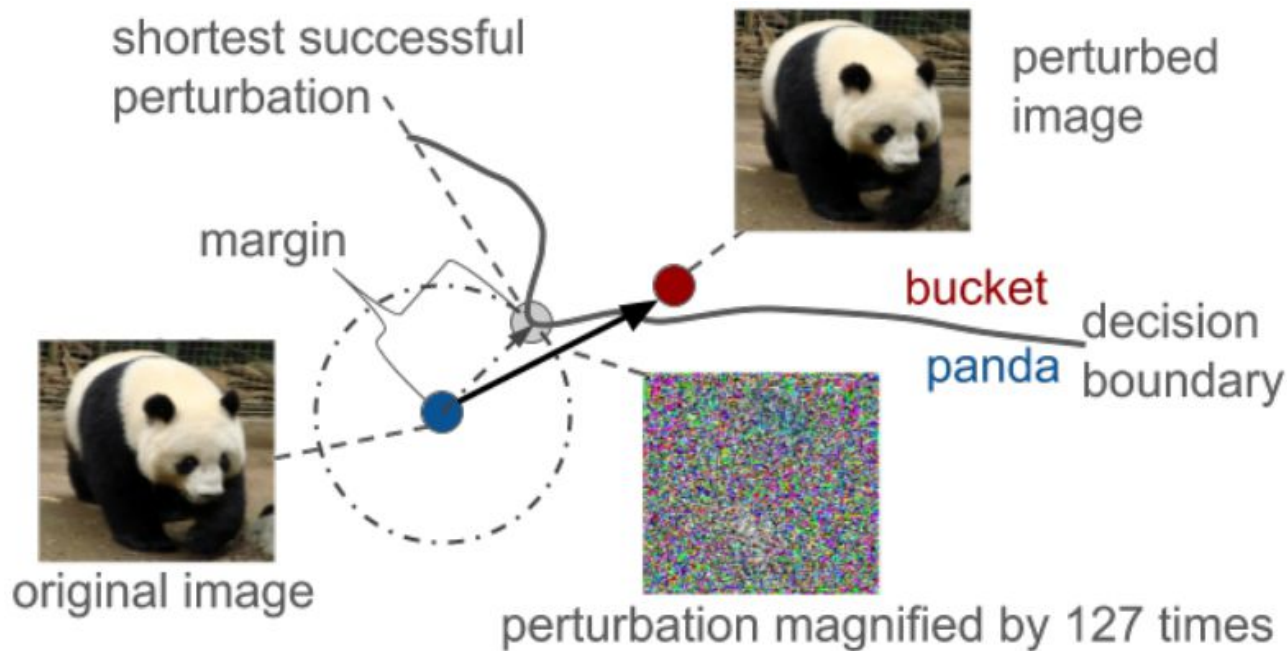


Figure 12: “Illustration of decision boundary, margin, and shortest successful perturbation on application of an adversarial perturbation.”

[10]

[10] Image taken from “MMA Training: Direct input space margin maximization through adversarial training” by Ding et al.

# Margin Maximization

- maximize margin
- margin = smallest successful perturbation  $\delta^*$

$$\begin{aligned} d_\theta(x, y) &= \|\delta^*\| = \min \|\delta\| \\ \text{s.t. } \delta &: L_\theta^{01}(x + \delta, y) = 1 \end{aligned}$$

- Two fold problem:

$$\min_{\theta} \left\{ \sum_{i \in S_\theta^+} \max\{0, d_{\max} - d_\theta(x_i, y_i)\} + \beta \sum_{j \in S_\theta^-} l_\theta(x_j, y_j) \right\}$$

# Review

Method	Robust accuracy	Training time
K-PGD	baseline	baseline
FGSM	--	+
Free Training	-	+
Fast Training	-	+
Universal Training	--	++
Class-wise universal training	-	+
Margin Maximization	0	0

# Open Research Questions

- Precision of finding maximum
- Speed for finding maximum
- Robustness against multiple attack models
- Influence of hyperparameters for robustness



Thank you!

# References

- [1] Goodfellow et al., Explaining and Harnessing Adversarial Examples. <https://arxiv.org/abs/1412.6572>.
- [2] Eykholt et al., Robust physical-world attacks on deep learning visual classification. 2018. <https://arxiv.org/pdf/1707.08945.pdf>.
- [3] Express, Optical illusion BAFFLES the internet – can YOU spot the straight parallel blue lines?, <https://www.express.co.uk/life-style/life/944779/optical-illusions-illusion-pictures-best-viral-puzzle-blue-lines-picture>.
- [4] Aleksander Madry et al., Towards Deep Learning Models Resistant to Adversarial Attacks. 2019.

# References

- [5] Goodfellow. Adversarial Examples and Adversarial Training. 2016, [https://berkeley-deep-learning.github.io/cs294-dl-f16/slides/2016\\_10\\_5\\_CS294-131.pdf](https://berkeley-deep-learning.github.io/cs294-dl-f16/slides/2016_10_5_CS294-131.pdf).
- [6] Medium. Ignorance is Bliss: Adversarial Robustness by Design with LightOn OPUs. 2020, <https://medium.com/@LightOnO/ignorance-is-bliss-adversarial-robustness-by-design-with-lighton-opus-4f143fa629b>
- [7] PyImageSearch. Targeted adversarial attacks with Keras and TensorFlow. <https://www.pyimagesearch.com/2020/10/26/targeted-adversarial-attacks-with-keras-and-tensorflow/>

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- [8] Tramer et al. Ensemble adversarial training: Attacks and defenses. 2018.
- [9] Moosavi-Dezfooli et al. Universal adversarial perturbations. 2017. <https://arxiv.org/pdf/1610.08401.pdf>.
- [10] Ding et al. MMA Training: direct input space margin maximization through adversarial training. 2020. <https://arxiv.org/pdf/1812.02637.pdf>.