Project II: 2021 Prof. Manevitz.

Kohonen (SOM) Algorithm

Try to get both Part A and Part B in by June 9, however, the penalties for lateness are as indicated.

Part A (Due June 9)

(-5 points by June 16, -15 by June 15, additional -10 for each week afterward).

This project requires you to implement the Kohonen (SOM) algorithm.

You should use your code.

You are responsible for experimenting with and finding the appropriate parameters that make it work well. You may submit with a partner. You cannot share code between groups, but you can discuss the problem freely on the forum or WhatsApp group.

1. Implement the Kohonen algorithm and use it to fit a line of neurons to a disk (That is, the data set is $\{(x,y) \mid 0 \le x \le 1, 0 \le y \le 1\}$ for which the distribution is uniform while the Kohonen level is linearly ordered).

Do this when you use only a few neurons (15), when Do you use many (200)? What happens as the number of iterations of the algorithm increases?

Do the same with at least **two non-uniform distributions** on the disk (For example, when the likelihood of picking a point in the data set is proportional to the size of x, but uniform to the size of y).

You should report with snapshots of the space as the Kohonen map evolves as the number of iterations grows.

2. Now do the same experiments as above for fitting a circle of neurons on a "donut" shape i.e. $\{\langle x.y \rangle \mid 1 \leq x^2 + y^2 \leq z\}$. The line of neurons has 30 neurons. Be sure to report on the results of your different attempts (Give snapshot as the map evolves over iterations).

Part B (Due June 30)

(-10 if done by July 7, -20 if done by July 14, last submission time). You may find it helpful to look over the diagrams in the chapter at https://www.ks.uiuc.edu/Services/Class/PHYS498TBP/spring2002/neuro_7.pdf

Now reproduce the experiment on the "monkey hand" as described in class. For this part, you can use your code or the Kohonen algorithm in a package (like the SOM package in Matlab). Be sure to state what code you are using

In more detail:

- **1.** given diagram like the following; where the data is $\langle x,y \rangle$ is inside the "hand" which is located as a subset of $\{\langle x,y \rangle \mid 0 <= x <= 1, 0 <= y <= 1\}$ and the Kohonen space is 225 neurons arranged in a 15 x 15 mesh (That means data points are only within the "hand"). Show how the mesh is superimposed on the plane that contains the hand and how it changes over iterations (You can use any "hand like" figure with 4 "fingers" you wish).
- **2.** Now "cut off a finger" (i.e. data points come only from the "hand with 3 fingers"), and then continuing from the stopping point in the previous section. Show over snapshots how the mesh is rearranged.



