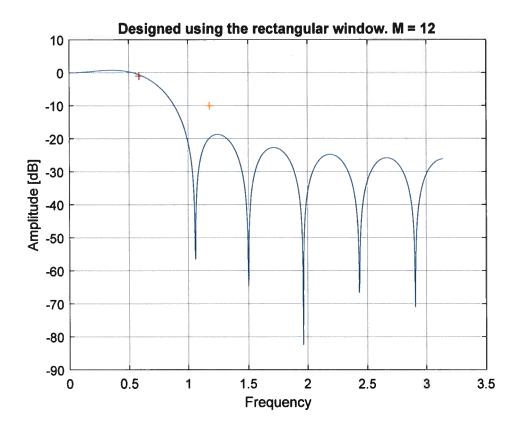
The LECTURE SUGGESTED SOLUTION. o Design a TYPE-I File filter with we="14 using the Window method. The filter should comply with the specifications for the LP-filter designed in Lecture 3. Desired trequercy response; $\frac{-j\omega \frac{1}{2}}{4} = \frac{-j\omega \frac{1}{2}}{4} = \frac{1}{4}$ $\frac{1}{4}(e^{j\omega}) = 0 \quad \frac{1}{4}(1\omega) \leq 1$ from which we can derive the ideal impulse regarde hy[n] = 211 | 4 -jw/2 jwn -11/2 $= 2\pi \int_{-\pi/2}^{\pi/4} \left(\cos \left((n - \frac{1}{2}) \omega \right) + j \sin \left((n - \frac{1}{2}) \omega \right) d\omega$ $= 2\pi \left[\sin \left((1 - \frac{1}{2}) \omega \right) \right]^{\frac{1}{4}} \cdot \frac{1}{1 - \frac{1}{4}}$ $= \frac{1}{2\pi(n-\frac{1}{2})} \cdot \left\{ \sin(\frac{\pi}{4(n-\frac{1}{2})}) - \sin(-\frac{\pi}{4(n-\frac{1}{2})}) \right\}$ $\lim_{n \in \mathbb{N}} \frac{\sin(\sqrt{y}(n-\frac{y}{2}))}{\sin(n-\frac{y}{2})} - \infty \ln(\infty)$

	& Symmetric around 1/2.
0	Now, hy [n] is = infinite > non-causal
	> non-causal
	Inus we stuncate helid with a symmetric
	Thus we truncate h [i] with a symmetric window function;
	h[n] = h[n]. w[n], w[n] +0 0 ≤ n < H
0	Using equ. 140a (p.343), we can now write the frequency response for the filter (TYPE-I)
100 311	$H(e) = e^{\int w/2} \left(\frac{\sqrt{2}}{2} \cdot a[k] \cdot cos(wk) \right)$
	K=0
	Where
	where $a[o] = h[\frac{1}{2}]$ $a[k] = 2 \cdot h[\frac{1}{2} - k]$ for $k = 1, 2,, \frac{1}{2}$ Due to the symmetric impulse response $h[n]$.
0	
	Due to the symmetric impulse response h[n], the filter has linear phase response.
-	
	Thus we need to concern only about the auptitude response
	auplitude response
	1 1/2
0	$ H(e^{j\omega}) = \int_{k=0}^{\infty} a[k] \cdot cos(\omega k) $
400	K=0

0	In order to fulfill the OdB DC Gain requirement we need to find G given as;
	we need to find G given as:
	$G(H(e^{i\omega}) = 1)$
	W=0
	G/ a[k] = 1
	(51/2 alk]=1
	\ k=0
0_	1
	G= Mana alk]
	k=0
	and thus the overall Complitude response is
	Way
	He a[k]. cos(wk)
0	k=0
	Now, for given Window function Wind our task
	is to find the smallest value of M which
	Now, for given Window function Win] our task is to find the smallest value of M which satisfies the design specifications
<u></u>	
	In order to do that, white a program
	and conduct experiments with the
	In order to do that, write a program and conduct experiments with the rectangular as well as the Haming Window.
	<u></u>

```
% The program calculates the amplitude response of an M'th order TYPE-I FIR
% filter, given the desired impulse response h_d[n]
% The Rectangular Window is used for truncation of h_d[n]
clear
% Filter order (has to be even for TYPE-I FIR filters)
% Frequency sweep from 0 til PI with 1000 points
for i=0:999,
omega(i+1) = pi*i/999;
end;
% The amplitude response is now calculated for the 1000 discrete frequency
% values.
% The amplitude response has the form |H| = N(\text{omega}, k)/D(k)
for i=0:999
 % The numerator N is calculated using the summation variable sum_n
 sum_n = 0;
 % The denominator D is calculated using the summation variable sum_d
 sum_d = 0;
 % Each sum has a total of M/2+1 terms
 for k=1:(M/2)
   % First calculate the ideal impulse response sample. Note that the
   % symmetri point (k=0) is not included. This final term will be added
   % later.
   h(k) = (\sin((pi/4)*k)/(pi*k));
   a(k) = 2*h(k);
   % Now both N and D are updated
   sum_n = sum_n + (a(k) * cos(k * omega(i+1)));
   sum_d = sum_d + a(k);
 end
 % Finally, add the contribution from the symmetri point, i.e., k=0
 % For the given impulse response, this value equals 1/4
 sum_n = sum_n + 0.25;
 sum_d = sum_d + 0.25;
 % Finally, the amplitude value at the actual frequency point is calculated
 amp(i+1) = abs(sum_n)/abs(sum_d);
end,
% Plot the amplitude response (in dB) together with the specifications.
plot(omega, 20*log10(amp), omega(187), -1, '+', omega(375), -10, '+')
grid;
xlabel('Frequency')
ylabel('Amplitude [dB]')
title(sprintf('Designed using the rectangular window. M = %.0f', M))
```



```
% The program calculates the amplitude response of an M'th order TYPE-I FIR
% filter, given the desired impulse response h_d[n]
% The Hamming Window is used for truncation of h_d[n]
clear
% Filter order (has to be even for TYPE-I FIR filters)
% Frequency sweep from 0 til PI with 1000 points
for i=0:999,
omega(i+1) = pi*i/999;
end;
% The amplitude response is now calculated for the 1000 discrete frequency
% values.
% The amplitude response has the form |H| = N(\text{omega}, k)/D(k)
for i=0:999
 % The numerator N is calculated using the summation variable sum_n
 sum_n = 0;
 % The denominator D is calculated using the summation variable sum_d
 sum_d = 0;
 % Each sum has a total of M/2+1 terms
 for k=1:(M/2)
   % First calculate the ideal impulse response sample. Note that the
   % symmetri point (k=0) is not included. This final term will be added
   % later.
   h_d(k) = (\sin((pi/4)*k)/(pi*k));
   % The impulse response is now multiplied with the Hamming window
   h(k) = h_d(k) * (0.54 - 0.46*cos((2*pi)*(k + M/2)/M));
   a(k) = 2*h(k);
   % Now both N and D are updated
   sum_n = sum_n + (a(k) * cos(k * omega(i+1)));
   sum_d = sum_d + a(k);
 end
 % Finally, add the contribution from the symmetri point, i.e., k=0
 % For the given impulse response, this value equals 1/4
 sum_n = sum_n + 0.25;
 sum_d = sum_d + 0.25;
 % Finally, the amplitude value at the actual frequency point is calculated
 amp(i+1) = abs(sum_n)/abs(sum_d);
end,
% Plot the amplitude response (in dB) together with the specifications.
plot(omega, 20*log10(amp), omega(187), -1, '+', omega(375), -10, '+')
grid;
xlabel('Frequency')
ylabel('Amplitude [dB]')
title(sprintf('Designed using the Hamming window. M = %.0f', M))
```

