Digital Tignal Processing, I lecture?

Singgested Solutions Discrete-Time Impolee Response  $h(t) = \frac{1}{RC} \cdot \frac{-t}{RC}$   $h(t) = \frac{1}{RC} \cdot \frac{-t}{RC}$   $h(t) = \frac{1}{RC} \cdot \frac{-nT}{RC}$   $h(t) = \frac{1}{RC} \cdot \frac{-nT}{RC}$   $T = \frac{1}{8000} = 125.10^{6} sec.$ h[n] = 0.125. e

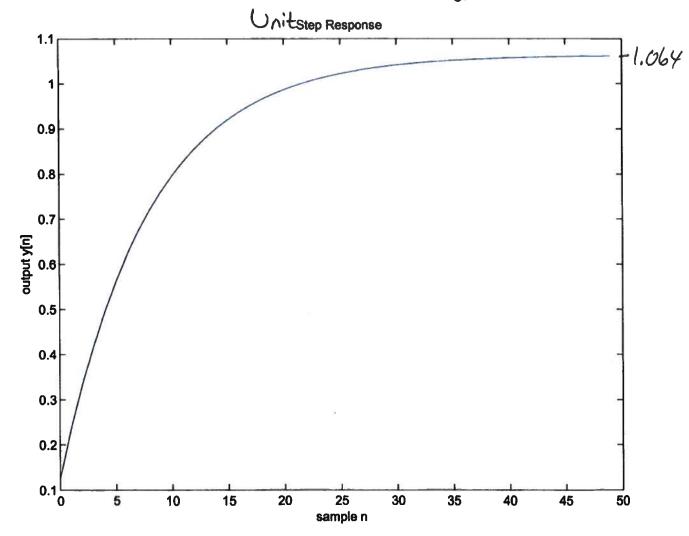
Step response is the autiput when XCT=UCT is applied to the input; push;

Write a Hallat-program to do the calculation.

```
% Beregning af Step-respons vha. foldnings-summen
y[n] = SUM[m=0..infinite] 0.125e^{-0.125m} x[n-m]
% Steprespons'en beregnes ved hjælp af to nestede loops
% Den ydre løkke opdaterer sample nummeret mens den indre
% løkke beregner selve produkt-summen.
% Der beregnes 50 samples.
clear;
for n=0:49, % n er sample-nummeret
  sum = 0; % sum benyttes til beregning af produktsummen for sample n
            % og sættes følgelig lig 0 initialt
  % Den indre løkke beregner selve produktsummen -- baseres på 100 led
  for m=0:99,
    % Bestem værdien af impulsresponsen til tidspunktet ✗俽️️️️️
    h = 0.125*exp(-0.125*m);
    % Bestem værdien af step-funktionen u[n-m]
    if (n-m) >= 0
      u = 1;
    else
      u = 0;
    end;
    sum = sum + (h * u);
  end:
  % Opdater output-sekvensen
  y(n+1) = sum; % Bemærk at MatLab ikke kan indeksere 0
end;
% Plot stepresponsen %
x(1:50)=0:49;
plot(x,y)
title('Step Response');
xlabel('sample n');
ylabel('output y[n]');
```



Bemærk, at filteret i steady\_state har et output, som numerisk er stærre erd input (UCNI). Se side 12.





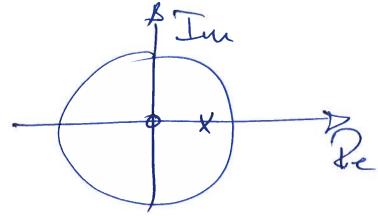
3) Transfer function.

$$\begin{cases}
 4(cz) = \frac{1}{X(cz)} = \frac{b}{1 - az^{-1}} \\
 b = \frac{T}{Rc} \text{ and } a = e^{-T/Rc}
\end{cases}$$

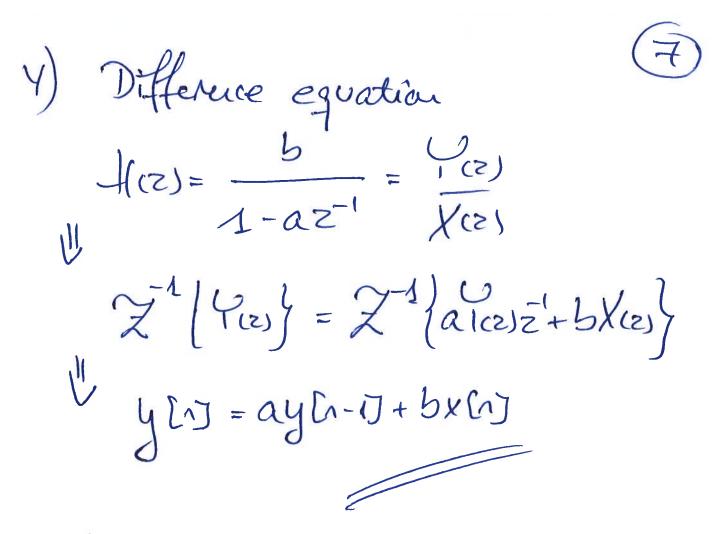
Poles and Zeros

$$H(7) = \frac{0.125}{1 - 0.88252!} = \frac{0.1252}{2 - 0.8825}$$

pode in z = 0,8825 and zero in z=0



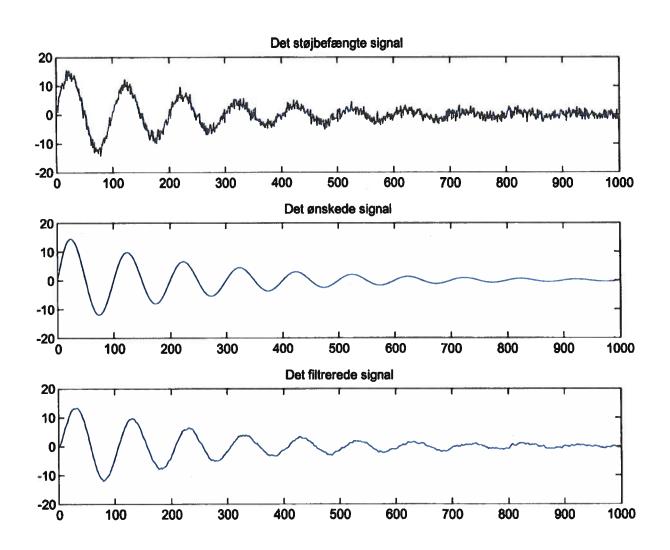
Tole is inside the unit circle



Day use this diff. equation to do the filtering of the noise contaminated signal.

```
% Anvend den styrende differens-ligning til beregning af et filtreret
% output givet et inout-signal, som er overlejret med støj
clear;
load signal_noise.dat % 1000 samples af støjbefængt signal %
load signal.dat % 1000 samples af støjfrit signal %
y(1) = 0.125 * signal_noise(1);
for n=2:1000,
  y(n) = 0.8825 * y(n-1) + 0.125 * signal_noise(n);
end;
subplot (3,1,1);
plot(signal_noise);
title('Det støjbefængte signal')
subplot(3,1,2);
plot(signal);
title('Det ønskede signal')
subplot(3,1,3);
plot(y);
title('Det filtrerede signal')
```





5) Frequercy response H(e) = H(z) | z= ejw Hier) = 0.125.edw - 6.8125 Complitude response = 0.125.  $\cos \omega + j \sin \omega$   $\cos \omega - 0.8825 + j \sin \omega$  $|H(e^{i\omega})| = 6.125 - \frac{|\cos\omega + j\sin\omega|}{|\cos\omega - 0.8825 + j\sin\omega|}$ 

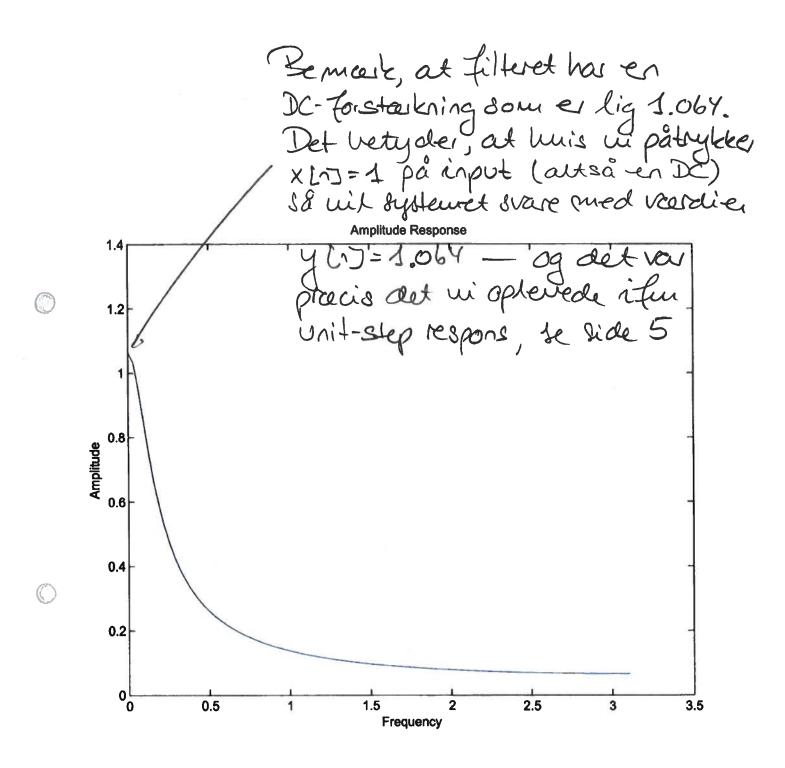
```
% Plot filterets amplituderespons
% Først genereres en frekvens-akse med 100 punkter i intervallet [0;PI]
for i=0:99,
   omega(i+1) = (pi*i)/100;
end;

% Dernæst beregnes amplitude-værdierne for hvert enkelt frekvens-værdi
amplitude = zeros(100,1);
for i=1:100,
   naevner = sqrt((cos(omega(i)) - 0.8825)^2 + (sin(omega(i)))^2);
   amplitude(i) = 0.125/naevner;
end;

plot(omega,amplitude)
xlabel('Frequency');
ylabel('Amplitude');
title('Amplitude Response');
```



PY



3dB frequercies on The analog filter has His);  $H(s) = \frac{1}{sRC+1}$  $\frac{1}{1} + \frac{1}{1} = \frac{1}{1}$   $\frac{1}{1} = \frac{1}{1}$ 1 | H(jx) = | - 1 | 1+ jxrc | (H) (jQ) = - (erc)2

The 3dB freq. is the freq. where the applitude has decreased 3dB as related to DC (SL=0).

 $-3dB = 20\log x \Rightarrow x = 6,707 \sim \frac{1}{2}$ 

1 (2.RC = 1  $V = \frac{1}{RC}$ 1 2 Tf = 1 J= 159 Hz Similarly, we can countate the freq. for the discrete-time filter;

| H(e) = 1/2. | H(e) |

= 1.06383 1.41421 = 0.7522

Thus; | H(e) 348) = 0,7522 V(cosw - 0,8825)2+ sin water (After several calculations)  $\omega = \frac{2\pi f_{3aB}}{1}$  $0.125 = \frac{2\pi \cdot f_{3dR}}{8000}$ So, the 3DB freq. is identical for the analog and the digital