

# Communication Systems

## Antenna and Propagation.

( Lecture 1 Basic Antenna parameters)

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# Overview

Function of antennas

How antennas work

Antenna types

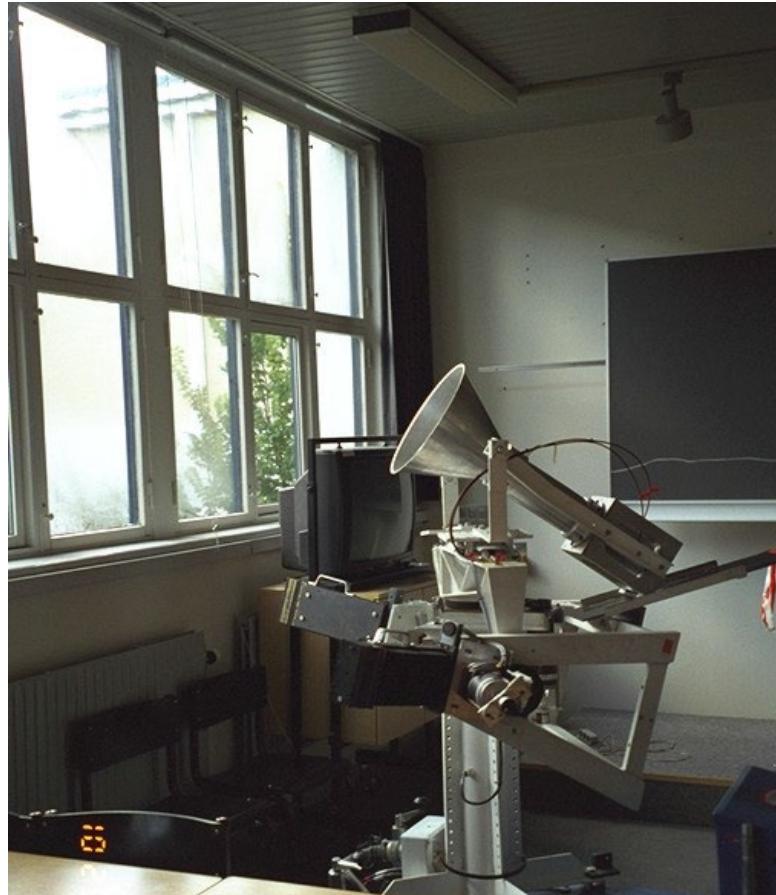
Field regions

Directive properties, (Gain and Directivity)

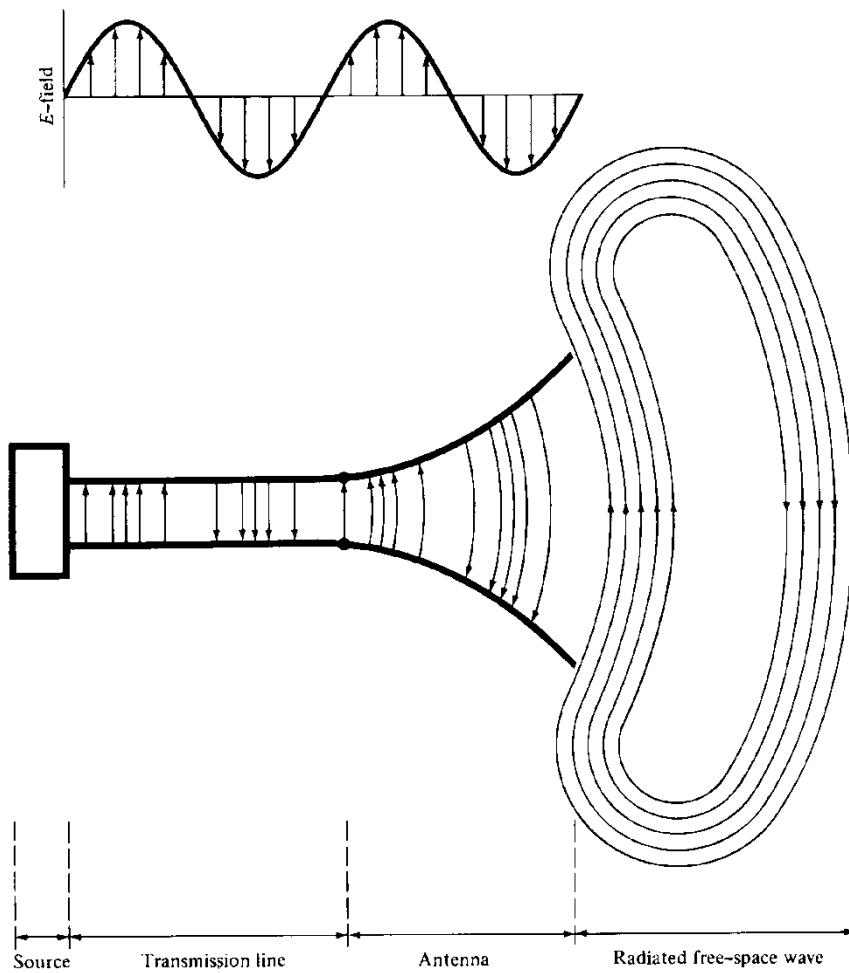
Radiation from simple dipoles

Antenna Efficiency

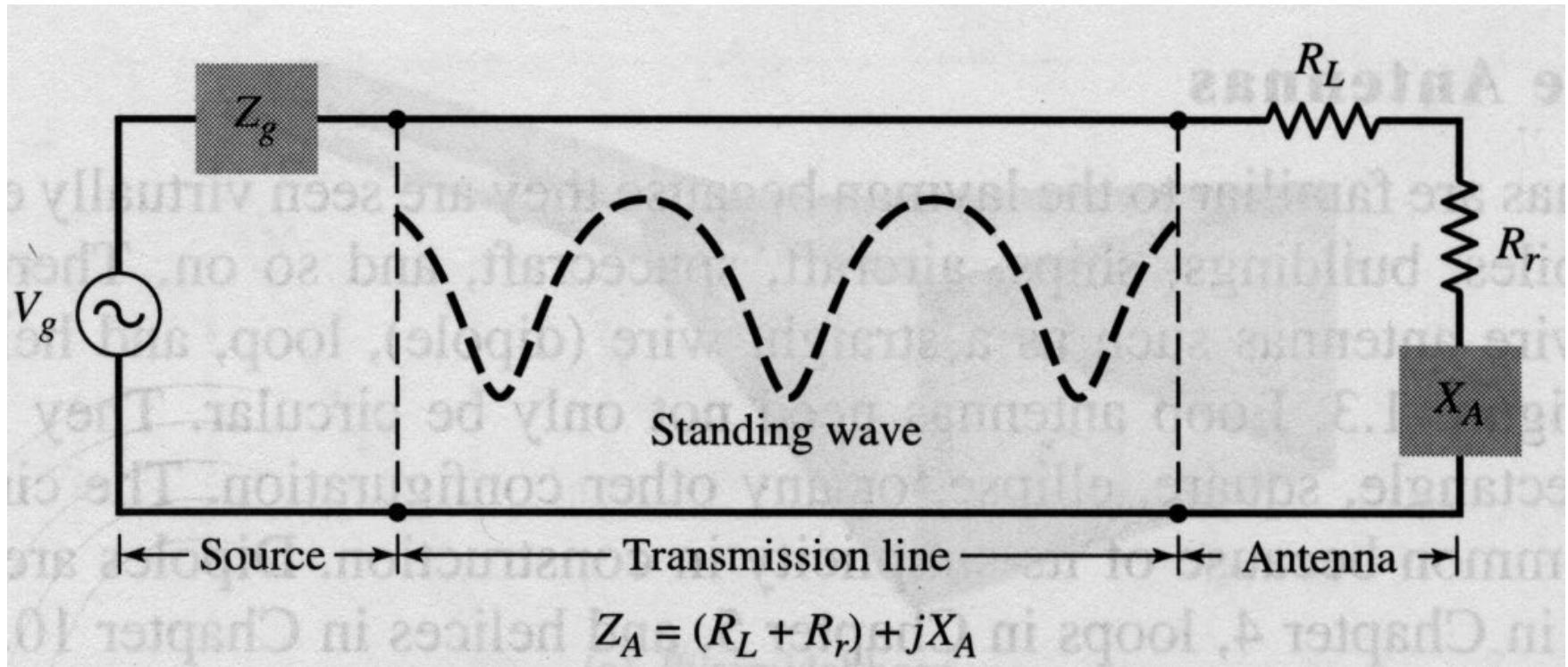
# Based on IEEE Standard Definitions and C. A. Balanis *Antenna Theory*



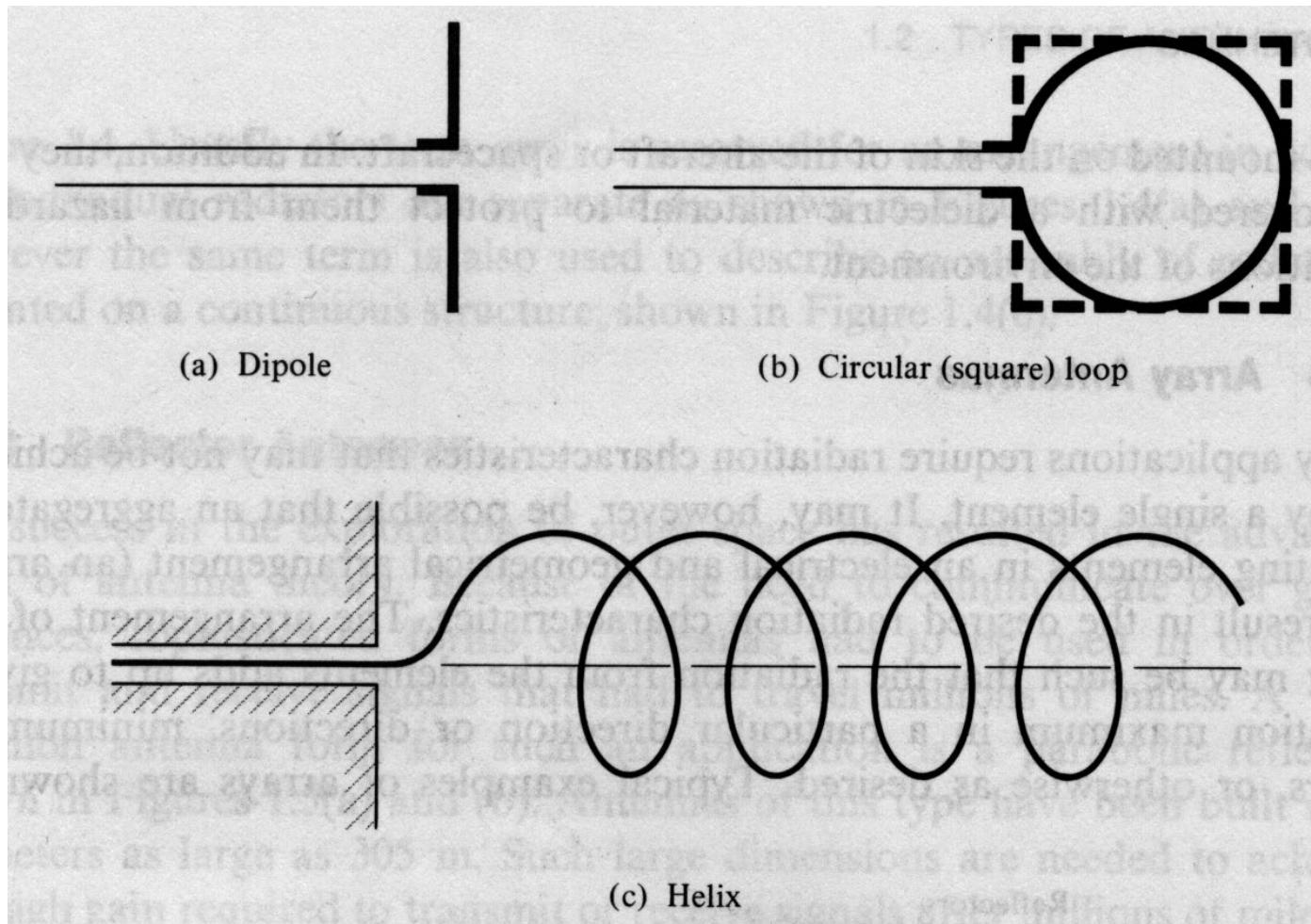
# What is an Antenna



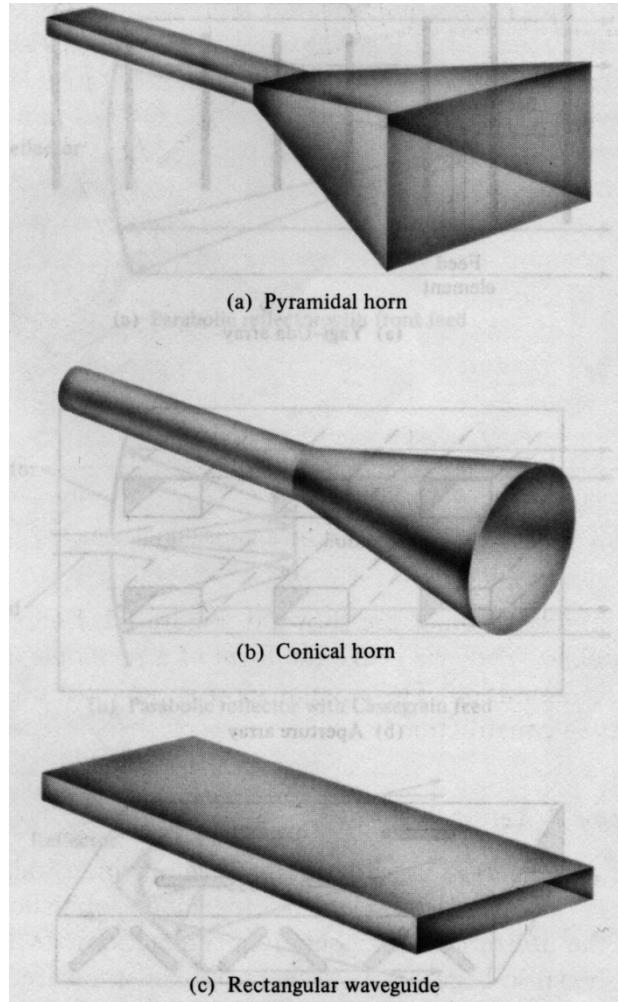
# Transmission line equivalent of antenna



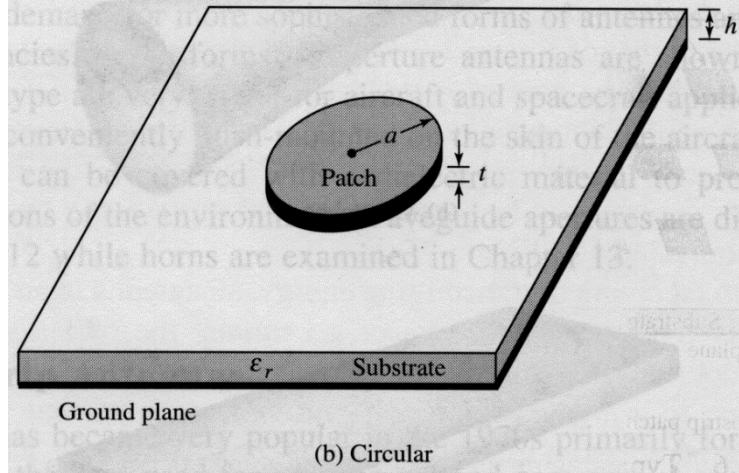
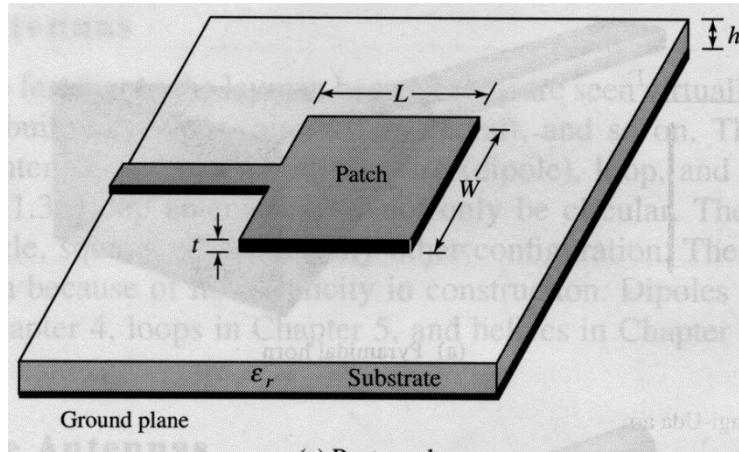
# Wire Antennas



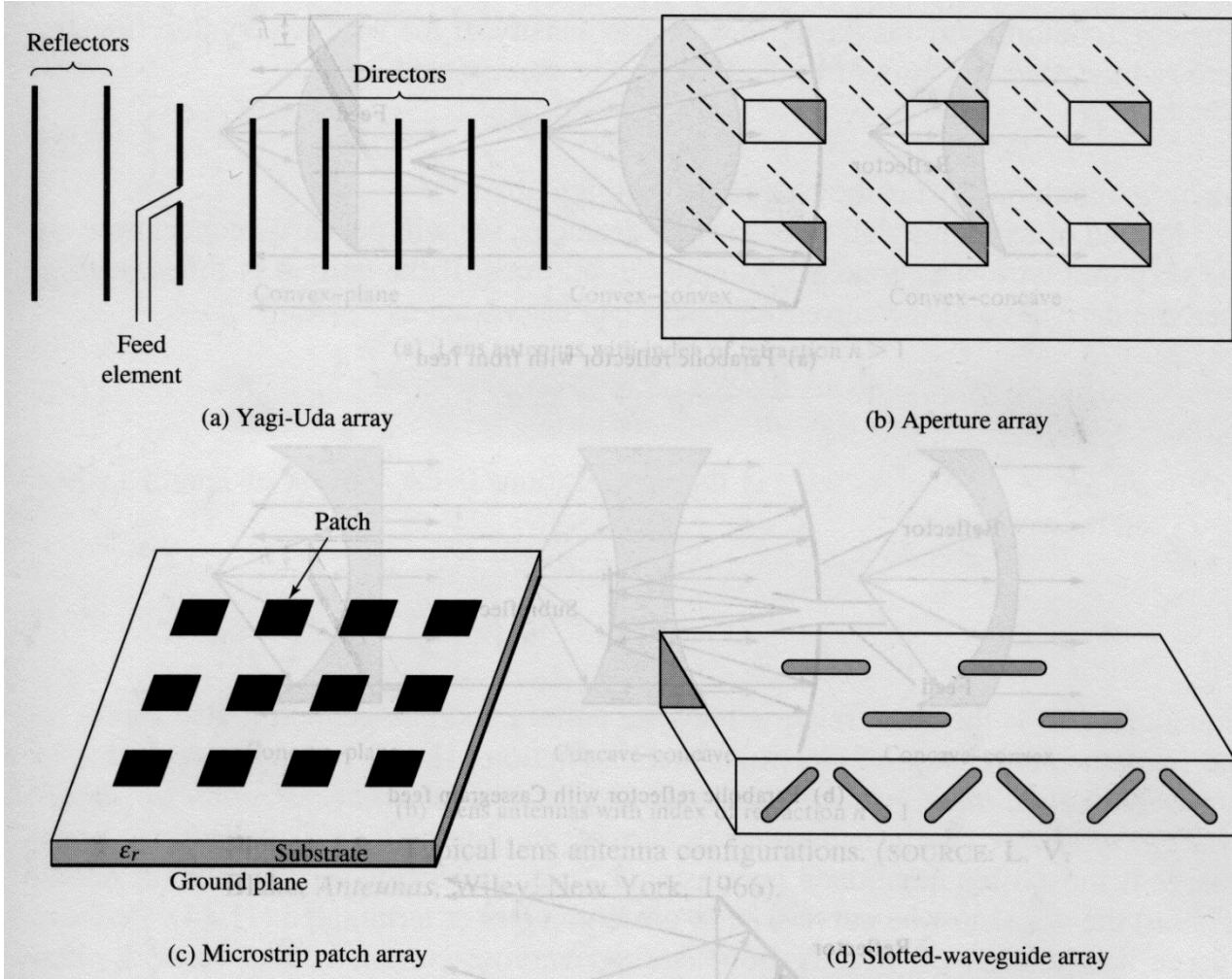
# Aperture Antennas



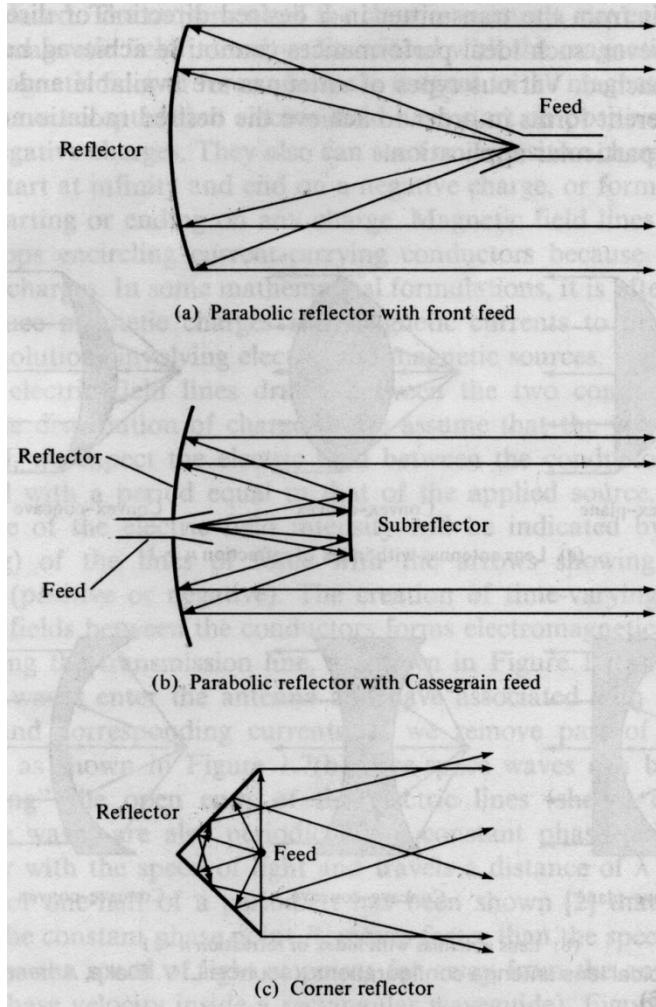
# Patch Antennas



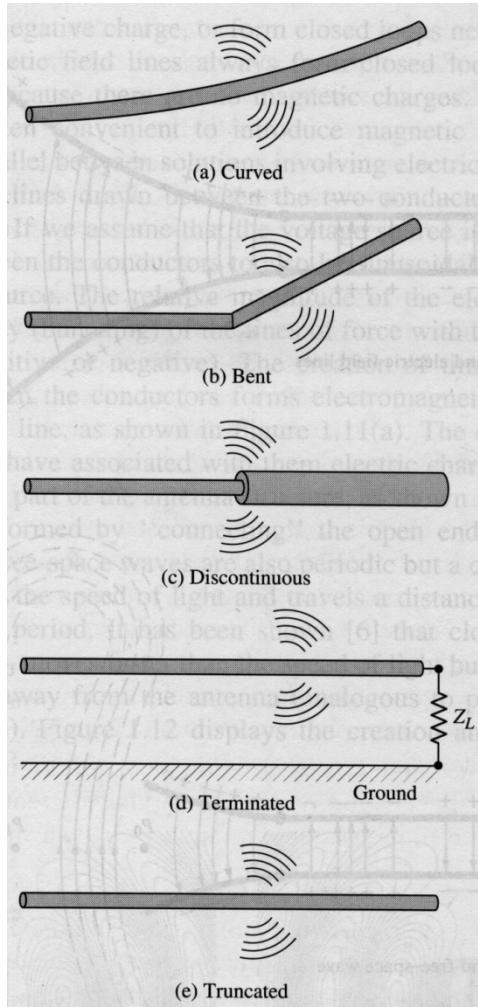
# Array Antennas



# Reflector Antennas

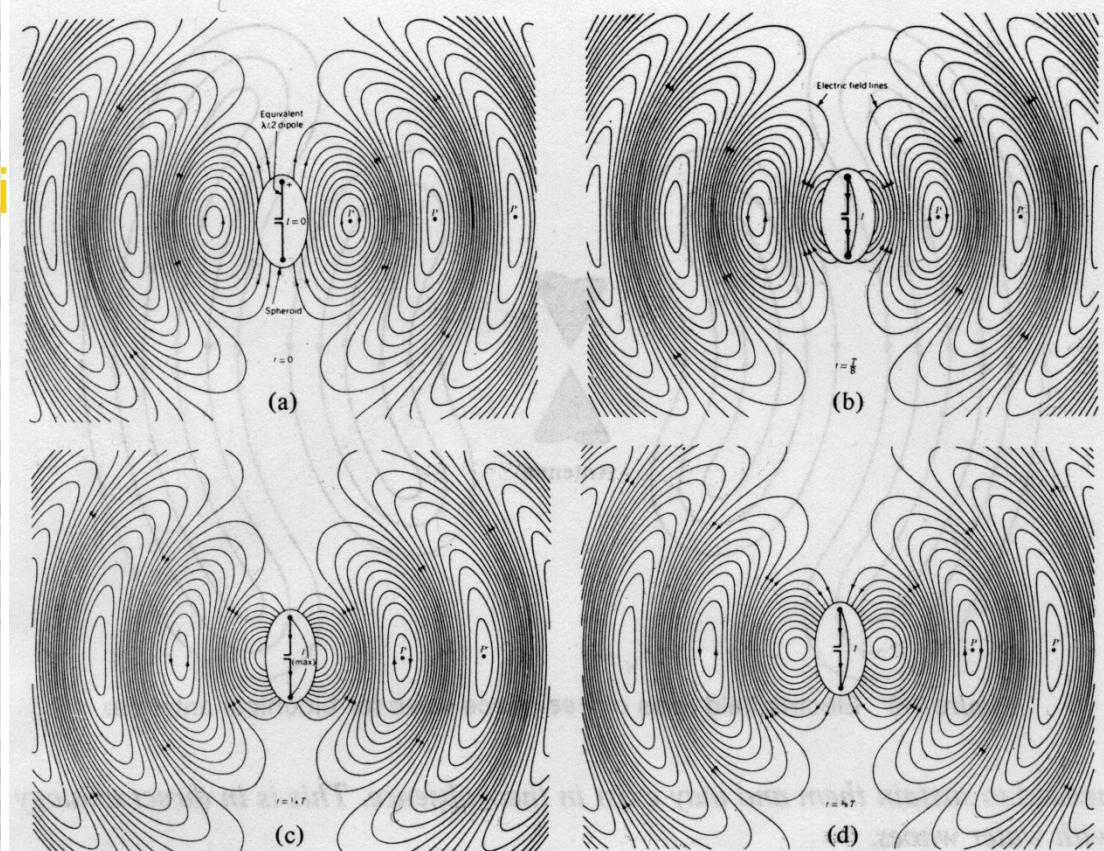
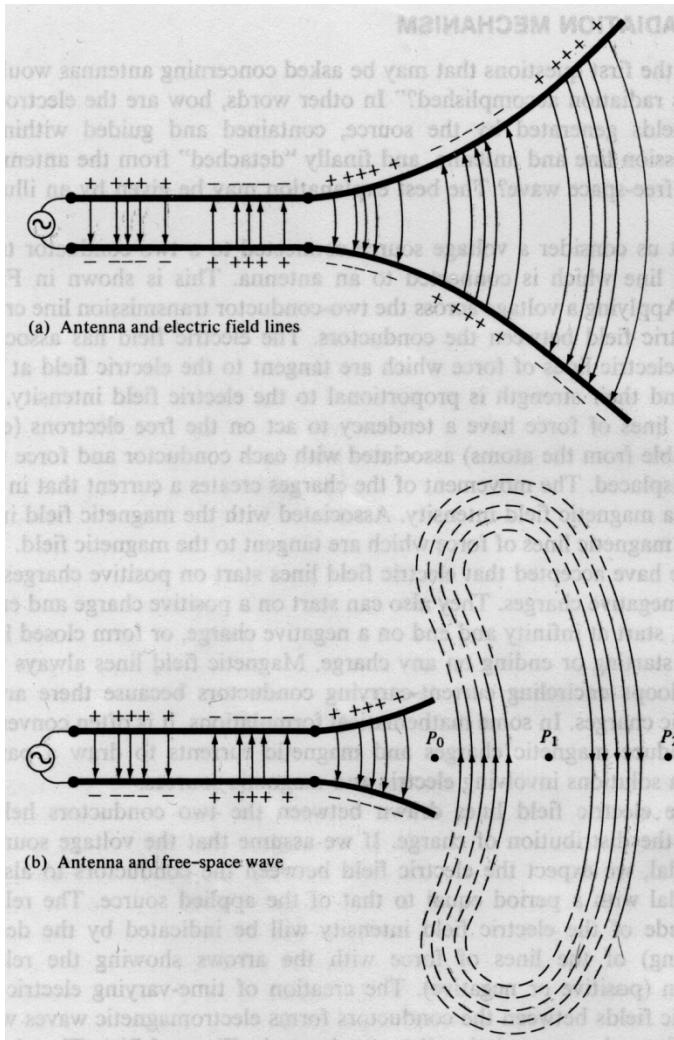


# Radiation from Wires



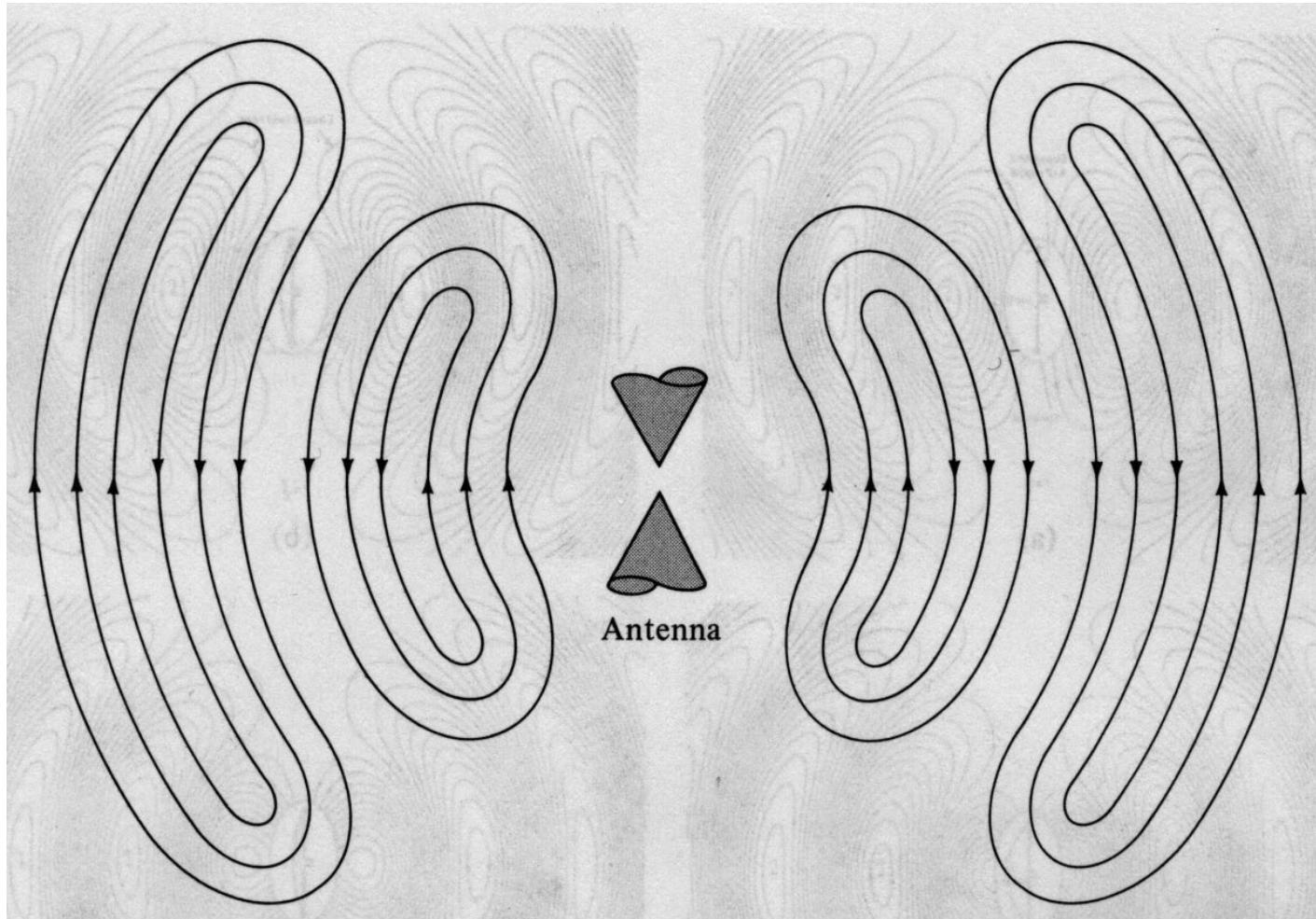
- 1 No charge moving => no current created => No Radiation
- 2 Charge moving @ uniform velocity:
  - A) Long straight wire => no radiation
  - B) Curved, Bent, Discontinuous, Terminated or Truncated => Radiation
- 3 Oscillating charge => Radiation

# Two Wires

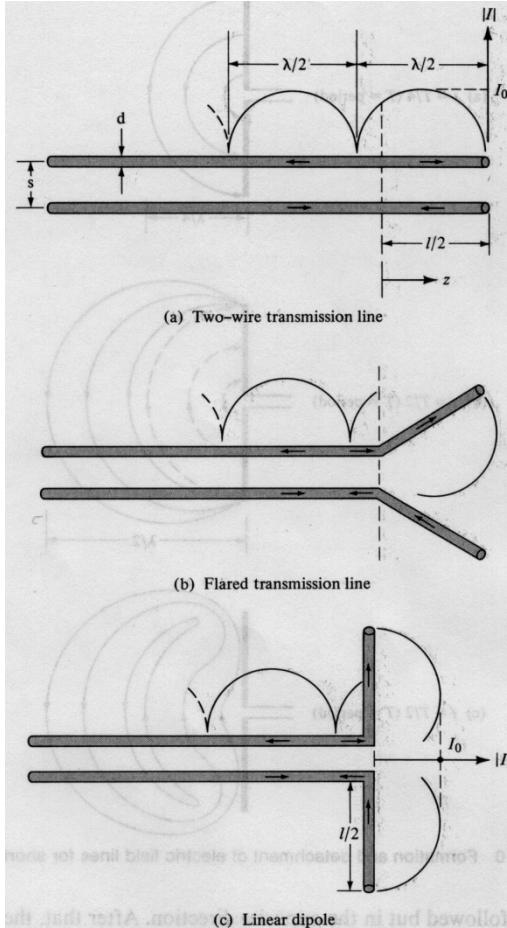


**Figure 1.8** Electric field lines of free-space wave for a  $\lambda/2$  antenna at  $t=0$ ,  $T/8$ ,  $T/4$ , and  $3T/8$ . (SOURCE: J. D. Kraus and K. R. Carver, *Electromagnetics*, 2nd ed., McGraw-Hill, New York, 1973. Reprinted with permission of J. D. Kraus and John D. Cowan, Jr.)

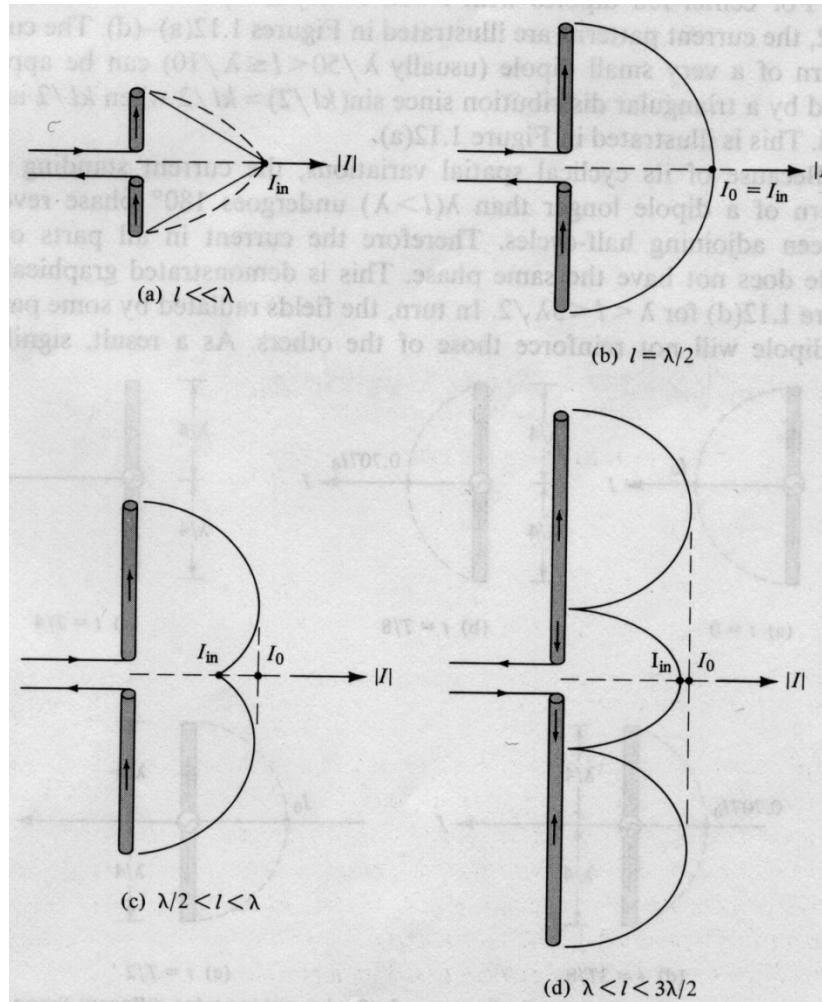
# Dipole



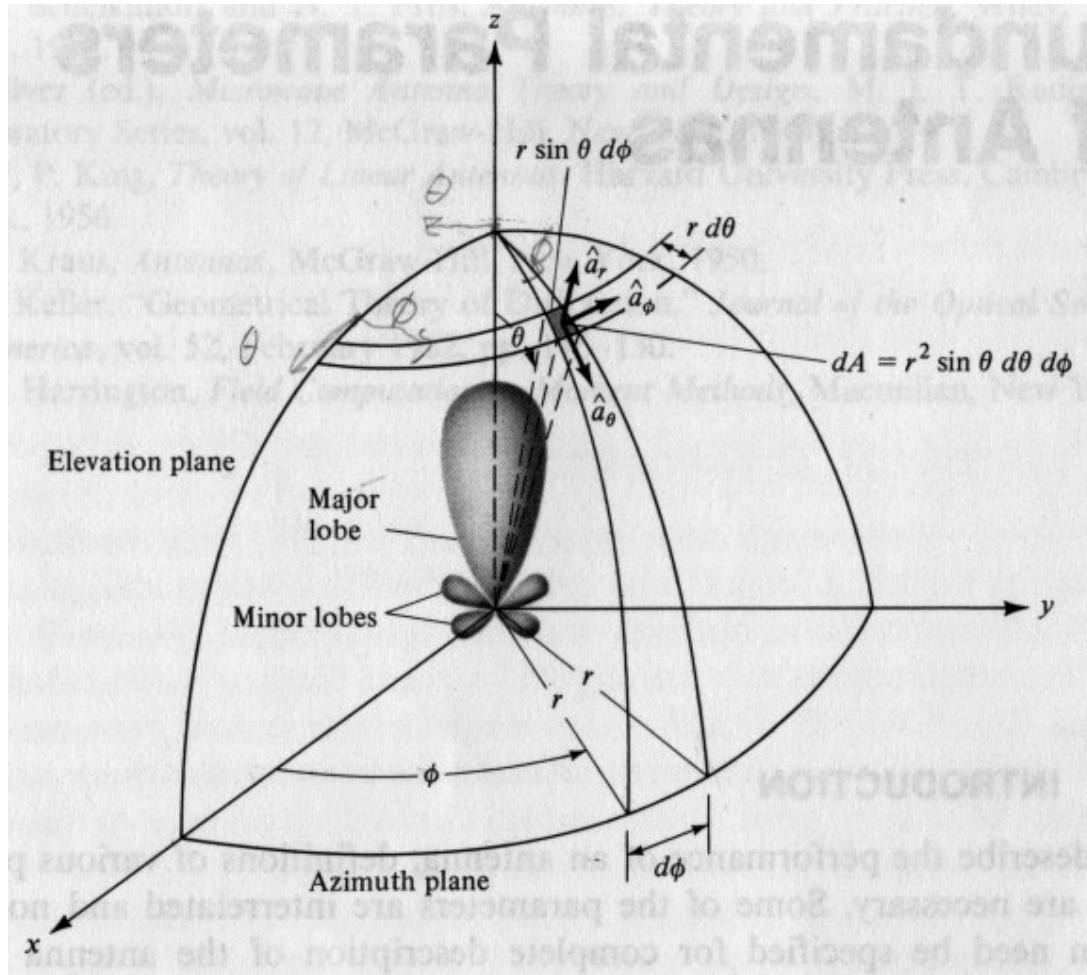
# Current Distribution on two wire transmission line and Dipole



# Current Distribution on Dipoles



# Coordinate system for antenna analysis



# Coordinate system for antenna analysis

$$\int_0^{2\pi} \left[ \int_0^{\pi} r^2 \sin(\theta) d\theta \right] d\phi = 4\pi r^2$$

$$0 \leq \theta \leq \pi$$

$$0 \leq \phi \leq 2\pi$$

# Radiation Pattern

A mathematical and/or graphical representation  
of the radiation properties of an antenna, such as

The:

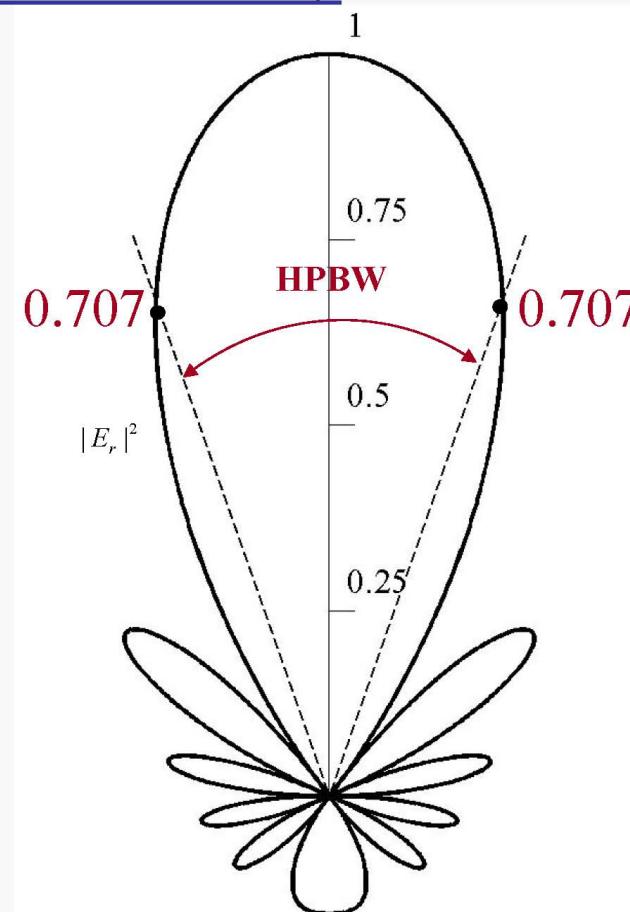
- Amplitude
- Phase
- Polarization

As a function of the ANGULAR space coordinates  
 $\theta$  and  $\phi$

## 2-D Normalized *Field* $|\underline{E}_n|$ Pattern of a Linear Array

Linear Scale  
 $N = 10$  elements  
 $d = \lambda/4$  spacing  
HPBW =  $38.64^\circ$

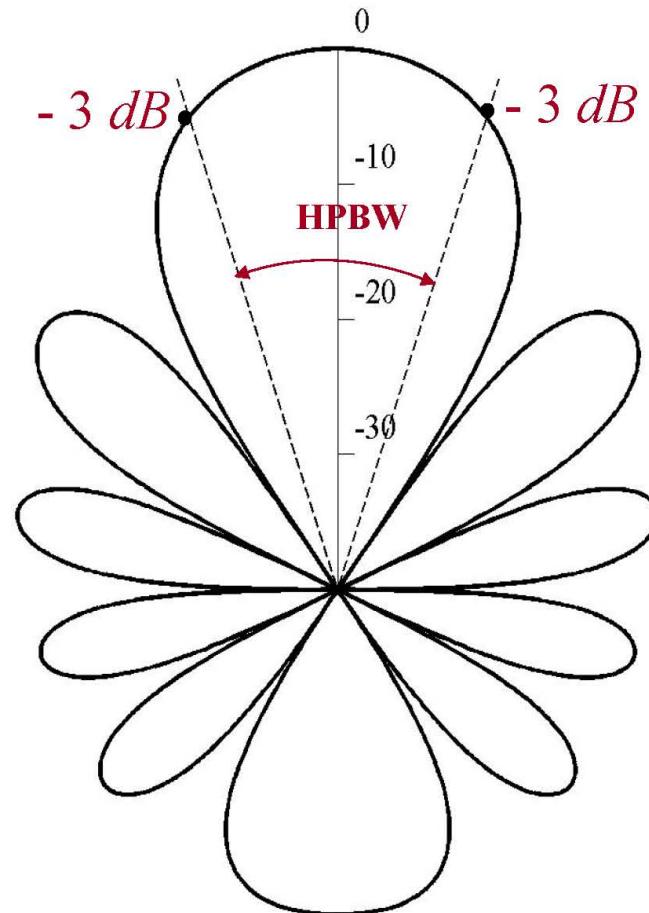
Fig. 2.2(a)



## 2-D Normalized *Power* $|\underline{E}_n|^2$ Pattern of a Linear Array

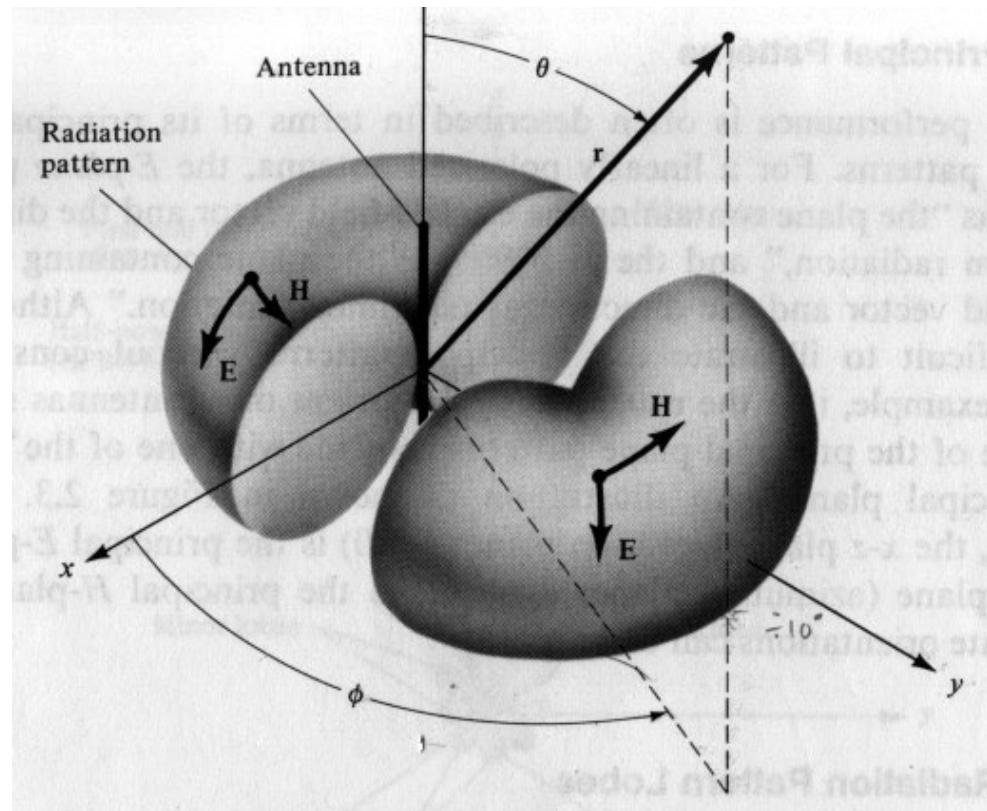
dB Scale  
 $N = 10$  element  
 $d = \lambda/4$  spacing  
 $\text{HPBW} = 38.64^\circ$

Fig. 2.2(c)

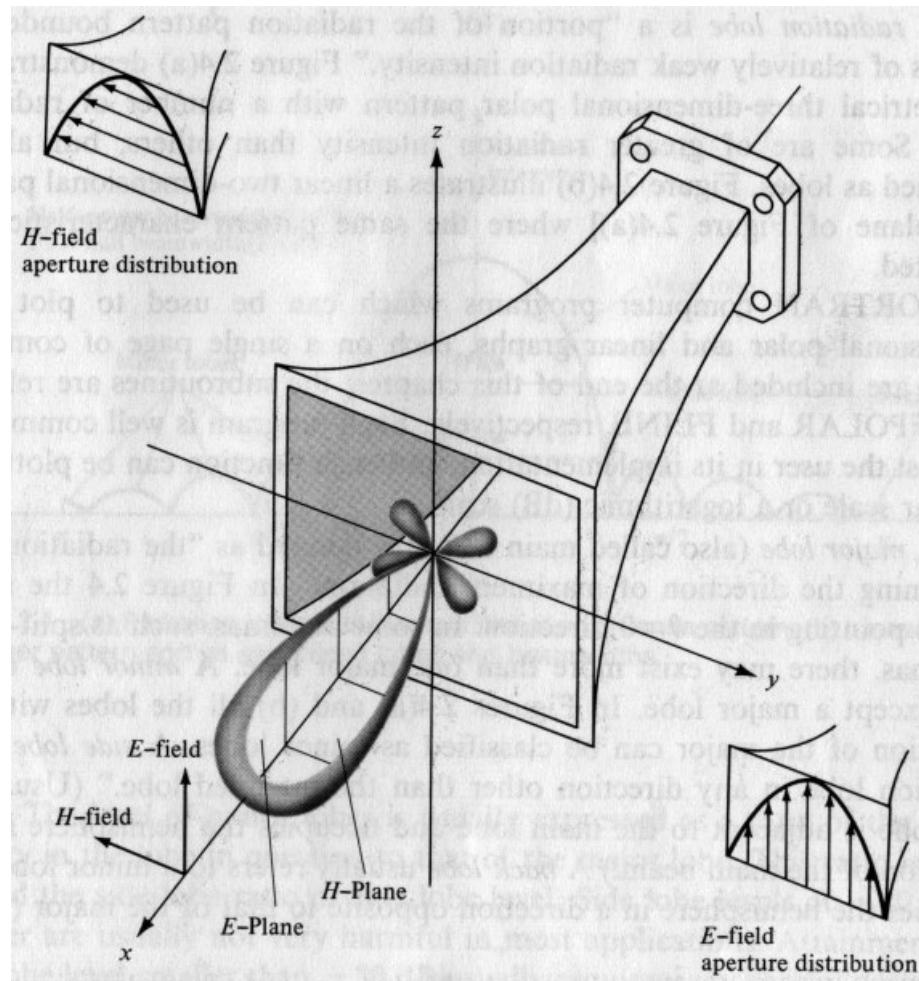


# Directional Radiation pattern

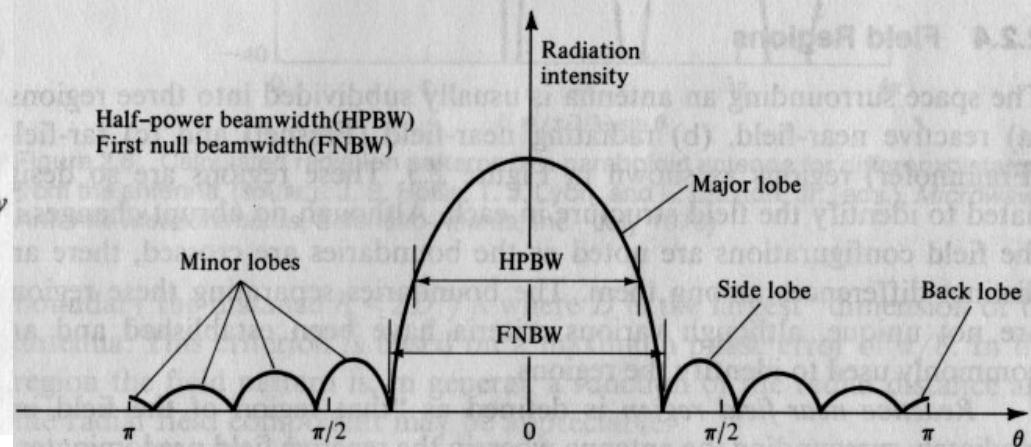
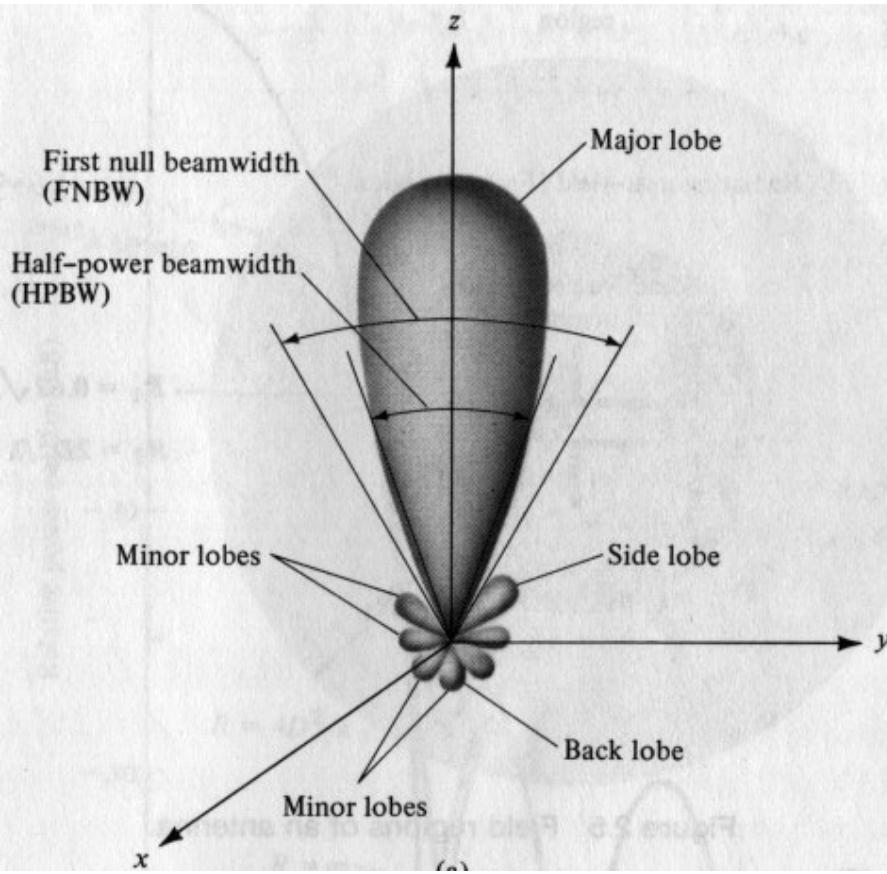
- Isotropic radiation
- Omnidirectional
- Directional



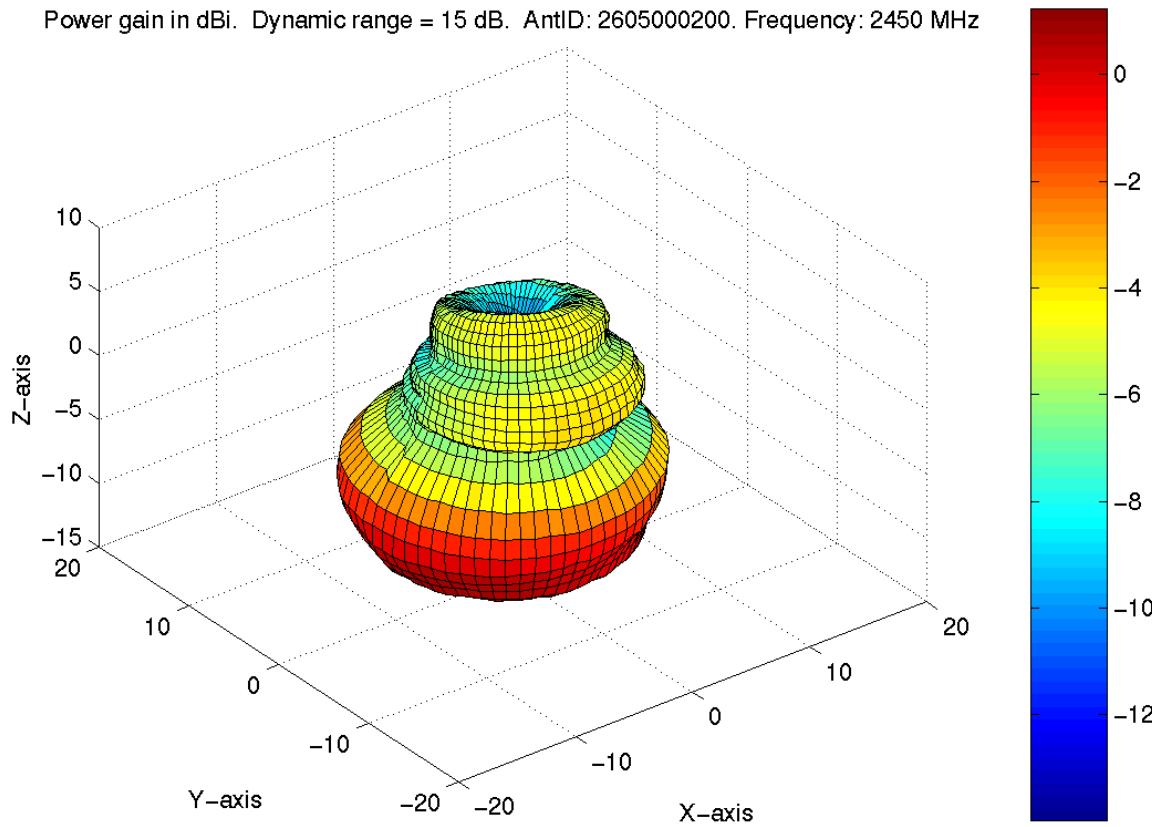
# Principal E- and H-Plane patterns



# Directional Radiation pattern

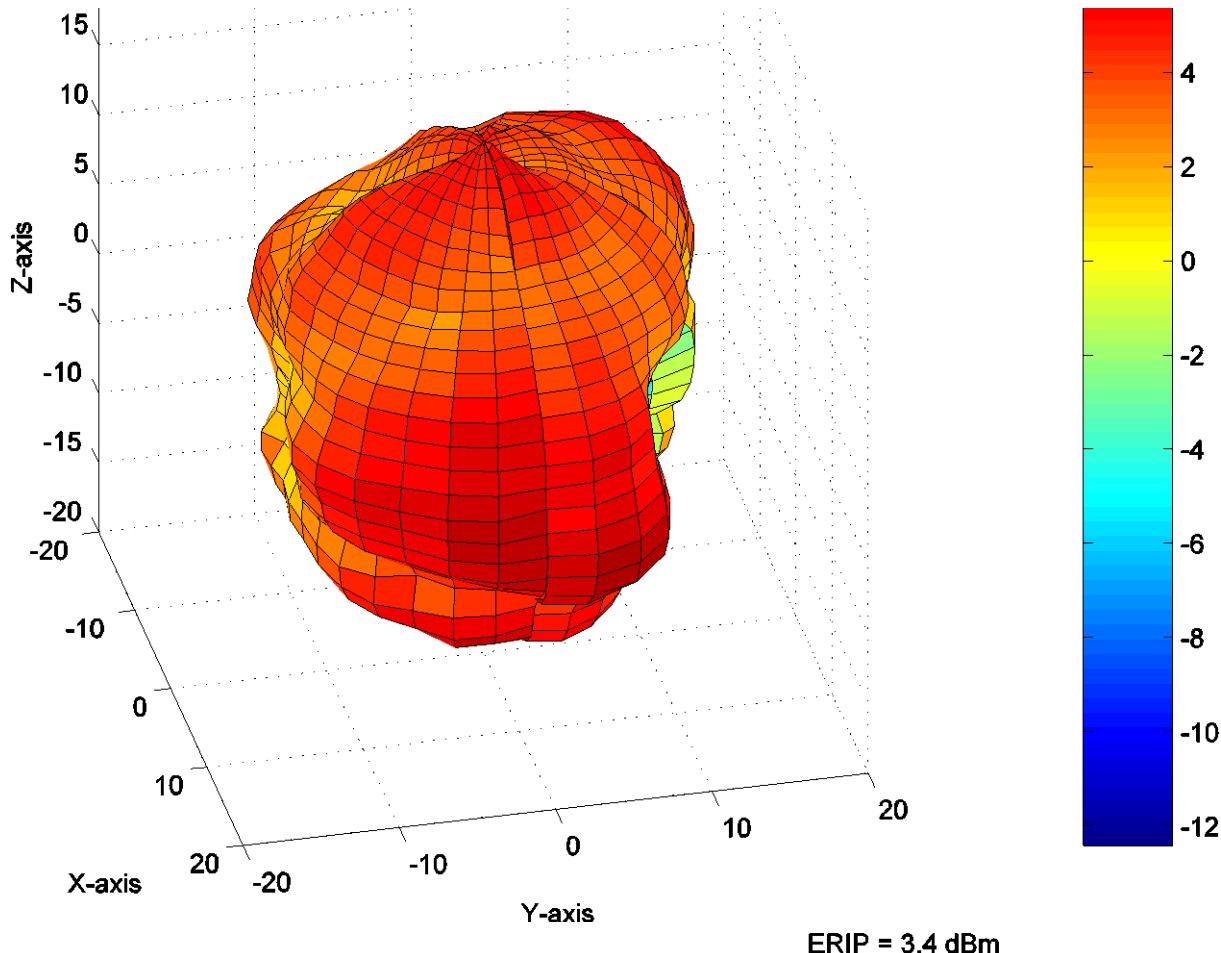


# Directional Radiation pattern?



5/9, 2002, 19:37. File: BtMitsubishiAHD12-2.450.gai. TotPwr = -3.6 dBi

# Directional Radiation pattern?



# Field Regions around an Antenna

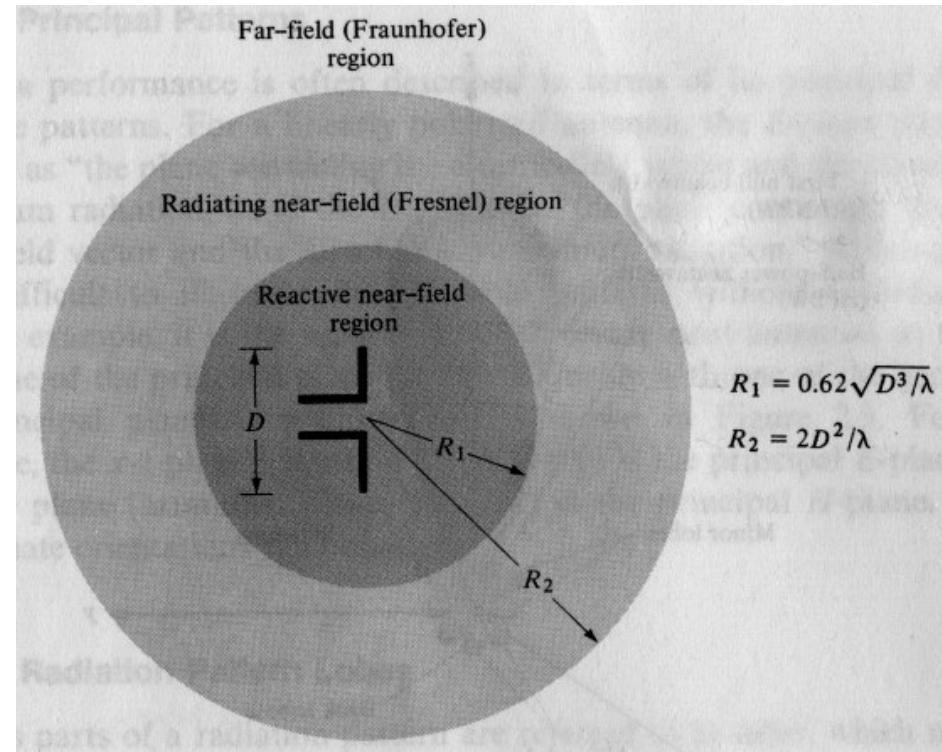
- Reactive Near field

$$R < 0.62 \sqrt{\frac{D^3}{\lambda}}$$

- Radiating Near field

- Farfield

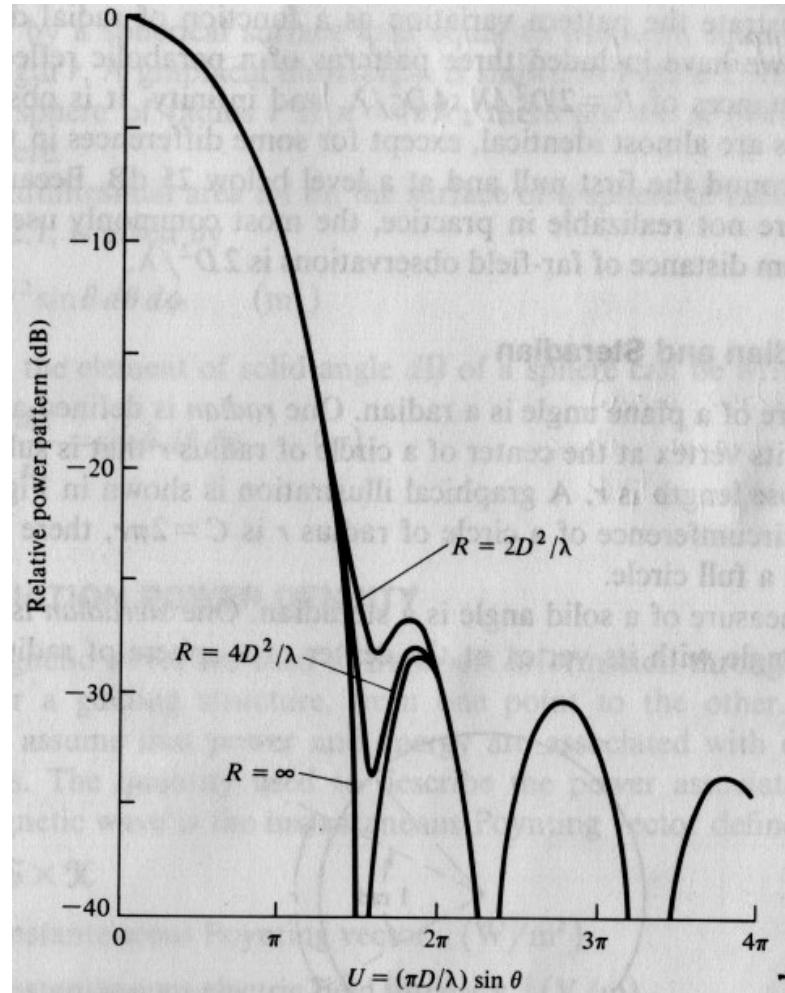
$$R > \frac{2D^2}{\lambda}$$



# Farfield Criterion

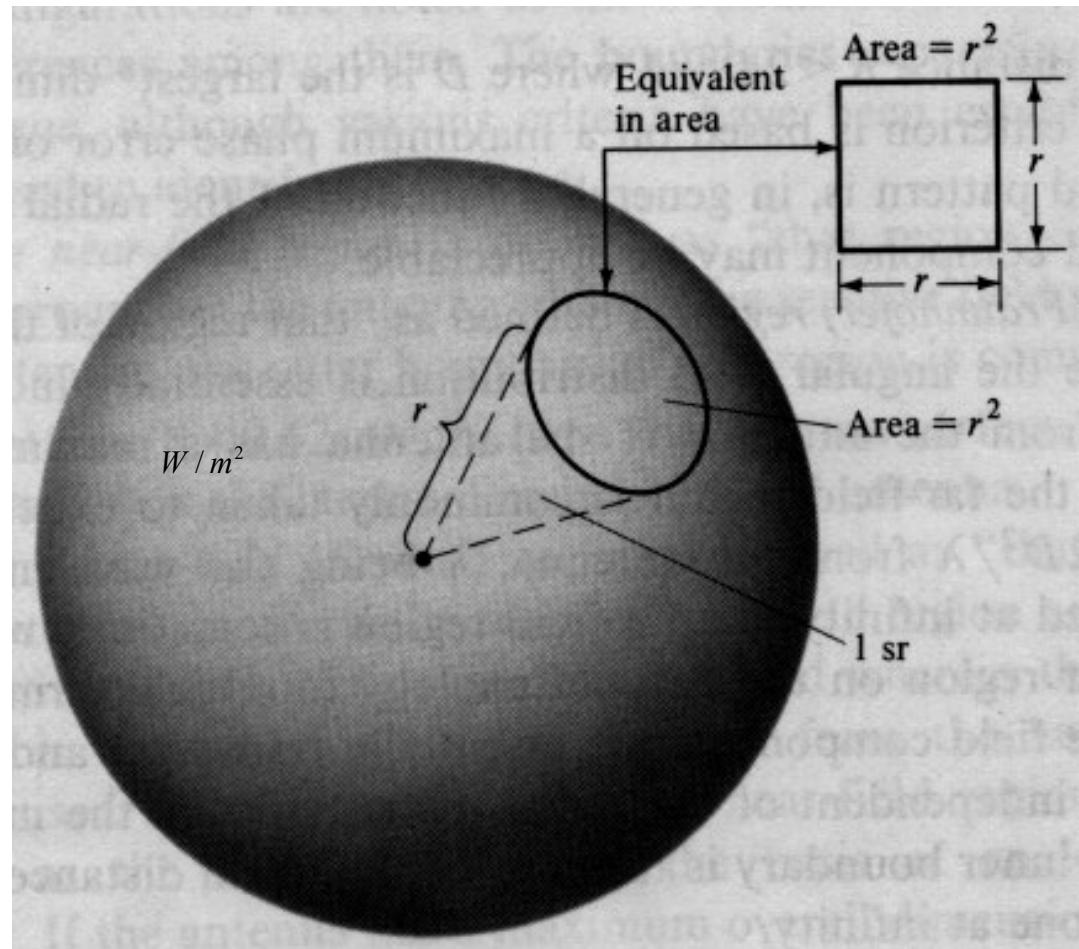
Farfield

$$R > \frac{2D^2}{\lambda}$$



# Radiation Power Density [W/m<sup>2</sup>]

$$P_{RAD} = P_{AV} = \iint_S \mathbf{W}_{RAD} d\mathbf{S} = \frac{1}{2} \iint_S \text{Re}(\mathbf{E} \times \mathbf{H}^*) d\mathbf{S}$$



# Radiation Intensity

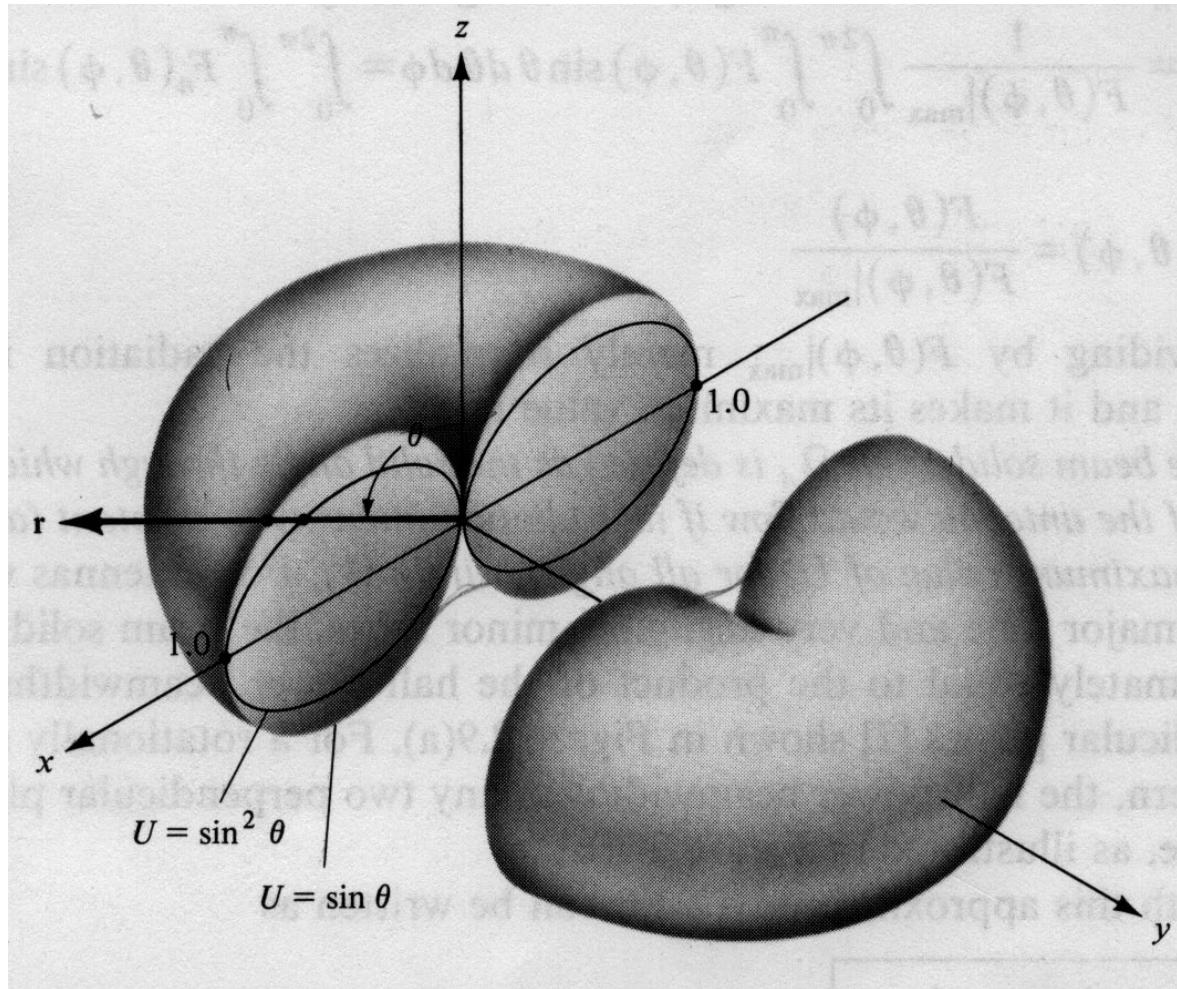
$$U = r^2 W_{RAD}$$

$U$  = Radiation intensity (W/unit Solid Angle)

$W_{RAD}$  = Radiation density  $(W / m^2)$

$$U(\theta, \varphi) = \frac{r^2}{2\eta} |\mathbf{E}(r, \theta, \varphi)|^2 \approx \frac{1}{2\eta} [ |E_\theta(\theta, \varphi)|^2 + |E_\varphi(\theta, \varphi)|^2 ]$$

# Radiation Intensity Patterns



# Directivity

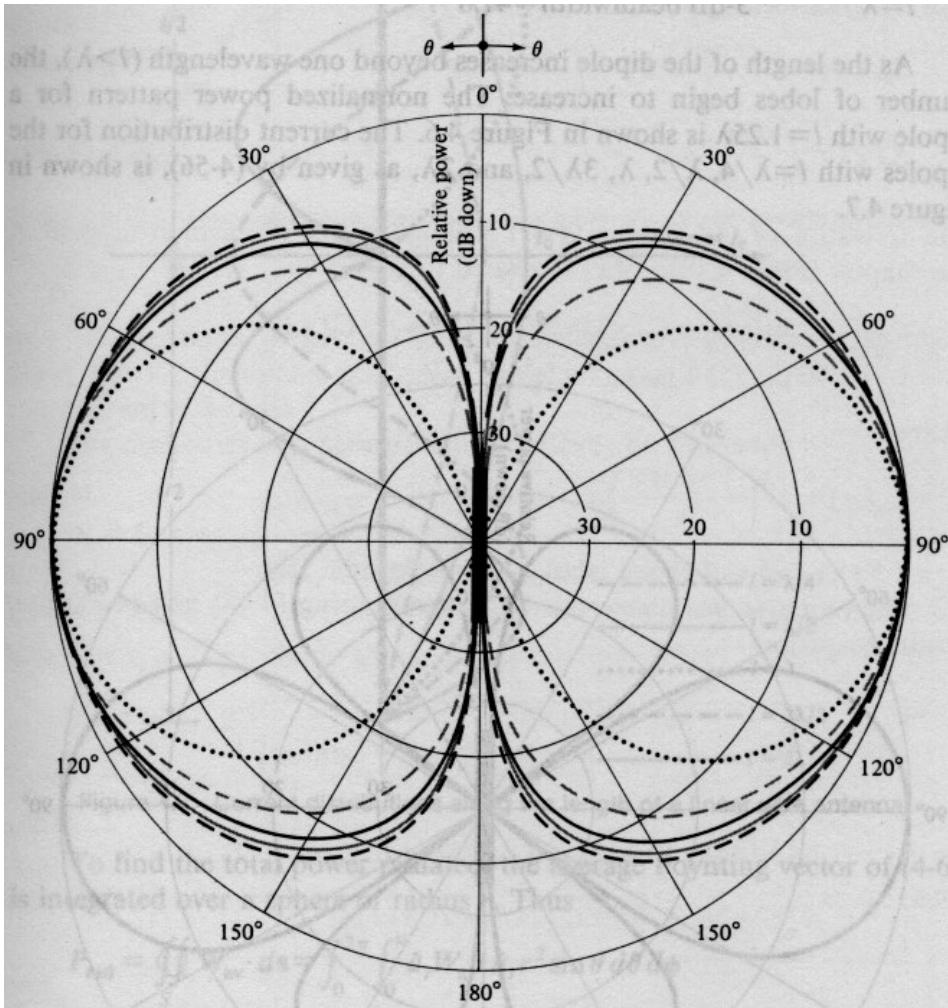
Directive  
gain

$$D_g(\theta, \varphi) = \frac{U(\theta, \varphi)}{U_0} = \frac{U(\theta, \varphi)}{P_{RAD}/4\pi}$$

Directivity

$$D_0 = \frac{U_{\max}}{U_0} = \frac{U_{\max}}{P_{RAD}/4\pi}$$

# 2D Directivity Patterns



$$E_r \cong H_r = H_\theta = E_\phi = 0$$

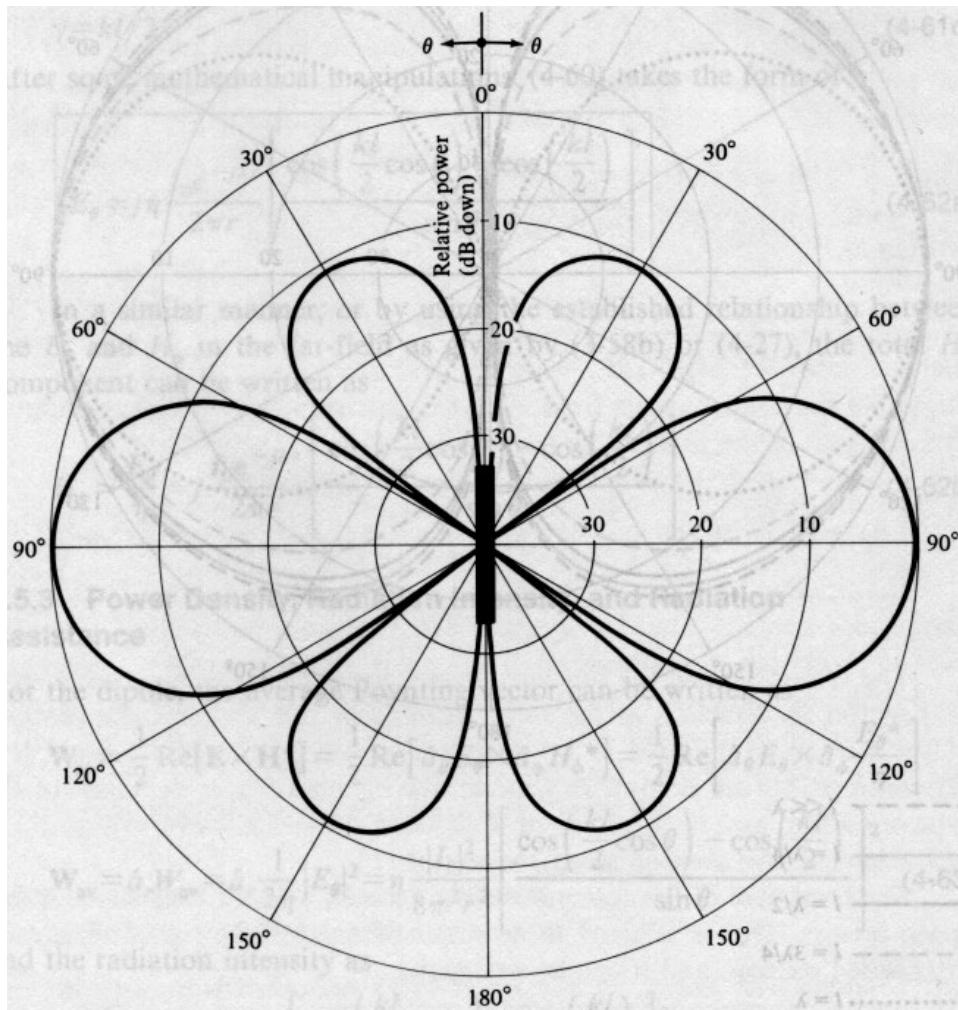
$$H_\phi \cong j \frac{k I_0 l \sin(\theta)}{4\pi r} e^{-jkr}$$

$$E_\theta \cong j \eta \frac{k I_0 l \sin(\theta)}{4\pi r} e^{-jkr}$$

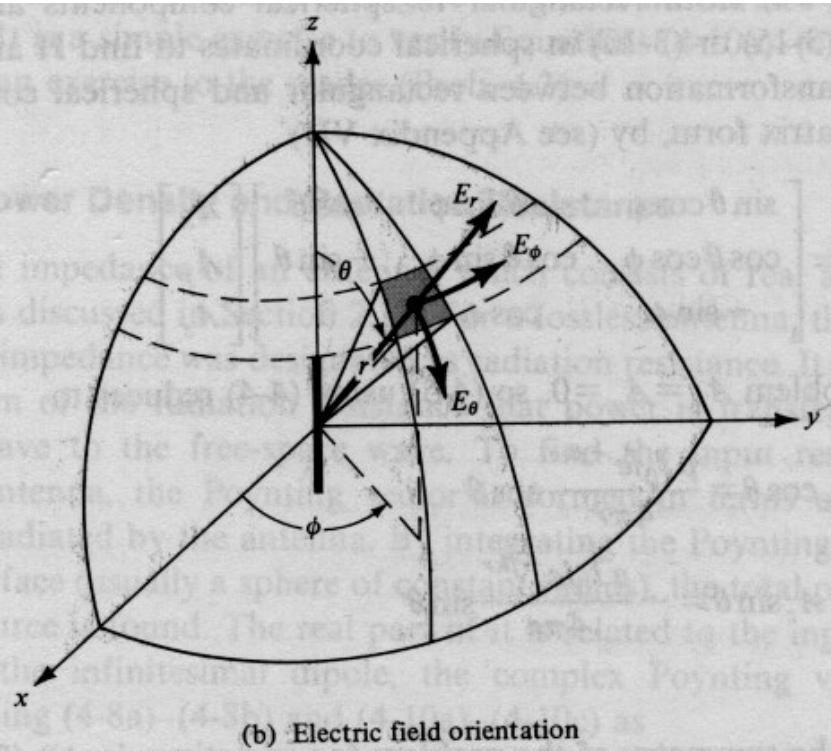
$$\Rightarrow Z = \frac{E_\theta}{H_\phi} \cong \eta$$

- $l \ll \lambda$
- $l = \lambda/4$
- $l = \lambda/2$
- $l = 3\lambda/4$
- ·  $l = \lambda$

# Farfield for a Dipole larger than one wavelength



# Field Radiated from a small Dipole Antenna



$$H_r = H_\theta = 0$$

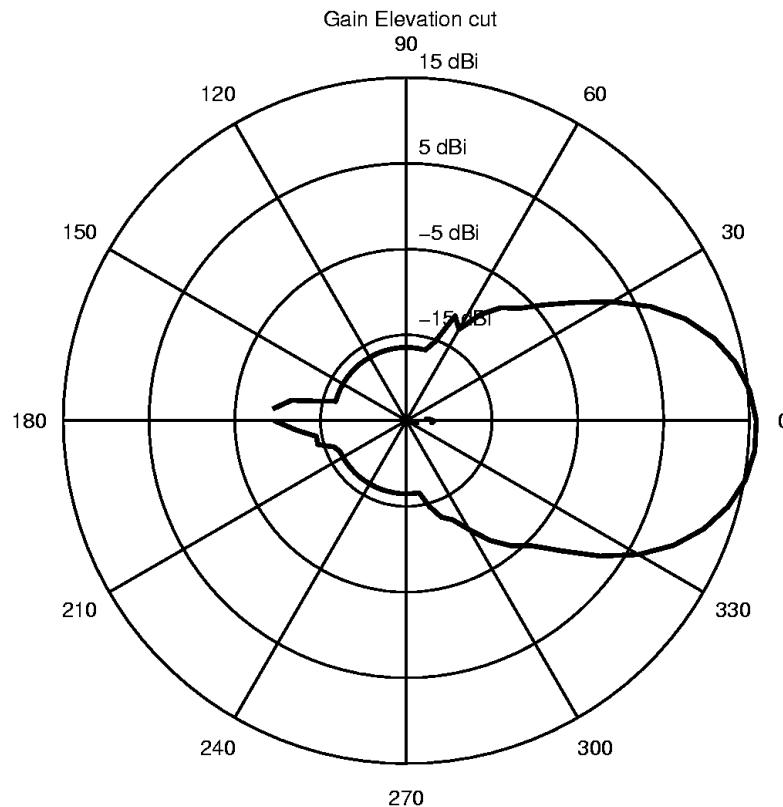
$$H_\phi = j \frac{kI_0 l \sin(\theta)}{4\pi r} \left[ 1 + \frac{1}{jkr} \right] e^{-jkr}$$

$$E_r = \eta \frac{I_0 l \cos(\theta)}{2\pi r^2} \left[ 1 + \frac{1}{jkr} \right] e^{-jkr}$$

$$E_\theta = j\eta \frac{kI_0 l \sin(\theta)}{4\pi r} \left[ 1 + \frac{1}{jkr} - \frac{1}{(kr)^2} \right] e^{-jkr}$$

$$E_\phi = 0$$

# Antenna Gain



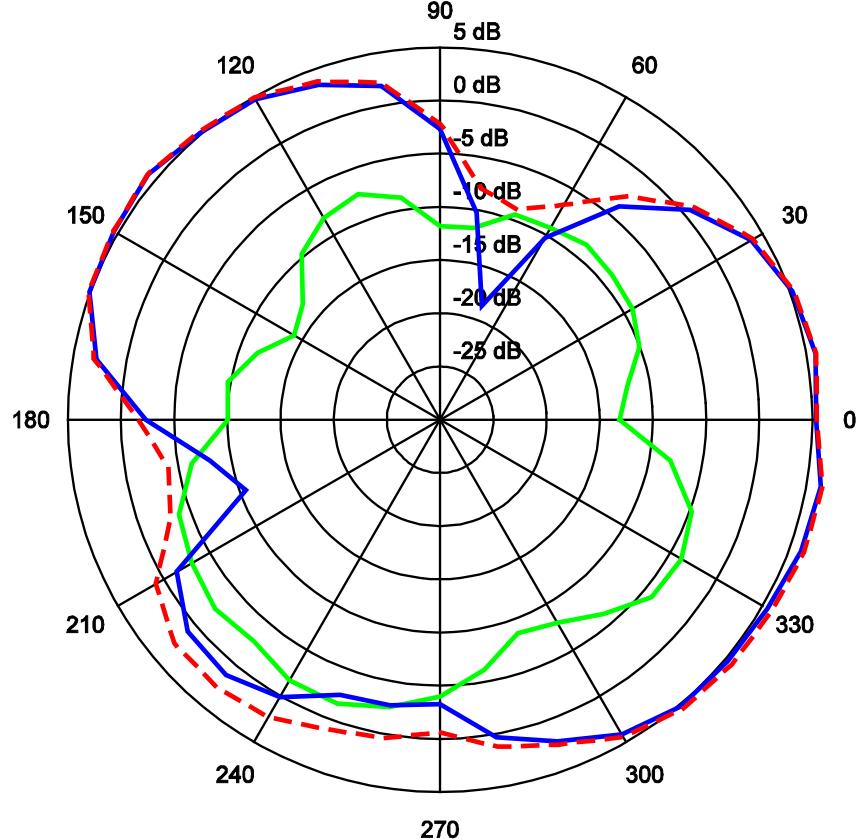
$$G_g(\theta, \varphi) = \frac{U(\theta, \varphi)}{P_{IN} / 4\pi}$$

$$G_g(\theta, \varphi) = e_t D_g(\theta, \varphi)$$

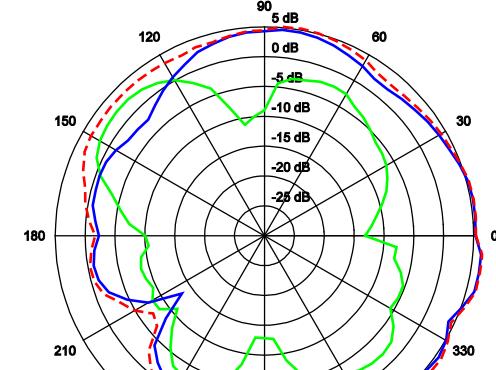
$$G_0 = e_t D_0$$

# Directional Radiation pattern?

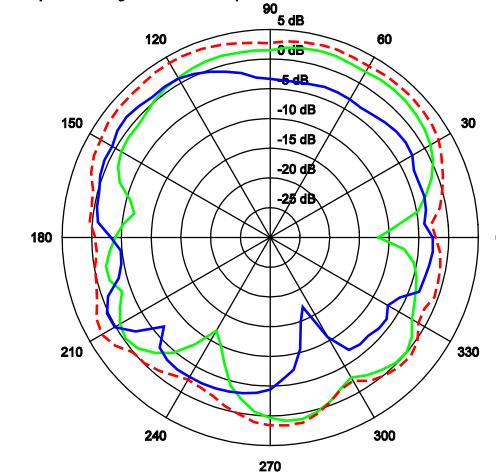
Radiation pattern for PgnHeadset620Freespace26October2005-2.441000 2610050725 in XY plane



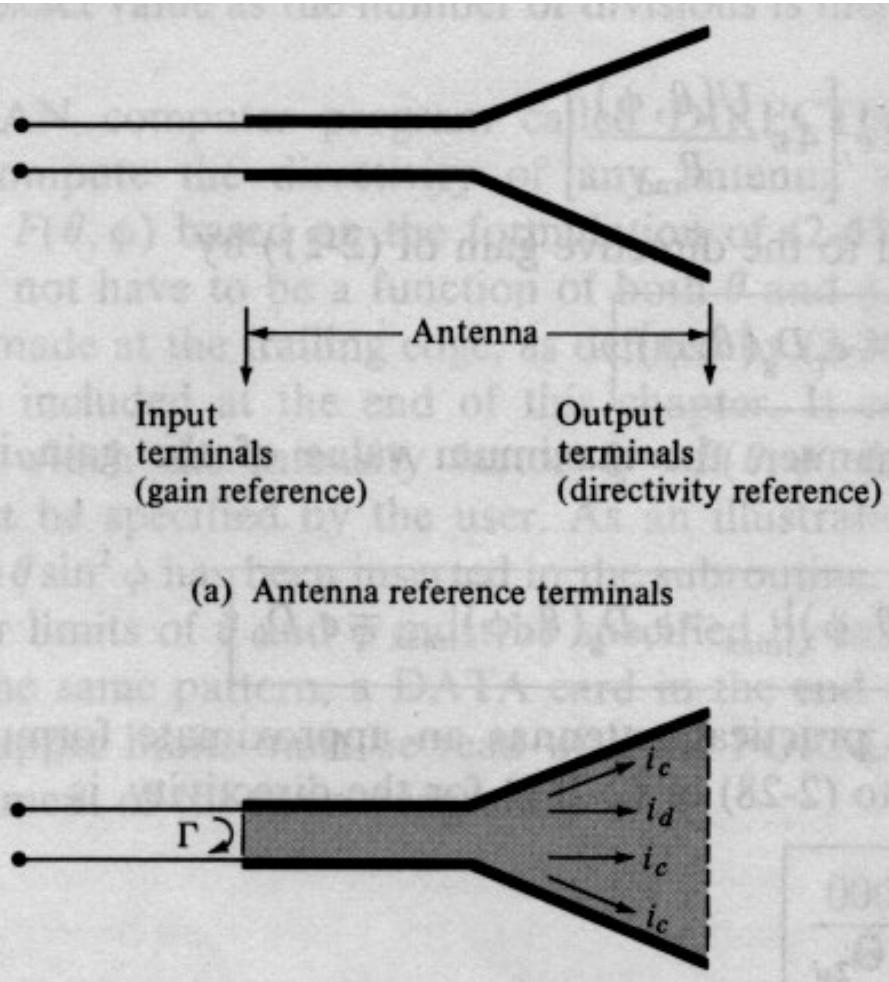
Radiation pattern for PgnHeadset620Freespace26October2005-2.441000 2610050725 in XZ plane



Radiation pattern for PgnHeadset620Freespace26October2005-2.441000 2610050725 in YZ plane



# Antenna Efficiency



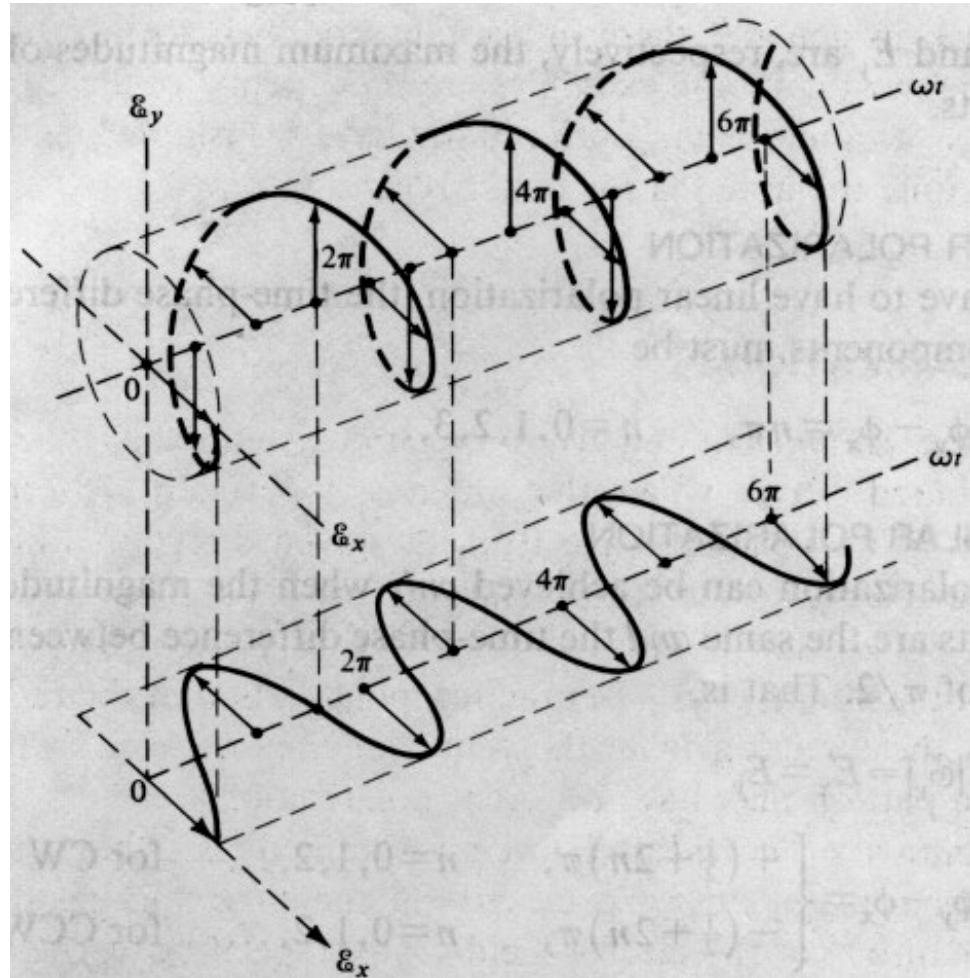
$$e_t = e_r e_c e_d$$

- Total efficiency
- Reflection efficiency  $(1 - |\Gamma|^2)$
- Conduction efficiency
- Dielectric efficiency

# Polarization

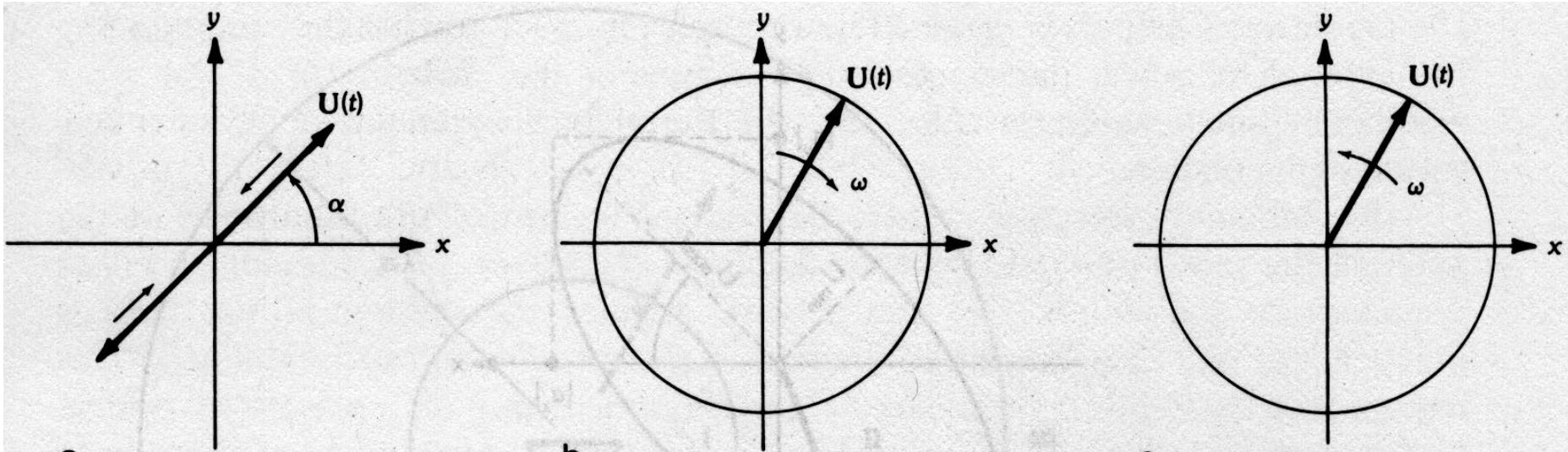
- Linear
- Circular
  - Clock Wise (CW) or Right Hand (RH)
  - Counter Clockwise (CCW) or LH
- Elliptical (Axial Ratio)
  - CW) or RH
  - CCW or LH

# Polarization



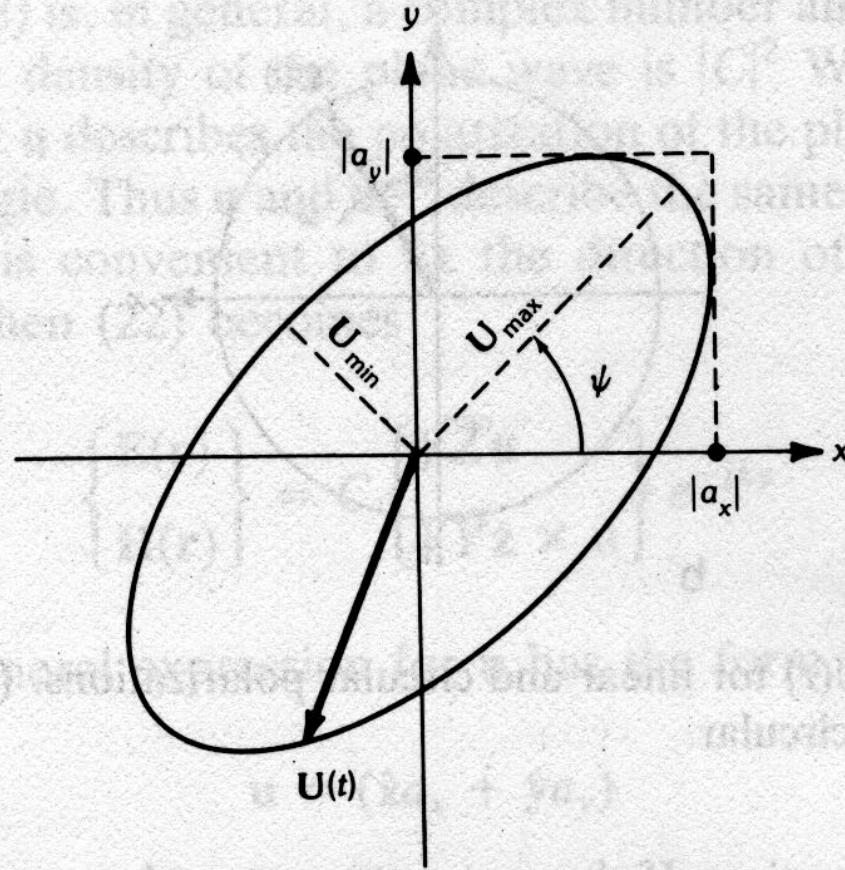
Rotation of plane EM  
Wave propagation in the  
Positive Z direction

# Polarization



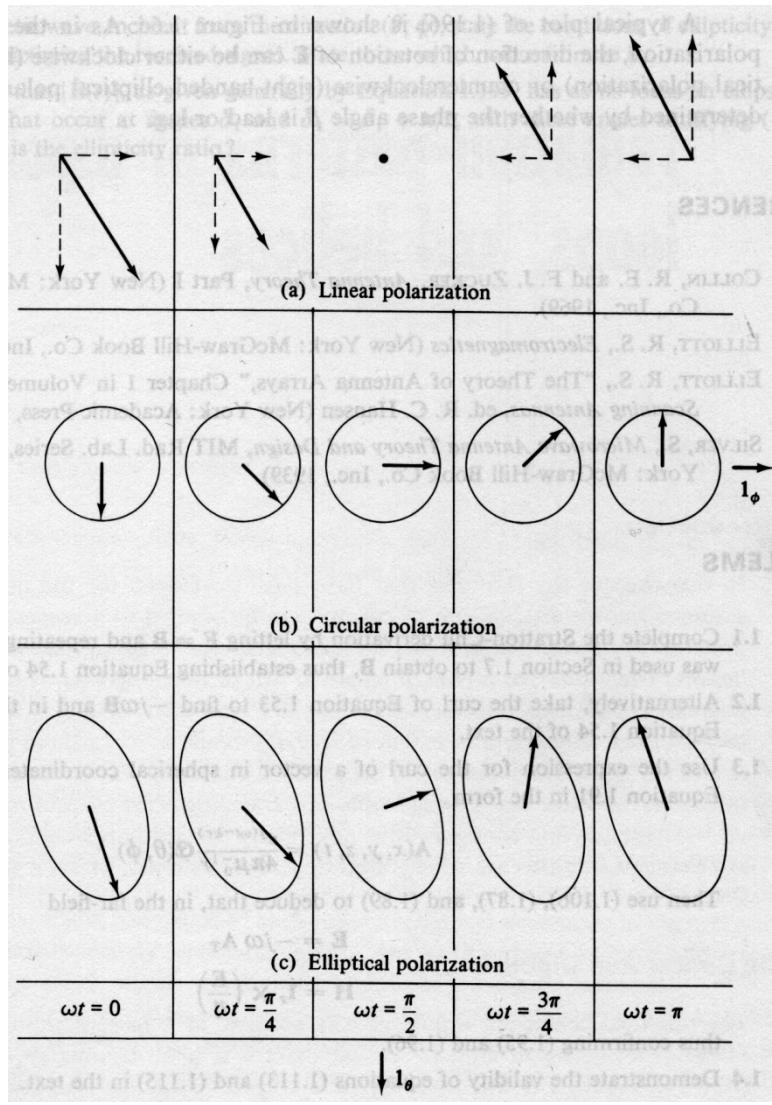
**Fig. 7.** Rotating vector  $\mathbf{U}(t)$  for linear and circular polarizations. (a) Linear. (b) Left-hand circular. (c) Right-hand circular.

# Polarization

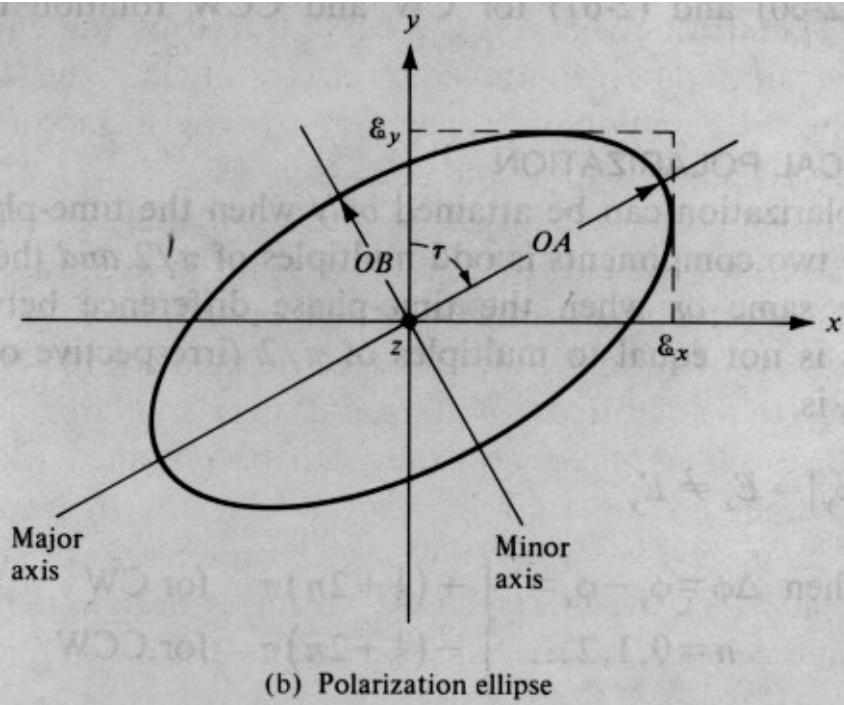


**Fig. 8.** Elliptical polarization: the tip of the rotating vector  $\mathbf{U}(t)$  traces out an ellipse.

# Polarization



# Polarization



A Linear

$$\Delta\varphi = \varphi_Y - \varphi_X = n\pi$$

B Circular

$$E_X = E_Y \wedge$$

$$\Delta\varphi = \varphi_Y - \varphi_X = \begin{cases} (\frac{1}{2} + 2n)\pi \\ -(\frac{1}{2} + 2n)\pi \end{cases}$$

C Elliptical

# Problems

## Problem 1.1.

A hypothetical isotropic antenna is radiating in freespace. At a distance of 100 meters from the antenna the total electrical field ( $E_\Theta$ ) is measured to be 5 V/m. Find the

- a) Power density ( $W_{rad}$ )
- b) Power radiated ( $P_{rad}$ )

# Problems

## Problem 1.2

The maximum radiation intensity of a 90% efficient antenna is 200 mW/unit solid angle.

Find the directivity and gain (dimensionless and in dB) when the:

- a) Input power is 125.66 mW
- b) Radiated power is 125.66 mW

# Problems

## Problem 1.3

In target-search ground-mapping radars it is desirable to have echo power received from target, of constant cross section, to be independent of its range. For one such application, the desireble radiation intensity of the antenna is given by

$$U(\Theta, \Phi) = 1 \text{ for } 0^\circ \leq \Theta < 20^\circ$$

$$U(\Theta, \Phi) = 0,342 \csc(\Theta) \text{ for } 20^\circ \leq \Theta < 60^\circ$$

$$U(\Theta, \Phi) = 0 \text{ for } 60^\circ \leq \Theta \leq 180^\circ$$

Find the directivity in dB using the exact formula.

# Problems

## Problem 1.4

The radiation intensity of an antenna is given by

$$U(\Theta, \Phi) = \cos^4(\Theta) \sin^2(\Phi),$$

for  $0 \leq \Theta \leq \pi/2$  and  $0 \leq \Phi \leq 2\pi$  (i.e. In the upper half-space)

It is 0 in the lower half-space.

Find the:

- Exact directivity (dimensionless and in dB).
- Elevation plane half-power beamwidth in degrees.