

Controller design using root locus

Exercise 1

A simple unity feedback system has a time delay of 0.3 sec-

$$G(s) = \frac{K e^{-0.3s}}{s + 1}$$

Approximate the time delay function using a Pade approximation

Draw the root locus

Find the limit for K giving stability

Exercise 2

In a unity feedback system

$$G(s) = \frac{K(s^2 + 2s + 4)}{s(s+4)(s+6)(s^2 + 1.4s + 1)}$$

Plot the root locus for the system.

Find the K values that gives stability.

Exercise 3

A system G(s) has the transfer function $G(s) = \frac{10}{s(s+1)}$

Design a lead compensator using root locus so the closed loop system has a damping ratio $\xi=0.5$ and $\omega_n = 3$.

corresponding to

$$s^2 + 2\xi\omega_n s + \omega_n^2 = s^2 + 3s + 9$$

Test your result by a step response