

# Formelsamling Ellära FY502G

Konstanter:  $e = 1.602 \cdot 10^{-19} \text{ [C]}$   $\epsilon_0 = 8.8541878176 \cdot 10^{-12} \text{ [F/m]}$   $\mu_0 = 4\pi \cdot 10^{-7} \text{ [N/A}^2\text{]}$

Ohms, Joules och Kirchhoffs lagar etc:  $R = \frac{U}{I}$   $P = UI$   $\sum_{k=1}^N I_k = 0$   $\sum_{k=1}^M U_k = 0$   $G = \frac{1}{R}$

Ledning:  $R_l = \rho \frac{L}{A}$

Kapacitans:  $C = \frac{Q}{U} \text{ [F]}$   $U_C(t) = \frac{1}{C} \int_0^t I(\tau) d\tau$   $W_C = \frac{CU_C^2}{2}$  för plattkondensator:  $C = \epsilon_0 \epsilon_r \frac{A}{d} \text{ [F]}$

Induktans:  $L = N \frac{\Phi}{I} \text{ [H]}$   $U_L(t) = L \frac{dI(t)}{dt}$   $W_L = \frac{LI_L^2}{2}$  för solenoid:  $L = \mu_0 \mu_r \frac{N^2 A}{l} \text{ [H]}$

Växelspänning:  $u_{RMS} = u_{eff} = \frac{\hat{u}}{\sqrt{2}}$   $i_{RMS} = i_{eff} = \frac{\hat{i}}{\sqrt{2}}$   $f = \frac{1}{T} \text{ [Hz]}$   $\omega = 2\pi f \text{ [rad/s]}$

Effekt:  $S = u_{eff} i_{eff} \text{ [VA]}$   $P = S \cos(\phi) \text{ [W]}$   $Q = S \sin(\phi) \text{ [VAr]}$

Komplex effekt, om **effektivvärden** (rms) används:

$$\tilde{S} = \tilde{U} \tilde{I}^* \text{ [VA]}$$

om **toppvärden** används:

$$\tilde{S} = \frac{1}{2} \tilde{U} \tilde{I}^* \text{ [VA]}$$

Komplexa impedanser:  $\tilde{Z} = R + jX$   $\tilde{Z}_R = R$

$$\tilde{Z}_C = -jX_C = -j \frac{1}{\omega C} = -j \frac{1}{2\pi f C}$$

$$\tilde{Z}_L = jX_L = j\omega L = j2\pi f L$$

Trefas:  $U_h = \sqrt{3} U_f$  Faradays induktionslag:  $E = N \frac{d\Phi}{dt}$

Coulombs kraftlag:  $F = \frac{1}{4\pi\epsilon} \frac{Q_1 Q_2}{r^2} \text{ [N]}$  Faradays kraftlag:  $\frac{F}{L} = \frac{\mu I_1 I_2}{2\pi r} \text{ [N]}$   $\epsilon = \epsilon_0 \epsilon_r$   $\mu = \mu_0 \mu_r$

Ideal transformator:  $\frac{U_2}{U_1} = \frac{N_2}{N_1}$   $\frac{I_1}{I_2} = \frac{N_2}{N_1}$   $\frac{Z_2}{Z_1} = \left(\frac{N_2}{N_1}\right)^2$

Decibel:  $H_{dB} = 10 \log\left(\frac{P_2}{P_1}\right) = 20 \log\left(\frac{U_2}{U_1}\right)$

Eulers formel:  $e^{j\alpha} = \cos(\alpha) + j \sin(\alpha)$   $j = \sqrt{-1}$

Kartesiskt/polärt:  $A = a + jb$   $|A| = \sqrt{a^2 + b^2}$   $\angle A = \arctan\left(\frac{b}{a}\right)$   $a = |A| \cos(\angle A)$   $b = |A| \sin(\angle A)$   
vänd!

**Serieresonanskrets**

Överdämpat system:  $\zeta > 1$   $I(t) = a \left( \frac{1}{r_1 - r_2} e^{r_1 t} + \frac{1}{r_2 - r_1} e^{r_2 t} \right)$   $r_1 = -\omega_0 (\zeta - \sqrt{\zeta^2 - 1})$   
 $r_2 = -\omega_0 (\zeta + \sqrt{\zeta^2 - 1})$

Kritiskt dämpat system:  $\zeta = 1$   $I(t) = a t e^{rt}$   $r = r_1 = r_2 = -\omega_0$

Underdämpat system:  $\zeta < 1$   $I(t) = a e^{-\omega_0 \zeta t} \sin(\omega_d t)$

Odämpad resonansfrekvens:  $\omega_0 = \frac{1}{\sqrt{LC}}$

Dämpad resonansfrekvens:  $\omega_d = \omega_0 \sqrt{1 - \zeta^2}$

Dämpfaktor:  $\zeta = \frac{R}{2} \sqrt{\frac{C}{L}}$

**RC-nät**  $\tau = RC$   $U_c(t) = E \left( 1 - e^{-\frac{1}{RC}t} \right)$   $U_c(t) = E e^{-\frac{1}{RC}t}$

**RL-nät**  $\tau = \frac{L}{R}$   $I(t) = \frac{E}{R} \left( 1 - e^{-\frac{R}{L}t} \right)$   $I(t) = \frac{E}{R} e^{-\frac{R}{L}t}$