

/6.21 [p420]

01 Våg - och mekanik fysik

M8

$$\gamma \approx mg \times 98.2 \text{ N}$$

$$M_{Al} = \frac{1.25 \cdot 10^{-2} [\text{cm}^2] \cdot 2.60 \left[\frac{\text{g}}{\text{cm}^3} \right] \cdot \gamma}{\gamma_1} = 0.0325 \frac{\text{g}}{\text{cm}} = 0.00325 \frac{\text{kg}}{\text{m}}$$

$$M_{st} = \frac{A_{st} \cdot \rho_{st} \cdot \gamma_2}{\gamma_2} = 1.25 \cdot 10^{-2} [\text{cm}^2] \cdot 7.80 \left[\frac{\text{g}}{\text{cm}^3} \right] = 0.0975 \frac{\text{g}}{\text{cm}} = 0.00975 \frac{\text{kg}}{\text{m}}$$

$$v_{Al} = \sqrt{\frac{\gamma}{M_{Al}}} \approx 173.83 \text{ m/s} \quad v_{st} = \sqrt{\frac{\gamma}{M_{st}}} \approx 100.36 \text{ m/s}$$

$$L_1 = 60.0 \text{ cm} \quad L_2 = 86.6 \text{ cm}$$

"having the joint as one of the nodes"

Antag: n_{Al} loops i Al $\Rightarrow n_{Al} \cdot \frac{\lambda_{Al}}{2} = L_1 \Rightarrow \lambda_{Al} = \frac{2L_1}{n_{Al}}$ (*)

n_{st} loops i st. $\Rightarrow n_{st} \cdot \frac{\lambda_{st}}{2} = L_2$

$$v_{Al} = f_{Al} \lambda_{Al} \quad , \quad v_{st} = f_{st} \lambda_{st}$$

$$\text{Om } f_{Al} = f_{st} = f \Rightarrow \frac{v_{Al}}{\lambda_{Al}} = \frac{v_{st}}{\lambda_{st}}$$

$$\text{Kombinera med (*)} \Rightarrow \frac{v_{Al} n_{Al}}{2L_1} = \frac{v_{st} n_{st}}{2L_2}$$

Lös ut variabeln n_{Al}/n_{st} :


$$\frac{n_{Al}}{n_{st}} = \frac{v_{st}}{v_{Al}} \cdot \frac{L_1}{L_2} = \frac{100.36}{173.83} \cdot \frac{60.0}{86.6} = 0.4 \text{ (0000)}$$

Finn (de minsta) heltalen $n_{st} > n_{Al}$ som uppfyller detta

Kandidater $\frac{n_{Al}}{n_{st}} = \frac{1}{2} = 0.5$, $\frac{1}{3} \approx 0.33$, $\frac{2}{3} \approx 0.667$

a) $\frac{2}{4} = 0.5$, $\frac{2}{5} = 0.4 (!) \Rightarrow \underline{n_{Al} = 2, n_{st} = 5}$

$$f_{\min} = f_{Al} = \frac{v_{Al}}{\lambda_{Al}} = \frac{v_{Al} \cdot n_{Al}}{2L_1} = \frac{173.83 \cdot 2}{2 \cdot 0.60 [\text{m}]} = 289.72 \approx \underline{290 \text{ s}^{-1} [\text{Hz}]} \quad [289]$$

b)  8st noder inkl. ändpunkterna