

Problem 20

Triangle ABC has a right angle at B . $AB = 1$, and $BC = 2$. The bisector of $\angle BAC$ meets \overrightarrow{BC} at D . What is \overrightarrow{BD} ?

(A) $\frac{\sqrt{3}-1}{2}$

(B) $\frac{\sqrt{5}-1}{2}$

(C) $\frac{\sqrt{5}+1}{2}$

(D) $\frac{\sqrt{6}+\sqrt{2}}{2}$

(E) $2\sqrt{3} - 1$

Problem 22

A cubical cake with edge length 2 inches is iced on the sides and the top. It is cut vertically into three pieces as shown in this top view, where \mathcal{M} is the midpoint of a top edge. The piece whose top is triangle \mathcal{B} contains \mathcal{C} cubic inches of cake and \mathcal{S} square inches of icing. What is $\mathcal{C} + \mathcal{S}$?

(A) $\frac{24}{5}$

(B) $\frac{32}{5}$

(C) $8 + \sqrt{5}$

(D) $5 + \frac{16\sqrt{5}}{5}$

(E) $10 + 5\sqrt{5}$

The keystone arch is an ancient architectural feature. It is composed of congruent isosceles trapezoids fitted together along the non-parallel sides, as shown. The bottom sides of the two end trapezoids are horizontal. In an arch made with 9 trapezoids, let \mathcal{X} be the angle measure in degrees of the larger interior angle of the trapezoid. What is \mathcal{X} ?

(A) 100

(B) 102

(C) 104

(D) 106

(E) 108

10a

Problem 16

Nonagenerate $\triangle ABC$ has integer side lengths, \overrightarrow{BD} is an angle bisector, $AD = 3$, and $DC = 8$. What is the smallest possible value of the perimeter?

(A) 30

(B) 33

(C) 35

(D) 36

(E) 37