Decipherment as Regression

Solving Historical Substitution Ciphers by Learning Symbol Recurrence Relations

Nishant Kambhatla, Logan Born, Anoop Sarkar

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1. Why this paper?

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Relevancy

• Homophonic substitution ciphers

Ranking

Core2023 Ranking: A

Recency

• May 2023

Decipherment as Regression: Solving Historical Substitution Ciphers by Learning Symbol Recurrence Relations

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Abstract

Solving substitution ciphers involves mapping sequences of cipher symbols to fluent text in a target language. This has conventionally been formulated as a search problem, to find the decipherment key using a character-level language model to constrain the search space. This work instead frames decipherment as a sequence prediction task, using a Transformer-based causal language model to learn recurrences between characters in a ciphertext. We introduce a novel technique for transcribing arbitrary substitution ciphers into a common recurrence encoding. By leveraging this technique, we (i) create a large synthetic dataset of homophonic ciphers using random keys, and (ii) train a decipherment model that predicts the plaintext sequence given a recurrence-encoded ciphertext. Our method achieves strong results on synthetic 1:1 and homophonic ciphers, and cracks several real historic homophonic ciphers. Our analysis shows that the model learns recurrence relations between cipher symbols and recovers decipherment keys in its self-attention.1

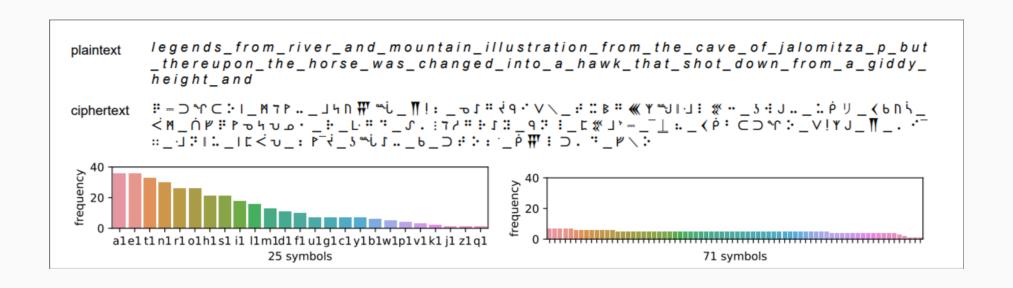
Figure 1: The homophonic substitution key for the Simeone de Crema written in Mantua in 1401 AD. The top line maps each character in the alphabet to its reversedalphabet equivalent; each vowel is substituted by three additional symbols.

sequences (D'Ascoli et al., 2022). We rethink decipherment as a regression task that predicts a natural language plaintext by learning a recurrence relation between integer-coded ciphertext symbols.

There exist large collections of historical ciphers (see de-crypt.org)², in the form of encrypted letters and more informal communications, of which many remain undeciphered. Many of these texts employ complex homophonic substitution ciphers, which mask the frequencies of letters by using a larger alphabet than the underlying language. Figure 1 shows the first known homophonic cipher from 1401 AD ³. Automated computational deci-

2. Methodology

2.1 Recurrent Integer Sequences



Monoalphabetic (1:1)

Trivially solved with frequency analysis

Homophonic (1:>0)

- Harder to solve frequencies can be hidden 😔
- More symbols = More mappings

2.1 Recurrent Integer Sequences

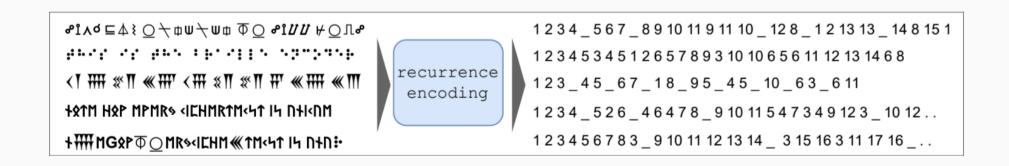
Capturing first/repeated symbol occurences

- Spaces denoted as underscore
- Unseen symbols denoted as incremental integer
- Recurring symbols denoted as represented previous integer
- Works for ciphers with different symbol sets

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The authors consider this a novel approach

Remember: Ciphertext is now a Recurrent Integer Sequence

This makes every cipher comparable

Dataset made by authors

- 2 million unique homophonic substitution ciphers
- Including their corresponding plaintexts
- Uses Modern English

CausalLM

- Reads from left to right can only look back
- Past words affect predicted words (sort of like autocorrect)

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$$[X^{l}, Y^{l}] = \text{FFN} \circ \text{SelfAtn}([X^{l-1}, Y^{l-1}], \text{Mask})$$

- $X^{l-1} \to \text{Cipher at layer previous to } l$
- $Y^{l-1} \to \text{Text}$ at layer previous to l
- SelfAtn \rightarrow Captures positions related to previous symbols/letters
- Mask \rightarrow The attention mask used by SelfAtn
- FFN \rightarrow Result is fed to Feed-Forward Neural Network X

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Above produces the representation at $[X^l, Y^l]$

Remember: CausalLM only looks back!

Loss function

$$L^{\operatorname{CLM}}(X,Y) = L^{\operatorname{SRC}} + L^{\operatorname{TGT}} = -\mathrm{logP}(X) - \mathrm{logP}(Y|X)$$

- $L^{\text{SRC}} \to \text{Source loss}$ error predicting cipher seq
- $L^{\text{TGT}} \to \text{Target loss}$ error predicting plaintext seq
- $-\log P(X) \to Probability$ of reproducing correct cipher symbols
- $-\log P(X|Y) \to Probability$ of predicting plaintext given cipher

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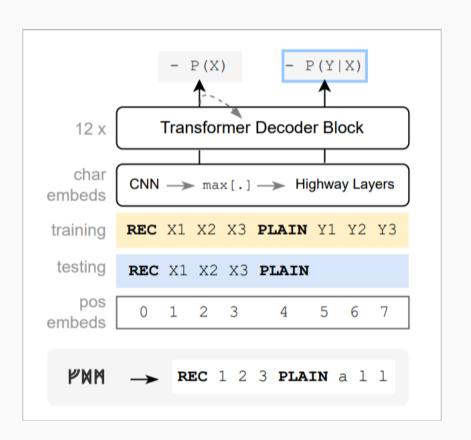
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Low probability = high loss, and vice versa

Probability can be seen as confidence

Why CausalLM?

- Predict the cipher symbols in a sequence
- Predict plaintext in the sequence
- Model learns the mappings



Considered models

- Seq2seq
- Target-Only CausalLM
- PrefixLM

Why are they weaker?

- Only predicts plaintext
- Does not learn cipher symbol recurrence patterns

3. Results

3.1 Synthetic Ciphers

How can we measure?

- Symbol Error Rate (SER)
- 0% = Perfect decipherment
- 100% Total gibberish

What can we observe?

- Between 400 700 chars
- Three key ranges
- CausalLM outperforms the others



#keys	Model	Max Len.	
		400	700
	Seq-to-Seq	72.30	fail
20.45	PrefixLM	54.73	69.50
30-45	CausalLM (tgt)	29.99	37.20
	CausalLM	0.40	0.21
	PrefixLM	69.50	54.73
40-65	CausalLM (tgt)	29.99	37.20
	CausalLM	0.83	0.80
	PrefixLM	70.52	71.82
30-85	CausalLM (tgt)	42.05	42.69
	CausalLM	2.25	2.19

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30-85	CausalLM (tgt)	42.05	42.69
	CausalLM	2.25	2.19

Fun observation: seq2seq does not even converge at longer ciphers



3.2 Z408 Cipher

But what about real ciphers?

- Z408 = 408 characters
- 54 symbols
- From the 1960's
- No spaces



https://zodiackiller.fandom.com/wiki/408-cipher

3.2 Z408 Cipher

Hill-climbing

• Keep the best candidates

Beam search

• Keep N best candidates

Method	Search	SER (%)	Speed
LM+EM (2013)	1M restarts	11.0	_
n-gram LM (2013)	beam 100K	94.6	4000
	beam 1M	2.7	35000
LSTM LM (2018)	beam 100K	2.4	5600
	beam 1M	1.9	50000
Ours (greedy)	beam 1	1.9	1 sec
Ours (best)	beam 200	1.9	2 sec

3.2 Z408 Cipher

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CausalLM 🎉

- Faster (it does not search)
- Better (even with smaller beam)

What about historical ciphers?

TNA_SP106/5

- 1624, UK
- Homophonic substitution
- 171 characters
- 47 symbols to 27 letters
- Not many reccurences (3.6 avg)

The homophonic 40-65 key model

- They used beam size 1000
- Achieved 18% SER

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Remember: This is a hard cipher in an out-of-domain language

BnF_fr2988_f01

- 1524-1549, Italy
- Homophonic substitution
- 2 pages long
- 35 symbols
- More reccurences but older language

The homophonic 30-45 key model

• Achieved 1.13% SER

```
95 ~ dx 8 A + e a: + + ax + adv A e vdx , = 11 A+ ) adv 5 dx AVA
AV~ 11 01 81229 acoro 8x 11 = 0 91 9++58 x > 59~ 4 co + 6
  CONVATO VO ## 2+ 59 A 11 a cd) 29 100 97 # 1 #5 × ac+d*A
AVIA SAHE NIA # TO 91 21+87+1 = a cdx 11 = TO di DAVA JE ~
peeis_jour_hes_bein_er
nist_to_obtein_licence_t
o_kis_|j|oue_hand_bot_cul
d_not_obtein_permissione
_to_do_it_my_erand_is_to
_hayf_publictly_ecrauit_
pardone_and_humbly_offer
_it_my_faythful
pleis_your_hes_bein_erni
st_to_obtein_licence_to_
kis_youe_hand_bot_culd_n
ot_obtein_permissione_to
_do_it_my_erand_is_to_ha
yf_publictly_ecrauit_par
done_and_humbly_offer_it
_my_faythful
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95 ~ dx 8 A + e a: + + ax + a dv A e vdx , e) A A+) adv 5 dx AVX. AV~ 11 01 81229 ~ にでいるX 11 # かりは 9#+58*159~ * cでける COAVA TO VO ## 2+ 59 Ail a cd) 29 100 97 # 1 #5 x ac#d*A AVIA SAte NIA = togi 21+8)+1+ a cdx 1A = todi DAVA J ~ peeis_|j|our_hes_bein_er nist_to_obtein_licence_t o_kis_|j|oue_hand_bot_cul d_not_obtein_permissione _to_do_it_my_erand_is_to _hayf_publictly_ecrauit_ pardone_and_humbly_offer _it_my_faythful pleis_your_hes_bein_erni st_to_obtein_licence_to_ kis_youe_hand_bot_culd_n ot_obtein_permissione_to _do_it_my_erand_is_to_ha yf_publictly_ecrauit_par done_and_humbly_offer_it _my_faythful

Notice how words are different in old English!

3.4 Monoalphabetic Ciphers

CausalLM + Rec

• Recurrence Integer Sequence

CausalLM + Freq

- Described in another paper
- Summary:
 - encoded with frequency rank
 - unlike REC which is left to right order

CausalLM Observations

- CausalLM
 - Weaker on short ciphers
 - Still comparable to other models!

(Near) perfect SER on >128 ciphers!

$cipher \ length \to$	<128	>128
Beam + 6-gram (Nuhn et al., 2013) Beam + LM ((Kambhatla et al., 2018)) Beam + LM + Freq. Match (ibid.) Seq2Seq + Freq. (Aldarrab and May)	22.00 10.89 11.32 7.68	0.00 0.00 0.00 0.00
Causal LM + Freq. Causal LM + Rec.	10.56 11.30	0.00 0.02

3.5 Unseen Language Ciphers

What if we don't know the language of the cipher?

- Multilingual model
- Trained on 13 languages (Latin included)
- No language ID's during training!
- Frequency based encoding
 - Likely due to Zipfian consistency

	SER (%)
Multilingual Seq2Seq (2021)	5.47
Multilingual Causal LM (ours)	4.10

Results on the monoalphabetic Borg cipher in 17th century Latin

3.5 Unseen Language Ciphers

What about the main model?

Zero-shot on 400 chars of Borg

- SER 45.14%
- Not too good

But in real life...

- Domain expert evaluate output
- If they correct 3 words manually:
 - ► SER 3.89%
 - Pretty good!

3.5 Unseen Language Ciphers

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Remember:

The main model has never seen Latin before!

4. Contributions

4. Contributions

1. The Seq2seq dataset

2. Novel Recurrence Integer Sequence

- Captures repetition and position
- Works for both mono- and homophonic

3. Analysis of REC in Transformer LM

Faster and more accurate

4. Practical application of solver

- Fully automated
- Solved real historical ciphers

5. Limitations

5. Limitations

Cipher Sizes

- Not superior for shorter ciphers <128 with less frequencies
- Inefficient for longer ciphers >1500

The paper tries a lot!

- The model tries to do it all
- ... But it does it well!

Where is the data from?

- Authors use 3 different datasets + ciphers
- Hard to keep track of which and when?

They did not compare with AZDecrypt

5. Limitations

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- Not superior for shorter ciphers <128 with less frequencies
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What happens with transpositioned ciphers like Z340?

6. Relevance

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Does not solve modern encryption \(\bigcap{\lambda}{\} \)

• They are too advanced

Historical Value 📚

• Solve other ciphers

Cryptanalysis advancement 29

• Deeper knowledge of classic ciphers

More LM use cases 🔖

• What else can we use LMs for?

7. Questions?