

Decipherment as Regression

Solving Historical Substitution Ciphers by Learning Symbol Recurrence Relations

Nishant Kambhatla, Logan Born, Anoop Sarkar

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1. Why this paper?

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Relevancy

- Homophonic substitution ciphers

Ranking

- Core2023 Ranking: A

Recency

- May 2023

Decipherment as Regression: Solving Historical Substitution Ciphers by Learning Symbol Recurrence Relations

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Abstract

Solving substitution ciphers involves mapping sequences of cipher symbols to fluent text in a target language. This has conventionally been formulated as a search problem, to find the decipherment key using a character-level language model to constrain the search space. This work instead frames decipherment as a sequence prediction task, using a Transformer-based causal language model to learn recurrences between characters in a ciphertext. We introduce a novel technique for transcribing arbitrary substitution ciphers into a common *recurrence encoding*. By leveraging this technique, we (i) create a large synthetic dataset of homophonic ciphers using random keys, and (ii) train a decipherment model that predicts the plaintext sequence given a recurrence-encoded ciphertext. Our method achieves strong results on synthetic 1:1 and homophonic ciphers, and cracks several real historic homophonic ciphers. Our analysis shows that the model learns recurrence relations between cipher symbols and recovers decipherment keys in its self-attention.¹

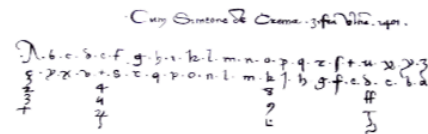


Figure 1: The homophonic substitution key for the *Simeone de Crema* written in Mantua in 1401 AD. The top line maps each character in the alphabet to its reversed-alphabet equivalent; each vowel is substituted by three additional symbols.

sequences (D’Ascoli et al., 2022). We rethink decipherment as a regression task that predicts a natural language plaintext by learning a recurrence relation between integer-coded ciphertext symbols.

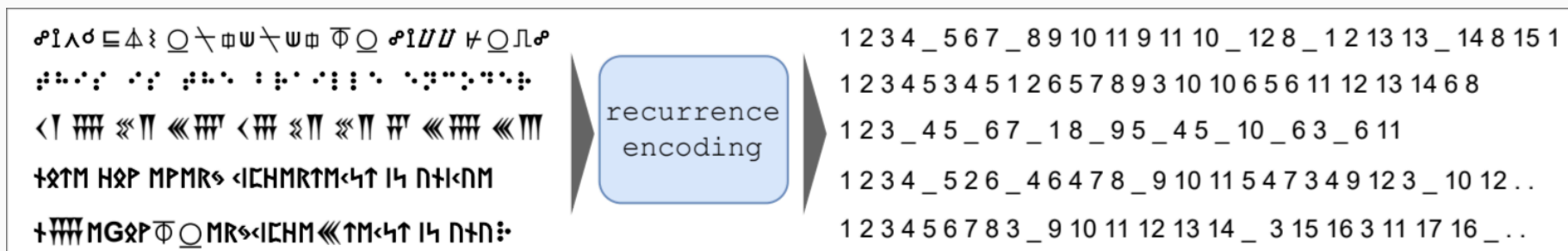
There exist large collections of historical ciphers (see de-crypt.org)², in the form of encrypted letters and more informal communications, of which many remain undeciphered. Many of these texts employ complex *homophonic substitution ciphers*, which mask the frequencies of letters by using a larger alphabet than the underlying language. Figure 1 shows the first known homophonic cipher from 1401 AD³. Automated computational deci-

2. Methodology

2.1 Recurrent Integer Sequences

Capturing first/repeated symbol occurrences

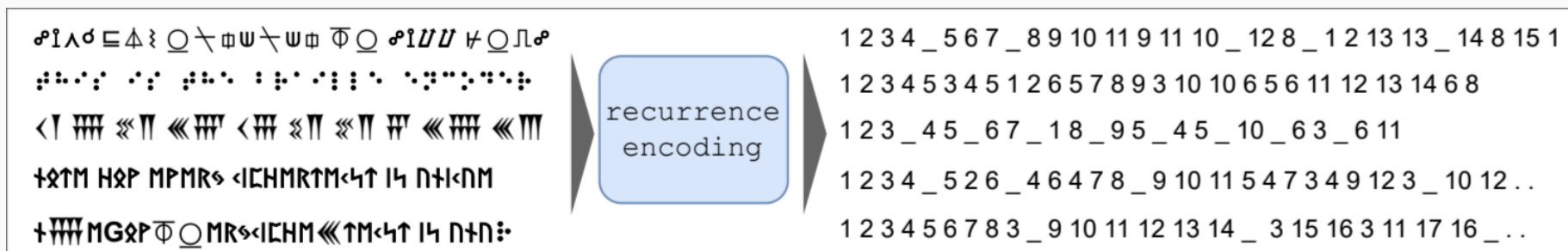
- Spaces denoted as **underscore**
- Unseen symbols denoted as **incremental integer**
- Recurring symbols denoted as represented **previous integer**
- Works for ciphers with different symbol sets



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The authors consider this a novel approach

2.2 Generative Decipherment Model

Remember: Ciphertext is now a Recurrent Integer Sequence

This makes every cipher comparable

Dataset made by authors

- 2 million unique homophonic substitution ciphers
- Including their corresponding plaintexts
- Uses Modern English

2.2 Generative Decipherment Model

CausalLM

- Reads from left to right - can only look back
- Past words affect predicted words - (sort of like autocorrect)

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$$[X^l, Y^l] = \text{FFN} \circ \text{SelfAttn}([X^{l-1}, Y^{l-1}], \text{Mask})$$

- $X^{l-1} \rightarrow$ Cipher at layer previous to l
- $Y^{l-1} \rightarrow$ Text at layer previous to l
- SelfAttn \rightarrow Captures positions related to previous symbols/letters
- Mask \rightarrow The attention mask used by SelfAttn
- FFN \rightarrow Result is fed to Feed-Forward Neural Network X

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Above produces the representation at $[X^l, Y^l]$

Remember: CausalLM only looks back!

2.2 Generative Decipherment Model

Loss function

$$L^{\text{CLM}}(X, Y) = L^{\text{SRC}} + L^{\text{TGT}} = -\log P(X) - \log P(Y|X)$$

- $L^{\text{SRC}} \rightarrow$ Source loss - error predicting cipher seq
- $L^{\text{TGT}} \rightarrow$ Target loss - error predicting plaintext seq
- $-\log P(X) \rightarrow$ Probability of reproducing correct cipher symbols
- $-\log P(X|Y) \rightarrow$ Probability of predicting plaintext given cipher

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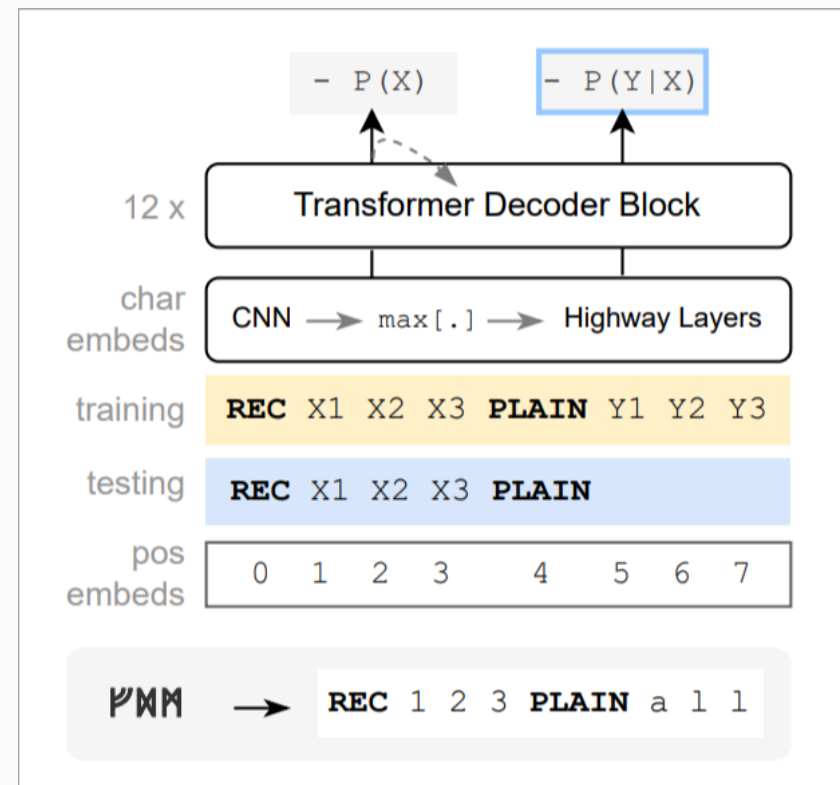
Low probability = high loss, and vice versa

Probability can be seen as confidence

2.2 Generative Decipherment Model

Why CausalLM?

- Predict the cipher symbols in a sequence
- Predict plaintext in the sequence
- Model learns the mappings



2.2 Generative Decipherment Model

Considered models

- Seq2seq
- Target-Only CausalLM
- PrefixLM

Why are they weaker?

- Only predicts plaintext
- Does not learn cipher symbol recurrence patterns

3. Results

3.1 Synthetic Ciphers

How can we measure?

- Symbol Error Rate (SER)
- 0% = Perfect decipherment
- 100% Total gibberish

What can we observe?

- Between 400 - 700 chars
- Three key ranges
- CausalLM outperforms the others 🎉

#keys	Model	Max Len.	
		400	700
30-45	Seq-to-Seq	72.30	fail
	PrefixLM	54.73	69.50
	CausalLM (tgt)	29.99	37.20
	CausalLM	0.40	0.21
40-65	PrefixLM	69.50	54.73
	CausalLM (tgt)	29.99	37.20
	CausalLM	0.83	0.80
30-85	PrefixLM	70.52	71.82
	CausalLM (tgt)	42.05	42.69
	CausalLM	2.25	2.19

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	CausalLM (tgt)	42.05	42.69
	CausalLM	2.25	2.19

Fun observation: seq2seq does not even converge at longer ciphers 🤖

3.2 Z408 Cipher

But what about real ciphers?

- Z408 = 408 characters
- 54 symbols
- From the 1960's
- No spaces !



<https://zodiackiller.fandom.com/wiki/408-cipher>

3.2 Z408 Cipher

Hill-climbing

- Keep the best candidates

Beam search

- Keep N best candidates

Method	Search	SER (%)	Speed
LM+EM (2013)	1M restarts	11.0	–
<i>n</i> –gram LM (2013)	beam 100K	94.6	4000
	beam 1M	2.7	35000
LSTM LM (2018)	beam 100K	2.4	5600
	beam 1M	1.9	50000
Ours (greedy)	beam 1	1.9	1 sec
Ours (best)	beam 200	1.9	2 sec

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CausalLM 🎮

- Faster (it does not search)
- Better (even with smaller beam)

3.3 Historical Ciphers

What about historical ciphers?

TNA_SP106/5

- 1624, UK
- Homophonic substitution
- 171 characters
- 47 symbols to 27 letters
- Not many recurrences (3.6 avg)

The homophonic 40-65 key model

- They used beam size 1000
- Achieved 18% SER

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Remember: This is a hard cipher in an out-of-domain language

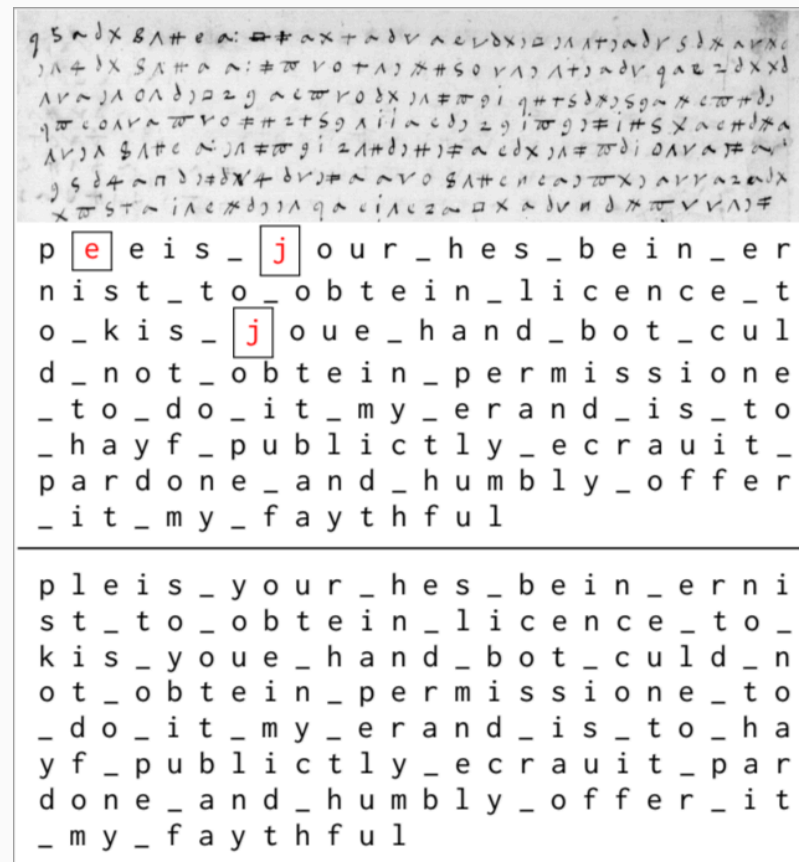
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BnF_fr2988_f01

- 1524-1549, Italy
- Homophonic substitution
- 2 pages long
- 35 symbols
- More recurrences but older language

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- Achieved 1.13% SER



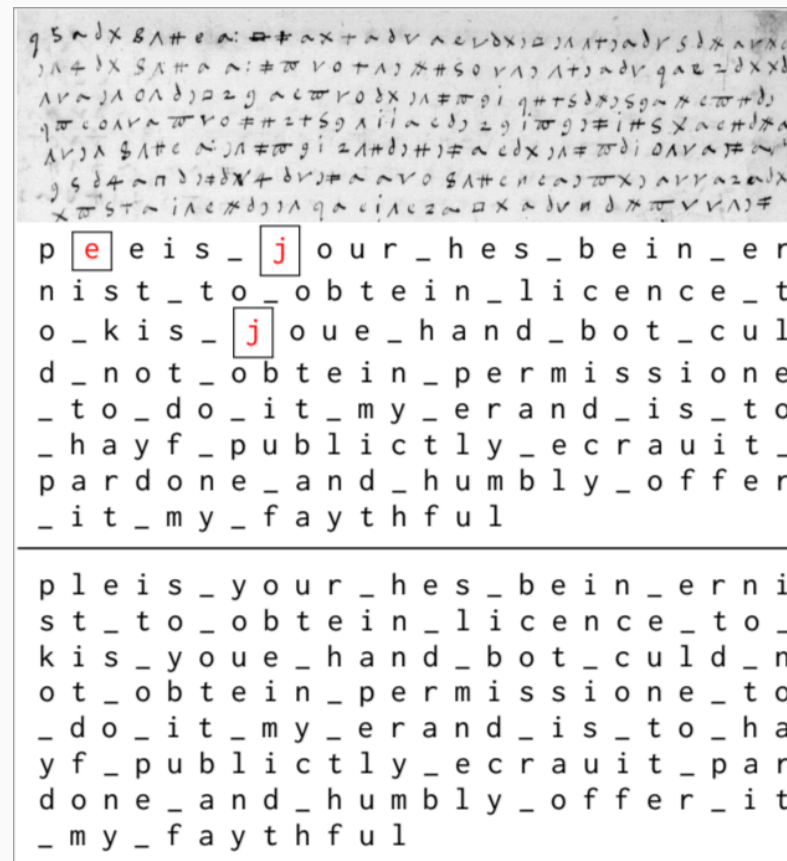
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Notice how words are different in old English!

3.4 Monoalphabetic Ciphers

CausalLM + Rec

- Recurrence Integer Sequence

CausalLM + Freq

- Described in another paper
- Summary:
 - encoded with frequency rank
 - unlike REC which is left to right order

CausalLM Observations

- CausalLM
 - Weaker on short ciphers
 - Still comparable to other models!

(Near) perfect SER on >128 ciphers!

cipher length →	<128	>128
Beam + 6-gram (Nuhn et al., 2013)	22.00	0.00
Beam + LM ((Kambhatla et al., 2018))	10.89	0.00
Beam + LM + Freq. Match (ibid.)	11.32	0.00
Seq2Seq + Freq. (Aldarrab and May)	7.68	0.00
Causal LM + Freq.	10.56	0.00
Causal LM + Rec.	11.30	0.02

3.5 Unseen Language Ciphers

What if we don't know the language of the cipher?

- Multilingual model
- Trained on 13 languages (Latin included)
- No language ID's during training!
- Frequency based encoding
 - Likely due to Zipfian consistency

	SER (%)
Multilingual Seq2Seq (2021)	5.47
Multilingual Causal LM (ours)	4.10

Results on the monoalphabetic Borg cipher in 17th century Latin

3.5 Unseen Language Ciphers

What about the main model?

Zero-shot on 400 chars of Borg

- SER 45.14%
- Not too good

But in real life...

- Domain expert evaluate output
- If they correct 3 words manually:
 - SER 3.89%
 - Pretty good!

3.5 Unseen Language Ciphers

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Remember:

The main model has never seen Latin before!

4. Contributions

4. Contributions

1. The Seq2seq dataset

2. Novel Recurrence Integer Sequence

- Captures repetition and position
- Works for both mono- and homophonic

3. Analysis of REC in Transformer LM

- Faster and more accurate

4. Practical application of solver

- Fully automated
- Solved real historical ciphers

5. Limitations

5. Limitations

Cipher Sizes

- Not superior for shorter ciphers < 128 with less frequencies
- Inefficient for longer ciphers > 1500

The paper tries a lot!

- The model tries to do it all
- ... But it does it well!

Where is the data from?

- Authors use 3 different datasets + ciphers
- Hard to keep track of which and when?

They did not compare with AZDecrypt

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What happens with transpositioned ciphers like Z340? 🐱

6. Relevance

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Does not solve modern encryption ⚠️

- They are too advanced

Historical Value 📖

- Solve other ciphers

Cryptanalysis advancement 🧐

- Deeper knowledge of classic ciphers

More LM use cases 🤖

- What else can we use LMs for?