Decipherment as Regression

Solving Historical Substitution Ciphers by Learning Symbol Recurrence Relations

Nishant Kambhatla, Logan Born, Anoop Sarkar

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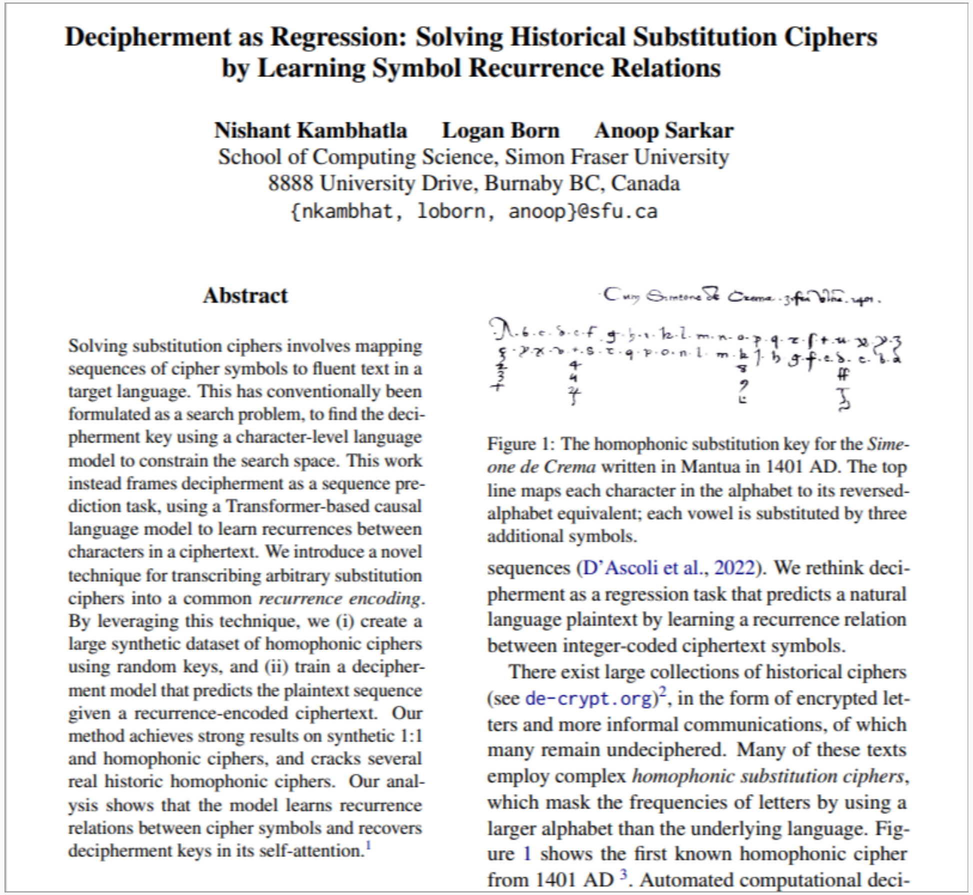

Decipherment as Regression: Solving Historical Substitution Ciphers by Learning Symbol Recurrence Relations

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Abstract

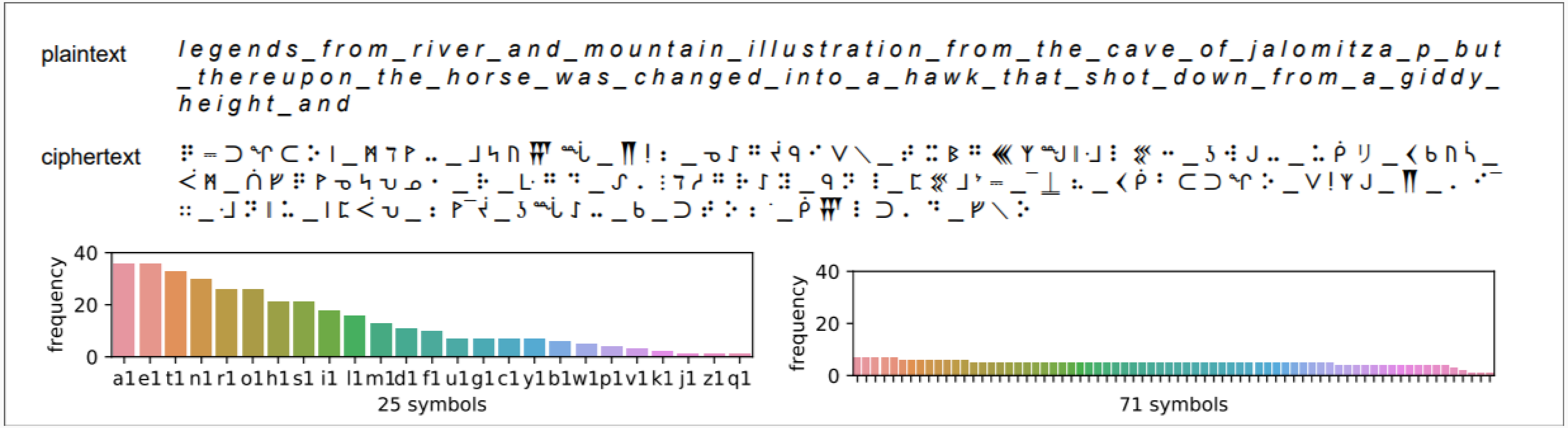
Solving substitution ciphers involves mapping sequences of cipher symbols to fluent text in a target language. This has conventionally been formulated as a search problem, to find the decipherment key using a character-level language model to constrain the search space. This work instead frames decipherment as a sequence prediction task, using a Transformer-based causal language model to learn recurrences between characters in a ciphertext. We introduce a novel technique for transcribing arbitrary substitution ciphers into a common *recurrence encoding*. By leveraging this technique, we (i) create a large synthetic dataset of homophonic ciphers using random keys, and (ii) train a decipherment model that predicts the plaintext sequence given a recurrence-encoded ciphertext. Our method achieves strong results on synthetic 1:1 and homophonic ciphers, and cracks several real historic homophonic ciphers. Our analysis shows that the model learns recurrence relations between cipher symbols and recovers decipherment keys in its self-attention.[1]

Figure 1: The homophonic substitution key for the *Simeone de Crema* written in Mantua in 1401 AD. The top line maps each character in the alphabet to its reversed-alphabet equivalent; each vowel is substituted by three additional symbols.

sequences (D'Ascoli et al., 2022). We rethink decipherment as a regression task that predicts a natural language plaintext by learning a recurrence relation between integer-coded ciphertext symbols.

There exist large collections of historical ciphers (see `de-crypt.org`)[2], in the form of encrypted letters and more informal communications, of which many remain undeciphered. Many of these texts employ complex *homophonic substitution ciphers*, which mask the frequencies of letters by using a larger alphabet than the underlying language. Figure 1 shows the first known homophonic cipher from 1401 AD [3]. Automated computational deci-

2. Methodology



Monoalphabetic (1:1)

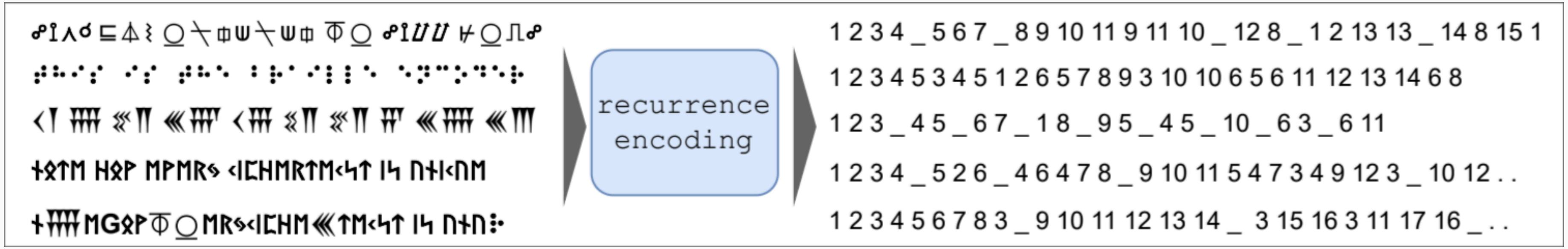
- Trivially solved with frequency analysis

Homophonic (1:>0)

- Harder to solve - frequencies can be hidden 😔
- More symbols = More mappings

Capturing first/repeated symbol occurences

- Spaces denoted as **underscore**
- Unseen symbols denoted as **incremental integer**
- Recurring symbols denoted as represented **previous integer**
- Works for ciphers with different symbol sets



2.1 Recurrent Integer Sequences

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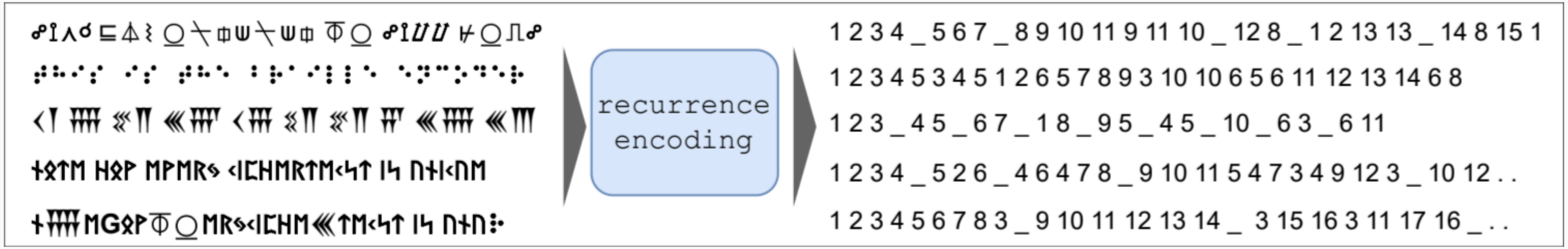

The authors consider this a novel approach

2.2 Generative Decipherment Model

Remember: Ciphertext is now a Recurrent Integer Sequence

This makes every cipher comparable

Dataset made by authors

- 2 million unique homophonic substitution ciphers
- Including their corresponding plaintexts
- Uses Modern English

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CausalLM

- Reads from left to right - can only look back
- Past words affect predicted words - (sort of like autocorrect)

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$$[X^l, Y^l] = \mathrm{FFN} \circ \mathrm{SelfAtn}\big([X^{l-1}, Y^{l-1}], \mathrm{Mask}\big)$$

- X^{l-1} → Cipher at layer previous to l
- Y^{l-1} → Text at layer previous to l
- SelfAtn → Captures positions related to previous symbols/letters
- Mask → The attention mask used by SelfAtn
- FFN → Result is fed to Feed-Forward Neural Network X

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Above produces the representation at $[X^l, Y^l]$