Activation functions

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Activation functions

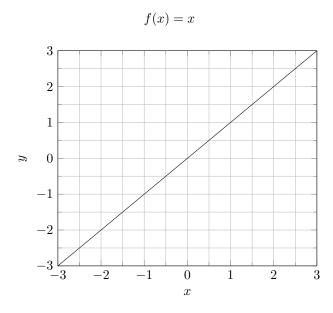
Activation functions are mathematical functions applied to the output of a neuron in neural network. They introduce non-linearity into the model so it can learn more complex patterns.

An Activation class is Layer subclass that can be attached to a <u>layer</u> (another Layer subclass) in the network (Scroll to a specific activation function for examples).

Activation class:

Linear function

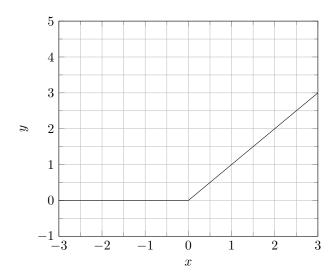
Linear activation function returns the value itself. It can be used as a place-holder for an activation function when one isn't needed.



ReLU function

ReLU (Rectified Linear Unit) is an activation function that returns 0 for all negative input values and the input value itself for all positive values.

$$f(x) = max(0, x)$$



ReLu can be attached as activation function to a layer like this:

Sigmoid function

Sigmoid is an activation function that maps input values to a range between 0 and 1.

$$f(x) = \frac{1}{1 + e^{-x}}$$

$$1.25$$

$$0.75$$

$$0.25$$

$$0.25$$

$$-4$$

$$-2$$

$$0$$

$$x$$

Sigmoid can be attached as activation function to a layer like this:

```
Dense(input_size = input_size,
    output_size = output_size,
    activation = 'sigmoid')
```

Softmax function

Softmax is an activation function used for multi-class classification problems. It takes a vector of raw scores (logits) and converts them into a probability distribution over multiple classes meaning that each value will be in range [0,1] and the sum of those values is 1.

$$y(x_i) = \frac{e^{x_i}}{\sum_{j=1}^{N} e^{x_j}}$$

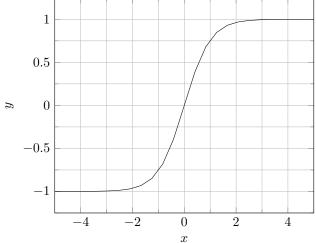
Softmax can be attached as activation function to a layer like this:

NB! Because the derivative for Softmax function is calculated together with Categorical Cross-Entropy loss, they can only be used in combination with each other. The last layer of the model should have Softmax as the activation function and the model should use Categorical Cross-Entropy loss.

Tanh function

Tanh is an activation function that maps input values to a range between -1 and 1.

$$f(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$



Tanh can be attached as activation function to a layer like this:

Layers

Layer is a functional unit that takes input data, applies a mathematical transformation to it and produces an output. Each layer consists of a set of neurons each of which computes a weighted sum of its inputs and applies an activation function to the result.

Base layer class:

```
class Layer:
    def __init__(self) -> None:
        self.input = None
        self.output = None

    def forward(self, input):
        raise NotImplementedError

def backward(self, output_error, learning_rate):
        raise NotImplementedError

def update(self, learning_rate):
    raise NotImplementedError
```

Each layer has a forward() function, backward() function and update() function. Forward function calculates the output given an input, backward function calculates the gradients that will be applied to the weights and update function updates the weights accordingly.

Dense layer

A Dense layer is a type of layer where each neuron is connected to every neuron in the preceding layer. It performs a weighted sum of the inputs from the previous layer and then applies an activation function to produce an output.

The Dense layer has the following functions:

```
def create_weights(self)
# Creates the weight and bias matrices for the layer.
```

Input layer

An Input layer is the very first layer of the network. It's only function is to pass on the input data to the next layer.

Input layer has the following functions:

Loss functions

A loss function is a mathematical function used to measure the error between the predicted outputs of a model and the actual target values. The goal during learning is to minimize this loss.

The Loss class:

```
class Loss:
    def __init__(self, loss_function) -> None:
        loss = loss_functions.get_loss(loss_function)
        self.name = loss_function
        self.loss = loss[0]
        self.loss_derivative = loss[1]

def forward(self, y_true, y_pred):
        return self.loss(y_true, y_pred)

def backward(self, y_true, y_pred):
        return self.loss_derivative(y_true, y_pred)
```

Mean Squared Error

Mean Square Error is a loss function used primarily in regression problems. It measures the average of the squared differences between the predicted values and the actual values.

$$MSE = \frac{1}{N} \sum_{i=1}^{N} (y_i - \hat{y}_i)^2$$

where y_i is the true value, $\hat{y_i}$ is the predicted value and N is the number of samples.

To use Mean Squared Error as the loss function, it should be added as "mse" as an argument while compiling the model:

model.compile(loss_fn='mse')

Categorical Cross-Entropy

Catgeorical Cross-Entropy is a loss function used in multi-class classification problems. It quantifies the dissimilarity between the predicted class probabilities and the true class probabilities.

$$CCE = -\sum_{i=1}^{N} y_i \cdot \log(\hat{y_i})$$

where y_i is the true value, $\hat{y_i}$ is the predicted value and N is the number of samples.

To use Categorical Cross-Entropy as the loss function, it should be added as an argument when compiling the model:

```
model.compile(loss_fn='categorical_cross_entropy')
```

PS! Because the derivatives of Categorical Cross-Entropy and Softmax activation function are calculated together, they should be used in combination. The Softmax function should be the activation function of (only!) the last layer in the model when Categorical Cross-Entropy is used as loss function.

Models

A model is a mathematical or computational structure that comprises layers of interconnected neurons each performing mathematical operations on input data. The model is trained using labeled data to learn patterns and relationships allowing it to make predictions or decisions on new, unseen data.

Model has the following methods:

A model can be created by defining an input layer and then calling every next layer with the previous one as an argument. Example:

```
inputs = Dense(input_size=2, output_size=16, activation='tanh')
x = Dense(output_size=8, activation='relu')(inputs)
x = Dense(output_size=4, activation='relu')(x)
x = Dense(output_size=2, activation='relu')(x)
outputs = Dense(output_size=1, activation='sigmoid')(x)
model = Model(inputs, outputs)
```

When the model is defined, it can be compiled as follows:

```
model.compile(loss_fn='mse')
```

For training, the fit() method should be called with

- training data
- labels
- number of epochs
- learning rate

as arguments. The parameter print_loss determines whether the loss is printed out after every epoch or not. The fit() method returns the final loss:

Finally, a predict() method can be called to get some predictions:

```
predictions = model.predict(x_test)
```