

# Measuring Fairness in the US Mortgage Market

Hadi Elzayn

*Stanford University*

Simon Freyaldenhoven

*Federal Reserve Bank of Philadelphia*

Ryan Kobler

*Federal Reserve Bank of Philadelphia*

Minchul Shin

*Federal Reserve Bank of Philadelphia\**

May 21, 2024

## Abstract

Black Americans are both substantially more likely to have their mortgage application rejected and substantially more likely to default on their mortgages, compared to white Americans. We take these stark inequalities as a starting point to ask the question: How fair or unfair is the US mortgage market? We find that the answer to this question crucially depends on the definition of fairness. We consider six competing and widely used definitions of fairness, and find that they lead to very different conclusions. We then combine these six definitions into a series of stylized facts that offer a more comprehensive view of fairness in this market. An interactive Online Appendix allows the user to explore our fairness measurements further across both time and space.

JEL-Classification: D63, G21, G28, J15, R21

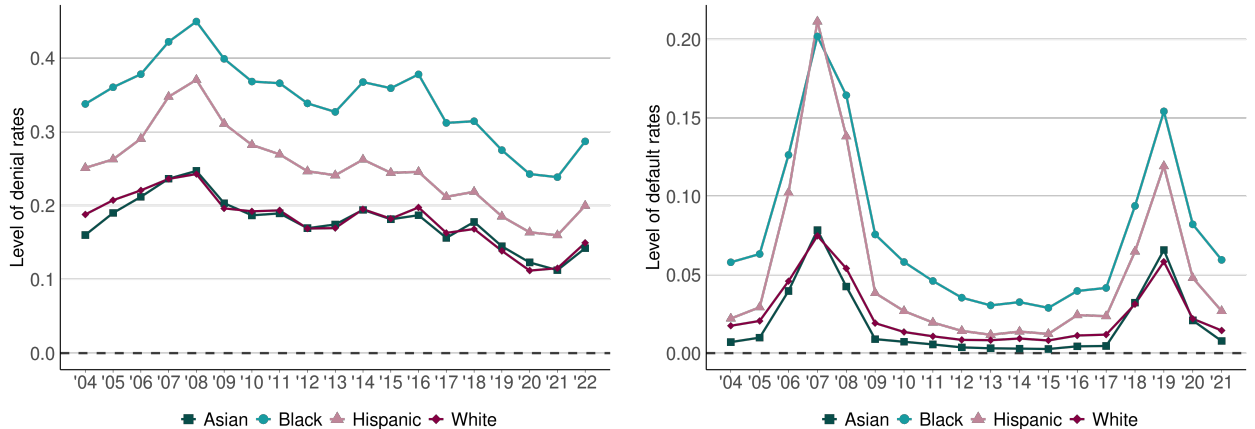
KEYWORDS: fairness, discrimination, inequality, measurement, algorithmic decisions, hmda

---

\*We thank Andrew Gross, Kellen O'Connor, and Eliana Sena Sarmiento for excellent research assistance. The views expressed herein are those of the authors and do not necessarily reflect the views of the Federal Reserve Bank of Philadelphia, or the Federal Reserve System. Emails: hselzayn@law.stanford.edu, simon.freyaldenhoven@phil.frb.org, ryan.kobler@phil.frb.org, minchul.shin@phil.frb.org.

# 1 Introduction

Is the \$2 trillion U.S. mortgage market *fair*? In this paper, we consider fairness in this market with respect to the race of an applicant. We start by noting that outcomes are very unequal in this market: Figure 1 depicts the default rates and denial rates by demographic group for mortgage applications filed in the US in recent years. In Figure 1a we see that Black and Hispanic borrowers are substantially more likely to have their loan application rejected than White and Asian borrowers. In Figure 1b we see that Black and Hispanic borrowers exhibit a substantially higher default rate than White and Asian borrowers.



(a) Percentage of mortgage application denied by year of application.

(b) Percentage of mortgage that default by year of origination.

**Figure 1:** Summary statistics by demographic group for mortgage applications filed in the US.

We take these stark inequalities as a starting point, but in order to assess fairness in this market, we first need a formal definition of fairness. Many competing definitions of Fairness exist. For example, Narayanan [2018] reviews a total of 21 fairness definitions. Similarly, as we discuss in Section 3, different parts of existing laws and regulatory guidance use different definitions of fairness. A second question we therefore address in this paper is whether it matters what definition of fairness we use: are the conclusions and policy implications the same across fairness definitions or do they differ?

Understanding fairness in the US mortgage market is important for several reasons. Mortgage balances are the largest source of debt for most Americans: by the end of 2022, out of a total household debt in the US of \$17 trillion, mortgage balances made up \$12 trillion (Federal Reserve Bank of New York [2023]). Additionally, any disparities in this market can translate into inequality in home ownership and thus wealth accumulation; indeed, it is well known that the mortgage market plays a prominent role in the persistence of wealth gaps across generations (Charles and Hurst [2003], Kuhn et al. [2020]), and that, historically, racial discrimination through practices such as redlining and racial covenants contributed to

today’s racial wealth gaps. We further note that mortgage underwriting has seen a shift towards algorithmic underwriting over the past two decades. As we argue in Section 3 this makes some of the traditional ways to measure (and regulate) fairness challenging. We thus also consider recent definitions of fairness developed in the algorithmic fairness literature.

Our paper contributes to an extensive literature on fairness and discrimination in the mortgage market, building upon works such as those by Black et al. [1978], Munnell et al. [1996], Berkovec et al. [1998], Ross and Yinger [2002], Cheng et al. [2015]. Recent advancements in data availability have spurred a new wave of studies incorporating default outcomes, as seen in works by Bhutta and Hizmo [2021], Giacoletti et al. [2022], Bartlett et al. [2022]. Further, our work is related to a recent literature that explores how Machine Learning algorithms can mitigate racial differences in lending (Tantri [2021], Bartlett et al. [2022], Fuster et al. [2022], Bhutta et al. [2022]). Existing studies usually focus on observing differences in a single outcome of interest (e.g., denial rates, pricing, or mortgage performance) across race. For example, Munnell et al. [1996] focuses on denial rate and finds that minorities in Boston had denial rates up to twice as high as White applicants. Berkovec et al. [1998] focuses on loan performance and finds that Black borrowers are more than twice as likely to default. Our paper stands out by considering a comprehensive list of fairness definitions. This allows us to empirically show that different definitions of fairness can lead to very different conclusions and policy implications.

We stylize our setting as one in which a sequence of people comes before a decision-maker, who reaches a decision about each person based on a set of features. These decisions may be made by a human or an algorithm. We assume that we can observe some applicant features including the race of an applicant, the decisions made, and the resulting outcomes of originated mortgages (default/non-default). We do not assume that we have access to the algorithm or process by which decisions are made, and explicitly allow for the possibility that it includes additional, unobserved applicant characteristics. This formulation corresponds to our empirical setting, for which we combine two sources of data. First, we utilize a confidential version of the Home Mortgage Disclosure Act (HMDA) data. This includes the vast majority of all mortgage applications filed in the US and contains applicant features including protected characteristics, as well as the loan decisions. Second, we leverage the Intercontinental Exchange (ICE) McDash dataset, which contains the servicing portfolios of the largest residential mortgage servicers in the US and covers approximately two-thirds of installment-type loans in the residential mortgage servicing market. Matching the approved loans in HMDA to their servicing records in ICE McDash allows us to track the performance of approved mortgages over time.

The fairness definitions we consider, and contrast, include: Statistical Parity, Predictive Parity, the Marginal Outcome Test, Equalized Odds and Equality of Opportunity, Conditional Statistical Parity and Representativeness (we formally define these in Section 3). Some of these definitions are straightforward to compute and have been studied extensively in the literature. Others are more complex and, to the best of our knowledge, have not been applied in this setting. For example, leveraging machine learning techniques, our paper introduces

a novel strategy to detect applicants that submit multiple applications (“cross-applicants”). We then use these cross-applicants to construct two of our measures of fairness. Our paper thus also makes progress on empirically evaluating definitions that have thus far primarily been considered in more theoretical papers. Our findings are consistent with existing theoretical results showing that satisfying all or even multiple definitions at once is generally impossible (Kleinberg et al. [2017], Chouldechova [2017]).

We argue that any single fairness definition comes with significant drawbacks, and, in Section 4, describe five stylized facts based on a combination of the six fairness measures above. While this allows us to highlight recent trends and geographic patterns in fairness and inequality in the US Mortgage market, we encourage the reader to further explore our results interactively through our online interactive appendix. This dashboard includes all of our fairness measures at the state-year level and will be updated annually. It is available at <https://mortgagefairness.github.io/>.

Before we proceed, we caveat two important limitations to our setup. First, we do not delve into other aspects of the decision process. There is evidence suggesting that minority applicants may receive less assistance during the process [Frame et al., 2021, Kim and Squires, 1995] and may even be discouraged from applying in the first place [Ladd, 1998, Yinger, 1991, Lubin, 2008, Ross et al., 2008]. We also do not study fairness with respect to pricing. For recent papers on discrimination in pricing in the context of mortgage applications, see Ambrose et al. [2021], Bhutta and Hizmo [2021], Bartlett et al. [2022], Willen and Zhang [2020]. Second, we restrict ourselves to measures of group fairness and do not consider notions of procedural [Grgić-Hlača et al., 2018], individual [Dwork et al., 2012], or compositional fairness [Dwork and Ilvento, 2019].

## 2 The Data

We draw our data from two high-quality administrative data sources:

1. **Home Mortgage Disclosure Act (HMDA).** This dataset contains data on mortgage applications. With few exceptions, all mortgage applications filed in the US are subject to HMDA reporting and thus included in this database.<sup>1</sup> HMDA data has been one of the primary datasets in the literature to study inequality in mortgage finance across protected classes (e.g. Munnell et al. [1996], Berkovec et al. [1998], Ross and Yinger [2002], Bayer et al. [2018], Bhutta et al. [2022] to mention but a few). In fact, “identifying possible discriminatory lending patterns” was one of the stated purposes of establishing HMDA in 1975<sup>2</sup>. Unusual for financial datasets, HMDA contains protected attributes of the applicants, such as an applicant’s race, ethnicity, and gender. While a publicly available version of this dataset exists, we work directly with a confi-

---

<sup>1</sup>Previous studies have estimated HMDA captures between 80 to 92 percent of mortgages across the US, with coverage being higher in metropolitan relative to non-metropolitan areas (Bhutta et al. [2017]).

<sup>2</sup>For more background, see <https://www.ffiec.gov/hmda/history.htm>

dential version that is available to users within the Federal Reserve System and includes more detailed information for each loan application (e.g. the exact date an application was filed, applicant and coapplicant age, credit score, automated underwriting system results, among others).

2. **Intercontinental Exchange McDash (McDash).** This dataset is comprised of the servicing portfolios of the largest residential mortgage servicers in the US, covering approximately two-thirds of loans in the residential mortgage servicing market. It allows us to track the performance of originated mortgages over time. In particular, it includes a monthly variable indicating loan delinquency status. McDash also includes a richer set of borrower and loan characteristics across a longer time span relative to HMDA, such as the credit score, and the loan-to-value ratio (LTV). On the other hand, McDash does not include a number of borrower characteristics available in HMDA, such as a borrower’s race and ethnicity, and by definition only includes approved (and originated) applications.

All tables and figures in this paper are based on authors’ calculations using these two datasets.

On its own, HMDA has some notable shortcomings. Since the dataset consists of mortgage applications, it does not include any information on the subsequent performance of the originated loans, such as whether a loan becomes delinquent. The set of observed features associated with an application also changes throughout the sample period in the HMDA dataset and a number of important borrower and loan characteristics, such as the credit score and the loan-to-value ratio (LTV) are only available starting in 2018.

Our second dataset, McDash, addresses some of these shortcomings. While we can compute some of our fairness measures using only the HMDA dataset (e.g. Statistical Parity), other fairness measures are infeasible to compute with HMDA alone because we need access to the subsequent performance of originated loans. We therefore match the loan applications in HMDA with the servicing records in McDash. Individual observations in HMDA and McDash are matched using origination date, loan amount, property ZIP code, lien type, loan purpose (e.g., purchase or refinance), loan type (e.g., conventional or FHA), and occupancy type (e.g., owner-occupied, absentee or investment property) using the same matching logic that is standard in the literature (e.g. Fuster et al. [2022]).

Overall, among McDash mortgages originated between 2004 and 2021, each year 61-80% of the servicing records are matched to at least one HMDA loan. We limit our analysis to loans that can be uniquely matched, meaning that each McDash loan is matched to just one HMDA loan and that each HMDA loan has only one McDash match candidate. Using this conservative sample reduces our match rate to between 47% and 67% depending on the year, although it tends to improve over time.

Throughout this paper we focus our attention on four major demographic groups. These are Asian applicants, Black applicants, Hispanic White applicants, and White non-Hispanic

applicants.<sup>3</sup> We denote the variable that encodes the four groups by  $G_i$ .

For the HMDA dataset, since alternate race and ethnicity categories are introduced in 2004 (in accordance with changes made to the U.S. Census), our analysis includes mortgage applications filed between 2004 and 2022 to avoid ambiguity in the definition of  $G_i$ . We further retain only first-lien mortgages and applications that are either approved or denied, dropping applications that are withdrawn by the applicant before a decision was made, applications closed for incompleteness, loan purchases, and applications that only went through the preapproval process. Finally we drop applications filed outside the 50 states and Washington D.C.

For the matched sample that links the loans in the HMDA sample above to their servicing records, we further restrict our analysis to mortgage applications filed until 2021. This allows us to observe the servicing record of each originated loan for at least two years using servicing records in McDash through 2023. Accordingly, we use two-year probabilities of delinquency throughout to ensure comparability of different vintages. Specifically, we consider a loan delinquent,  $D_i = 1$ , if its status is ever more than 90 days past due (i.e., three or more missed payments) within 24 months of origination.<sup>4</sup>

We further restrict the matched sample to loans with a term of 10, 15, 20, or 30 years, an LTV between 0% and 200%, a credit score between 500 and 820, DTI within 0% to 250%, income between 0 and \$1 million, and a loan amount up to \$1.5 million. These restrictions both reduce the amount of data errors and facilitate the estimation of our default model by restricting the heterogeneity of the matched sample.

We conclude the discussion of our data with a number of summary statistics. The HMDA data contains 403.8 million mortgage applications filed between 2004 and 2021. After filtering for first-lien mortgage applications that are either approved or denied in which the applicant identifies as Asian, Black, Hispanic white or white non-Hispanic, and imposing our geographic restriction, we retain about 207.3 million applications in our sample. For ease of notation, we will refer to these four groups simply as Asian, Black, Hispanic and white respectively. The full matched sample of originated mortgages and their subsequent servicing record contains 74.0 million loans originated between 2004 and 2020. After imposing our additional data filters, we end up with about 39.3 million loans.

Table 1 presents summary statistics for a subset of observable features. It includes the median loan amount, income, credit score, and LTV ratio, broken down by demographic group. We calculate these separately for our two datasets. Table 1 further includes the default probability of originated loans in the merged HMDA-McDash data. Perhaps unsurprisingly, we see that there are large differences across demographic groups. For example, White borrowers tend to have substantially higher income and credit scores compared to Black and Hispanic borrowers.

---

<sup>3</sup>Applicants are classified into mutually exclusive groups based on the first race and ethnicity reported.

<sup>4</sup>Note that this coincides with the default outcome targeted by the most widely used credit scoring models.

		Obs	Amount (1000s)	Income (1000s)	Credit Score	LTV	P(Default) (%)
Group	Dataset						
Total	HMDA	207,251,742	179	72	732	75	
	HMDA-McDash	39,315,215	193	79	747	79	2.9
Asian	HMDA	12,409,624	292	103	761	74	
	HMDA-McDash	2,452,690	283	105	765	75	1.8
Black	HMDA	18,594,961	152	57	678	80	
	HMDA-McDash	2,589,285	177	64	694	89	8.3
Hispanic	HMDA	19,133,364	190	64	708	80	
	HMDA-McDash	3,209,508	191	65	717	82	5.5
White	HMDA	157,113,793	174	74	739	75	
	HMDA-McDash	31,063,732	190	80	751	79	2.3

**Table 1:** Descriptive Statistics across demographic groups. Depicted across the columns is the median of loan amount, income, credit score, and LTV, as well as the empirical frequency of default. The HMDA sample contains mortgage applications filed 2004-2022, HMDA-McDash contains mortgages originated between 2004-2021. In HMDA, credit score and LTV are only available starting in 2018. The corresponding columns for both HMDA and HMDA-McDash are therefore based only on applications filed in 2018 and later.

### 3 Fairness Measures

To define the fairness measures, we first introduce some notation. An applicant  $i$  applies for a mortgage at a potential lender  $l$ . Applicants have a vector of features partitioned into  $Z_i$ ,  $\eta_i$ , and  $G_i$ , observed by the lender, and there is a joint distribution  $\mathcal{D}$  over which these features are drawn.  $G_i$  is a discrete variable indicating membership in a protected class (e.g. a binary indicator for applicant gender or a categorical variable for applicant race).  $Z_i$  and  $\eta_i$  are covariates that may be related to the default probability of individual  $i$ . An applicant may apply for a mortgage at multiple lenders, and we denote the number of applications applicant  $i$  submits by  $N_i$ .

The lender  $l$  decides whether to approve or deny an application submitted by an applicant  $i$ . Then,  $L_{il}$  is a binary indicator variable that takes a value of one if the application is approved and zero otherwise.  $D_{il} \in \{0, 1\}$  indicates whether a person defaults on his loan that was approved by lender  $l$ . Throughout, we maintain that  $E(D_{il}|Z_i, \eta_i, G_i, l) = E(D_{il}|Z_i, \eta_i, G_i)$ , implying that the default probability does not depend on  $l$  conditional on  $i$  and will thus simply write  $D_i$ . Note that  $D_i$  is only realized (and thus observed) when at least one application by applicant  $i$  is approved and originated.

The econometrician (or regulator) who wants to measure the fairness of the decision process observes  $Z_i$  and  $G_i$ , but not  $\eta_i$ . Thus,  $Z_i$  and  $G_i$  are visible to both the lender and to the regulator, while  $\eta_i$  is visible only to the lender.

We maintain the following Assumption, which states that the group membership  $G_i$  has no *direct* impact on an individual’s default probability.

**Assumption 1.**

$$E(D_i|Z_i, \eta_i) = E(D_i|Z_i, \eta_i, G_i) \quad (1)$$

However, since  $G_i$  may be correlated with both  $Z_i$  and  $\eta_i$ , we allow for differential default probabilities across groups, both unconditionally and conditional on the observed covariates  $Z_i$  (i.e. we do not assume that  $E(D_i|Z_i) = E(D_i|Z_i, G_i)$ ).

Furthermore, we denote the geographic state and time of a loan application by  $S_i$  and  $T_i$ , with realizations  $s$  and  $t$  respectively. We additionally denote by  $\mathcal{I}_{\mathcal{A}} := \{i : a_i \in \mathcal{A}\}$  the set of individuals  $i$  for which the condition  $a_i \in \mathcal{A}$  holds. For example,  $\mathcal{I}_{s,t,g}$  denotes the set of individuals  $i$  whose application is in state  $s$  during year  $t$  and of demographic group  $g$ . Finally, we define  $N_{s,t,g} = |\mathcal{I}_{s,t,g}|$ , which is the cardinality of the set  $\mathcal{I}_{s,t,g}$ .

We consider 6 classes of fairness definitions, which we will define more formally below:

1. Statistical Parity (difference in denial rates)
2. Predictive Parity (difference in default rates)
3. Marginal Outcome Test (difference in lending standards)
4. Equalized Odds (difference in denial rates for creditworthy borrowers)
5. Conditional Statistical Parity (conditional difference in denial rates)
6. Representativeness (amount of under-representation among approved)

As we explain below in more detail, these correspond to common notions of fairness frequently alluded to in either current regulations or public debate.

### 3.1 Statistical Parity

We begin with the notion of Statistical Parity (“SP”), which is arguably the most elementary notion of fairness. Statistical Parity requires that borrowers have equal approval (equivalently, denial) probabilities regardless of their group.

Thus, we say that Statistical Parity holds if  $P(L_i = 0|G_i = g) = P(L_i = 0|G_i = g')$  and define any violation of Statistical Parity,  $\delta_{SP}$  as the difference in denial rates between groups  $g$  and  $g'$ :

$$\delta_{SP}(g, g') := P(L_i = 0|G_i = g) - P(L_i = 0|G_i = g'). \quad (2)$$

Throughout,  $g'$  represents a “reference group”. Throughout the paper, this will always be non-Hispanic White applicants and all Fairness violations are defined such that larger numbers correspond to worse outcomes for minority applicants relative to non-Hispanic White applicants. In practice, we then simply replace the population quantities on the



right by their empirical counterpart.<sup>5</sup> Statistical Parity is easy to compute and captures an intuitive notion about inequality across groups. It also corresponds with language used in current federal regulations. The Uniform Guidelines for Employee Selection Procedures 1978 (also see Civil Rights Act of 1964 and the Equal Employment Opportunity Act 1972) state in §1607.4D:

“Adverse impact and the ‘four-fifths rule.’ A selection rate for any race, sex, or ethnic group which is less than four-fifths (4/5) (or eighty percent) of the rate for the group with the highest rate will generally be regarded by the Federal enforcement agencies as evidence of adverse impact.”

In 2015, in “Texas Department of Housing and Community Affairs v. Inclusive Communities Project, Inc.” the Supreme Court ruled that adverse impact claims are also cognizable under the Fair Housing Act (Civil Rights Act of 1968, Titles VIII-IX), extending the notion of disparate impact to housing cases.

Figure 2 illustrates the inequality in mortgage decisions between minority and White applicants for applications filed between 2004 and 2022. Figure 2a depicts violations of Statistical Parity, defined in (2), with respect to White applicants. Figure 2b depicts an alternative measure of Statistical Parity violations that uses the ratio of approvals rather than the difference in denials between minority and White borrowers, in line with the “four-fifths” rule we mention above. Both plots point to a large and persistent gap between denial rates for Black and White applicants. Focusing on the gap between Black and White applicants, we note that gap appears relatively stable until 2016, but then has improved over the last six years of our data. In fact, following the aforementioned Supreme Court ruling, the approval ratio has in recent years for the first time consistently been above 80%.

### 3.2 Predictive Parity

We now turn to Predictive Parity (“PP”). Instead of comparing the probability of loan approval across groups (cf. Figure 1a), Predictive Parity asks that the default rate be similar among approved borrowers regardless of their group (cf. Figure 1b).

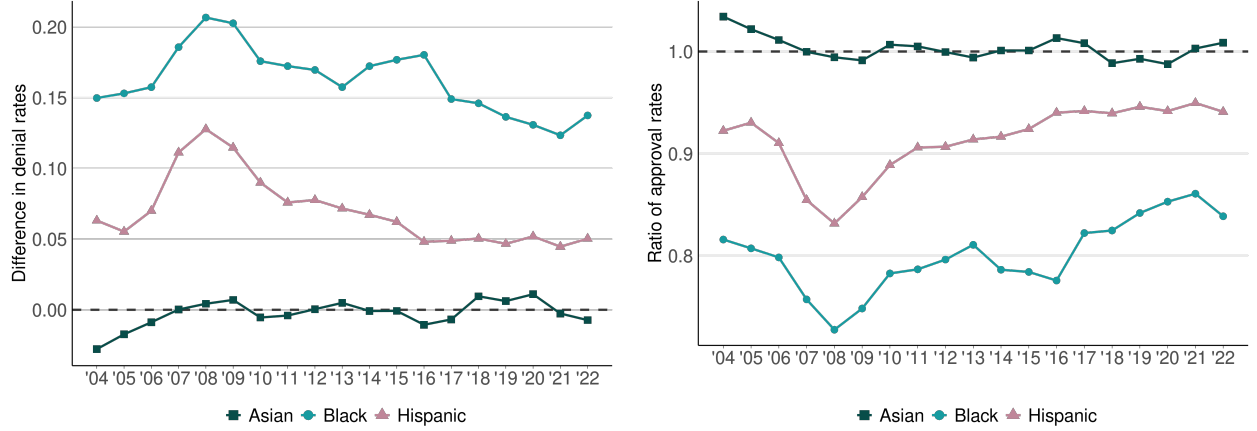
Thus, we say that Predictive Parity holds if  $P(D_i = 1|L_i = 1, G_i = g) = P(D_i = 1|L_i =$

---

<sup>5</sup>We sometimes construct our measures of fairness on a subset of the data, based on a set of discrete variables, for example the year and state of an application. The violation of Statistical Parity for a state-year combination  $s, t$  is then computed as:

$$\delta_{\text{SP}_{s,t}}(g, g') := \frac{1}{N_{s,t,g}} \sum_{i \in \mathcal{I}_{s,t,g}} \mathbf{1}[L_i = 0] - \frac{1}{N_{s,t,g'}} \sum_{i \in \mathcal{I}_{s,t,g'}} \mathbf{1}[L_i = 0]$$

To simplify notation, we will omit the corresponding subscripts to denote a subset of the data in the remainder of the paper when it is clear from context. For example, any regression-based measures at the state-year level will be based on a separate regression for each state-year combination.



(a) Difference in denial rates between minority applicants and White applicants.

(b) Ratio of approval rates relative to White applicants.

**Figure 2:** Figure based on mortgage applications filed in the US between 2004 and 2022.

1,  $G_i = g'$ ) and define violation of Predictive Parity,  $\delta_{PP}$  as the difference in default rates between groups  $g$  and  $g'$ :

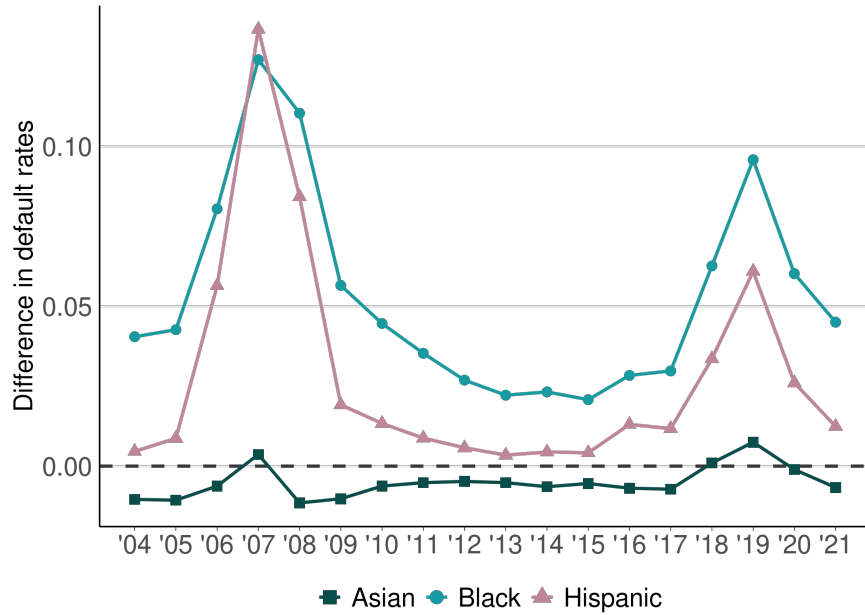
$$\delta_{PP}(g, g') := P(D_i = 1 | L_{il} = 1, G_i = g) - P(D_i = 1 | L_{il} = 1, G_i = g'). \quad (3)$$

Figure 3 illustrates the inequality in default rates between minority and White applicants for applications filed between 2004 and 2021. We note a persistent inequality in default rates across demographic groups. For example, Figure 3 shows that the default rate for Black borrowers is 3-12 percentage points higher than that of White borrowers during our sample period.

Figure 3 further highlights a substantial increase in the *differences* in default rates between demographic groups during the 2007/2008 Financial Crisis and the 2020 COVID-19 Pandemic: Minority homebuyers suffered disproportionately from these crises (also see Bayer et al. [2016]).

Predictive Parity is again easy to compute and captures a meaningful notion of inequality across groups. For example, the fact that Black borrowers default at substantially higher rates reflects the systematically worse financial outcomes Black Americans face, and may further compound existing economic and financial disparities. However, we note that different default rates among approved applicants are not necessarily suggestive of different lending standards.

This is because, as Simoiu et al. [2017] notes, such outcome-based tests suffer from the problem of “infra-marginality”—in other words, even without discrimination, default rates may differ between groups if they have different underlying risk distributions (also see Yinger [1996], Ross [1997]).



**Figure 3:** Difference in default rates between minority borrowers and White borrowers. Figure based on mortgage originations between 2004 and 2021.

We thus look directly at candidates “on the margin” next.

### 3.3 Marginal Outcome Test

One intuitive notion of fairness widely used in economics and current law requires that the same credit standards are applied across protected classes. In order to assess whether this is indeed the case, much of the economics literature, going back to the classic theory of Becker [1957], has focused on marginal candidates, both in lending decisions and other contexts (see, e.g., Anwar and Fang [2015] Arnold et al. [2018] in the context of the criminal justice system; Dobbie et al. [2021] in consumer lending; Berkovec et al. [1998] in mortgage lending). The idea is that, if the same threshold on creditworthiness is used for Black and White applicants, people at this threshold (or “on the margin”) should default at the same rate. We call this the “Marginal Outcome Test” (“MOT”).

This focus on marginal applications and/or applicants is also reflected in the Interagency Fair Lending Examination Procedures<sup>6</sup>, for example:

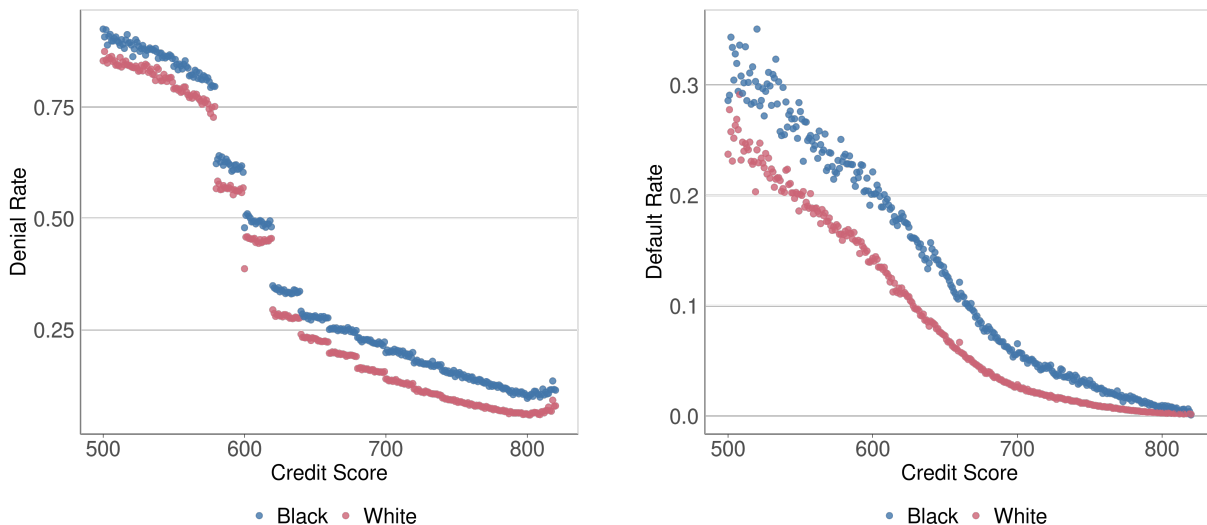
“The examiner-in-charge should, during the following steps, judgmentally select from the initial sample only those denied and approved applications which constitute marginal transactions.”

Empirically, the key step to a fairness measure based on the Marginal Outcome Test is thus

<sup>6</sup>These are publicly available online at <https://www.ffiec.gov/pdf/fairlend.pdf>.

to identify a set of marginal candidates: candidates who were just barely offered a loan. However, obtaining marginal candidates or transactions is often difficult, as evident by the fact that examiners are instructed to “judgmentally” select them in the guidelines above.

One approach to identifying marginal candidates is via observables. Figure 4 illustrates how this approach could work with a single observable, in this case the credit score of an applicant. The left panel plots the denial rate for Black and White applicants at each credit score. Consistent with credit score being a major determinative factor of lending decisions, we observe a strong relationship between credit score and the denial rate. We see major



(a) Denial rate across groups based on applications filed in 2018-2021. (b) Default rate across groups based on applications filed in 2004-2021.

**Figure 4:** Denial and default rates as a function of credit scores for mortgage applications.

discontinuities at 570, 590, and 610 (This is in line with the findings in Bubb and Kaufman 2014). In particular, denial rates discretely decrease to around 50% at 590, and then jump further down at 610, suggesting “marginal” candidates might be those in the 590-610 range. Recall that the Marginal Outcome Test is satisfied if Black and White borrowers on the margin default at the same rate. In contrast, the right panel of Figure 4 shows that the default rate for Black applicants inside this marginal credit score range is higher than the default rate of White applicants in the same range. Taken in isolation, this could be seen as evidence of a violation of the Marginal Outcome Test.

But from another lens, Figure 4b merely indicates that credit score by itself is not a well-calibrated default model in this context: Black and White applicants with the same credit score are associated with different default risks (cf. Kermani and Wong 2021). This suggests that additional variables are needed to determine creditworthiness. In Appendix B, we show a strikingly similar pattern even for more sophisticated default models. Training a Machine

Learning model<sup>7</sup> to predict default on a large set of observable features (not including race), we obtain a similar degree of miscalibration, again systematically underestimating the default risk of Black applicants. Such miscalibration of the underlying default risk model reflects an inherent concern with any approach that uses estimated creditworthiness to identify marginal candidates. That is, identifying marginal candidates based on this type of approach is imprecise at best.

Therefore, we propose an alternative way to construct marginal applicants by identifying candidates who apply for multiple mortgages. An applicant is then marginal if she submits two (near) identical applications, and receives one approval and one denial. We consider such an applicant marginal by “revealed preference”: The fact that one loan officer approved the loan application, while another loan officer rejected the same application, reveals that the corresponding applicant is on the threshold between acceptance and denial.

While we describe the algorithm we use to identify our marginal candidates in more detail in a companion paper, we briefly outline the main idea here. The HMDA dataset is at the application level and does not include a person identifier. Therefore, we first need to identify pairs of applications that correspond to applicants who submit multiple (near-identical) applications, which we refer to as cross-applicants. In order to do so, we apply a state-of-the-art agglomerative hierarchical clustering algorithm to find clusters (usually pairs) of applications that are near-identical. We then use the rate at which clusters contain multiple originations to both fine-tune our algorithm and to estimate the frequency with which our clusters correctly correspond to single individuals. The idea is the following: if all clusters are pairs of applications from two applicants, most clusters with two approvals would have two originations. On the other hand, if all clusters are pairs of applications from one applicant, no clusters with two approvals can have two originations, since it is impossible to take out two first-lien loans on the same property. Using this logic, we estimate that 92% of our estimated cross-applicants indeed represent single individuals. (see Elzayn et al. [2023] for more detail).

We can then select from these (estimated) individuals that submitted two near-identical applications those who received one approval and one denial, and calculate any violations of our Marginal Outcome Test in our dataset as follows:

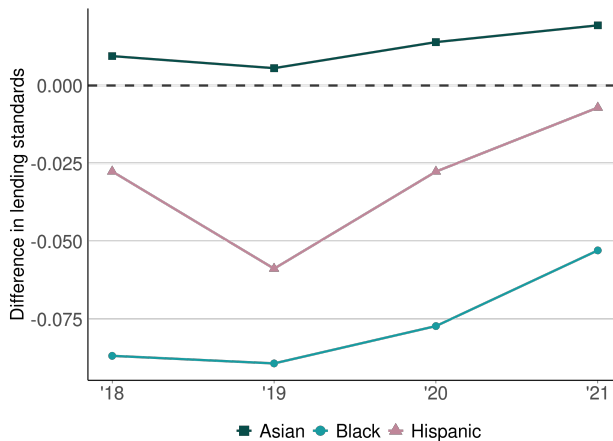
$$\delta_{MOT}(g, g') := P(D_i = 1 | i \in \mathcal{M}_{g'}) - P(D_i = 1 | i \in \mathcal{M}_g), \quad (4)$$

where  $\mathcal{M}_g$  denotes the set of applicants (clusters) in group  $g$  that submitted multiple applications and experienced both an approval and a denial. Note that  $\delta_{MOT}(g, g') > 0$  if the default rate of minority applicants is *lower* than that of White applicants. This is because lower default rates at the margin for members of group  $g$  imply higher lending standards for this group.

---

<sup>7</sup>In particular, we use a histogram-based gradient-boosted classification tree (HGBC) to capture the rich nonlinear relationships between observable features such as credit score, loan-to-value ratio, applicant income, loan type, among others and default. See Appendix B for more detail.

Figure 5 depicts the implied difference in lending standards between minority marginal applicants and White marginal applicants based on (4). We find that marginal Black and Hispanic applicants default more frequently. This is not consistent with higher lending standards for Black applicants. In fact, since higher default rates for minority applicants imply slightly *lower* lending standard for minority applicants, our fairness violation is “negative” for Black and Hispanic borrowers, following our definition in (4).



**Figure 5:** Difference in default rates between minority and White marginal borrowers.

There are multiple possible explanations for why the default rates of Black marginal applicants are higher than those of White marginal applicants. One possibility for this pattern is that there are indeed some differences in lending standards, possibly due to industry efforts or existing public programs aimed at approving more minority borrowers and to reduce inequality. Alternatively, this pattern may also arise as the result of miscalibrated default models. As we discussed above we find that default models that do not explicitly take into account the race of an applicant, tend to underestimate the default risk of Black applicants. If lenders based their underwriting decisions on such a miscalibrated model, marginal Black applicants would tend to be riskier than White applicants.

### 3.4 Equalized Odds

While the Interagency Fair Lending Examination Procedures explicitly invoke *marginal applicants* to measure fairness (see our discussion in the previous section), the Equal Credit Opportunity Act instead explicitly invokes *creditworthy applicants*. In particular, the Equal Credit Opportunity Act states in Regulation B, 12 CFR § 1002.1(b):

“The purpose of this part is to promote the availability of credit to all creditworthy applicants without regard to race, color, religion, [...]”

Defining a “creditworthy applicant” ex post as a borrower that did not default (also see

Meursault et al. [2022]), this allows the construction of the following two measures of fairness.

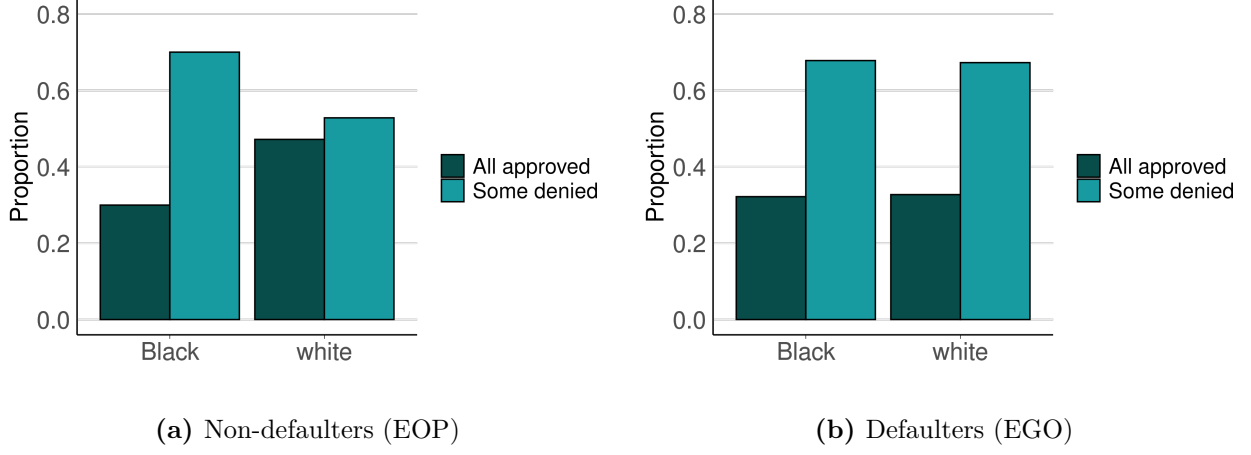
1. Equality of Opportunity (“EOP”): Consider cross-applicants with an originated loan that did not default. We can ask the question: How likely was such a “creditworthy applicant” denied at least once at the time of application? Intuitively this captures the notion of being *unfairly denied*, since the borrower repaid her loan. We can then ask whether the rate of these *unfair denials* varies by group membership.
2. Equality of Goodwill (“EGO”): Consider cross-applicants with an originated loan that defaulted. We can ask the question: How likely was such an “uncreditworthy applicant” to be approved across all her applications? Intuitively this captures the notion of being *unfairly approved*, since the borrower did not repay her loan. We can then ask whether the rate of these *unfair approvals* varies by group membership.

These two measures (Equality of Opportunity; Equality of Goodwill) are often combined into the term “Equalized Odds”(e.g. Hardt et al. [2016]). Both capture the idea of equal treatment to groups of individuals based on their “true type”: defaulters and non-defaulters.<sup>8</sup> In particular, Equality of Opportunity holds if the denial rates are identical for Black and White borrowers who do not default. Equality of Goodwill holds if the approval rates are identical for Black and White borrowers who default.

Unfortunately, computing Equality of Opportunity and Equality of Goodwill for all applicants is infeasible. This is due to the standard selective labels issue (e.g. Lakkaraju et al. [2017]): we only know whether the applicant defaulted if the loan is extended to (and originated by) the applicant. We can thus only calculate the two measures for cross-applicants who apply for multiple mortgages and are approved at least once. We therefore compute violations of Equality of Opportunity and Equality of Goodwill in our dataset using the estimated cross-applicants we obtained using our agglomerative hierarchical clustering algorithm explained in the previous section (and derived in more detail in Elzayn et al. [2023]). Specifically, we base our measure on applicants who i) applied to multiple mortgages ( $N_i \geq 2$ ); ii) had at least one of their applications is approved ( $\sum_l L_{il} \geq 1$ ); and iii) originated at least

---

<sup>8</sup>Also see Angwin et al. [2016] for an application of this fairness measure in a criminal justice context, where algorithms are widely used to rate a defendant’s risk of future crime. Angwin et al. [2016] find that, among defendants that re-offended, risk scores for White defendants are substantially lower than those of Black defendants, and therefore conclude that the algorithm is thus racially biased.



**Figure 6:** Distribution of unfair denials (a) and unfair approvals (b) across demographic groups.

one of their approved loans ( $O_i = 1$ ):

$$\delta_{EOP}(g, g') = P \left( \sum_l (1 - L_{il}) \geq 1 | N_i \geq 2, O_i = 1, D_i = 0, G_i = g \right) - P \left( \sum_l (1 - L_{il}) \geq 1 | N_i \geq 2, O_i = 1, D_i = 0, G_i = g' \right), \quad (5)$$

$$\delta_{EGO}(g, g') = P \left( \sum_l L_{il} = N_i | N_i \geq 2, O_i = 1, D_i = 1, G_i = g \right) - P \left( \sum_l L_{il} = N_i | N_i \geq 2, O_i = 1, D_i = 1, G_i = g' \right). \quad (6)$$

Thus, we say that Equality of Opportunity, defined by  $\delta_{EOP}(g, g') = 0$ , holds in our data if the frequency with which at least one application was denied for cross-applicants that 1) have at least one application originated and 2) did not default, is equal for members of group  $g$  and  $g'$ . We say that Equality of Goodwill, defined by  $\delta_{EGO}(g, g') = 0$ , holds in our data if the frequency with which all applications were approved for cross-applicants that 1) have at least one application originated and 2) defaulted, is equal for members of group  $g$  and  $g'$ .

Figure 6a depicts the frequency of unfair denials for cross-applicants that did not default on their mortgage. We see that, among these creditworthy cross-applicants, around half of White applicants had all of their applications approved, while the other half of White applicants experienced an unfair denial. On the other hand, more than two-thirds of Black creditworthy cross-applicants experienced an unfair denial. Figure 6b depicts the frequency of unfair approvals for cross-applicants that defaulted on their mortgage. We see that,



among cross-applicants that default on their loan, White and Black applicants are equally likely to have all of their applications approved: Around one-third of cross-applicants from each demographic group are unfairly approved at least once.

From our analysis, we find that Equality of Opportunity (5) is violated by around 17.4%, as determined by the difference in likelihood of receiving at least one denial for Black and White cross-applicants who did not default. On the other hand, since the likelihood of having all applications approved is close to equal between Black and White cross-applicants that defaulted, Equality of Goodwill is (approximately) satisfied in our data. Remarkably, Black non-defaulters are rejected at least once at effectively the same rate as Black defaulters.

### 3.5 Conditional Statistical Parity

As mentioned above, conditioning on the true outcome (default/non-default) requires both multiple applications and an approved loan, limiting the sample for which we can compute the previous measures. To sidestep these difficulties, we next turn to Conditional Statistical Parity. Instead of conditioning on the true outcome, this involves conditioning on other features of the applicant or application.

Formally, we define violations of Conditional Statistical Parity (“CSP”) for a given  $y$  as

$$\delta_{CSP}(g, g', y) := P(L_{il} = 0 | Y_i = y, G_i = g) - P(L_{il} = 0 | Y_i = y, G_i = g'), \quad (7)$$

where  $Y_i$  denotes a subset of features in  $(Z_i \cup \eta_i)$ .<sup>9</sup> This can then be translated into a scalar value by, for example, aggregating over the distribution of  $Y_i$ .

Intuitively, Conditional Statistical Parity states that a decision maker’s decision is “race-blind” after taking into account all other relevant characteristics collected in  $Y_i$ : the denial rates are identical for Black and White borrowers with the same characteristics. Several papers on measuring discrimination in the US mortgage market are based on variations of Conditional Statistical Parity (for example, Avery et al. [1997], Black et al. [2001], Bhutta et al. [2022], and Hurtado and Sakong [forthcoming]).

But Conditional Statistical Parity also involves a number of issues that make this definition challenging in practice. The first obstacle to implementing Conditional Statistical Parity as a practical notion is to define the right conditioning set  $Y_i$ . Clearly, different choices of  $Y_i$  will lead to different measures of Conditional Statistical Parity. In our experience, the “correct” choice of  $Y_i$  is often far from obvious; a too narrow choice of  $Y_i$  can omit economically relevant dimensions of the decision, while too wide a choice can mask discrimination.<sup>10</sup>

<sup>9</sup>Note that one can think of EGO/EOP as (an infeasible version of) CSP if  $D_i = Y_i$ .

<sup>10</sup>For instance, a lender could include a proxy that is irrelevant for the default probability of an applicant, yet correlates with race. Including this proxy in the conditioning set would result in no CSP violation. See e.g. Prince and Schwarcz [2019] for a comprehensive discussion of proxy discrimination. To give a specific example, the CFPB Examination Procedures ([https://files.consumerfinance.gov/f/201306\\_cfpb\\_laws-and-regulations\\_ecoa-combined-june-2013.pdf](https://files.consumerfinance.gov/f/201306_cfpb_laws-and-regulations_ecoa-combined-june-2013.pdf)) explicitly caution against using underwriting models that use ZIP codes, postulating a negative disparate impact on protected classes.

Conditional Statistical Parity is also frequently used in legal settings. How any violations are interpreted depends on the choice of the conditioning set  $Y_i$ . For example, as [Ayres, 2010] argues “Disparate treatment tests [...] control for any and all variables that plausibly had a causal impact on a defendant’s decision making.” On the other hand, “disparate impact tests should only include controls for attributes that are plausibly business justified” [Ayres, 2010].

We therefore present results for a variety of conditioning sets  $Y_i$ <sup>11</sup>:

1.  $Y_i = \emptyset$  (“Unconditional”)
2.  $Y_i = \{Z_i^{small}\}$  (“few covariates”)
3.  $Y_i = \{Z_i\}$  (“many covariates”)
4.  $Y_i = \{AUS_i, Z_i\}$  (“including AUS”)

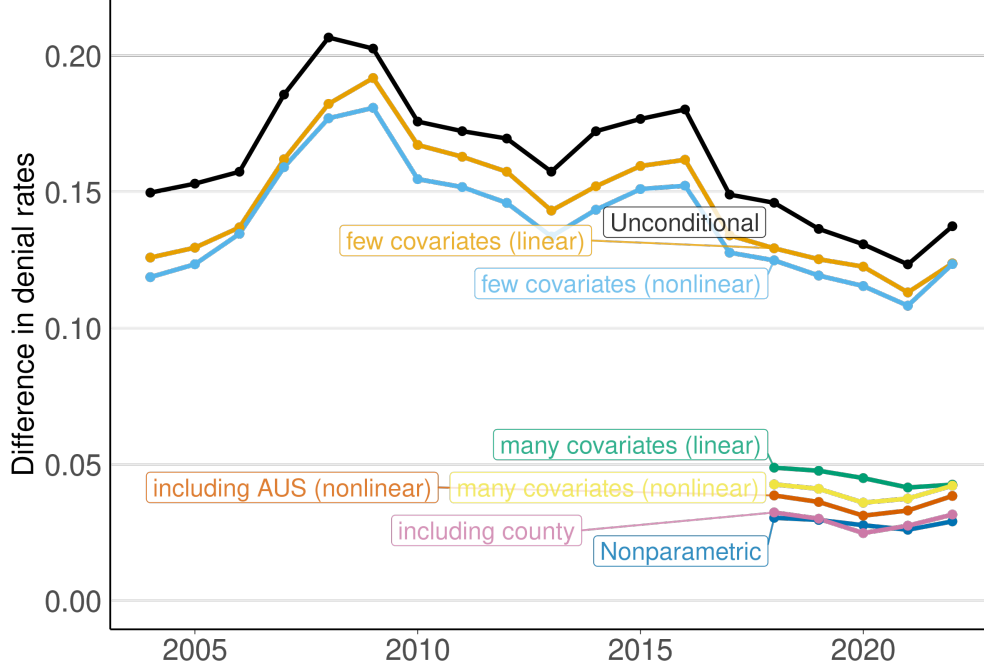
where  $Z_i^{small} \subset Z_i$  includes loan purpose, loan amount, applicant income, and an indicator for co-applicant, and  $Z_i$  additionally includes the applicant’s credit score, loan term, debt-to-income, and loan-to-value (which are only available in HMDA starting in 2018).  $AUS_i$  denotes the recommendation from an Automated Underwriting System (AUS), typically provided by one of the government-sponsored enterprises (GSEs). The AUS provides a recommendation to underwriters based on a statistical default model.<sup>12</sup>

Further, while Conditional Statistical Parity may be easy to calculate for a regulator in simple models, it can become increasingly difficult under more sophisticated models: If the lender’s decision rule is known to be linear in the elements of  $Y_i$ , and if  $Y_i$  is observed by the regulator, it simply states that the coefficient on  $G_i$  is equal to zero in a multivariate regression of  $L_{il}$  on  $Y_i$  and  $G_i$ . On the other hand, if models are highly non-linear through machine learning algorithms and may access rich feature sets, testing Conditional Statistical Parity becomes challenging. This is exacerbated by the fact that more sophisticated models will be better at triangulating the protected class of an applicant. Intuitively, more flexible models are better able to proxy for the relationship between  $G_i$  and the default probability of an applicant using nonlinear functions of the variables in  $Y_i$  (also see Prince and Schwarcz [2019] and Fuster et al. [2022]).

Figure 7 depicts the difference in denial rates between Black and white applicants after conditioning on the aforementioned conditioning sets. Each line corresponds to a different specification in terms of both which covariates are included and how flexible a model we allow. We first define our measure of Conditional Statistical Parity maintaining additive separability

<sup>11</sup>Also see Bohren et al. [2022] for a discussion on what makes a “good” covariate in the context of measuring discrimination.

<sup>12</sup>The most commonly used AUS in our dataset is Fannie Mae’s Desktop Underwriter. While the statistical model used in the Desktop Underwriter is unknown to us, Fannie Mae publishes a list of risk factors it considers in its AUS (Fannie Mae [2023]). These include both credit report variables, such as an applicant’s credit history, as well as non-credit risk factors, such as an applicant’s liquid reserves and housing expense ratio. Also see Bhutta et al. [2022] for a more detailed description of Automated Underwriting Systems.



**Figure 7:** Conditional Statistical Parity over time for various implementations

in  $G_i$  and  $Y_i$  for  $P(L_i|G_i, Y_i)$ . That is, we base these measures of Conditional Statistical Parity on estimates that take the form  $P(L_i|G_i, Y_i) = f(G_i) + h(Y_i)$ . While restrictive, this reduces our measure of Conditional Statistical Parity for group  $g$  to a single number which allows for convenient visualization and interpretation of our results. In particular, our first two measures of Statistical Parity (with respect to reference group  $g'$ ),  $\delta_{CSP}(g, g', y)$  are equal to  $\beta_g$  estimated from the the following regression model:

$$(1 - L_i) = \beta_0 + \sum_{g \in \mathcal{G} \setminus g'} \beta_g \mathbf{1}[G_i = g] + h(Y_i).$$

Our first version (“linear”) imposes linearity on the variables in  $Y_i$  (i.e.  $(h(Y_i) = \sum_j \alpha_j \iota_{ij})$  for  $\iota_{ij} \in Y_i$ ), and is thus based on a simple linear regression of  $L_i$  on a group dummy and the variables in  $Y_i$ . Our second version (“nonlinear”) creates 20 bins with roughly the same number of observations for each variable in  $Y_i$  and controls for dummies indicating membership in each of those bins.

Further, we add two additional specifications. First, we add the county of the property to the conditioning set of our largest nonlinear model (“including county”). While this suggests an even smaller difference between Black and White applicants, we may be concerned

that including location fixed effects induces included-variable bias (Ayres [2010], Jung et al. [2018]). In fact, denying an applicant a loan for housing based on a certain neighborhood is, in general, considered *redlining* and illegal.<sup>13</sup>

Second, since additive separability in  $G$  and  $Y_i$  for  $P(L_i = 0|G_i, Y_i)$  may be overly restrictive, we also consider the following fully nonparametric specification. First, we use Machine Learning to estimate the conditional expectation function  $E(L_i = 0|Y_i, G_i) = g(Y_i, G_i)$ .<sup>14</sup> This attempts to capture the underlying relationship between application outcomes and applicant features, *including race*. Then, we can define the individual effect  $b_i \equiv g(Y_i, 1) - g(Y_i, 0)$  to capture the individual-specific impact of being a minority applicant on the denial probability. In other words, it captures the change in probability of denial for applicant  $i$  if she belonged to a different group. Once we have the individual specific coefficients  $b_i$ , we average them across the entire population to yield a nonparametric estimate of  $\beta_g$  (“nonparametric”).

While all measures point to a disproportionate rate of denials for Black applicants, the difference in denial rate between Black and White applicants tends to decline as we increase the size of the conditioning set  $Y_i$ . Similarly, more flexible functional forms tend to reduce the size of our estimate, with our nonparametric specification suggesting the smallest deviation from Conditional Statistical Parity between White and Black applicants.

We conclude that the choice of both the conditioning set and the functional form assumptions are extremely important and can lead to vastly different results when calculating violations of Conditional Statistical Parity (in our case the measures based on alternative specifications differ by a factor of more than six). While we find that all of our specifications maintain a racial gap in denial rates, this gap becomes smaller for increasingly rich conditioning sets. On the one hand, this could be consistent with a “race-blind” decision maker that has access to additional attributes in  $\eta_i$  that are correlated with group membership (e.g. following similar arguments as in Altonji et al. [2005] and Oster [2019]). On the other hand, richer conditioning sets may be more likely to include covariates that are themselves racially biased, illegal to use, decision-irrelevant proxies, or otherwise inappropriate controls. Thus, the significance of the declining gap is not clear. Taken together, our estimates of Conditional Statistical Parity are suggestive of some disparity but their range make it difficult to assess magnitude and economic significance. Regardless, the large degree of sensitivity of this measure to its particulars is a clear weakness of this approach.

<sup>13</sup>However, a bank may under certain conditions consider such economic factors as the condition, use, or design of nearby properties, the availability of neighborhood amenities or city services, and the need of the lender to hold a balanced real estate loan portfolio, with a reasonable distribution of loans among various neighborhoods (see the Federal Fair Lending Regulations and Statutes available at [https://www.federalreserve.gov/boarddocs/supmanual/cch/fair\\_lend\\_fhact.pdf](https://www.federalreserve.gov/boarddocs/supmanual/cch/fair_lend_fhact.pdf)).

<sup>14</sup>Specifically, we use a similar model to the default model introduced in Appendix B. We again train a monotonically constrained HGBC model using HMDA data to predict denial with similar covariates to those used to estimate the default model. These are the state of the property for which the application is filed, the loan purpose, applicant income, DTI, LTV, credit score, loan amount, whether a coapplicant is present on the application, the loan term in months, and an indicator for whether an applicant is Black.

### 3.6 Representativeness

Finally, we consider a notion of fairness called Representativeness (“RP”, Ross and Yinger [2002]). Intuitively, it corresponds to the idea that the population of approved candidates should be “representative” of the creditworthy candidates. Conceptually, a decision process would be representative if:

$$P(G_i = g | L_i = 1) = P(G_i = g | E[D_i = 1 | Z_i, \eta_i] < c), \quad (8)$$

In practice, since  $\eta$  is unobserved, it is of course infeasible to compute the right-hand-side term in (8). We thus replace  $E[D_i = 1 | Z_i, \eta_i] < c$  with a feasible counterpart,  $E[D_i | \mathcal{I}_i] < c$ , and implement our measure of Representativeness as follows.

First, we rank all applicants according to their default risk,  $E[D_i | Y_i]$ .<sup>15</sup> Denote by  $n_a$  the number of approved loans in the data. We then compare the group composition of the  $n_a$  applicants with the lowest estimated default risk to the group composition of the approved applicants. This means we calculate any deviations from Representativeness as

$$\delta_{RP}(g) := P(G_i = g | E[D_i | Y_i] < \hat{c}) - P(G_i = g | L_i = 1), \quad (9)$$

where  $Y_i$  denotes a conditioning set in the estimation of default risk and  $\hat{c}$  is defined as

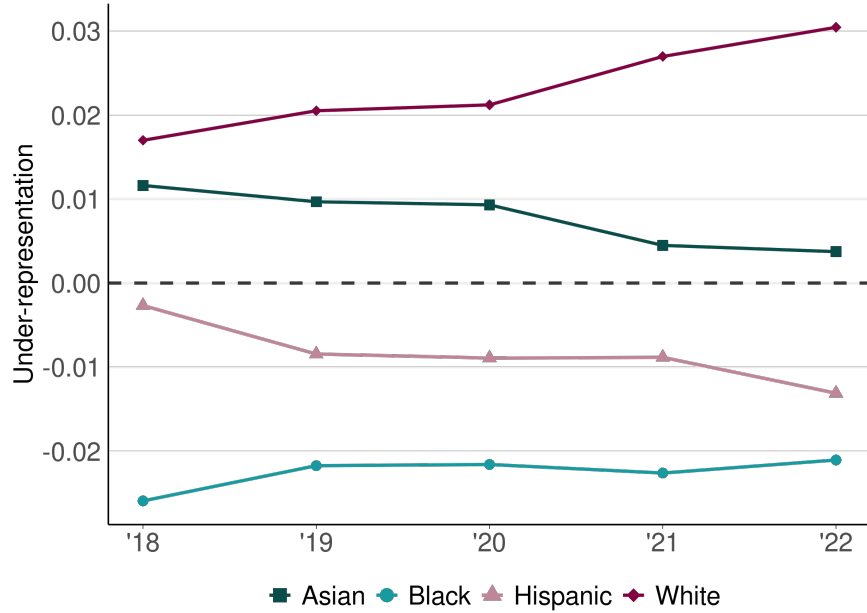
$$\hat{c} = \min c \quad \text{such that} \quad \sum_i 1[E[D_i | Y_i] \leq c] \geq \sum_i 1[L_i = 1] \equiv n_a.$$

Representativeness has the following intuitive interpretation. If  $\delta_{RP}(g) > 0$  for  $G_i = g$ , this means that individuals in group  $g$  are accepted less frequently in the data than they “deserve based on their merit” (i.e., riskier individuals from one group are accepted at the expense of less risky applicants from another group). Thus, a positive value indicates that group  $g$  is *under-represented* among approved borrowers, while a negative value indicates over-representation of group  $g$ .

We note that the choice of the conditioning set  $Y_i$  is again crucial. We start by following Ross and Yinger [2002] and use  $Y_i = \{Z_i, G_i\}$ , in which case  $E[D_i | Z_i, G_i]$  becomes the expected default probability conditional on all observed variables, *including group membership*  $G$ . Figure 8 depicts our measure of Representativeness for the four demographic groups using mortgage applications submitted across the United States between 2018 and 2022. We observe persistent differences in Representativeness across groups. In particular, this measure suggests that minorities (in particular Black applicants) are slightly over-represented among approved applicants relative to their model-implied riskiness.

---

<sup>15</sup>To construct  $E[D_i | Y_i]$  in practice, we estimate default probabilities of applications submitted in year  $t$  from an HGBC model trained on data from year  $t - 3$ . This training data is comprised of mortgages originated in year  $t - 3$  along with the subsequent two years of loan performance in which we count defaults. The covariates include credit score, LTV, DTI, original loan amount, loan type (conventional, VA, etc.), an indicator for whether a coapplicant is present, the state of the property’s location, and loan term in months, among others. See Appendix B for the full specification and more details.



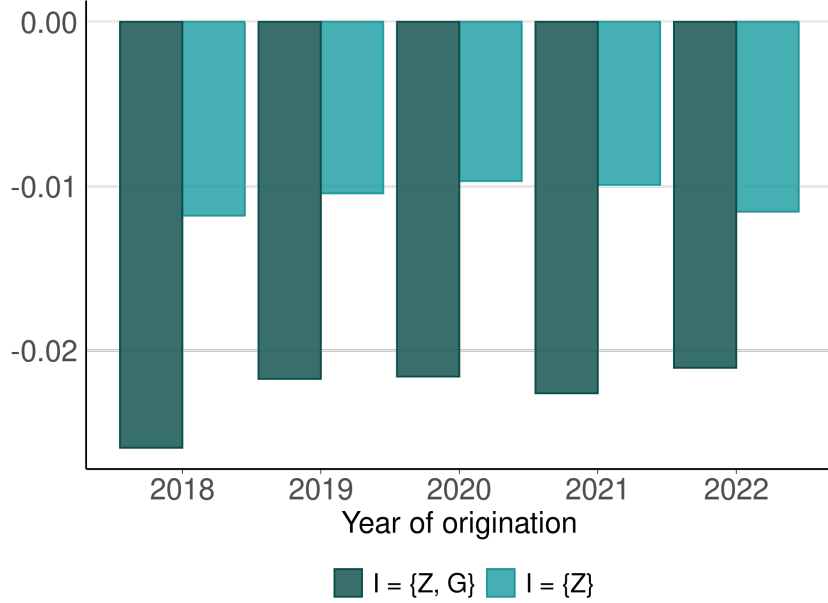
**Figure 8:** Representativeness for mortgages originated in 2018-2022.

This is again suggestive that approved Black borrowers on the margin are slightly riskier than approved White borrowers on the margin, consistent with our finding based on the Marginal Outcome Test. In Figure 9 we illustrate our measure of Representativeness for Black applicants with and without including  $G_i$  in  $Y_i$ . Dropping  $G_i$ , the difference between the actual approval rate and a hypothetical approval rate based on  $E[D_i|Y_i]$  becomes smaller. This suggests that being Black is associated with a higher default probability in the default model that includes  $G_i$ . In other words, a default model that does not have access to group membership will result in lower predicted default probabilities for minority applicants. In turn, this implies that Black borrowers are less overrepresented when using  $Y_i = \{Z_i\}$ . Note that, since in both specifications we find that Black applicants are overrepresented, our fairness violation is “negative” using this definition.

## 4 Stylized Facts

We next summarize and combine the six measures we introduced in the previous section to describe five stylized facts that highlight recent trends and geographic patterns in fairness and inequality in the US mortgage market.

**Stylized Fact 1: Broad measures suggest stark systemic inequality.** We find strong evidence of systematically worse outcomes for Black Americans. Black applicants are denied at a significantly higher rate, restricting their access to home ownership and thus wealth accumulation. At the same time, Black borrowers default at higher rates, thus disproporti-



**Figure 9:** Representativeness for Black applicants, with/without  $G_i$  in  $\mathcal{I}_i$ .

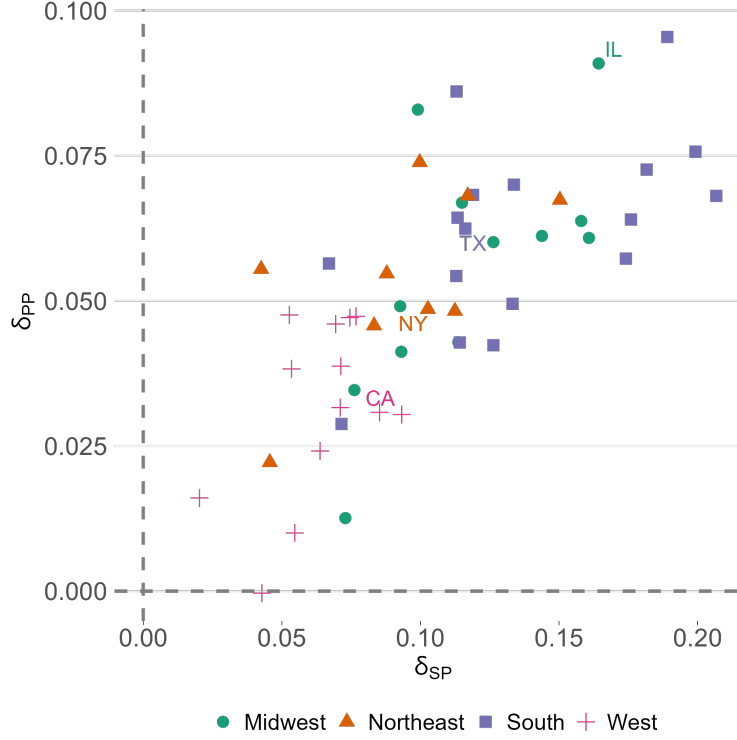
nally bearing the associated costs (for a discussion of the cost of bankruptcy, see Argyle et al. [2023]). This paints a picture of a society with large racial disparities in financial well-being and economic opportunity.

This holds true across the United States. Figure 10 presents the violations of Statistical Parity and Predictive Parity between Black and White Americans across states. Each state corresponds to one of the 51 observations depicted (50 states plus DC). We have also labeled the most populous state in each of the four census regions. The dashed lines correspond to equal outcomes in both dimensions. It is evident that Black applicants in all states face higher denial rates than White applicants. Similarly, Black borrowers have higher default rates in all states. Furthermore, there is a pronounced positive correlation across states between racial gaps in denial rates and default rates.

While this paints a stark picture of inequality in the mortgage sector, which may perpetuate existing inequalities in wealth and economic well-being, these differences are not necessarily reflective of explicit discrimination in the mortgage sector. They may also reflect existing systemic and historical inequalities in the United States between Black and White Americans.

**Stylized Fact 2: Decision-driven fairness measures provide mixed evidence.** More narrow definitions of fairness that try to isolate the decision of the loan officer on mortgage applications yield a nuanced picture. We illustrate this at the state-level in Figure 11.

First, to isolate the decision of the loan officer, we compare default rates at the decision boundary by restricting to a sample of marginal borrowers. We find that marginal Black



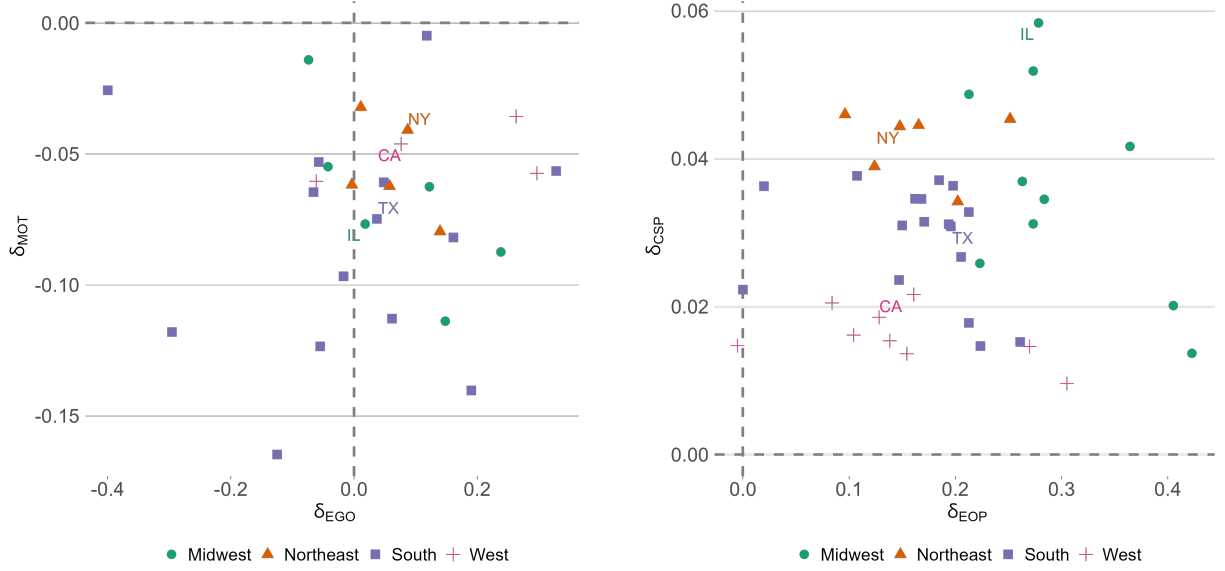
**Figure 10:** Fairness violations at the state level as measured by Statistical Parity ( $\delta_{SP}$ ) and Predictive Parity ( $\delta_{PP}$ ) based on applications filed in 2018-2021.

borrowers are more likely to default than marginal White borrowers. Since the higher default rate for minority applicants implies a slightly *lower* lending standard for minority applicants, our fairness violation based on the Marginal Outcome Test is negative for Black borrowers in almost all states. This is reflected by the fact that all but one state in Figure 11a are below the dashed line indicating equality. We note that this is further in line with our results for Representativeness (cf. Section 3.6), which suggest that minority applicants are slightly *overrepresented* relative to their default risk. Second, we find violations of Equality of Goodwill are approximately equal to zero nationally, and distributed around zero at the state level, suggesting that there is no systematic fairness violation on aggregate using this definition of fairness.<sup>16</sup> In other words, Black applicants who submitted multiple applications and ultimately defaulted were as likely to obtain approvals on all their loans as White applicants were.

Third, in Figure 11b we observe positive violations of Equality of Opportunity for almost all depicted states (restricting our sample to those 40 states with at least five Black cross-applicants between 2018-2021 who did not default), indicating that Black applicants who did not default were denied more frequently than White applicants who did not default.

<sup>16</sup>Note that Figure 11a only includes 29 states since we restrict our sample to the 29 states with at least five Black crossapplicants between 2018-2021 who defaulted.





(a) Marginal Outcome Test ( $\delta_{MOT}$ ) and Equality of Goodwill ( $\delta_{EGO}$ ) (b) Conditional Statistical Parity ( $\delta_{CSP}$ ) and Equality of Opportunity ( $\delta_{EOP}$ )

**Figure 11:** Fairness violations at the state level comparing “more narrow” fairness measures based on applications filed in 2018-2021.

This is suggestive that for a qualified Black applicant it is still harder to obtain credit than for a qualified White applicant. Similarly, in Figure 11b we observe positive violations of Conditional Statistical Parity in all depicted states: Black applicants are more likely to be denied in their loan applications even conditional on a rich set of covariates.<sup>17</sup>

These seemingly contradictory patterns are perhaps not surprising, given existing impossibility results (e.g. Kleinberg et al. [2017]). On balance, they provide mixed evidence of unfairness. They do, however, emphasize that the choice of fairness definition matters, and show different definitions can lead to contrasting results. It is also suggestive that a regulator indeed faces inherent trade-offs when deciding which notion of fairness to measure, aim for, or enforce (Kleinberg et al. [2017], Kleinberg et al. [2020]).

**Stylized Fact 3 (HMDA is not consistent with a merit-based lender).** It is instructive to consider a hypothetical lender who makes *merit-based* lending decisions. To do so, we consider a profit-maximizing risk-neutral lender that does not exhibit any taste-based discrimination. Specifically, a merit-based decision maker (or lender  $l$ ) applies the following

<sup>17</sup>Here, we depict the specification “including AUS (nonlinear)”. The results are qualitatively similar for our alternative specifications.

	Merit-based decision maker	Empirical results
Statistical Parity	Violated	Violated
Predictive Parity	Violated	Violated
Marginal Outcome Test	<b>Satisfied</b>	Violated
Equalized Odds: Equality of Opportunity	Violated	Violated
Equalized Odds: Equality of Goodwill	Violated	<b>Satisfied</b>
Conditional Statistical Parity	Violated	Violated
Representativeness	Violated	Violated

**Table 2:** Fairness violations implied by a merit-based decision maker, and as observed in our data. See Appendix A for more detail.

decision rule:

$$P(L_{il} = 1) = \begin{cases} 1 & \text{if } E(D_i|Z_i, \eta_i) < c \\ 0.5 & \text{if } E(D_i|Z_i, \eta_i) = c \\ 0 & \text{if } E(D_i|Z_i, \eta_i) > c, \end{cases} \quad (10)$$

such that applicants with a default probability lower than  $c$  are approved, applicants with a default probability higher than  $c$  are rejected, and approval is random right at the cutoff. In particular, this decision rule does not take into account an applicant’s group membership, but is solely based on an individual’s “merit”.<sup>18</sup>

We again stress that, by allowing for the presence of  $\eta_i$  in the decision rule, we do not assume we observe all the loan and applicant characteristics that the lender considers. Table 2 contrasts the theoretical predictions about our various fairness measures under a merit-based decision maker in the presence of such unobserved characteristics with our empirical findings. The left column of Table 2 summarizes how data generated by a merit-based decision maker would manifest itself in terms of violation of our fairness measures. The right column presents the empirical violations of our fairness measure in our data.<sup>19</sup> Our main conclusion is that the data is not consistent with a merit-based decision maker.

The Marginal Outcome Test is expected to be satisfied under a merit-based decision maker while it is not satisfied empirically in our data. In fact, as presented in the previous section, minorities tend to have higher default rates at the decision boundary in the data. One possible explanation is that Assumption 1 is violated. In other words, the default model lenders use (which may include  $\eta_i$ ) may be miscalibrated, which means that lenders will underestimate the default risk of minority borrowers. On the other hand, Equality of Good-

<sup>18</sup>See Kasy and Abebe [2021] for a discussion why a merit-based decision-maker may be deemed normatively undesirable.

<sup>19</sup>We derive the results in Table 2 in detail in Appendix A.

will is (approximately) satisfied in our data, which will generally not be the case under a merit-based decision maker.

**Stylized Fact 4 (Common trends).** We next ask to what extent our seven measures are correlated (and thus move together). For this exercise, we consider Statistical Parity, Predictive Parity, Conditional Statistical Parity, the Marginal Outcome Test, Representativeness, and Equality of Opportunity<sup>20</sup>. Since we only observe some of our measures starting in 2018, we look at state-level correlation and calculate each measure for the pooled sample across 2018-2021.

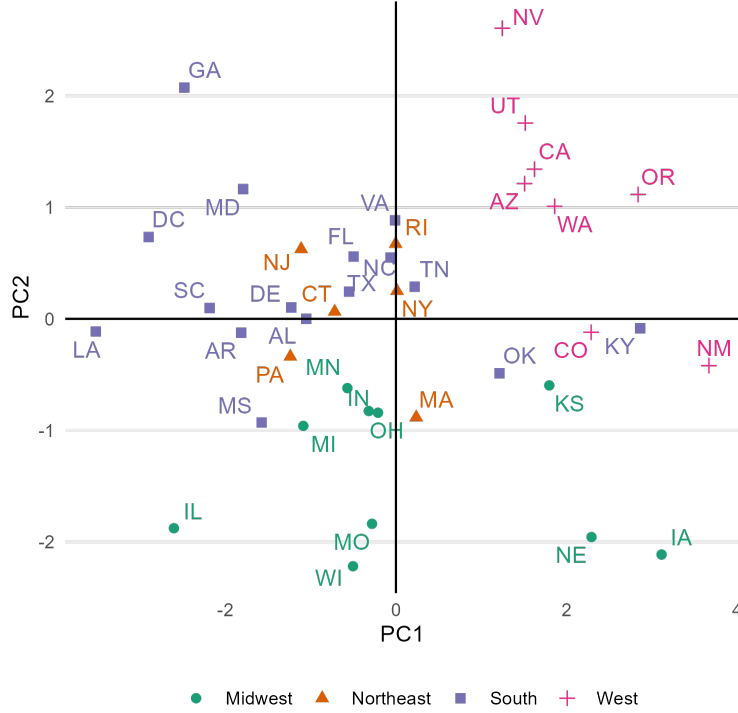
First, columns 1-6 of Table 3 present the correlation among fairness violation measures. Intuitively, Table 3 suggests that we can classify our measures into two distinct groups. The first group is formed by Statistical Parity, Predictive Parity and Conditional Statistical Parity, and the second group consists of the Marginal Outcome Test, Representativeness, and Equality of Opportunity. Measures within a group are positively correlated, while measures between groups are negatively correlated. We also see this clustering pattern reflected in the

	SP	PP	RP	CSP	MOT	EOP	PC1	PC2
SP	1						-0.81	-0.34
PP	0.66	1					-0.88	-0.2
RP	-0.59	-0.63	1				0.8	-0.27
CSP	0.51	0.58	-0.25	1			-0.64	-0.36
MOT	-0.49	-0.6	0.58	-0.32	1		0.78	-0.33
EOP	0.11	-0.01	0.33	-0.02	0.37	1	0.23	-0.89

**Table 3:** Correlation among *violations* of fairness measures and first two principal components. PC1 and PC2 denote the first two principal component. Recall that all fairness violations are defined such that larger numbers correspond to worse outcomes for Black applicants or borrowers.

results from principal component analysis. The first principal component explains 52% of the variation in fairness violations across states, is strongly negatively correlated with Statistical Parity, Predictive Parity and Conditional Statistical Parity, and strongly positively correlated with the Marginal Outcome Test, Representativeness, and Equality of Opportunity - in line with the group structure a visual inspection of the correlation matrix suggests. On the other hand, the second principal component (which explains another 21% of the total variation) is negatively correlated with all 6 fairness violations, and thus captures a tendency that states with high violations in one measure tend to indeed also have high violations in other measures.

<sup>20</sup>Equality of Goodwill is excluded because of sample limitations. Restricting our sample to those states with at least five Black marginal applicants and at least five Black cross-applicants who did not default, we are left with 40 states to analyze in Stylized Facts 4 and 5.



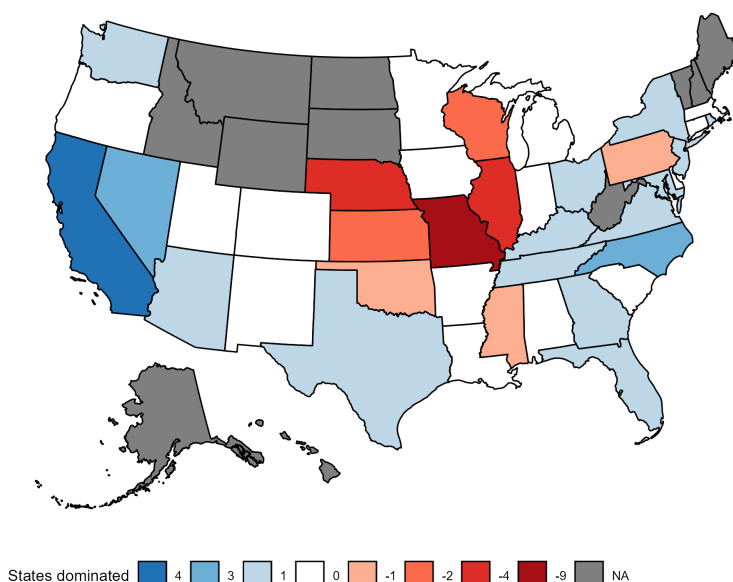
**Figure 12:** Fairness violations of 40 states over 2018-2021, projected into the space of the first two principal components.

One simple way to quantify whether states that have a high violation in one measure also tend to have high fairness violations according to all measures is to compute the largest number  $K$ , such that at least one state is in the top (bottom) 10 of all states according to all  $K$  measures. We find that there is no state that is ranked top 10 by more than 5 different measures. Similarly, there is no state that is ranked bottom 10 by more than 5 different measures.

**Stylized Fact 5 (Geographic patterns).** Finally, we illustrate the geographic heterogeneity across the United States in more detail. First, we project the six measures into the space spanned by the first two principal components. Figure 12 suggests a clustering of these states by region. The Southern states (purple squares) are primarily distributed on the left-hand side, with negative loadings on the first principal component. This suggests that states in the South tend to have larger violations of Statistical Parity, Predictive Parity and Conditional Statistical Parity, and lower violations of Representativeness, the Marginal Outcome Test, and Equality of Opportunity. The opposite is true for the Western states (pink crosses), which cluster mostly on the right-hand side of the figure. The Western states also tend to have positive loadings on the second principal component, which we recall is associated with smaller fairness violations across the board. On the other hand, the Mid-

western states (green circles) all have negative loadings on the second principal component, which suggests larger fairness violations overall.

Figure 13 attempts a partial overall ranking of states. We say that state A “strictly dominates” state B if state A has lower fairness violations than state B for all six measures. In other words, no matter what fairness measure (or combination of measures) one chooses, state A is more fair than state B according to this measure. In Figure 13, we depict for each state the number of states it strictly dominates. For example, California (with a value of four) has a smaller fairness violation according to all six measures than four states: Kansas, Missouri, Nebraska and Oklahoma. The map suggests that the Midwestern states in particular tend to be strictly dominated by other states, with Illinois, Nebraska, Missouri, Kansas and Wisconsin being strictly dominated by at least two other states.



**Figure 13:** Geographic visualization of how many other states a given geographic state strictly dominates across all measures. For a given state, positive numbers indicate the number of states with higher fairness violations across all six measures. Negative values indicate the number of states with lower fairness violations across all six measures. All numbers exclude the eleven grey regions with insufficient data.

This geographical pattern is further underlined if we rank all states according to each of the fairness measures, and then average these ranks. While the top five states (those with the lowest overall fairness violations according to this metric) fall into the Western region, the 9 Midwest states included are all ranked in the bottom 14 states.

**Interactive dashboard.** While we have presented five Stylized Facts that highlight recent trends in fairness and inequality in the mortgage market, we are only able to highlight

a small subset of interesting results in this section. To allow the reader to explore our results more, we have created an interactive appendix in the form of an online dashboard at <https://mortgagefairness.github.io/>. This interactive dashboard allows the user to explore our results further across both across time and space. For example, it also includes all of our measures for Hispanic and Asian borrowers, allows the visualization of time series trends at the state-level, allows the creation of geographic maps based on individual measures, and allows a user to interactively compare multiple measures in one figure.

## 5 Conclusion

The first question we set out to answer was whether it matters what definition of fairness one uses when assessing the outcomes of a market, in particular in the US mortgage market. To answer this question, we considered a wide range of fairness definitions stemming from the economics and computer science literature, law and regulatory guidance, as well as public debate.

We find strong evidence that the definition of fairness indeed matters, both theoretically and empirically. Different fairness definitions will lead to very different conclusions. This has important policy implications: depending on the context, policymakers and regulators should carefully decide on the appropriate definition of fairness to be used, as this choice will be important in shaping policy decisions.

The second question we set to answer was how fair or unfair the outcome of the US mortgage market looks. In light of the answer to our first question above, we do not find a conclusive answer. We find strong evidence of systematically worse outcomes for Black Americans. We are, however, unable to conclude whether these disparities are due to unfair decisions by loan officers. Different fairness definitions lead to different conclusions. One implication from this is that any one definition (or study) may be misleading, and a comprehensive analysis might include several competing definitions.

Finally, we document large differences in our fairness measures across both time and space in the United States. Exploring the drivers of these differences would be an interesting avenue for future research.

## References

- Uniform guidelines on employee selection procedures. 43 FR 38290, 1978. Federal Register.
- Stefania Albanesi and Domonkos F Vamossy. Predicting consumer default: A deep learning approach. Working paper, National Bureau of Economic Research, 2019.
- Joseph G. Altonji, Todd E. Elder, and Christopher R. Taber. Selection on observed and unobserved variables: Assessing the effectiveness of catholic schools. *Journal of Political Economy*, 113(1):151–184, 2005.

- Brent W Ambrose, James N Conklin, and Luis A Lopez. Does borrower and broker race affect the cost of mortgage credit? *The Review of Financial Studies*, 34(2):790–826, 2021.
- Julia Angwin, Jeff Larson, Surya Mattu, and Lauren Kirchner. Machine bias: There’s software used across the country to predict future criminals. and it’s biased against blacks. *ProPublica*, 2016.
- Shamena Anwar and Hanming Fang. Testing for racial prejudice in the parole board release process: Theory and evidence. *The Journal of Legal Studies*, 44(1):1–37, 2015.
- Bronson Argyle, Sasha Indarte, Benjamin Iverson, and Christopher Palmer. Explaining racial disparities in personal bankruptcy outcomes. Working paper, 2023.
- David Arnold, Will Dobbie, and Crystal S Yang. Racial bias in bail decisions. *The Quarterly Journal of Economics*, 133(4):1885–1932, 2018.
- R.B. Avery, P.E. Beeson, and P.S. Calem. Using hmda data as a regulatory screen for fair lending compliance. *Journal of Financial Services Research*, 11:9–42, 1997.
- Ian Ayres. Testing for discrimination and the problem of “included variable bias”. *Yale Law School Mimeo*, 2010.
- Robert Bartlett, Adair Morse, Richard Stanton, and Nancy Wallace. Consumer-lending discrimination in the fintech era. *Journal of Financial Economics*, 143(1):30–56, 2022.
- Patrick Bayer, Fernando Ferreira, and Stephen L Ross. The vulnerability of minority homeowners in the housing boom and bust. *American Economic Journal: Economic Policy*, 8(1):1–27, 2016.
- Patrick Bayer, Fernando Ferreira, and Stephen L Ross. What drives racial and ethnic differences in high-cost mortgages? the role of high-risk lenders. *The Review of Financial Studies*, 31(1):175–205, 2018.
- Gary S Becker. *The economics of discrimination*. University of Chicago press, 1957.
- James A Berkovec, Glenn B Canner, Stuart A Gabriel, and Timothy H Hannan. Discrimination, competition, and loan performance in FHA mortgage lending. *Review of Economics and Statistics*, 80(2):241–250, 1998.
- Neil Bhutta and Aurel Hizmo. Do minorities pay more for mortgages? *The Review of Financial Studies*, 34(2):763–789, 2021.
- Neil Bhutta, Steven Laufer, and Daniel Ringo. Residential mortgage lending in 2016: Evidence from the home mortgage disclosure act data. Technical report, Board of Governors of the Federal Reserve System, 2017.

- Neil Bhutta, Aurel Hizmo, and Daniel Ringo. How much does racial bias affect mortgage lending? evidence from human and algorithmic credit decisions. FEDS working paper, 2022.
- H.A. Black, B.L. Robinson, and R.L. Schweitzer. Comparing lending decisions of minority-owned and white-owned banks: Is there discrimination in mortgage lending? *Review of Financial Economics*, 10:23–39, 2001.
- Harold Black, Robert L Schweitzer, and Lewis Mandell. Discrimination in mortgage lending. *The American Economic Review*, 68(2):186–191, 1978.
- Interagency Fair Lending Examination Procedures*. Board of Governors of the Federal Reserve System, Office of the Comptroller of the Currency, Federal Deposit Insurance Corporation, Consumer Financial Protection Bureau, 2009. URL <https://www.ffiec.gov/pdf/fairlend.pdf>.
- J Aislinn Bohren, Peter Hull, and Alex Imas. Systemic discrimination: theory and measurement. Working paper, National Bureau of Economic Research, 2022.
- Ryan Bubb and Alex Kaufman. Securitization and moral hazard: Evidence from credit score cutoff rules. *Journal of Monetary Economics*, 63:1–18, 2014.
- Kerwin Kofi Charles and Erik Hurst. The correlation of wealth across generations. *Journal of Political Economy*, 111(6):1155–1182, 2003.
- Ping Cheng, Zhenguo Lin, and Yingchun Liu. Racial discrepancy in mortgage interest rates. *The Journal of Real Estate Finance and Economics*, 51:101–120, 2015.
- Alexandra Chouldechova. Fair prediction with disparate impact: A study of bias in recidivism prediction instruments. *Big Data*, 5(2):153–163, 2017.
- Yuliya Demyanyk. Your credit score is a ranking, not a score. *Economic Commentary*, (2010-16), 2010.
- Will Dobbie, Andres Liberman, Daniel Paravisini, and Vikram Pathania. Measuring bias in consumer lending. *The Review of Economic Studies*, 88(6):2799–2832, 2021.
- Cynthia Dwork and Christina Ilvento. Fairness under composition. *10th Innovations in Theoretical Computer Science*, 2019.
- Cynthia Dwork, Moritz Hardt, Toniann Pitassi, Omer Reingold, and Richard Zemel. Fairness through awareness. In *Proceedings of the 3rd Innovations in Theoretical Computer Science Conference*, pages 214–226, 2012.
- Hadi Elzayn, Simon Freyaldenhoven, and Minchul Shin. Using marginal candidates to measure fairness in the U.S. mortgage market. Working paper, 2023.



- Fannie Mae. Fannie Mae Selling Guide B3-2-03, Risk Factors Evaluated by DU. <https://selling-guide.fanniemae.com/Selling-Guide/Origination-thru-Closing/Subpart-B3-Underwriting-Borrowers/Chapter-B3-2-Desktop-Underwriter-DU-/1032994121/B3-2-03-Risk-Factors-Evaluated-by-DU-09-01-2021.htm>, 2023. Accessed: 2023-02-22.
- Federal Reserve Bank of New York. Quarterly Report on Household Debt and Credit 2022:Q4. [https://www.newyorkfed.org/medialibrary/interactives/householdcredit/data/pdf/HHDC\\_2022Q4](https://www.newyorkfed.org/medialibrary/interactives/householdcredit/data/pdf/HHDC_2022Q4), 2023. Accessed: 2023-02-28.
- W Scott Frame, Ruidi Huang, Erik J Mayer, and Adi Sunderam. The impact of minority representation at mortgage lenders. *SMU Cox School of Business Research Paper*, (22-08), 2021.
- Andreas Fuster, Paul Goldsmith-Pinkham, Tarun Ramadorai, and Ansgar Walther. Predictably unequal? the effects of machine learning on credit markets. *The Journal of Finance*, 77(1):5–47, 2022.
- Marco Giacoletti, Rawley Heimer, and Edison G Yu. Using high-frequency evaluations to estimate discrimination: Evidence from mortgage loan officers. Working paper, 2022.
- Alex Goldstein, Adam Kapelner, Justin Bleich, and Emil Pitkin. Peeking inside the black box: Visualizing statistical learning with plots of individual conditional expectation. *Journal of Computational and Graphical Statistics*, 24(1):44–65, 2015.
- Nina Grgić-Hlača, Muhammad Bilal Zafar, Krishna P Gummadi, and Adrian Weller. Beyond distributive fairness in algorithmic decision making: Feature selection for procedurally fair learning. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 32, 2018.
- Moritz Hardt, Eric Price, and Nati Srebro. Equality of opportunity in supervised learning. *Advances in Neural Information Processing Systems*, 29, 2016.
- Agustin Hurtado and Jung Sakong. Racial disparities in the us mortgage market. In *AEA Papers and Proceedings*. American Economic Association, forthcoming.
- Jongbin Jung, Sam Corbett-Davies, Ravi Shroff, and Sharad Goel. Omitted and included variable bias in tests for disparate impact. *arXiv preprint arXiv:1809.05651*, 2018.
- Maximilian Kasy and Rediet Abebe. Fairness, equality, and power in algorithmic decision-making. In *Proceedings of the 2021 ACM Conference on Fairness, Accountability, and Transparency*, pages 576–586, 2021.
- Amir Kermani and Francis Wong. Racial disparities in housing returns. Technical report, National Bureau of Economic Research, 2021.

- Sunwoong Kim and Gregory D Squires. Lender characteristics and racial disparities in mortgage lending. *Journal of Housing Research*, pages 99–113, 1995.
- J. Kleinberg, J. Ludwig, S. Mullainathan, and Ashesh Rambachan. An economic approach to regulating algorithms. Working paper, National Bureau of Economic Research, 2020.
- Jon Kleinberg, Sendhil Mullainathan, and Manish Raghavan. Inherent trade-offs in the fair determination of risk scores. In Christos H. Papadimitriou, editor, *8th Innovations in Theoretical Computer Science Conference*, volume 67, pages 43:1–43:23. Schloss Dagstuhl–Leibniz-Zentrum fuer Informatik, 2017.
- Moritz Kuhn, Moritz Schularick, and Ulrike I Steins. Income and wealth inequality in america, 1949–2016. *Journal of Political Economy*, 128(9):3469–3519, 2020.
- Helen F Ladd. Evidence on discrimination in mortgage lending. *Journal of Economic Perspectives*, 12(2):41–62, 1998.
- Himabindu Lakkaraju, Jon Kleinberg, Jure Leskovec, Jens Ludwig, and Sendhil Mullainathan. The selective labels problem: Evaluating algorithmic predictions in the presence of unobservables. In *Proceedings of the 23rd ACM SIGKDD International Conference on Knowledge Discovery and Data Mining*, pages 275–284, 2017.
- Paul C Lubin. Fair lending testing: Best practices, trends and training. *Joint Centre for Housing Studies, Harvard University*, 2008.
- Vitaly Meursault, Daniel Moulton, Larry Santucci, and Nathan Schor. The time is now: Advancing fairness in lending through machine learning. Frb of philadelphia working paper no. 22-39, 2022.
- Alicia H Munnell, Geoffrey MB Tootell, Lynn E Browne, and James McEneaney. Mortgage lending in Boston: interpreting HMDA data. *American Economic Review*, pages 25–53, 1996.
- Arvind Narayanan. Translation tutorial: 21 fairness definitions and their politics. In *Proceedings Conference on Fairness, Accountability, and Transparency*, volume 1170, page 3, New York, NY, 2018.
- Alexandru Niculescu-Mizil and Rich Caruana. Predicting good probabilities with supervised learning. In *Proceedings of the 22nd International Conference on Machine Learning*, pages 625–632, 2005.
- Supreme Court of the United States. Texas department of housing and community affairs v. inclusive communities project, inc., 2015. URL [https://www.supremecourt.gov/opinions/14pdf/13-1371\\_m64o.pdf](https://www.supremecourt.gov/opinions/14pdf/13-1371_m64o.pdf). 135 S. Ct. 2507.
- Emily Oster. Unobservable selection and coefficient stability: Theory and validation. *Journal of Business Economics and Statistics*, 37(2):187–204, 2019.

- Anya ER Prince and Daniel Schwarcz. Proxy discrimination in the age of artificial intelligence and big data. *Iowa L. Rev.*, 105:1257, 2019.
- Stephen L Ross. Mortgage lending discrimination and racial differences in loan default: A simulation approach. *Journal of Housing Research*, pages 277–297, 1997.
- Stephen L Ross and John Yinger. *The color of credit: Mortgage discrimination, research methodology, and fair-lending enforcement*. MIT press, 2002.
- Stephen L Ross, Margery Austin Turner, Erin Godfrey, and Robin R Smith. Mortgage lending in chicago and los angeles: A paired testing study of the pre-application process. *Journal of Urban Economics*, 63(3):902–919, 2008.
- Camelia Simoiu, Sam Corbett-Davies, and Sharad Goel. The problem of infra-marginality in outcome tests for discrimination. *The Annals of Applied Statistics*, 11(3):1193–1216, 2017.
- Prasanna Tantri. Fintech for the poor: Financial intermediation without discrimination. *Review of Finance*, 25(2):561–593, 2021.
- United States Congress. Civil rights act of 1964. U.S. Code Congressional and Administrative News, 1964. Public Law 88-352, 78 Stat. 241.
- United States Congress. Civil rights act of 1968. U.S. Statutes at Large, 1968. URL <https://www.govinfo.gov/content/pkg/STATUTE-82/pdf/STATUTE-82-Pg73.pdf>. Public Law 90-284.
- United States Congress. Equal employment opportunity act of 1972. U.S. Code Congressional and Administrative News, 1972. Public Law 92-261, 86 Stat. 103.
- United States Congress. Fair housing act (fhact), title viii of the civil rights act of 1968, as amended (42 usc 3601 et seq.). Federal Fair Lending Regulations and Statutes, Consumer Compliance Handbook, 2006. URL [https://www.federalreserve.gov/boarddocs/supmanual/cch/fair\\_lend\\_fhact.pdf](https://www.federalreserve.gov/boarddocs/supmanual/cch/fair_lend_fhact.pdf).
- Paul Willen and David Hao Zhang. Do lenders still discriminate? a robust approach for assessing differences in menus. Working paper, National Bureau of Economic Research, 2020.
- John Yinger. Acts of discrimination: Evidence from the 1989 housing discrimination study. *Journal of Housing Economics*, 1(4):318–346, 1991.
- John Yinger. Why default rates cannot shed light on mortgage discrimination. *Cityscape*, pages 25–31, 1996.

## A Merit-based decision maker

**Definition 1.** We call a decision maker (lender)  $l$  a **merit-based decision maker** if she applies the following decision rule:

$$P(L_{il} = 1) = \begin{cases} 1 & \text{if } E(D_i|Z_i, \eta_i) < c \\ 0.5 & \text{if } E(D_i|Z_i, \eta_i) = c \\ 0 & \text{if } E(D_i|Z_i, \eta_i) > c, \end{cases} \quad (11)$$

such that applicants with a default probability lower than  $c$  are approved, applicants with a default probability higher than  $c$  are rejected, and there is some randomness right at the cutoff. In particular, this decision rule does not take into account an applicant's group membership, but is solely based on an individual's "merit".

Under such a merit-based decision maker in the presence of such unobserved characteristics, we then ask whether our varying measures of fairness are satisfied or violated.

Let us introduce an auxiliary random variable  $\phi$  which takes 1 with probability  $1/2$  otherwise 0. This random variable is independent to all other variables. When  $\phi = 1$ , the loan officer accepts the application with  $E[D|Z, \eta] = c$ .

We will illustrate any violations by means of a simple counterexample. In this example there exist two potential realizations for  $Z_i$  and  $\eta_i$ . Table 4 displays the conditional probabilities of  $(Z_i, \eta_i)$  conditional on  $G$  and the conditional probabilities of default.

**Table 4:** A simple example

$Z$	$\eta$	Conditional probability		Conditional default probability
		$P(Z, \eta G = 0)$	$P(Z, \eta G = 1)$	$P(D = 1 Z, \eta)$
1	1	0	1/3	2/3
1	2	1/3	1/3	1/3
2	1	1/3	1/6	1/3
2	2	1/3	1/6	0

### A.1 Statistical Parity

Unconditional Statistical Parity will generally not be satisfied under a merit-based decision maker. To see this, we first define the set  $\Phi^c = \{(z, \eta^*) : E(D_i|Z_i = z, \eta_i = \eta^*) < c\}$  and  $\Psi^c = \{(z, \eta^*) : E(D_i|Z_i = z, \eta_i = \eta^*) = c\}$ . Then, we have

$$P(L_{il} = 1|G_i = g) = P((Z_i, \eta_i) \in \Phi^c|G_i = g) + \frac{1}{2}P((Z_i, \eta_i) \in \Psi^c|G_i = g)$$

But if the joint distribution of  $(Z_i, \eta_i)$  depends on  $G_i$ ,  $P[(Z_i, \eta_i) \in \Phi^c | G_i = g]$  and  $P[(Z_i, \eta_i) \in \Psi^c | G_i = g]$  may not be equal to  $P[(Z_i, \eta_i) \in \Phi^c | G_i = g']$  and  $P[(Z_i, \eta_i) \in \Psi^c | G_i = g']$ , respectively. Hence,  $P[L_{il} = 0 | G_i = g]$  and  $P[L_{il} = 0 | G_i = g']$  may differ, and Unconditional Statistical Parity will not hold in general.

As a specific counterexample, take the data generating process from Table 4. Let  $c = 1/3$ , then

$$\begin{aligned} P(L = 1 | G = 0) &= P((Z, \eta) = (1, 2), \phi = 1 | G = 0) \\ &\quad + P((Z, \eta) = (2, 1), \phi = 1 | G = 0) \\ &\quad + P((Z, \eta) = (2, 2) | G = 0) \\ &= 1/3 \cdot 1/2 + 1/3 \cdot 1/2 + 1/3 = 2/3. \end{aligned}$$

while

$$\begin{aligned} P(L = 1 | G = 1) &= P((Z, \eta) = (1, 2), \phi = 1 | G = 1) \\ &\quad + P((Z, \eta) = (2, 1), \phi = 1 | G = 1) \\ &\quad + P((Z, \eta) = (2, 2) | G = 1) \\ &= 1/3 \cdot 1/2 + 1/6 \cdot 1/2 + 1/6 = 5/12. \end{aligned}$$

## A.2 Predictive Parity

Predictive Parity will generally not be satisfied under a merit-based decision maker. The general argument closely follows the one above, and we thus illustrate this using the example introduced at the beginning of the section. We again set  $c$  to  $1/3$ .

Then,

$$\begin{aligned} P(D = 1 | L = 1, G = 0) &= \frac{P(D = 1, L = 1 | G = 0)}{P(L = 1 | G = 0)} \\ &= \frac{1/9}{2/3} = 1/6, \end{aligned}$$

because

$$\begin{aligned} P(D = 1, L = 1 | G = 0) &= P(D = 1, (Z, \eta) = (1, 2), \phi = 1 | G = 0) \\ &\quad + P(D = 1, (Z, \eta) = (2, 1), \phi = 1 | G = 0) \\ &\quad + P(D = 1, (Z, \eta) = (2, 2) | G = 0) \\ &= P(D = 1 | (Z, \eta) = (1, 2) | G = 0) P((Z, \eta) = (1, 2), G = 0, \phi = 1) P(\phi = 1) \\ &\quad + P(D = 1 | (Z, \eta) = (2, 1), G = 0) P((Z, \eta) = (2, 1) | G = 0) P(\phi = 1) \\ &\quad + P(D = 1 | (Z, \eta) = (2, 2), G = 0) P((Z, \eta) = (2, 2) | G = 0) \\ &= 1/3 \cdot 1/3 \cdot 1/2 + 1/3 \cdot 1/3 \cdot 1/2 + 0 \cdot 1/3 = 1/9 \end{aligned}$$

and the denominator is from the previous derivation for statistical parity.

Similarly,

$$\begin{aligned} P(D = 1|L = 1, G = 1) &= \frac{P(D = 1, L = 1|G = 1)}{P(L = 1|G = 1)} \\ &= \frac{1/12}{5/12} = 1/5, \end{aligned}$$

because

$$\begin{aligned} P(D = 1, L = 1|G = 1) &= P(D = 1, (Z, \eta) = (1, 2), \phi = 1|G = 1) \\ &\quad + P(D = 1, (Z, \eta) = (2, 1), \phi = 1|G = 1) \\ &\quad + P(D = 1, (Z, \eta) = (2, 2)|G = 1) \\ &= P(D = 1|(Z, \eta) = (1, 2), G = 1)P((Z, \eta) = (1, 2)|G = 1)P(\phi = 1) \\ &\quad + P(D = 1|(Z, \eta) = (2, 1), G = 1)P((Z, \eta) = (2, 1)|G = 1)P(\phi = 1) \\ &\quad + P(D = 1|(Z, \eta) = (2, 2), G = 1)P((Z, \eta) = (2, 2)|G = 1) \\ &= 1/3 \cdot 1/3 \cdot 1/2 + 1/6 \cdot 1/3 \cdot 1/2 + 0 = 1/12 \end{aligned}$$

### A.3 Marginal Outcome Test

The Marginal Outcome Test (based on loan decisions) will be satisfied under a merit-based decision maker. We define a set of marginal candidates as approved applicants who originated their loans but has been denied by some lenders.

$$\mathcal{M}_g = \{i : N_i > 1, \sum_l L_{il} < N_i\}$$

where  $N_i = \sum_l (L_{il} + |1 - L_{il}|)$  is the total number of applications submitted by  $i$  because  $|1 - L_{il}|$  is a denial indicator. Note that under a merit-based decision maker, we have that

$$\mathcal{M}_g = \{i : E[D_i|Z_i, \eta_i] = c, G_i = g\}$$

Because  $c$  does not depend on  $g$ , the desired result follows,

$$P(D_i = 1|i \in \mathcal{M}_g) = P(D_i = 1|i \in \mathcal{M}_{g'}).$$

### A.4 Equalized Odds

Equality of Opportunity will not be satisfied under a merit-based decision maker. Again, let us take the example from Table 4 with  $c = 1/3$ . First note that

$$P(L = 0|D = 0, G = 0) = \frac{P(L = 0, D = 0|G = 0)}{P(D = 0|G = 0)}$$

Note that the numerator is

$$\begin{aligned}
& P(L = 0, D = 0|G = 0) \\
&= P(D = 0, (Z, \eta) = (1, 1)|G = 0) \\
&\quad + P(D = 0, (Z, \eta) = (1, 2), \phi = 0|G = 0) \\
&\quad + P(D = 0, (Z, \eta) = (2, 1), \phi = 0|G = 0) \\
&= P(D = 0|(Z, \eta) = (1, 1), G = 0)P((Z, \eta) = (1, 1)|G = 0) \\
&\quad + P(D = 0|(Z, \eta) = (1, 2), \phi = 0, G = 0)P((Z, \eta) = (1, 2)|G = 0)P(\phi = 0) \\
&\quad + P(D = 0|(Z, \eta) = (2, 1), \phi = 0, G = 0)P((Z, \eta) = (2, 1)|G = 0)P(\phi = 0) \\
&= 1/3 \cdot 0 + 1/3 \cdot 1/3 \cdot 1/2 + 1/3 \cdot 1/3 \cdot 1/2 = 1/9.
\end{aligned}$$

And the denominator is  $1 - P(D = 1|G = 0)$ . We get that

$$\begin{aligned}
P(D = 1|G = 0) &= P(D = 1|G = 0, (Z, \eta) = (1, 1))P((Z, \eta) = (1, 1)|G = 0) \\
&\quad + P(D = 1|G = 0, (Z, \eta) = (1, 2))P((Z, \eta) = (1, 2)|G = 0) \\
&\quad + P(D = 1|G = 0, (Z, \eta) = (2, 1))P((Z, \eta) = (2, 1)|G = 0) \\
&\quad + P(D = 1|G = 0, (Z, \eta) = (2, 2))P((Z, \eta) = (2, 2)|G = 0) \\
&= 2/3 \cdot 0 + 1/3 \cdot 1/3 + 1/3 \cdot 1/3 + 0 \cdot 1/3 = 2/9.
\end{aligned}$$

So

$$P(L = 0|D = 0, G = 0) = \frac{P(L = 0, D = 0|G = 0)}{P(D = 0|G = 0)} = \frac{1/9}{1 - 2/9} = 1/7.$$

For  $G = 1$ ,

$$\begin{aligned}
& P(L = 0, D = 0|G = 1) \\
&= P(D = 0, (Z, \eta) = (1, 1)|G = 1) \\
&\quad + P(D = 0, (Z, \eta) = (1, 2), \phi = 0|G = 1) \\
&\quad + P(D = 0, (Z, \eta) = (2, 1), \phi = 0|G = 1) \\
&= P(D = 0|(Z, \eta) = (1, 1), G = 1)P((Z, \eta) = (1, 1)|G = 1) \\
&\quad + P(D = 0|(Z, \eta) = (1, 2), \phi = 0, G = 1)P((Z, \eta) = (1, 2)|G = 1)P(\phi = 0) \\
&\quad + P(D = 0|(Z, \eta) = (2, 1), \phi = 0, G = 1)P((Z, \eta) = (2, 1)|G = 1)P(\phi = 0) \\
&= 1/3 \cdot 1/3 + 2/3 \cdot 1/3 \cdot 1/2 + 2/3 \cdot 1/6 \cdot 1/2 = 5/18.
\end{aligned}$$

And denominator calculated similarly as above is  $1 - P(D = 1|G = 1) = 1 - (2/3 \cdot 1/3 + 1/3 \cdot 1/3 + 1/3 \cdot 1/6 + 0 \cdot 1/6) = 7/18$ , leaving us with a value of  $5/11$  in total.

Therefore,  $P(L = 0|D = 0, G = 0) \neq P(L = 0|D = 0, G = 1)$ .

We note that Equality of Goodwill will not be satisfied under a merit-based decision maker following similar arguments as above.

## A.5 Conditional Statistical Parity

Conditional Statistical Parity w.r.t.  $Z_i$  will generally not be satisfied under a merit-based decision maker. We use the same example as above with  $c = 1/3$ . Note that

$$\begin{aligned} P(L = 0|Z = 1, G = 0) &= \frac{P(L = 0, Z = 1|G = 0)}{P(Z = 1|G = 0)} \\ &= \frac{P(Z = 1, \eta = 1|G = 0) + P(Z = 1, \eta = 2, \phi = 0|G = 0)}{P(Z = 1|G = 0)} \\ &= \frac{0 + 1/3 \cdot 1/2}{1/3} = 1/2 \end{aligned}$$

and

$$\begin{aligned} P(L = 0|Z = 1, G = 1) &= \frac{P(L = 0, Z = 1|G = 1)}{P(Z = 1|G = 1)} \\ &= \frac{P(Z = 1, \eta = 1|G = 1) + P(Z = 1, \eta = 2, \phi = 0|G = 1)}{P(Z = 1|G = 1)} \\ &= \frac{1/3 + 1/3 \cdot 1/2}{2/3} = 3/4. \end{aligned}$$

## A.6 Representativeness

Representativeness with respect to  $Z$  and  $G$  will generally not be satisfied under a merit-based decision maker. This is because there is no  $\hat{c}$  such that  $L = 1\{E[D|Z, \eta] < c\} = 1\{E[D|Z, G] < \hat{c}\}$  unless the creditworthiness ordering by  $E[D|Z, \eta]$  and  $E[D|Z, G]$  is identical.

In our simple example from Table 4, it becomes evident that the creditworthiness orderings based on  $E[D|Z, \eta]$  and  $E[D|Z, G]$  can diverge. First note that for any applicant with  $Z = z$  and  $G = g$ , we can calculate the conditional probability of  $D$  given  $Z$  and  $G$ ,  $E[D|Z = z, G = g]$ , from Table 4. When we rank applicants by  $E[D|Z = z, G = g]$ , we observe that more applicants with  $(Z = 1, \eta = 1, G = 0)$  are included while applicants with  $(Z = 1, \eta = 2, G = 1)$  are excluded compared to ranking them by  $E[D|Z, \eta]$ . This discrepancy arises because  $\eta$  and  $G$  exhibit a negative correlation with each other when conditioned on  $Z = 1$ .

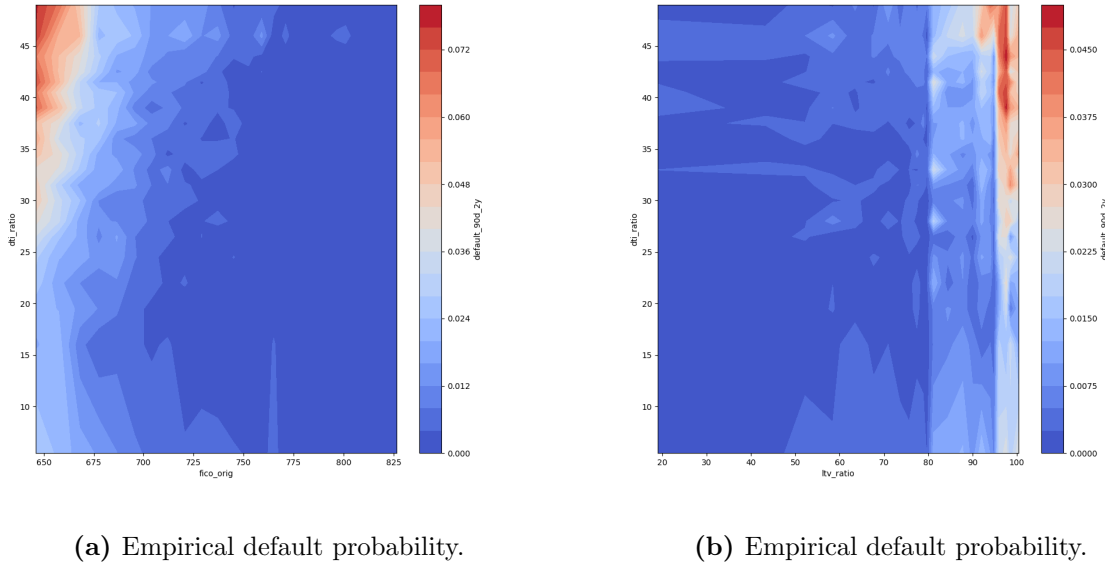
## B Modeling Default

Estimating Representativeness requires predicted default probabilities. Using the matched HMDA-McDash sample described in Section 2, we can construct such a model. That is, we use this sample to estimate  $P(D = 1|Z)$ , with the usual caveat that we only observe default behavior conditional on loan origination (and thus acceptance). In this section, we briefly describe our model and its performance.



**Features** Our baseline features are the following covariates observed at time of origination: credit score (-), Loan-to-Value (LTV) ratio (+), Debt-to-Income (DTI) ratio (+), original loan amount (+), applicant income (-), a dummy for whether a coapplicant is present on the application (-), a code for the geographic state of the property’s location, loan term (in months), funding source (the type of purchaser of the loan), a dummy indicating private mortgage insurance (PMI), and dummies for loan type (conventional, government-insured, VA, farm) and loan purpose (investment, refinancing). A plus or minus sign in brackets indicates that we impose a monotonicity constraint in the indicated direction in our model. We discuss these constraints in more detail below.

**Model Family** Figure 14 presents contour plots of the relation between the empirical default probability for mortgages originated in 2014 and a number of observed covariates.



**Figure 14:** Empirical default probability across a number of key observables

The observed patterns of non-linear interactions motivates the use of a flexible machine learning algorithm to develop a default prediction. In contrast with traditional econometric models, such as logistic regressions, this allows for highly non-linear relationships and rich interactions between the elements in  $Z$ .

Specifically, our main prediction model is a *histogram-based gradient-boosted classification tree* (HGBC) with monotonicity constraints. A HGBC tree is an ensemble method combining multiple decision trees. Unlike other ensemble methods, where combined elements are formally independent of one another, gradient-boosted trees instead proceed iteratively. That is, each subsequent iteration of the model is obtained by adding a new weak learner

that is fit to the *gradient* of the loss function at the total predictions so far.

Formally, given a loss function  $L(y, \hat{y})$ , a learning rate  $\gamma_m$ , and a class of weak learners  $\mathcal{F}$  (in the HGBC case shallow decision trees), the learning process can be described as the following algorithm:

First, obtain  $f_1$  such that

$$f_1 \in \operatorname{argmin}_{f \in \mathcal{F}} \sum_i L(y_i, f(X_i))$$

and set  $F_1 = f_1$ . Then, iterate the following steps for  $m \geq 2$ .

1. Get  $f_m$  from

$$f_m \in \operatorname{argmin}_{f \in \mathcal{F}} \sum_i L \left( \left. \frac{\partial L}{\partial \hat{y}} \right|_{F_{m-1}(X_i)}, f(X_i) \right).$$

We use mean-squared error loss, such that  $\frac{\partial L}{\partial \hat{y}} = y - \hat{y}$ , which can be viewed as a residual.

2. Update  $F_m$  based on

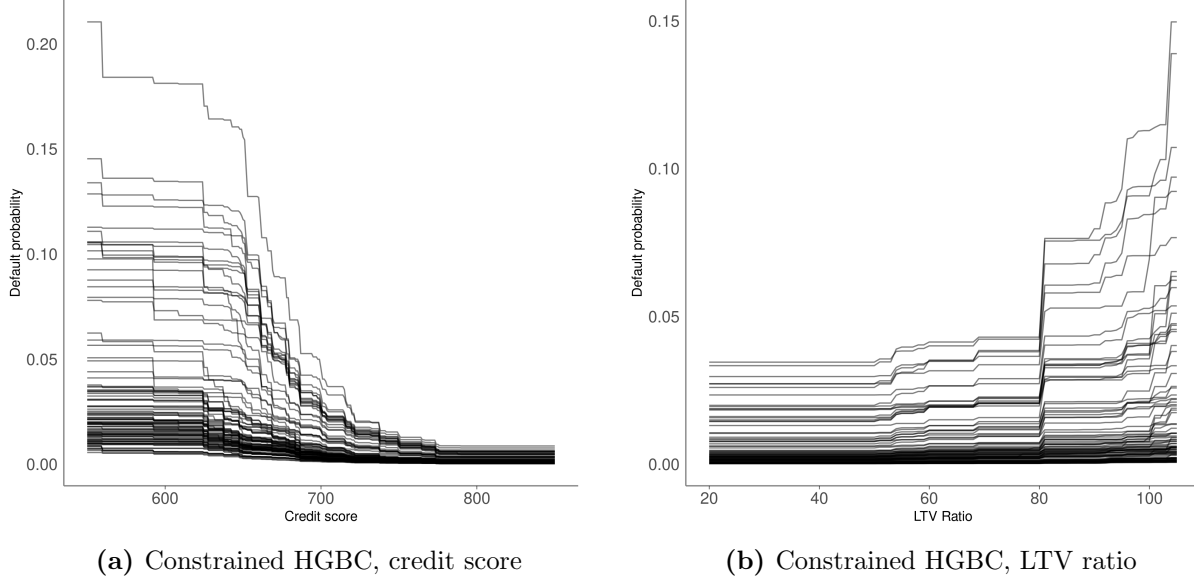
$$F_m(X) = \sum_{i=1}^m \gamma_i f_i(X) = F_{m-1}(X) + \gamma_m f_m(X)$$

and stop when the max number of iterations,  $M$ , has been reached, i.e.,  $m = M$ .

In our implementation, within a model we fix  $\gamma_m$  as a constant,  $\gamma$ . Additionally, because it is non-standard, we briefly discuss the monotonicity constraints that we impose on the algorithm. Such constraints both set a priori relationships based on economic arguments and serve as regularization. To visualize the effects the monotonicity constraints, we depict individual conditional expectations (Goldstein et al. [2015]) in Figure 15.

Each black line represents a mortgage application filed in 2014. For example, in panel (a), we construct each black line by varying the credit score from its actual value reported on the application and fixing all other features. The resulting line traces out predicted default probability at each value of the credit score and is called an Individual Conditional Expectation (Goldstein et al. [2015]). Our monotonicity constraints enforce that at an individual level, the relationship between the covariate and the default probability is always monotone.

Direct estimates of probability that come from tree-based models can sometimes be noisy and require an additional calibration step (Niculescu-Mizil and Caruana [2005]). However, in our application, our monotonicity constraint models lead to well-calibrated predictions on the test set, and so we do not recalibrate with an additional model.



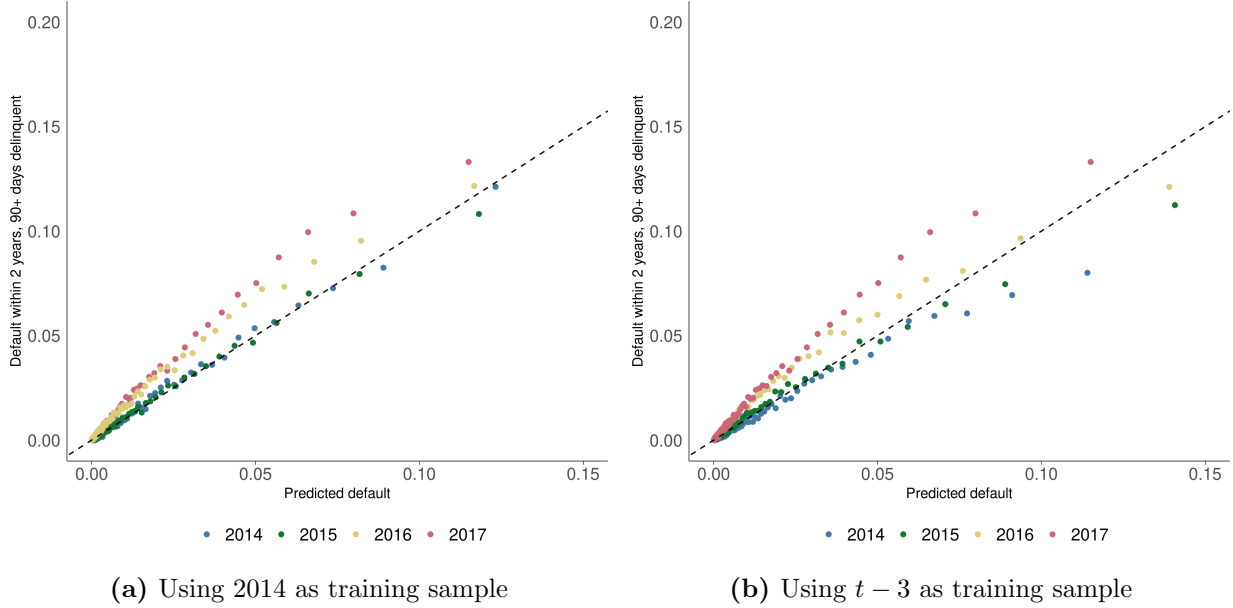
**Figure 15:** Individual conditional expectation plots for credit score and LTV ratio under the constrained HGBCs. Each black line represents a mortgage application filed in 2014.

**Train-test split** We start by applying a random 70%-30% split to create our training and testing sets in a given year. Within the training set we use 3-fold cross validation for hyperparameter tuning. In particular, we use a parameter grid of  $\gamma \in \{0.02, 0.025, 0.03\}$ ,  $M \in \{300, 350, 400\}$ , and maximum leaf nodes from  $\{16, 20, 24, 28\}$ . The models trained separately by year are then allowed to vary over all combinations of this set of hyperparameters and select the combination resulting in the lowest average mean squared error across folds.

However, evaluating a model against mortgages from the same year as the training set may be misleading because the model may incorporate future information during the span in which loan performance is measured (in our case, 24 months from origination). Thus, to account for this look-ahead bias, a test set that avoids any information leakage must contain mortgages originated at least three years after the training set. For instance, we first split mortgage applications filed in 2014 into two subsamples and use the 30% withheld as a first test set to evaluate the performance of our model. We then also evaluate the performance of our model, trained on 2014 data, on the following years. For mortgages originating in 2015 and 2016 we still have (decreasing) amounts of information leakage, while mortgages originating in 2017 and beyond are free of information leakage. For our fairness measures, we therefore use the model trained on data in year  $t - 3$  to estimate the default probabilities of mortgages originated in year  $t$ .

**Model Performance** We first illustrate our model performance using the model trained on 2014 data in Figure 16a. Here, we use a binscatter (a binned scatter plot) as a flexible, yet parsimonious way of summarizing the relationship between our predicted default probability

and the empirical default rates in the 2014 (hold-out), 2015, 2016 and 2017 samples. Visually, a well-ordered model corresponds to monotonically increasing empirical default rates.

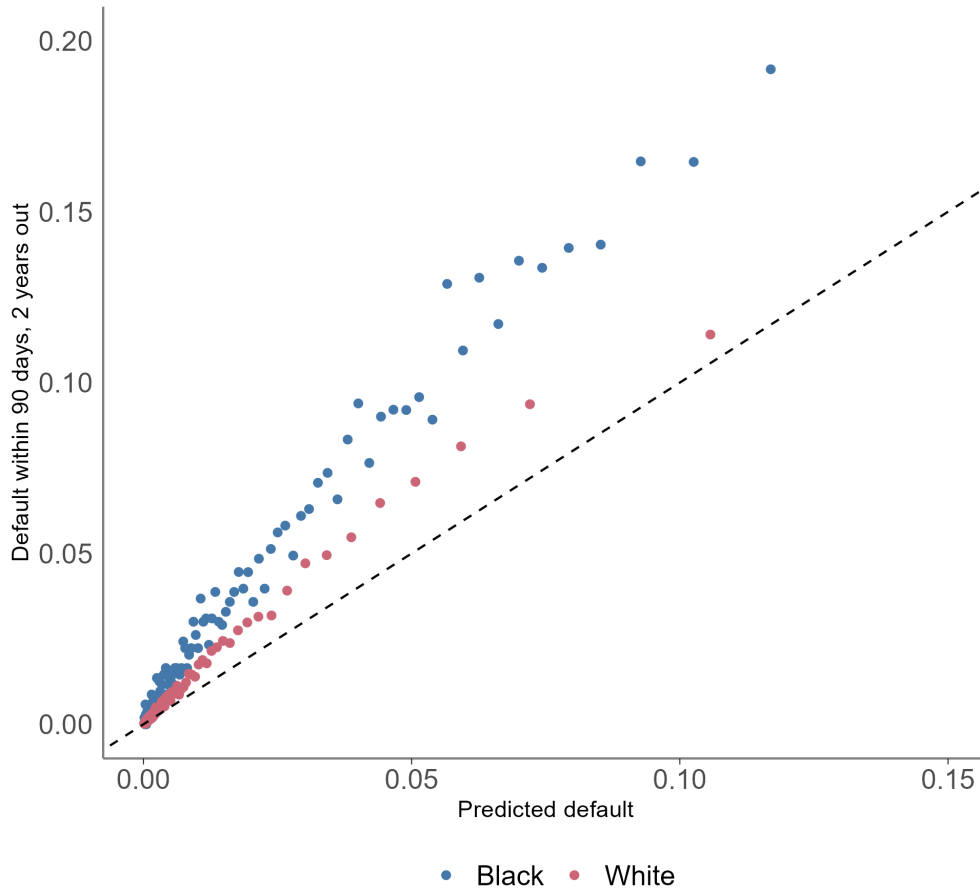


**Figure 16:** Binscatter depicting empirical default rates in year  $t$  as a function of predicted default probabilities. Each bin represents one percentage point.

We can also use Figure 16 to assess whether our model is well-calibrated. Ideally, a well-calibrated model will have the empirical vs. predicted default rate near the 45-degree line. As we can conclude from both panels, our default model performs very well at predicting the relative risk of applicants. While Figure 16a also delivers a good estimate of the absolute default risk, there is a general tendency to underestimate the default risk for subsequent years, and in particular, for our “true” test set of applications filed in 2017. This is in line with the performance of traditional credit scores, which do well in their relative ranking of consumers but are not designed to be time consistent (see, e.g. Demyanyk [2010], Albanesi and Vamossy [2019]). Additionally, in Figure 16b, as in our final specification, we depict the performance of our model on test samples ranging from 2014-2017—each of which is three years after the training year. Here, we see that even when evaluated with test sets free of information leakage, the models perform well at risk-ordering applicants across years with only a modest decrease in calibration as some points are slightly further from the 45 degree line relative to the blue and green points in panel (a).

Figure 17 depicts a binscatter for the model trained on 2014 data, with the predicted and observed default probabilities plotted for each demographic group. This lets us assess whether there are any clear discrepancies in model performance across demographic groups. We note that in the 2017 test data, our algorithm significantly underpredicts the default rates of Black applicants relative to White applicants, with the blue points lying farther above the

45 degree line relative to the other points, particularly at higher predicted probabilities of default. This pattern is repeated across subsequent years and for hold-out test sets as well. This further underlines the potential for miscalibration as observed in Figure 4b in which the credit score appears to underpredict the risk of Black applicants as well.



**Figure 17:** Binscatter depicting empirical 24 month out default rates for mortgages originated in 2017 as a function of predicted default probabilities based on a 2014 race-blind default model, separated by demographic groups: Black and White. Each bin represents one percentage point.

Finally, as is standard in Machine Learning literature, one method to measure the accuracy of our predictive model is the area under the receiver operator characteristic (ROC) curve. So models with a higher AUC (area under the curve) are preferred, as these are models with a higher true positive rate for any given level of the false positive rate. We measure the AUC of our predicted default probability relative to baseline linear and nonlinear logistic regression models, using the same covariates as our HGBC model and find that AUC is larger for our HGBC model across all years. This reinforces our choice of a nonparametric HGBC model employed in our calculation of Representativeness, in that the default probabilities estimated by our model are more accurate and precise than those based on both traditional

and nonlinear logistic regression.