## Censored skew-normal regression with delayed entry

André Moser

November 07, 2017

Reference: Moser A, Clough-Gorr K, Zwahlen M. (2015) Modeling absolute differences in life expectancy with a censored skew-normal regression approach. PeerJ 3:e1162 https://doi.org/10.7717/peerj.1162

```
library(knitr)
library(haven)

source(paste(path, "censn.r", sep=""))
data <- read_dta("http://www.stata-press.com/data/r12/cancer.dta")
data <- data.frame(data)
data$age1 <- data$age+data$studytime
head(data)</pre>
```

```
##
    studytime died drug age X_st X_d X_t X_t0 age1
## 1
                         61
## 2
                 1
                         65
                                       1
                                                66
                      1 59
            2
## 3
                 1
                                       2
                                            0
                                                61
                               1
## 4
            3
                 1
                      1 52
                                                55
                               1
            4
                               1
                                                60
## 5
                 1
                      1 56
                                   1 4
                                            0
## 6
                      1 67
                                                71
```

## Modeling results

```
### No censoring, no delayed-entry
mod <- censn(age1~1, ltrun=NULL, data=data, weights = rep(5, nrow(data)))</pre>
summary.censn(mod)
##
                            est
                                                  lci
                                                             uci
                                                                   z-ratio
                                        se
## location (mu)
                    71.2726473 0.63028951 70.0373026 72.507992 113.07922
                     9.9890295 0.50830328 8.9927734 10.985286 19.65171
## scale (alpha)
## skewness (gamma) 0.8824886 0.04790825 0.7885901 0.976387 18.42039
##
                    Pr\{>|z|\}
## location (mu)
                     0.00000
## scale (alpha)
                     0.00000
## skewness (gamma) 0.00000
### selm from package "sn"
modsn <- selm(age1~1, family = "SN", data=data, opt.method="BFGS", weights = rep(5, nrow(data)))</pre>
summary(modsn)
```

```
## Call: selm(formula = age1 ~ 1, family = "SN", data = data, weights = rep(5,
       nrow(data)), opt.method = "BFGS")
## Number of observations: 48
## Family: SN
## Estimation method: MLE
## Log-likelihood: -871.9305
## Parameter type: CP
##
## CP residuals:
      Min
                1Q Median
                                ЗQ
                                        Max
## -16.274 -7.274 -1.774
                            6.226 24.726
##
## Regression coefficients
        estimate std.err z-ratio Pr{>|z|}
                   0.6305 113.0514
## mean 71.2739
##
## Parameters of the SEC random component
##
          estimate std.err
## s.d.
            9.9907
                     0.508
## gamma1
          0.8826
                     0.048
### Censoring, but no delayed-entry
mod <- censn(age1~1, failure=died, ltrun=NULL, data=data, opt.method="BFGS")</pre>
summary.censn(mod)
##
                           est
                                                  lci
                                                            uci
                                                                   z-ratio
                                        se
## location (mu)
                    76.5436832 2.64304192 71.3634162 81.723950 28.960450
                    14.5681889 2.22360640 10.2100005 18.926377 6.551604
## scale (alpha)
## skewness (gamma) 0.9538285 0.04371477 0.8681491 1.039508 21.819364
##
                    Pr\{>|z|\}
## location (mu)
                     0.00000
## scale (alpha)
                     0.00000
## skewness (gamma) 0.00000
### Censoring and delayed entry
mod <- censn(age1~1, failure=died, ltrun=age, data=data)</pre>
summary.censn(mod)
##
                                                  lci
                                                            uci
                                                                   z-ratio
                           est
                                        se
                    74.7369823 2.65210688 69.5389483 79.935016 28.180230
## location (mu)
## scale (alpha)
                    14.4656133 2.14878460 10.2540728 18.677154 6.731998
## skewness (gamma) 0.9584917 0.06323546 0.8345525 1.082431 15.157505
##
                    Pr\{>|z|\}
## location (mu)
                     0.00000
## scale (alpha)
                     0.00000
## skewness (gamma) 0.00000
### Censoring and delayed entry, covariate drug
mod <- censn(age1~factor(drug), failure=died, ltrun=age, data=data)</pre>
summary.censn(mod)
```

```
##
                           est
                                     se
                                              lci
                                                           uci
                                                                 z-ratio
## location (mu)
                    56.8852674 4.8720673 47.336191 66.434343740 11.675797
## factor(drug)2
                    19.0146152 5.6825833 7.876957 30.152273811 3.346122
## factor(drug)3
                    30.0168067 6.1314072 17.999469 42.034144043 4.895582
## scale (alpha)
                    11.5008421 2.9451744 5.728406 17.273277886 3.904978
## skewness (gamma) -0.6021632 0.3087461 -1.207294 0.002968023 -1.950351
##
                    Pr{>|z|}
## location (mu)
                    0.00000
## factor(drug)2
                    0.00082
## factor(drug)3
                    0.00000
## scale (alpha)
                    0.00009
## skewness (gamma) 0.05113
```